Priority Queues: Binary Min Heaps

CSE 373
Data Structures and Algorithms

Today's Outline

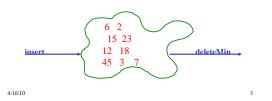
- Announcements
 - Midterm #1, Friday April 23.
 - Assignment #3 coming soon.
- · Today's Topics:
 - Dictionary
 - Balanced Binary Search Trees (AVL Trees)
 - Priority Queues
 - Binary Min Heap

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Priority Queue ADT

- Checkout line at the supermarket ???
- Printer queues ???
- operations: insert, deleteMin



Priority Queue ADT

- 1. PQueue data: collection of data with priority
- 2. PQueue operations
 - insert

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deleteMin

(also: create, destroy, is_empty)

3. PQueue property: for two elements in the queue, *x* and *y*, if *x* has a **lower** priority value than *y*, *x* will be deleted before *y*

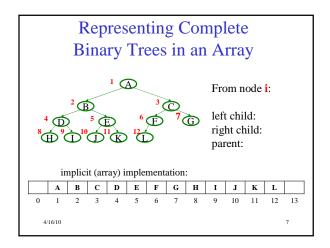
Applications of the Priority Q

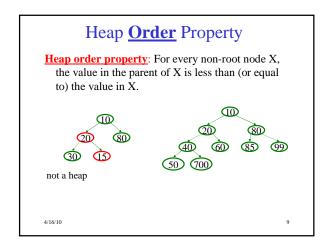
- Select print jobs in order of decreasing length
- Forward packets on network routers in order of urgency
- Select most frequent symbols for compression
- Sort numbers, picking minimum first
- · Anything greedy

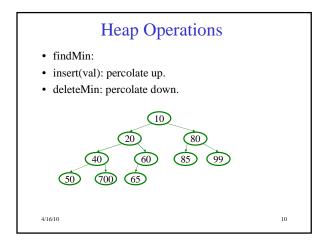
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Implementations of Priority Queue AD7		
	insert	deleteMin
Unsorted list (Array)		
Unsorted list (Linked-List)		
Sorted list (Array)		
Sorted list (Linked-List)		
Binary Search Tree (BST)		

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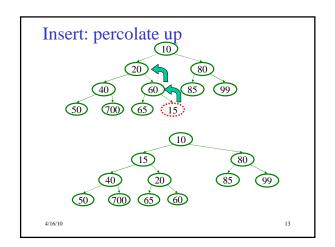






Heap – Insert(val) Basic Idea: 1. Put val at "next" leaf position 2. Repeatedly exchange node with its parent if needed

Insert pseudo Code (optimized) void insert(Object o) { int percolateUp(int hole, Object val) { while (hole > 1 && assert(!isFull()); size++; val < Heap[hole/2]) Heap[hole] = Heap[hole/2];</pre> newPos = percolateUp(size,o); hole /= 2; Heap[newPos] = o; return hole; } runtime: (Java code in book) 4/16/10 12



Heap – Deletemin

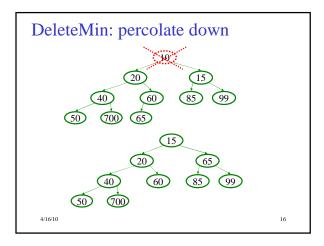
Basic Idea:

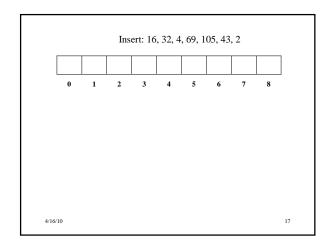
- 1. Remove root (that is always the min!)
- 2. Put "last" leaf node at root
- 3. Find smallest child of node
- 4. Swap node with its smallest child if needed.
- 5. Repeat steps 3 & 4 until no swaps needed.

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```
DeleteMin pseudo Code (Optimized)
                               int percolateDown(int hole,
Object deleteMin() {
                               while (2*hole <= size) {
  assert(!isEmpty());
                                   left = 2*hole;
right = left + 1;
if (right ≤ size &&
   returnVal = Heap[1];
  size--;
   newPos =
                                        Heap[right] < Heap[left])</pre>
                                      target = right;
     percolateDown(1,
                                   else
  target = left;
         Heap[size+1]);
  Heap[newPos] =
                                   if (Heap[target] < val) {
  Heap[hole] = Heap[target];</pre>
     Heap[size + 1];
   return returnVal;
                                      hole = target;
runtime:
                                      break;
                                 return hole;
        (Java code in book)
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                                                                   15
```





Other Priority Queue Operations

decreaseKey

- given a pointer to an object in the queue, reduce its priority value

Solution: change priority and _____

increaseKey

- given a pointer to an object in the queue, increase its priority value

Solution: change priority and _____

Why do we need a pointer? Why not simply data value?

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Other Heap Operations

decreaseKey(objPtr, amount): raise the priority of a object,
 percolate up

increaseKey(objPtr, amount): lower the priority of a object, percolate down

remove(objPtr): remove a object, move to top, them delete.
1) decreaseKey(objPtr, ∞)

2) deleteMin()

Worst case Running time for all of these:

FindMax?

ExpandHeap - when heap fills, copy into new space.

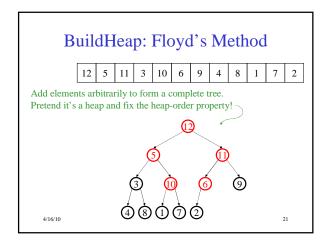
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Binary Min Heaps (summary)

- **insert**: percolate up. $\Theta(\log N)$ time.
- deleteMin: percolate down. $\Theta(\log N)$ time.
- Build Heap?

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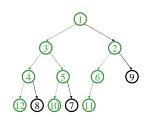
Buildheap pseudocode

```
private void buildHeap() {
  for ( int i = currentSize/2; i > 0; i-- )
     percolateDown( i );
}
```

runtime:

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Finally...



runtime:

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Facts about Binary Min Heaps

Observations:

- finding a child/parent index is a multiply/divide by two
- operations jump widely through the heap
- · each percolate step looks at only two new nodes
- inserts are at least as common as deleteMins

Realities:

- division/multiplication by powers of two are equally fast
- looking at only two new pieces of data: bad for cache!
- with huge data sets, disk accesses dominate

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