

Hierarchical Modeling

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Reading

Required

- ♦ Angel, sections 8.1 - 8.6

Optional

- ♦ *OpenGL Programming Guide*, chapter 3

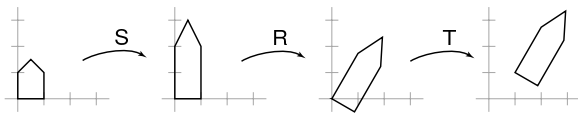
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Symbols and instances

Most graphics APIs support a few geometric primitives:

- ♦ spheres
- ♦ cubes
- ♦ cylinders

These symbols are **instanced** using an **instance transformation**.



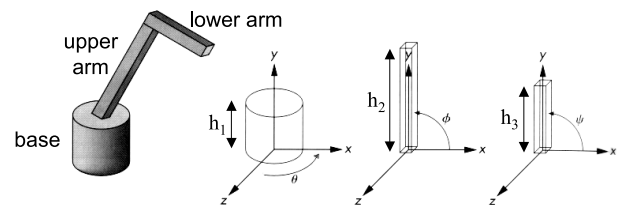
Q: What is the matrix for the instance transformation above?

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3D Example: A robot arm

Consider this robot arm with 3 degrees of freedom:

- ♦ Base rotates about its vertical axis by θ
- ♦ Upper arm rotates in its xy -plane by ϕ
- ♦ Lower arm rotates in its xy -plane by ψ



Q: What matrix do we use to transform the base?

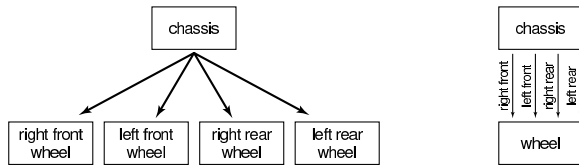
Q: What matrix for the upper arm?

Q: What matrix for the lower arm?

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Hierarchical modeling

Hierarchical models can be composed of instances using trees or DAGs:

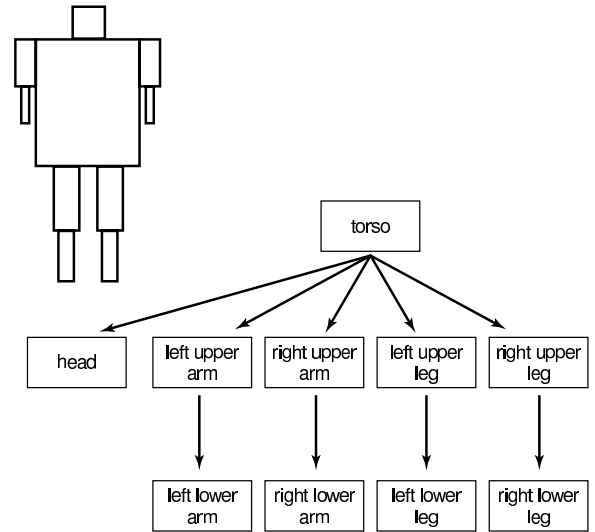


- ♦ edges contain geometric transformations
- ♦ nodes contain geometry (and possibly drawing attributes)

How might we draw the tree for the robot arm?

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A complex example: human figure



Q: What's the most sensible way to traverse this tree?

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Robot arm implementation

The robot arm can be displayed by keeping a global matrix and computing it at each step:

```
Matrix M_model;

main()
{
    . . .
    robot_arm();
    . . .
}

robot_arm()
{
    M_model = R_y(theta);
    base();
    M_model = R_y(theta)*T(0,h1,0)*R_z(phi);
    upper_arm();
    M_model = R_y(theta)*T(0,h1,0)*R_z(phi)
                *T(0,h2,0)*R_z(psi);
    lower_arm();
}
```

Do the matrix computations seem wasteful?

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Robot arm implementation, better

Instead of recalculating the global matrix each time, we can just update it *in place*:

```
Matrix M_model;

main()
{
    . . .
    M_model = Identity();
    robot_arm();
    . . .
}

robot_arm()
{
    M_model *= R_y(theta);
    base();
    M_model *= T(0,h1,0)*R_z(phi);
    upper_arm();
    M_model *= T(0,h2,0)*R_z(psi);
    lower_arm();
}
```

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Robot arm implementation, OpenGL

OpenGL maintains a global state matrix called the **model-view matrix**.

```
main()
{
    . . .
    glMatrixMode( GL_MODELVIEW );
    glLoadIdentity();
    robot_arm();
    . . .
}

robot_arm()
{
    glRotatef( theta, 0.0, 1.0, 0.0 );
    base();
    glTranslatef( 0.0, h1, 0.0 );
    glRotatef( phi, 0.0, 0.0, 1.0 );
    lower_arm();
    glTranslatef( 0.0, h2, 0.0 );
    glRotatef( psi, 0.0, 0.0, 1.0 );
    upper_arm();
}
```

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Human figure implementation

We can also design code for drawing the human figure, with a slight modification due to the branches in the tree:

```
figure()
{
    torso();
    M_save = M_model;
    M_model *= T(. . .)*R(. . .);
    head();
    M_model = M_save;
    M_model *= T(. . .)*R(. . .);
    left_upper_arm();
    M_model *= T(. . .)*R(. . .);
    left_lower_arm();
    M_model = M_save;
    .
    .
    .
}
```

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Human figure with hand

What if we add a hand?

```
figure()
{
    torso();
    M_save = M_model;
    M_model *= T(. . .)*R(. . .);
    head();
    M_model = M_save;
    M_model *= T(. . .)*R(. . .);
    left_upper_arm();
    M_model *= T(. . .)*R(. . .);
    left_lower_arm();
    M_model *= T(. . .)*R(. . .);
    left_hand();
    M_save2 = M_model;
    M_model *= T(. . .)*R(. . .);
    left_thumb();
    M_model = M_save2;
    M_model *= T(. . .)*R(. . .);
    left_forefinger();
    M_model = M_save2;
    . . .
}
```

Is there a better way to keep track of piles of matrices that need to be saved, modified, and restored?

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Human figure implementation, better

```

figure()
{
    torso();
    push(M_model);
        M_model *= T(. . .)*R(. . .);
        head();
    M_model = pop(M_model);
    push(M_model);
        M_model *= T(. . .)*R(. . .);
        left_upper_arm();
        M_model *= T(. . .)*R(. . .);
        left_lower_arm();
        M_model *= T(. . .)*R(. . .);
        left_hand();
        push(M_model);
            M_model *= T(. . .)*R(. . .);
            left_thumb();
        M_model = pop(M_model);
        push(M_model);
            M_model *= T(. . .)*R(. . .);
            left_forefinger();
        M_model = pop(M_model);
        push(M_model);
        . . .
}

```

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Human figure implementation, OpenGL

```

figure()
{
    torso();
    glPushMatrix();
        glTranslate( ... );
        glRotate( ... );
        head();
    glPopMatrix();
    glPushMatrix();
        glTranslate( ... );
        glRotate( ... );
        left_upper_arm();
        glTranslate( ... );
        glRotate( ... );
        left_lower_arm();
        glTranslate( ... );
        glRotate( ... );
        left_hand();
        glPushMatrix();
            glTranslate( ... );
            glRotate( ... );
            left_thumb();
        glPopMatrix();
        glPushMatrix();
            glTranslate( ... );
            glRotate( ... );
            left_forefinger();
        glPopMatrix();
        . . .
}

```

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The Matrix Stack

Trace of OpenGL calls

```

glLoadIdentity();
glPushMatrix();
glTranslatef(Tx,Ty,0);
glRotatef(u,0,0,1);
glTranslatef(-px,-py,0);
glPushMatrix();
glTranslatef(qx,qy,0);
glRotatef(v,0,0,1);
glTranslatef(-rx,-ry,0);
Draw(A);
glPopMatrix();
Draw(B);

```



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Animation

The above examples are called **articulated models**:

- ◆ rigid parts
- ◆ connected by joints

They can be animated by specifying the joint angles (or other display parameters) as functions of time.

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Kinematics and dynamics

Definitions:

- ♦ **Kinematics:** how the positions of the parts vary as a function of the joint angles.
- ♦ **Dynamics:** how the positions of the parts vary as a function of applied forces.

Questions:

Q: What do the terms **inverse kinematics** and **inverse dynamics** mean?

Q: Why are these problems more difficult?

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Key-frame animation

One way to get around these problems is to use **key-frame animation**.

- ♦ Each joint specified at various **key frames** (not necessarily the same as other joints)
- ♦ System does interpolation or **in-betweening**

Doing this well requires:

- ♦ A way of smoothly interpolating key frames: **splines**
- ♦ A good interactive system
- ♦ A lot of skill on the part of the animator

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Scene graphs

The idea of hierarchical modeling can be extended to an entire scene, encompassing:

- ♦ many different objects
- ♦ lights
- ♦ camera position

This is called a **scene tree** or **scene graph**.

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The peculiarity of OpenGL ordering

Let's revisit the very first simple example in this lecture.

To draw the transformed house, we would write OpenGL code like:

```
glMatrixMode( GL_MODELVIEW );
glLoadIdentity();
glTranslatef( ... );
glRotatef( ... );
glScalef( ... );
house();
```

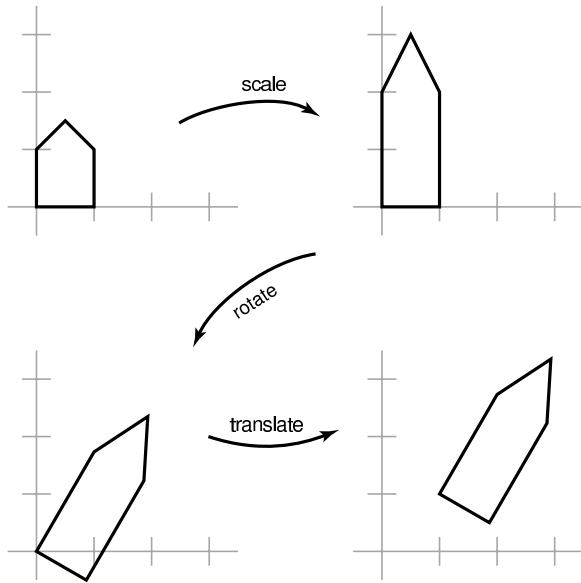
Is there something a little funny about the order of operations?

Why was OpenGL designed this way?

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Global, fixed coordinate system

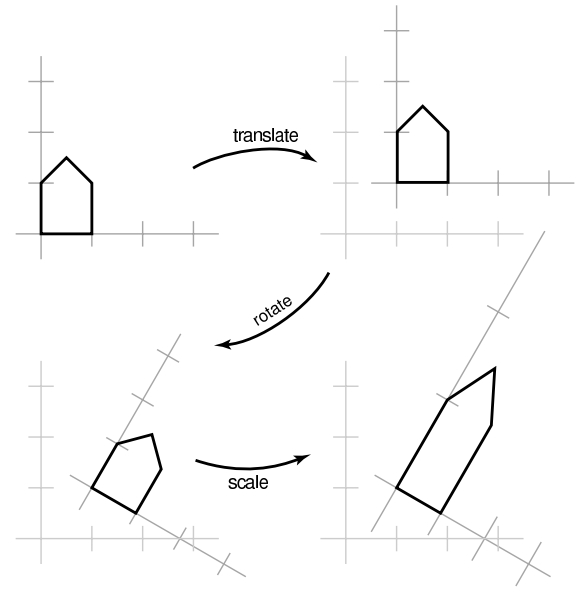
OpenGL's transforms, logical as they may be, still *seem backwards*. They are, if you think of them as transforming the object in a **fixed** coordinate system.



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Local, changing coordinate system

Another way to view transformations is as affecting a *local coordinate system* that the primitive is drawn in. Now the transforms appear in the "right" order.



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Summary

Here's what you should take home from this lecture:

- ♦ All the **boldfaced terms**.
- ♦ How primitives can be instanced and composed to create hierarchical models using geometric transforms.
- ♦ How the notion of a model tree or DAG can be extended to entire scenes.
- ♦ How keyframe animation works.
- ♦ How transforms can be thought of as affecting either the geometry, or the coordinate system which it is drawn in.

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