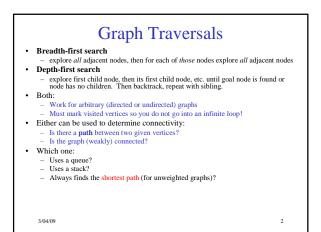
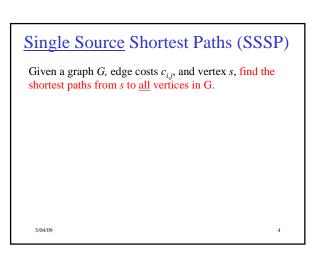
Graphs: Traversals and Shortest Path Algorithms

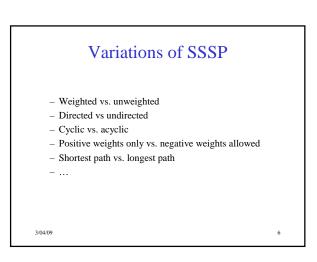
CSE 373 Data Structures and Algorithms

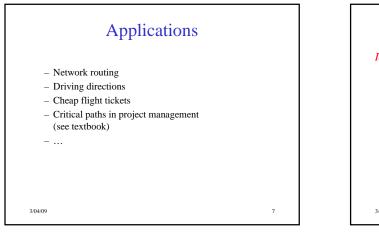


The Shortest Path ProblemGiven a graph G, edge costs $c_{i,j}$, and vertices s and t in
G, find the shortest path from s to t.For a path $p = v_0 v_1 v_2 \dots v_k$
 - unweighted length of path p = k (a.k.a. length)
 - weighted length of path $p = \sum_{i=0.k-1} c_{i,i+1}$ (a.k.a cost)Path length equals path cost when ?

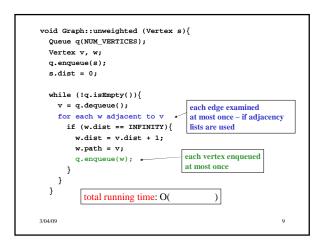


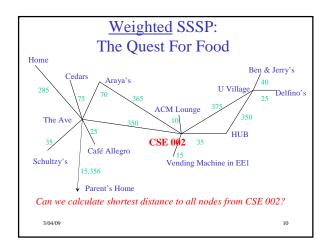
All Pairs Shortest Paths (APSP) Given a graph *G* and edge costs $c_{i,j}$, find the shortest paths between <u>all pairs</u> of vertices in *G*.

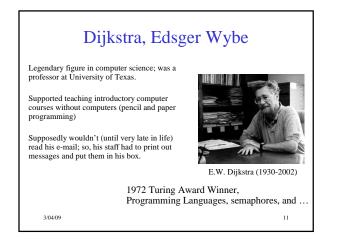


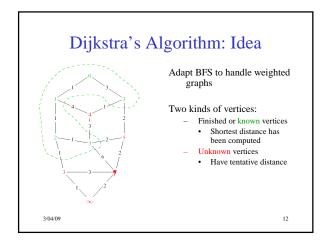


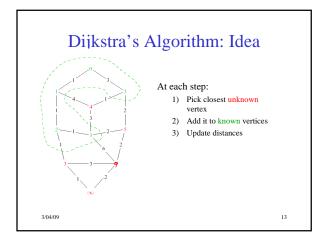


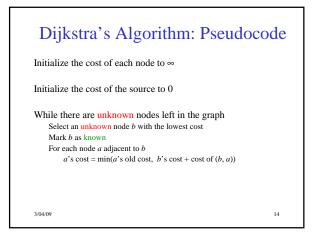


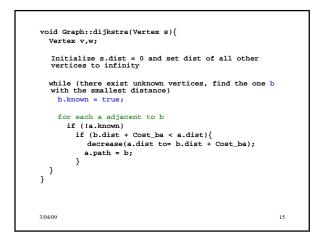


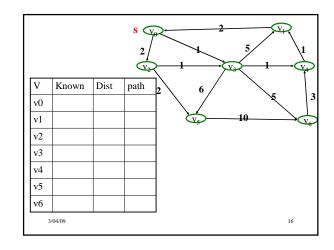


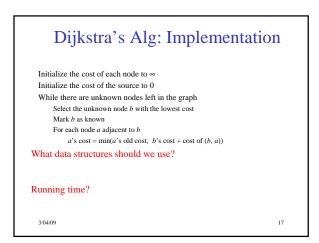


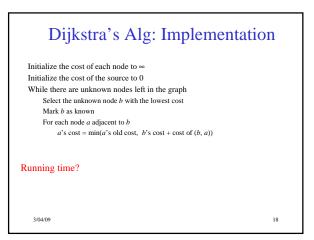












Dijkstra's Algorithm: a Greedy Algorithm

Greedy algorithms always make choices that

- currently seem the best
- Short-sighted no consideration of long-term or global issues
- Locally optimal does not always mean globally optimal!!

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Dijkstra's Algorithm: Summary

- Classic algorithm for solving SSSP in weighted graphs without negative weights
- A greedy algorithm (irrevocably makes decisions without considering future consequences)
- Intuition for correctness:
 - shortest path from source vertex to itself is 0
 - cost of going to adjacent nodes is at most edge weights
 - cheapest of these must be shortest path to that node
 update paths for new node and continue picking cheapest path

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