# Texture Mapping

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## Reading

Required

- Angel, 7.4-7.10

Recommended

- Paul S. Heckbert. Survey of texture mapping. **IEEE Computer Graphics and Applications** 6(11): 56--67, November 1986.

Optional

- Woo, Neider, & Davis, Chapter 9
- James F. Blinn and Martin E. Newell. Texture and reflection in computer generated images. **Communications of the ACM** 19(10): 542--547, October 1976.

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## Texture mapping



*Texture mapping (Woo et al., fig. 9-1)*

Texture mapping allows you to take a simple polygon and give it the appearance of something much more complex.
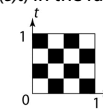
- Due to Ed Catmull, PhD thesis, 1974
- Refined by Blinn & Newell, 1976

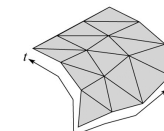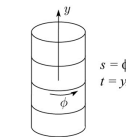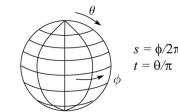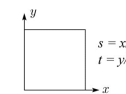A texture can modulate just about any parameter – diffuse color, specular color, specular exponent, …

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## Implementing texture mapping

A texture lives in it own abstract image coordinates paramaterized by $(s,t)$ in the range ([0..1], [0..1]):



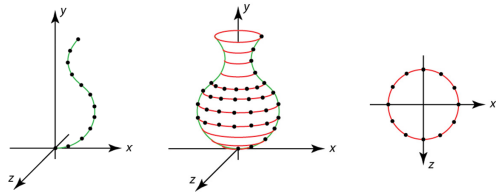It can be wrapped around many different surfaces:



$$s = x/w$$
$$t = y/h$$

$$s = \phi/2\pi$$
$$t = \theta/\pi$$

$$s = \phi/2\pi$$
$$t = y/h$$

With a ray caster, we can do the sphere and cylinder mappings directly (as we will see later). For z-buffers, everything gets converted to a triangle mesh with associated $(s,t)$ coordinates.

Note: if the surface moves/deforms, the texture goes with it.
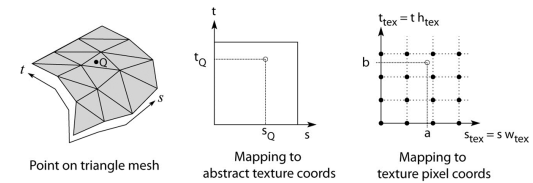
## Texture coordinates on a surface of revolution

## Mapping to texture image coords

The texture is usually stored as an image. Thus, we need to convert from abstract texture coordinate:

$$(s,t) \text{ in the range } ([0..1], [0..1])$$

to texture image coordinates:

$$(s_{tex}, t_{tex}) \text{ in the range } ([0.. w_{tex}], [0.. h_{tex}])$$



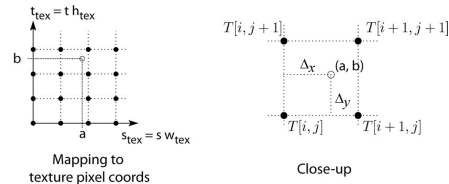Point on triangle mesh    Mapping to abstract texture coords    Mapping to texture pixel coords

**Q**: What do you do when the texture sample you need lands between texture pixels?

## Texture resampling

We need to resample the texture:



Mapping to texture pixel coords      Close-up

Thus, we seek to solve for: $T(a,b) = T(i + \Delta_x, j + \Delta_y)$

A common choice is **bilinear interpolation**:

$$T(i + \Delta_x, j) = \underline{\hspace{1cm}} T[i, j] + \underline{\hspace{1cm}} T[i+1, j]$$

$$T(i + \Delta_x, j+1) = \underline{\hspace{1cm}} T[i, j+1] + \underline{\hspace{1cm}} T[i+1, j+1]$$

$$T(i + \Delta_x, j+\Delta_y) = \underline{\hspace{1cm}} T(i + \Delta_x, j) + \underline{\hspace{1cm}} T(i + \Delta_x, j+1)$$

$$= \underline{\hspace{1cm}} T[i, j] + \underline{\hspace{1cm}} T[i+1, j] +$$

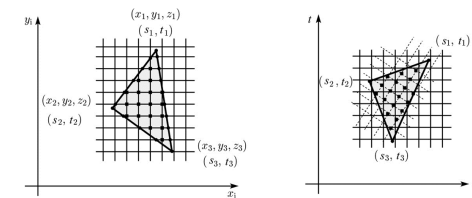$$\underline{\hspace{1cm}} T[i, j+1] + \underline{\hspace{1cm}} T[i+1, j+1]$$

## Texture mapping and the z-buffer

Texture-mapping can also be handled in z-buffer algorithms.

Method:

- Scan conversion is done in screen space, as usual
- Each pixel is colored according to the texture
- Texture coordinates are found by Gouraud-style interpolation
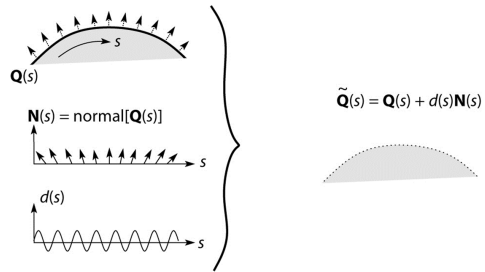


Note: Mapping is more complicated to handle perspective correctly!

## Displacement mapping

Textures can be used for more than just color.

In **displacement mapping**, a texture is used to perturb the surface geometry itself. Here's the idea in 2D:



$$\tilde{\mathbf{Q}}(s) = \mathbf{Q}(s) + d(s)\mathbf{N}(s)$$

- These displacements "animate" with the surface
- In 3D, you would of course have (s,t) parameters instead of just s.
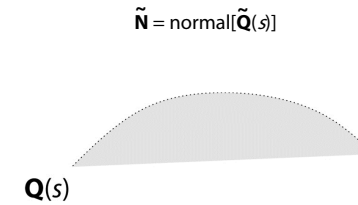
Suppose **Q** is a simple surface, like a cube. Will it take more work to render the modified surface $\tilde{\mathbf{Q}}$?

## Bump mapping

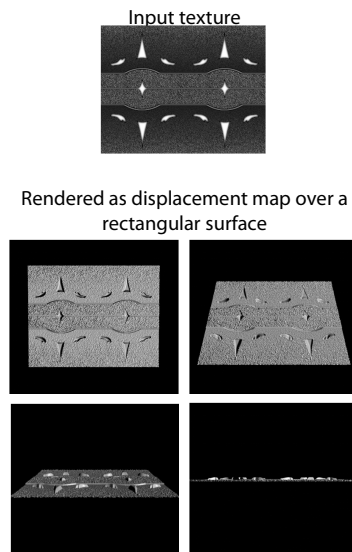In **bump mapping**, a texture is used to perturb the normal:

- Use the original, simpler geometry, **Q**(*s*), for hidden surfaces
- Use the normal from the displacement map for shading:

$$\tilde{\mathbf{N}} = \text{normal}[\tilde{\mathbf{Q}}(s)]$$



**Q**(*s*)

What artifacts in the images would reveal that bump mapping is a fake?

## Displacement vs. bump mapping

Input texture



Rendered as displacement map over a rectangular surface

## Displacement vs. bump mapping (cont'd)
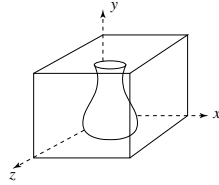


Original rendering     Rendering with bump map wrapped around a cylinder

*Bump map and rendering by Wyvern Aldinger*

## Solid textures

**Q**: What kinds of artifacts might you see from using a marble veneer instead of real marble?



One solution is to use **solid textures**:

- Use model-space coordinates to index into a 3D texture
- Like "carving" the object from the material

One difficulty of solid texturing is coming up with the textures.

## Solid textures (cont'd)

Here's an example for a vase cut from a solid marble texture:



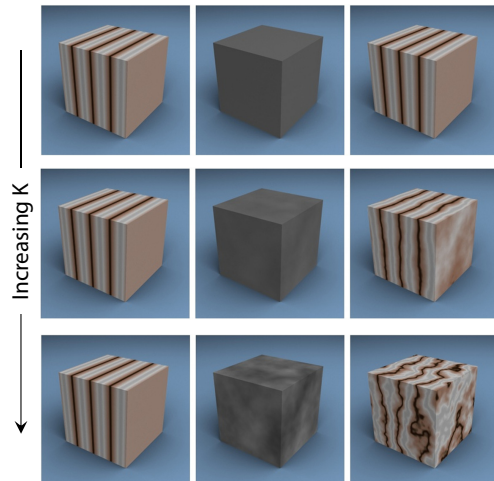*Solid marble texture by Ken Perlin, (Foley, IV-21)*

## Solid textures (cont'd)

| $in(x,y,z) =$ $stripes(x)$ | $shift(x,y,z) =$ $K \cdot noise(x,y,z)$ | $out(x,y,z) =$ $stripes(x+shift(x,y,z))$ |
|---|---|---|

Increasing K

## Environment mapping



In **environment mapping** (also known as **reflection mapping**), a texture is used to model an object's environment:

- Rays are bounced off objects into environment
- Color of the environment used to determine color of the illumination
- Environment mapping works well when there is just a single object – or in conjunction with ray tracing

This can be readily implemented (without interreflection) using a fragment shader, where the texture is stored in a "cube map" instead of a sphere.

With a ray tracer, the concept is easily extended to handle refraction as well as reflection (and interreflection).

**Summary**

What to take home from this lecture:

1. The meaning of the boldfaced terms.

2. Familiarity with the various kinds of texture mapping, including their strengths and limitations.

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