# Texture Mapping

CSE 457

Winter 2015

# Reading

Required

- Angel, 7.4-7.10

Recommended

- Paul S. Heckbert. Survey of texture mapping. **IEEE Computer Graphics and Applications** 6(11): 56--67, November 1986.

Optional

- Woo, Neider, & Davis, Chapter 9
- James F. Blinn and Martin E. Newell. Texture and reflection in computer generated images. **Communications of the ACM** 19(10): 542--547, October 1976.

# Texture mapping


*Texture mapping (Woo et al., fig. 9-1)*

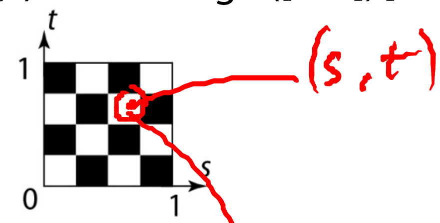
Texture mapping allows you to take a simple polygon and give it the appearance of something much more complex.

- Due to Ed Catmull, PhD thesis, 1974
- Refined by Blinn & Newell, 1976

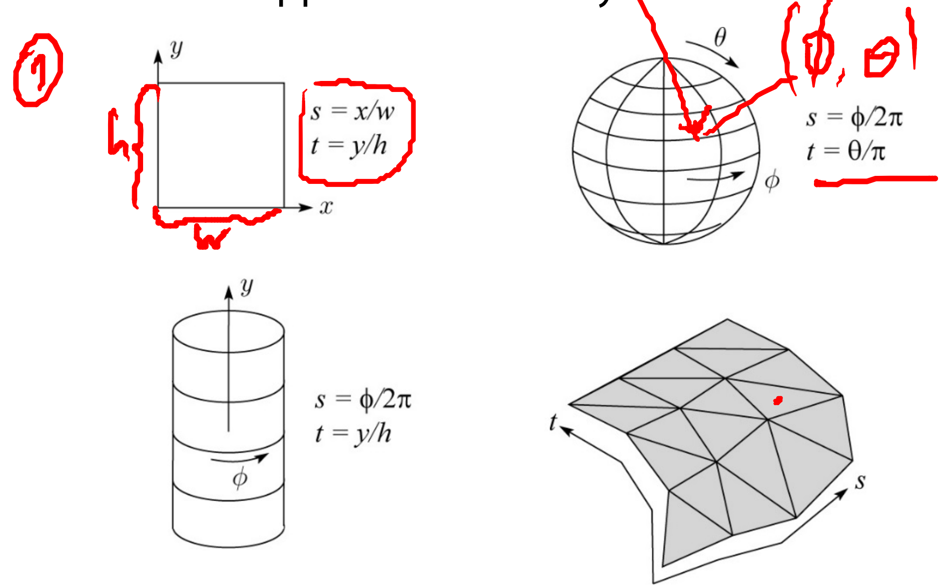
A texture can modulate just about any parameter – diffuse color, specular color, specular exponent, …

# Implementing texture mapping

A texture lives in it own abstract image coordinates paramaterized by (*s*,*t*) in the range ([0..1], [0..1]):

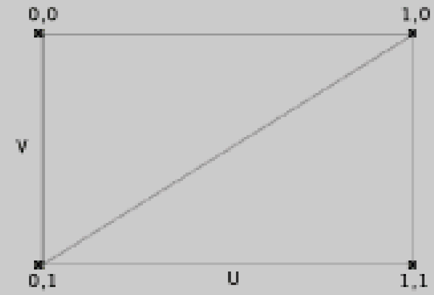



It can be wrapped around many different surfaces:



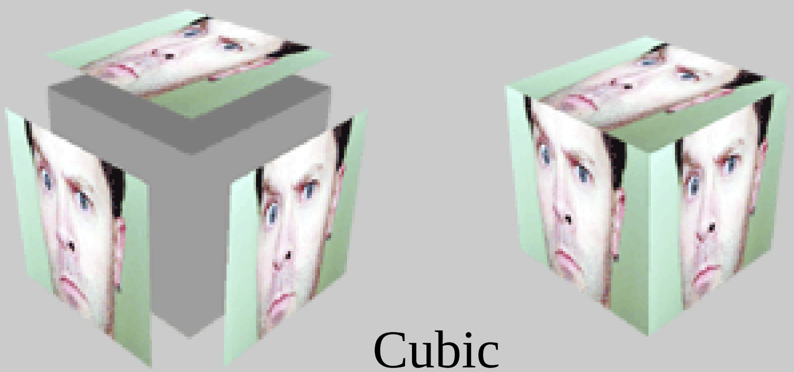

With a ray caster, we can do the sphere and cylinder mappings directly (as we will see later). For z-buffers, everything gets converted to a triangle mesh with associated (*s*,*t*) coordinates.

Note: if the surface moves/deforms, the texture goes with it.

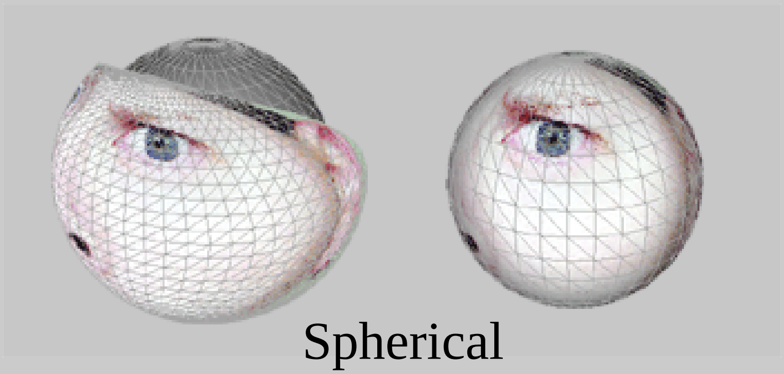




Planar

Cylindrical



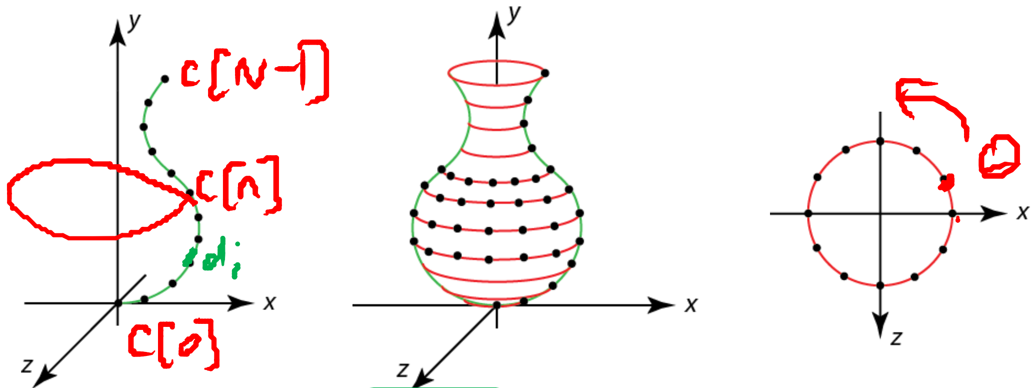
Cubic



Spherical

## Texture coordinates on a surface of revolution

texture $(s,t)$




$$s = \frac{\theta}{2\pi}$$

$$t = \frac{n}{N}$$

$$\boxed{t = \frac{\sum_{i=0}^{n} d_i}{\sum_{i=0}^{N-1} d_i}}$$

use this t

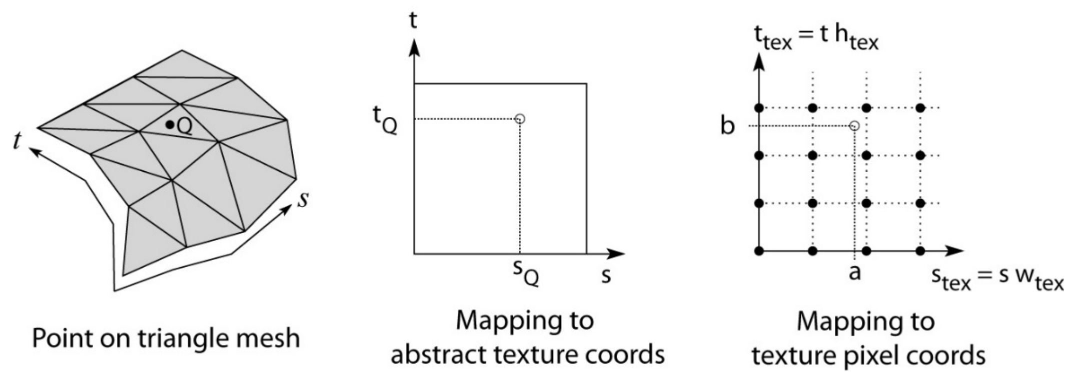
# Mapping to texture image coords

The texture is usually stored as an image. Thus, we need to convert from abstract texture coordinate:

$(s,t)$ in the range ([0..1], [0..1])

to texture image coordinates:

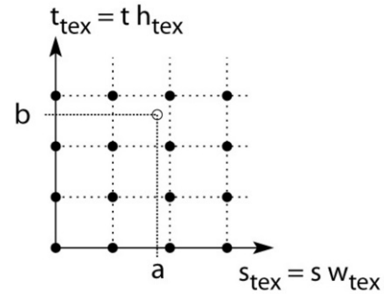
$(s_{tex},t_{tex})$ in the range ([0.. $w_{tex}$], [0.. $h_{tex}$])



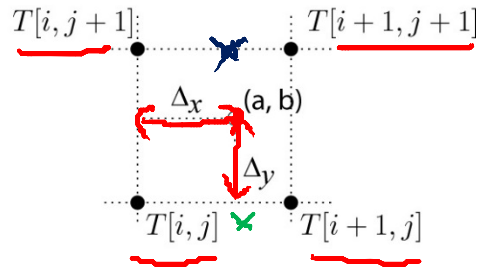

**Q**: What do you do when the texture sample you need lands between texture pixels?

# Texture resampling

We need to resample the texture:




Mapping to
texture pixel coords




Close-up

Thus, we seek to solve for: $\mathrm{T}(a,b) = \mathrm{T}\left(i+\Delta_x, j+\Delta_y\right)$

A common choice is **bilinear interpolation**:

$$\mathrm{T}\left(i+\Delta_x, j\right) = \underline{(1-\Delta x)}\,\mathrm{T}[i,j] + \underline{\Delta x}\,\mathrm{T}[i+1,j]$$

$$\mathrm{T}\left(i+\Delta_x, j+1\right) = \underline{(1-\Delta x)}\,\mathrm{T}[i,j+1] + \underline{\Delta x}\,\mathrm{T}[i+1,j+1]$$

$$\mathrm{T}\left(i+\Delta_x, j+\Delta_y\right) = \underline{(1-\Delta y)}\,\mathrm{T}\left(i+\Delta_x, j\right) + \underline{\Delta y}\,\mathrm{T}\left(i+\Delta_x, j+1\right)$$

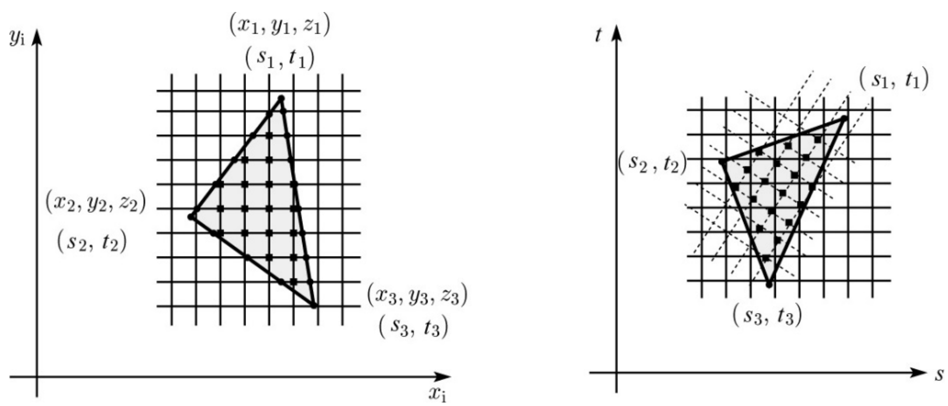
$$= \underline{(1-\Delta x)(1-\Delta y)}\,\mathrm{T}[i,j] + \underline{\Delta x(1-\Delta y)}\,\mathrm{T}[i+1,j] + \underline{(1-\Delta x)\,\Delta y}\,\mathrm{T}[i,j+1] + \underline{\Delta x\,\Delta y}\,\mathrm{T}[i+1,j+1]$$

## Texture mapping and the z-buffer

Texture-mapping can also be handled in z-buffer algorithms.

<u>Method</u>:

- Scan conversion is done in screen space, as usual
- Each pixel is colored according to the texture
- Texture coordinates are found by Gouraud-style interpolation



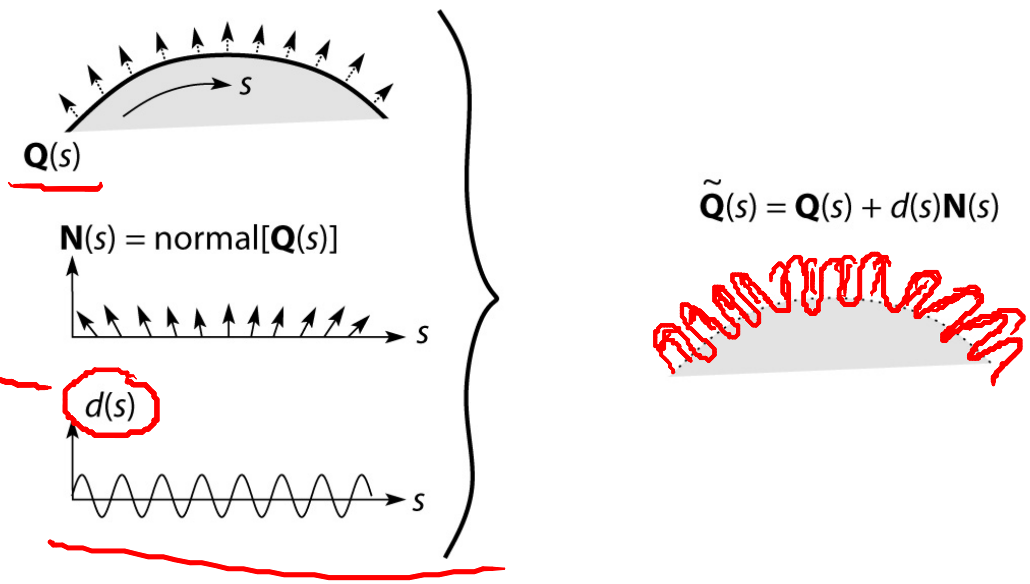

<u>Note</u>: Mapping is more complicated to handle perspective correctly!

## Displacement mapping

Textures can be used for more than just color.

In **displacement mapping**, a texture is used to perturb the surface geometry itself. Here's the idea in 2D:

displac. map.




- These displacements "animate" with the surface
- In 3D, you would of course have (s,t) parameters instead of just s.

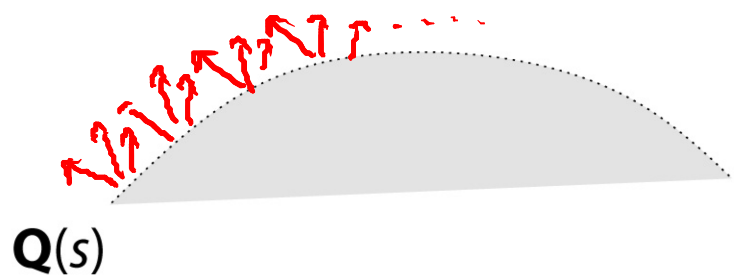
Suppose **Q** is a simple surface, like a cube. Will it take more work to render the modified surface $\tilde{\mathbf{Q}}$?

## Bump mapping

In **bump mapping**, a texture is used to perturb the normal:

- Use the original, simpler geometry, $\mathbf{Q}(s)$, for hidden surfaces
- Use the normal from the displacement map for shading:

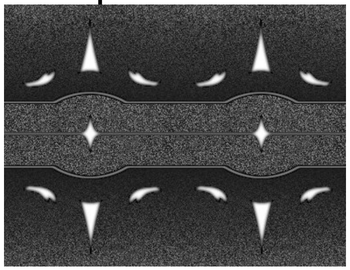
$$\tilde{\mathbf{N}} = \text{normal}[\tilde{\mathbf{Q}}(s)]$$



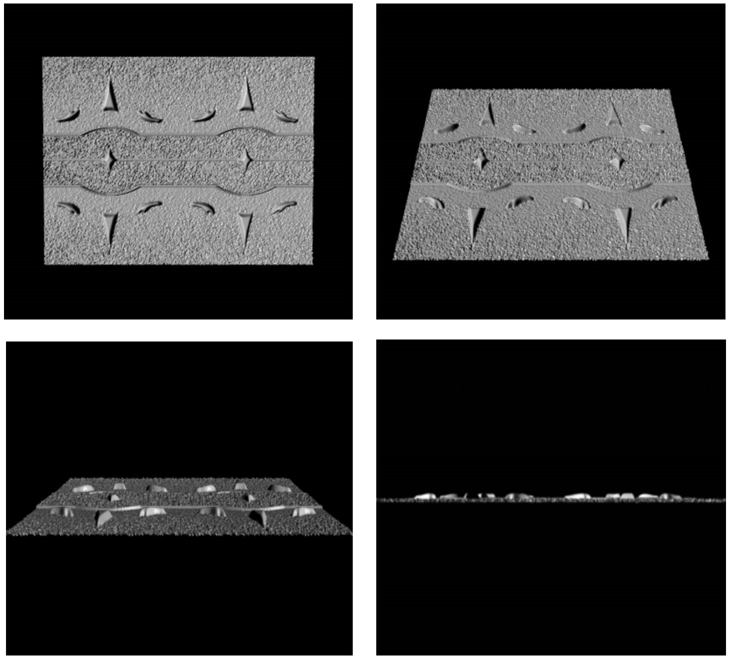

What artifacts in the images would reveal that bump mapping is a fake?

# Displacement vs. bump mapping

Input texture



Rendered as displacement map over a
rectangular surface



# Displacement vs. bump mapping (cont'd)

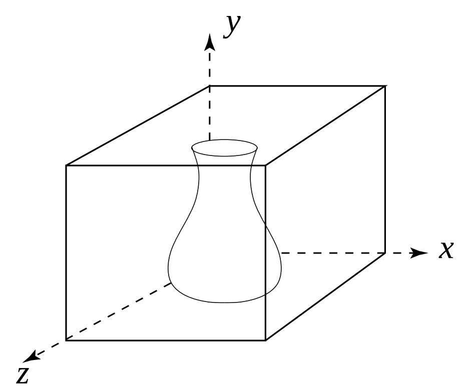
Original rendering

Rendering with bump map wrapped around a cylinder

*Bump map and rendering by Wyvern Aldinger*

## Solid textures

**Q**: What kinds of artifacts might you see from using a marble veneer instead of real marble?




One solution is to use **solid textures**:

- Use model-space coordinates to index into a 3D texture
- Like "carving" the object from the material

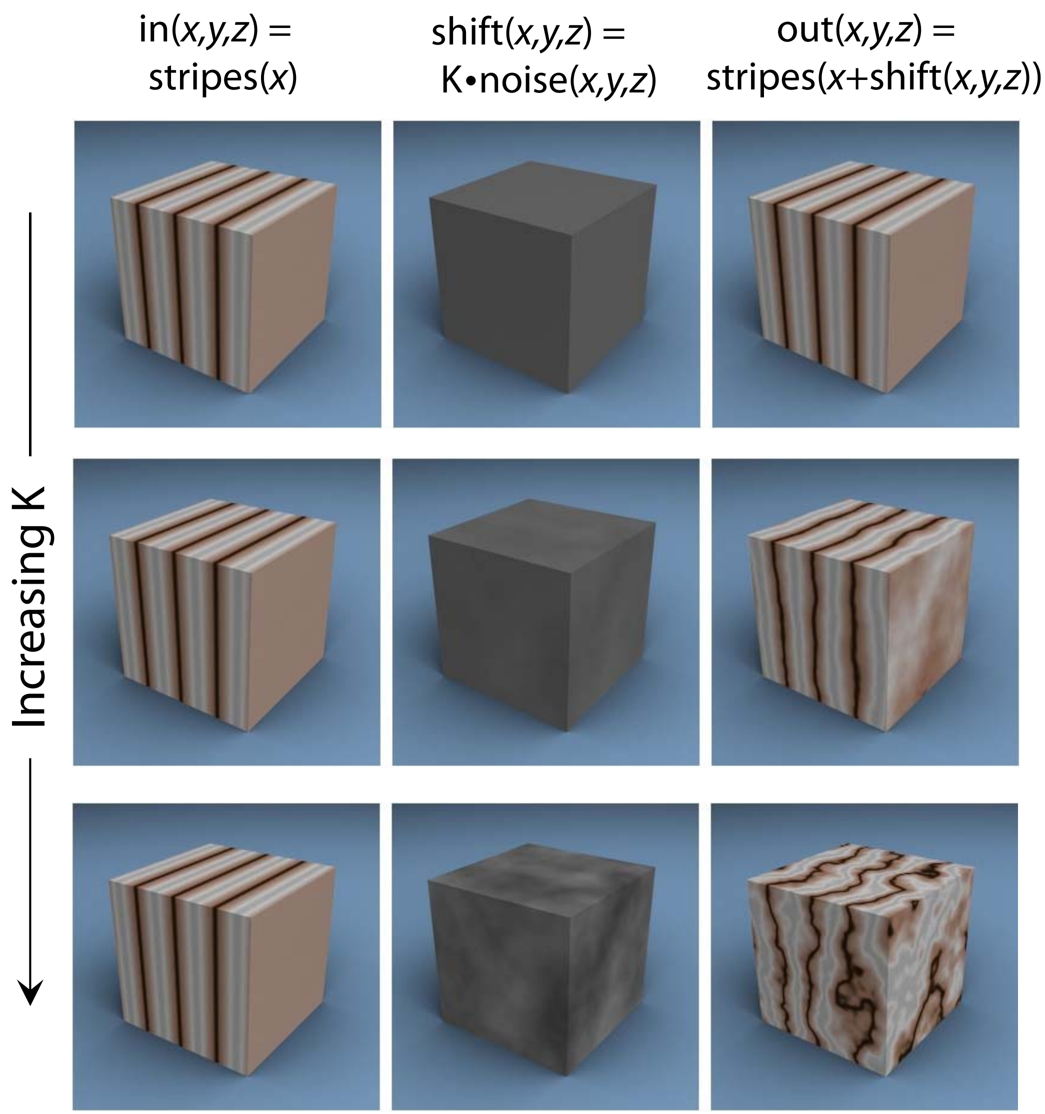
One difficulty of solid texturing is coming up with the textures.

## Solid textures (cont'd)

Here's an example for a vase cut from a solid marble texture:

*Solid marble texture by Ken Perlin, (Foley, IV-21)*

# Solid textures (cont'd)



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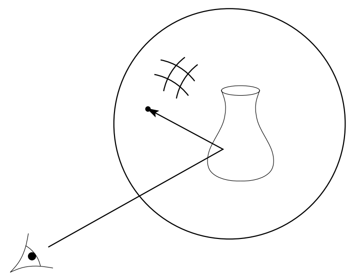
## Environment mapping

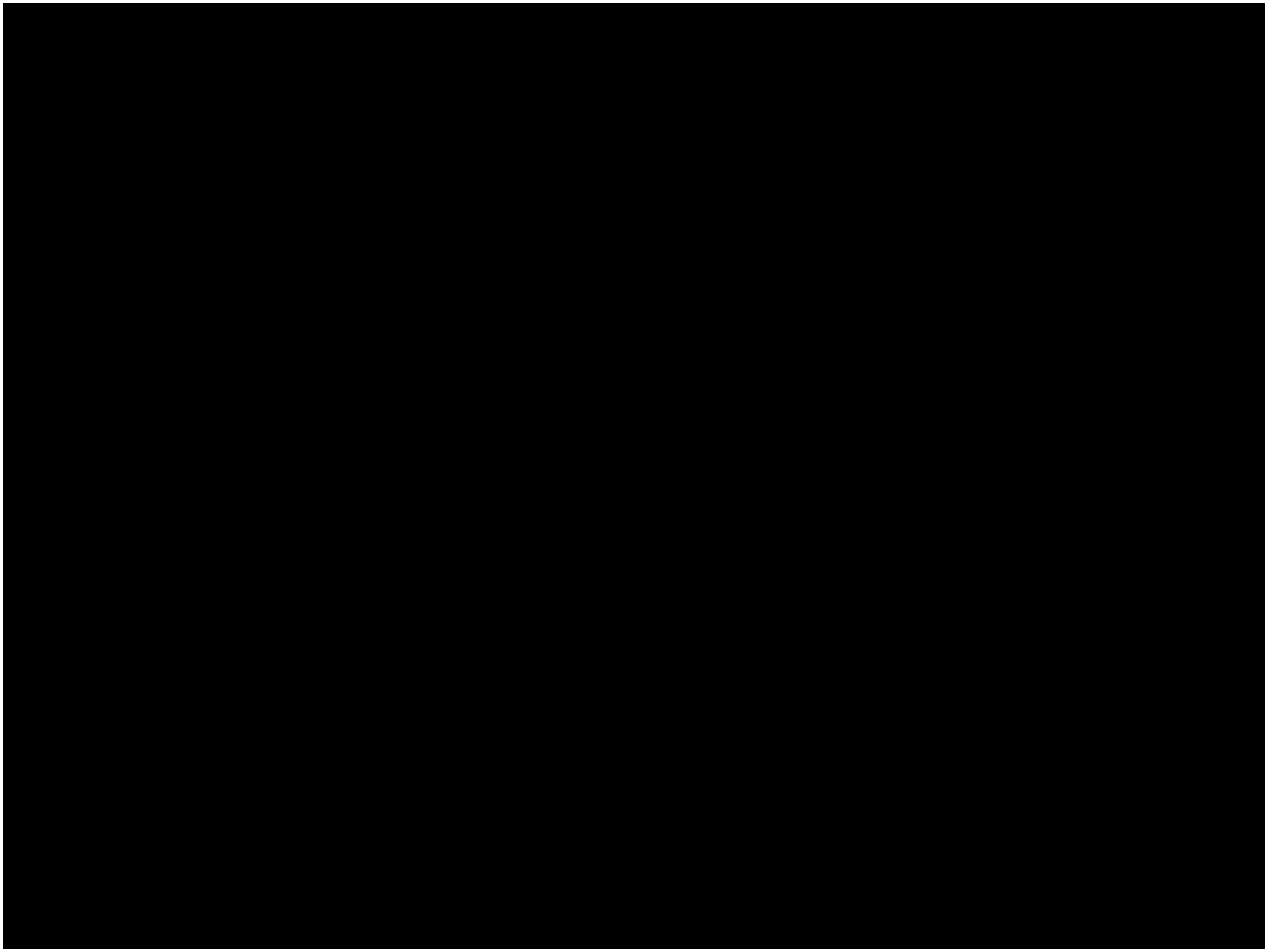


In **environment mapping** (also known as **reflection mapping**), a texture is used to model an object's environment:

- Rays are bounced off objects into environment
- Color of the environment used to determine color of the illumination
- Environment mapping works well when there is just a single object – or in conjunction with ray tracing

This can be readily implemented (without interreflection) using a fragment shader, where the texture is stored in a "cube map" instead of a sphere.

With a ray tracer, the concept is easily extended to handle refraction as well as reflection (and interreflection).



## Summary

What to take home from this lecture:

1. The meaning of the boldfaced terms.

2. Familiarity with the various kinds of texture mapping, including their strengths and limitations.