

# Priority Queues

CSE 373  
Data Structures & Algorithms  
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## Today's Outline

- **Admin:**
  - Midterm #1 (Wed April 23)
    - Topics posted on course web page
- **Priority Queues**
  - **Binary Min Heaps**

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## Priority Queues (Binary Min Heaps)

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## Priority Queue ADT

- Checkout line at the supermarket ???
- Printer queues ???
- operations: insert, deleteMin



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## Priority Queue ADT

1. **PQueue data** : collection of data with **priority**
2. **PQueue operations**
  - insert
  - deleteMin(also: create, destroy, is\_empty)
3. **PQueue property**: for two elements in the queue,  $x$  and  $y$ , if  $x$  has a **lower** priority value than  $y$ ,  $x$  will be deleted before  $y$

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## Applications of the Priority Q

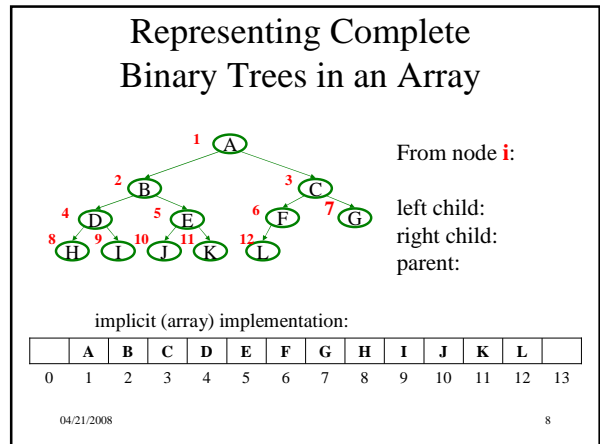
- Select print jobs in order of decreasing **length**
- Forward packets on network routers in order of **urgency**
- Select most **frequent** symbols for compression
- Sort numbers, picking **minimum** first
- **Anything greedy**

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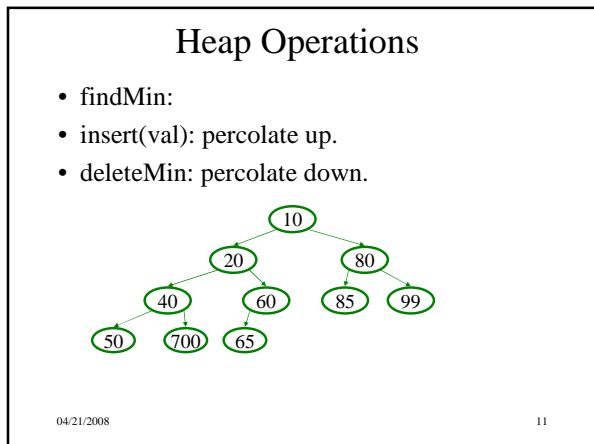
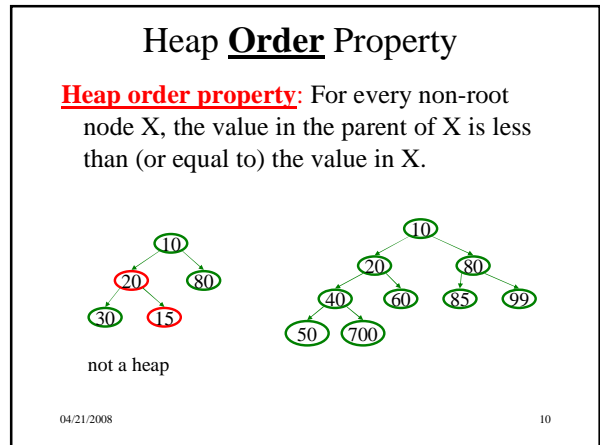
Implementations of Priority Queue ADT		
	insert	deleteMin
Unsorted list (Array)		
Unsorted list (Linked-List)		
Sorted list (Array)		
Sorted list (Linked-List)		
Binary Search Tree (BST)		

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### Why better than tree with pointers?

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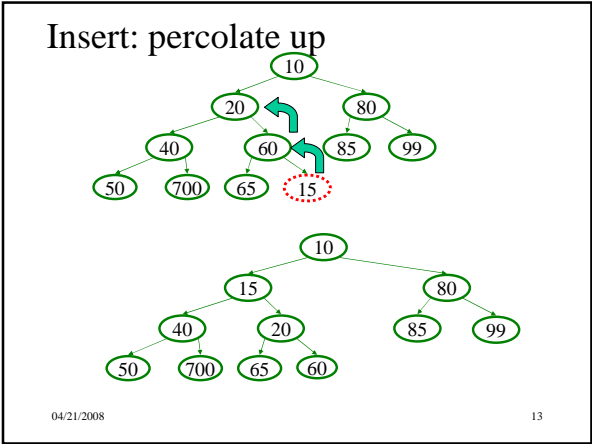


### Heap – Insert(val)

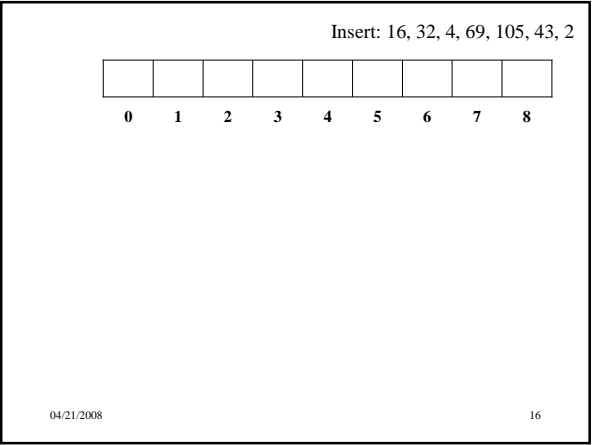
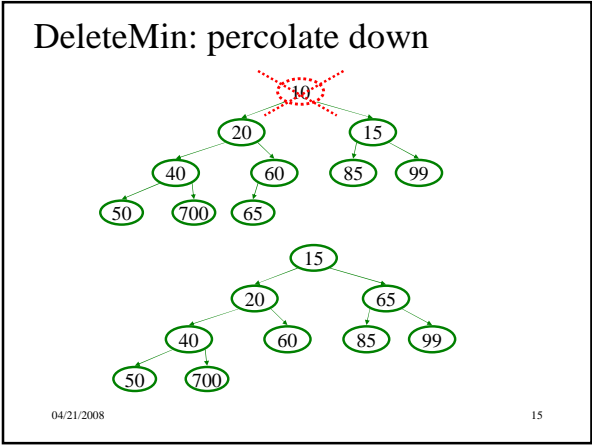
Basic Idea:

1. Put val at “next” leaf position
2. Repeatedly exchange node with its parent if needed

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- ### Heap – Deletemin
- Basic Idea:
1. Remove root (that is always the min!)
  2. Put “last” leaf node at root
  3. Find smallest child of node
  4. Swap node with its smallest child if needed.
  5. Repeat steps 3 & 4 until no swaps needed.
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- ### Other Priority Queue Operations
- **decreaseKey**
    - given a pointer to an object in the queue, reduce its priority value
    - Solution: change priority and \_\_\_\_\_
  - **increaseKey**
    - given a pointer to an object in the queue, increase its priority value
    - Solution: change priority and \_\_\_\_\_
- Why do we need a pointer? Why not simply data value?**
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- ### Other Heap Operations
- decreaseKey(objPtr, amount):** raise the priority of a object, percolate up
- increaseKey(objPtr, amount):** lower the priority of a object, percolate down
- remove(objPtr):** remove a object, move to top, them delete. 1) decreaseKey(objPtr, ∞)  
2) deleteMin()
- Worst case Running time for all of these:  
FindMax?  
ExpandHeap – when heap fills, copy into new space.
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## Binary Min Heaps (summary)

- **insert**: percolate up.  $O(\log N)$  time.
- **deleteMin**: percolate down.  $O(\log N)$  time.
- **Build Heap?**

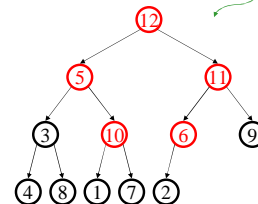
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## BuildHeap: Floyd's Method

12	5	11	3	10	6	9	4	8	1	7	2
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Add elements arbitrarily to form a complete tree.  
Pretend it's a heap and fix the heap-order property!



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## Buildheap pseudocode

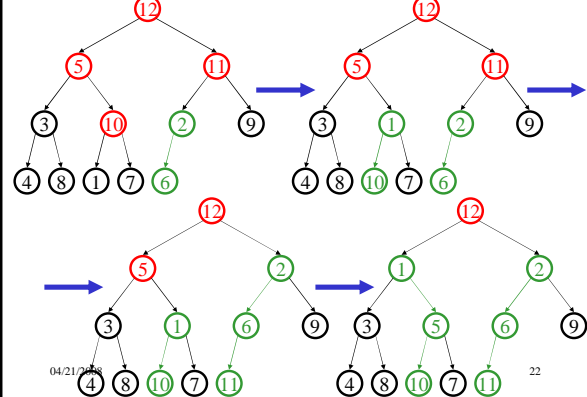
```
private void buildHeap() {
    for ( int i = currentSize/2; i > 0; i-- )
        percolateDown( i );
}
```

runtime:

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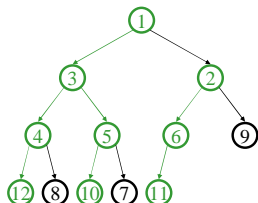
## BuildHeap: Floyd's Method



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## Finally...



runtime:

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## Facts about Binary Min Heaps

Observations:

- finding a child/parent index is a multiply/divide by two
- operations jump widely through the heap
- each percolate step looks at only two new nodes
- inserts are *at least* as common as deleteMins

Realities:

- division/multiplication by *powers* of two are equally fast
- looking at only two new pieces of data: bad for cache!
- with huge data sets, disk accesses dominate

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