Priority Queues: Binary Min Heaps

CSE 373

Data Structures and Algorithms

Today's Outline

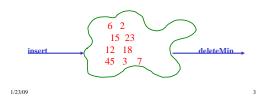
- Announcements
 - Assignment #2 due NOW.
 - Midterm #1: Friday, Jan 30th
 - Assignment #3 due Thurs, Feb5th.
- · Today's Topics:
 - Dictionary
 - Balanced Binary Search Trees (AVL Trees)
 - Priority Queues
 - Binary Min Heap

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Priority Queue ADT

- Checkout line at the supermarket ???
- Printer queues ???
- operations: insert, deleteMin



Priority Queue ADT

- 1. PQueue data: collection of data with priority
- 2. PQueue operations
 - insert

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deleteMin

(also: create, destroy, is_empty)

3. PQueue property: for two elements in the queue, *x* and *y*, if *x* has a **lower** priority value than *y*, *x* will be deleted before *y*

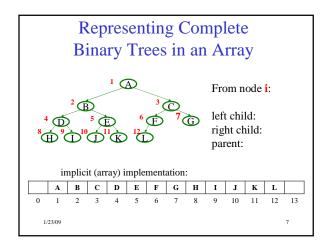
Applications of the Priority Q

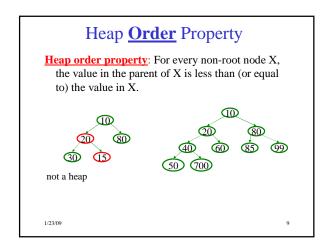
- Select print jobs in order of decreasing length
- Forward packets on network routers in order of urgency
- Select most frequent symbols for compression
- Sort numbers, picking minimum first
- · Anything greedy

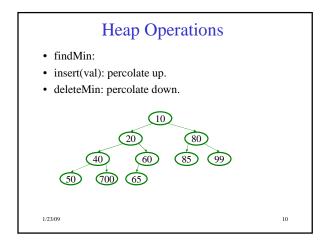
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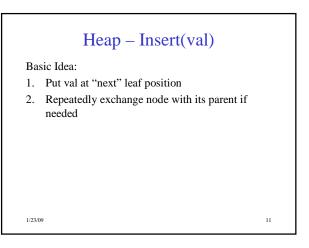
Implementations of	Priority (Queue AD'
	insert	deleteMin
Unsorted list (Array)		
Unsorted list (Linked-List)		
Sorted list (Array)		
Sorted list (Linked-List)		
Binary Search Tree (BST)		

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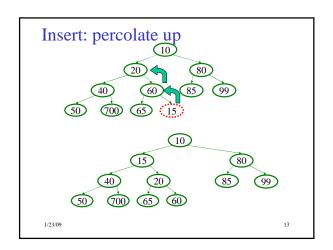








Insert pseudo Code (optimized) void insert(Object o) { int percolateUp(int hole, Object val) { while (hole > 1 && assert(!isFull()); size++; val < Heap[hole/2]) Heap[hole] = Heap[hole/2];</pre> newPos = percolateUp(size,o); hole /= 2; Heap[newPos] = o; return hole; runtime: (Java code in book) 1/23/09 12



Heap – Deletemin

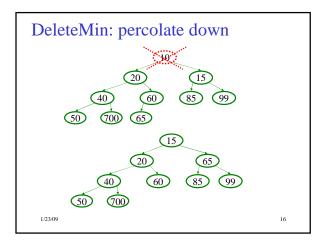
Basic Idea:

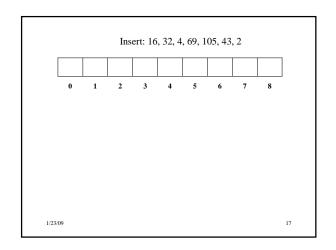
- 1. Remove root (that is always the min!)
- 2. Put "last" leaf node at root
- 3. Find smallest child of node
- 4. Swap node with its smallest child if needed.
- 5. Repeat steps 3 & 4 until no swaps needed.

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DeleteMin pseudo Code (Optimized) int percolateDown(int hole, Object deleteMin() { while (2*hole <= size) { assert(!isEmpty()); left = 2*hole; right = left + 1; if (right ≤ size && returnVal = Heap[1]; size--; newPos = Heap[right] < Heap[left])</pre> target = right; percolateDown(1, else target = left; Heap[size+1]); Heap[newPos] = if (Heap[target] < val) { Heap[hole] = Heap[target];</pre> Heap[size + 1]; return returnVal; hole = target; runtime: break; return hole; (Java code in book) 1/23/09 15





Other Priority Queue Operations

decreaseKey

- given a pointer to an object in the queue, reduce its priority value

Solution: change priority and _____

increaseKey

- given a pointer to an object in the queue, increase its priority value

Solution: change priority and _____

Why do we need a pointer? Why not simply data value?

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Other Heap Operations

decreaseKey(objPtr, amount): raise the priority of a object,
 percolate up

increaseKey(objPtr, amount): lower the priority of a object, percolate down

remove(objPtr): remove a object, move to top, them delete.
1) decreaseKey(objPtr, ∞)

2) deleteMin()

Worst case Running time for all of these:

FindMax?

ExpandHeap – when heap fills, copy into new space.

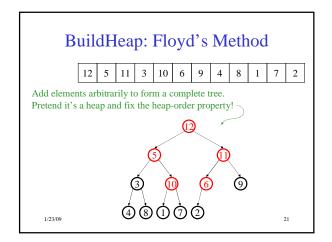
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Binary Min Heaps (summary)

- **insert**: percolate up. $\Theta(\log N)$ time.
- **deleteMin**: percolate down. $\Theta(\log N)$ time.
- Build Heap?

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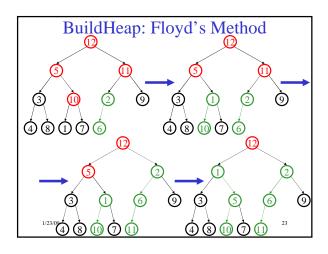


Buildheap pseudocode

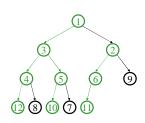
```
private void buildHeap() {
  for ( int i = currentSize/2; i > 0; i-- )
     percolateDown( i );
}
```

runtime:

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Finally...



runtime:

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Facts about Binary Min Heaps

Observations:

- finding a child/parent index is a multiply/divide by two
- operations jump widely through the heap
- · each percolate step looks at only two new nodes
- inserts are at least as common as deleteMins

Paglities

- division/multiplication by powers of two are equally fast
- looking at only two new pieces of data: bad for cache!
- with huge data sets, disk accesses dominate

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