

Facts about Binary Min Heaps Observations:

Observations:

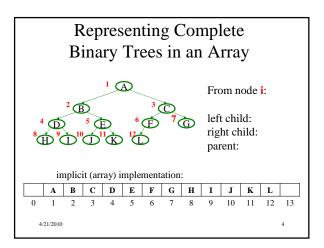
- finding a child/parent index is a multiply/divide by two
- operations jump widely through the heap
- each percolate step looks at only two new nodes
- inserts are at least as common as deleteMins

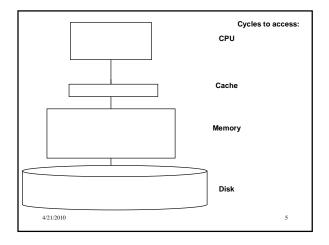
Realities:

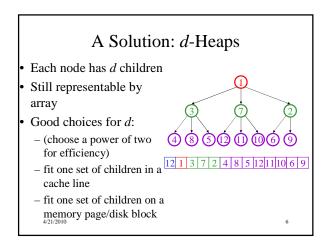
• division/multiplication by *powers* of two are equally fast

3

- looking at $\underline{only} \underline{two}$ new pieces of data: bad for cache!
- with huge data sets, disk accesses dominate 4/21/2010



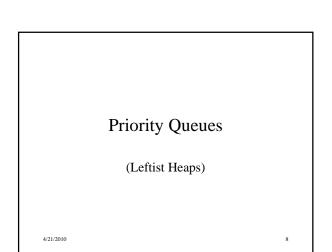


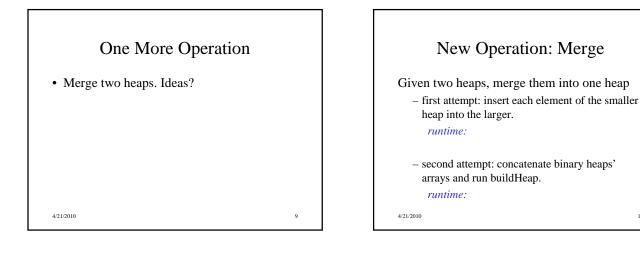


Operations on d-Heap

- Insert : runtime =
- deleteMin: runtime =

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11

7

Leftist Heaps

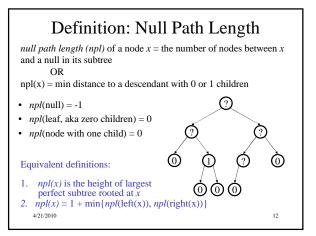
Idea:

Focus all heap maintenance work in one small part of the heap

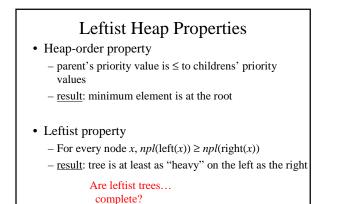
Leftist heaps:

- 1. Most nodes are on the left
- 2. All the merging work is done on the right

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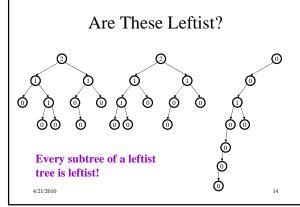
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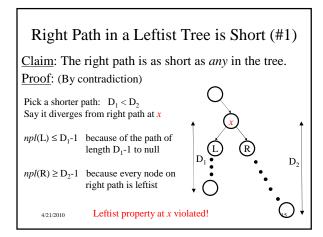


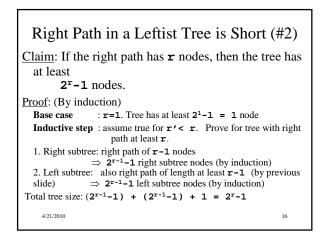
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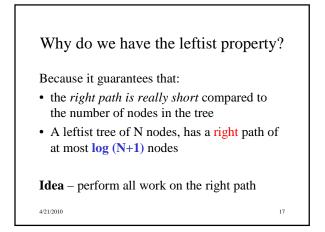
balanced?

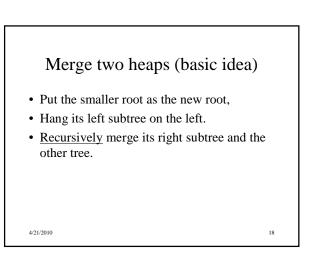
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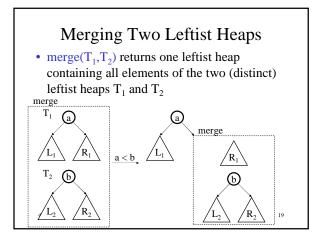


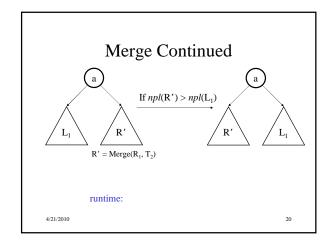


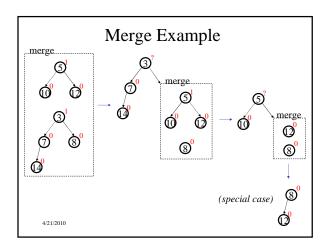


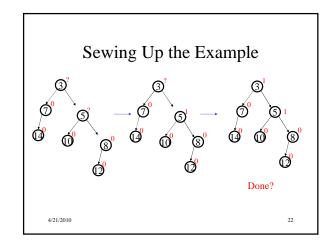


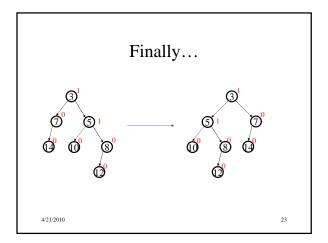


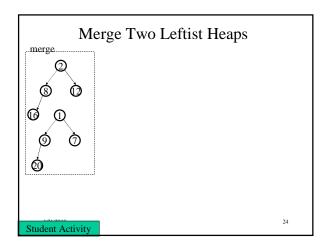


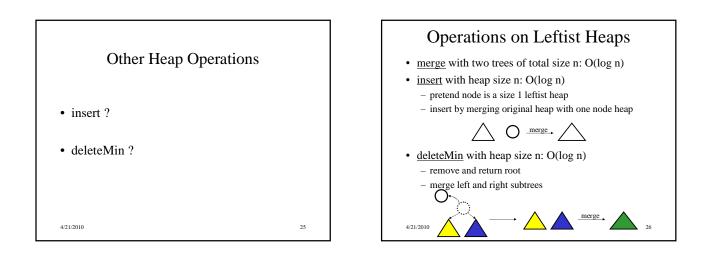


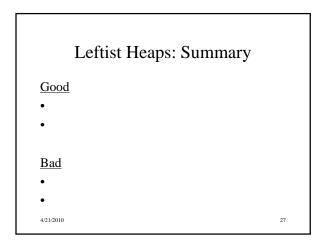


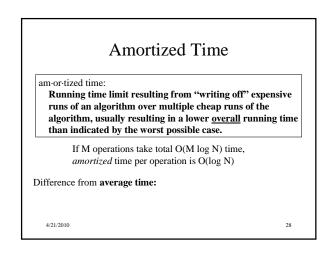


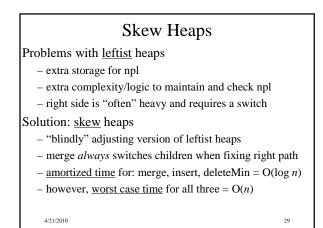


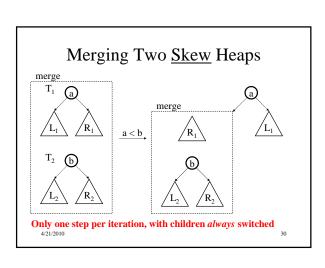


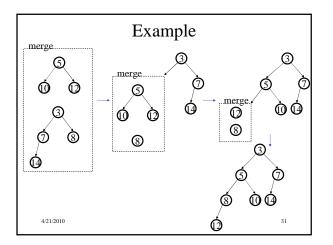


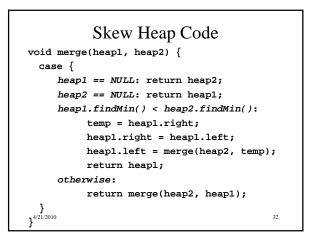












Runtime Analysis: Worst-case and Amortized • No worst case guarantee on right path length! • All operations rely on merge ⇒ worst case complexity of all ops = • Amortized Analysis (Chapter 11) • Result: *M* merges take time *M* log *n* ⇒ amortized complexity of all ops =

Comparing Priority Queues	
Binary Heaps	Leftist Heaps
• d-Heaps	Skew Heaps
-	
4/21/2010 Student Activity	34