### Graphs: Traversals and Shortest Path Algorithms (Chapter 9)

CSE 373 Data Structures and Algorithms

5/21/10

# Today's Outline

- Announcements - Homework #6/7 coming soon.
- Graphs

   Topological Sort
   Shortest Paths Algorithms

5/21/10

1

## Graph Traversals

#### • Breadth-first search

- explore all adjacent nodes, then for each of those nodes explore all adjacent nodes
- Depth-first search
- explore first child node, then its first child node, etc. until goal node is found or node has no children. Then backtrack, repeat with sibling.
- Both:
  - Work for arbitrary (directed or undirected) graphs
- Must mark visited vertices so you do not go into an infinite loop!
  Either can be used to determine connectivity:
  - Is there a path between two given vertices?
  - Is the graph (weakly) connected?
- Which one:
  - Uses a queue?
  - Uses a stack?
  - Always finds the shortest path (for unweighted graphs)?

5/21/10



2





1

### Variations of SSSP

- Weighted vs. unweighted
- Directed vs undirected
- Cyclic vs. acyclic
- Positive weights only vs. negative weights allowed
- Shortest path vs. longest path

- ...

5/21/10

## Applications

8

- Network routing
- Driving directions
- Cheap flight tickets
- Critical paths in project management (see textbook)

- ...

5/21/10

7

SSSP: Unweighted Version Ideas?







# Dijkstra's Algorithm for Single Source Shortest Path

- Similar to breadth-first search, but uses a heap instead of a queue:
  - Always select (expand) the vertex that has a lowest-cost path to the start vertex

13

• Correctly handles the case where the lowest-cost (shortest) path to a vertex is not the one with fewest edges

5/21/10























