

# Anti-aliasing and Acceleration

CSE 457, Autumn 2003  
Graphics

<http://www.cs.washington.edu/education/courses/457/03au/>

# Readings and References

## Readings

- Sections 12.5.3 – 12.5.4, 14.7, *3D Computer Graphics*, Watt

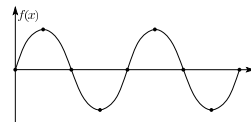
## Other References

- A. Glassner. *An Introduction to Ray Tracing*

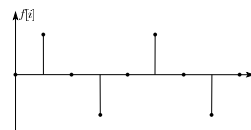
# Aliasing

- Ray tracing is a form of sampling and can suffer from annoying visual artifacts...
- Consider a continuous function  $f(x)$ . Now sample it at intervals  $\Delta$  to give  $f[i] = \text{quantize}[f(i\Delta)]$ .
  - » The question is, how well does  $f[i]$  approximate  $f(x)$ ?

- Consider sampling a sinusoid:



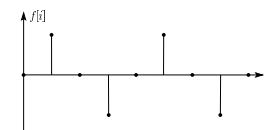
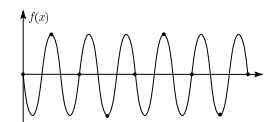
- In this case, the sinusoid is reasonably well approximated by the samples.

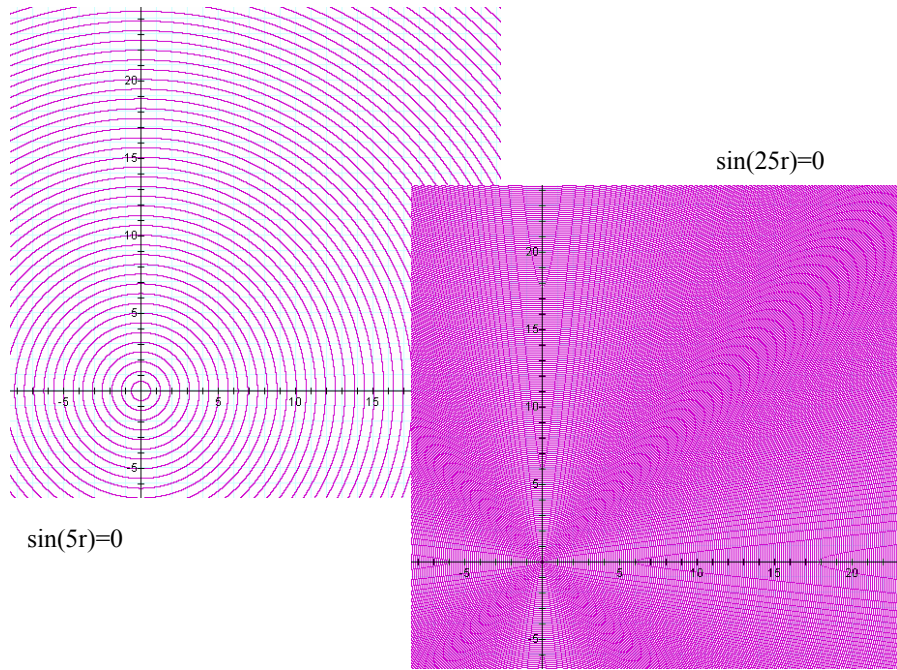


# Aliasing (con't)

- Now consider sampling a higher frequency sinusoid

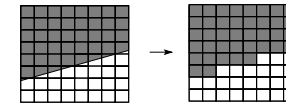
- We get the exact same samples, so we seem to be approximating the first lower frequency sinusoid again.
- We say that, after sampling, the higher frequency sinusoid has taken on a new “alias”, i.e., changed its identity to be a lower frequency sinusoid.



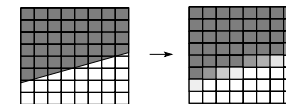


## Jaggies

- One of the most common rendering artifacts is the “jaggies”. Consider rendering a white polygon against a black background:

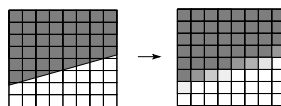


- We would instead like to get a smoother transition:



## Anti-aliasing

- **Q:** How do we avoid artifacts caused by sampling?
- Sampling:
- Pre-filtering:
- Combination:
- Example - polygon:



Without antialiasing



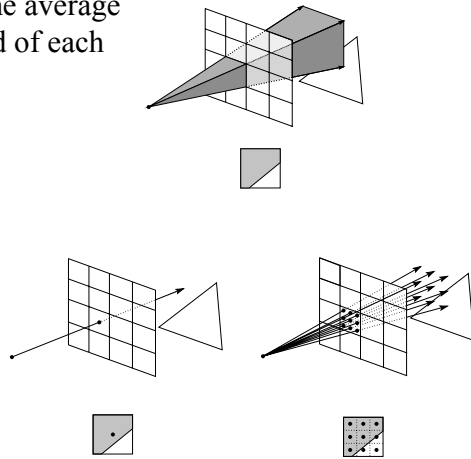
With antialiasing



Magnification →

## Antialiasing in a ray tracer

- We would like to compute the average intensity in the neighborhood of each pixel.
- When casting one ray per pixel, we are likely to have aliasing artifacts.
- To improve matters, we can cast more than one ray per pixel and average the result.
- A.k.a., **super-sampling and averaging down**.

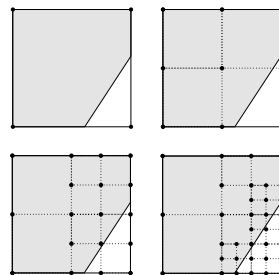


## Speeding it up

- Vanilla ray tracing is really slow!
- Consider:  $m \times m$  pixels,  $k \times k$  supersampling, and  $n$  primitives, average ray path length of  $d$ , with 1 or 2 rays cast recursively per intersection.
- Complexity =
- For  $m=1,000$ ,  $k=5$ ,  $n=100,000$ ,  $d=8$ ...very expensive!!
- In practice, some acceleration technique is almost always used.
- We've already looked at reducing  $d$  with adaptive ray termination. Now we look at reducing the effect of the  $k$  and  $n$  terms.

## Antialiasing by adaptive sampling

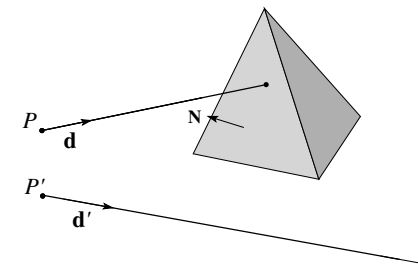
- Casting many rays per pixel can be unnecessarily costly.
- For example, if there are no rapid changes in intensity at the pixel, maybe only a few samples are needed.
- Solution: **adaptive sampling**.



- **Q:** When do we decide to cast more rays in a particular area?

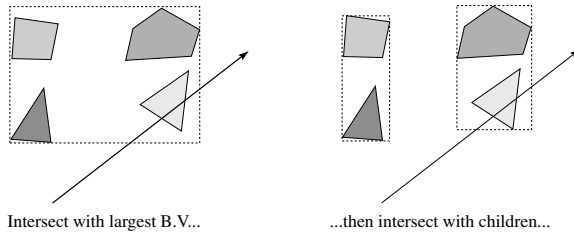
## Faster ray-polyhedron intersection

- Let's say you were intersecting a ray with a polyhedron:

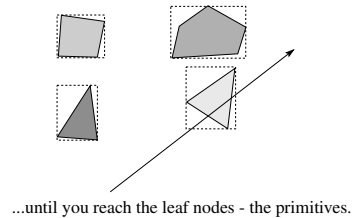


- Straightforward method
  - » intersect the ray with each triangle
  - » return the intersection with the smallest  $t$ -value.
- **Q:** How might you speed this up?

## Hierarchical bounding volumes

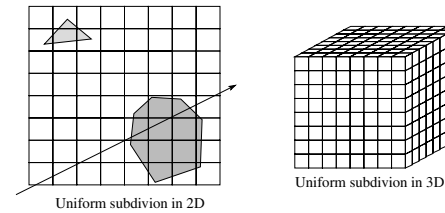


Balanced trees with tight bounding volumes.



## Uniform spatial subdivision

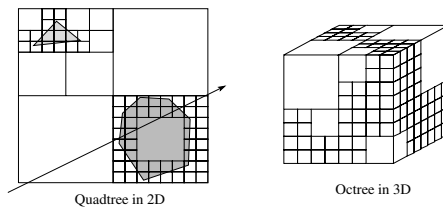
- Another approach is **uniform spatial subdivision**.



- Idea:
  - » Partition space into cells (voxels)
  - » Associate each primitive with the cells it overlaps
  - » Trace ray through voxel array *using fast incremental arithmetic* to step from cell to cell

## Non-uniform spatial subdivision

- Still another approach is **non-uniform spatial subdivision**.



- Other variants include k-d trees and BSP trees.
- Various combinations of these ray intersections techniques are also possible. See Glassner for more.

## Summary

- What to take home from this lecture:
  - » The meanings of all the boldfaced terms.
  - » An intuition for what aliasing is.
  - » How to reduce aliasing artifacts in a ray tracer
  - » An intuition for how ray tracers can be accelerated.