

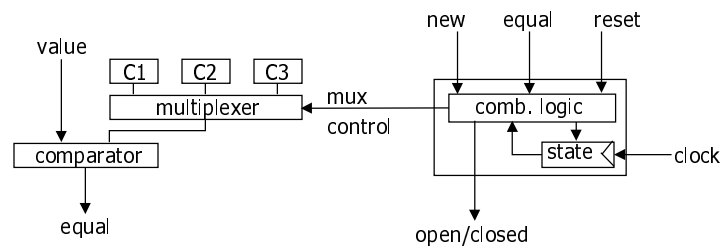
Sequential logic

- Sequential circuits
 - ┆ simple circuits with feedback
 - ┆ latches
 - ┆ edge-triggered flip-flops
- Timing methodologies
 - ┆ cascading flip-flops for proper operation
 - ┆ clock skew
- Asynchronous inputs
 - ┆ metastability and synchronization
- Basic registers
 - ┆ shift registers

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Sequential circuits

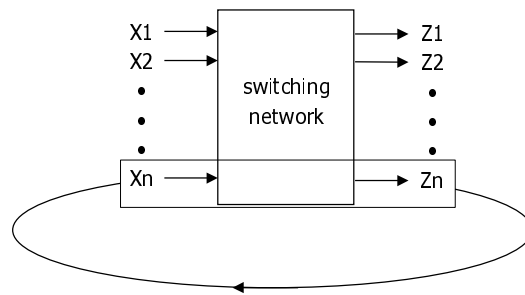
- Circuits with feedback
 - ┆ $\text{outputs} = f(\text{inputs}, \text{past inputs}, \text{past outputs})$
 - ┆ basis for building "memory" into logic circuits
 - ┆ door combination lock is an example of a sequential circuit
 - ┆ state is memory
 - ┆ state is an "output" and an "input" to combinational logic
 - ┆ combination storage elements are also memory



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Circuits with feedback

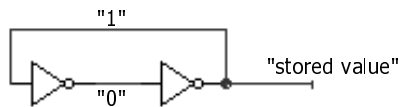
- How to control feedback?
 - what stops values from cycling around endlessly



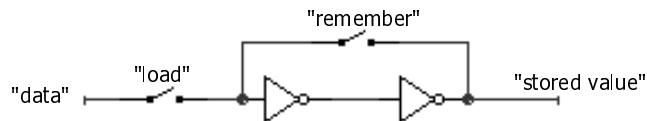
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Simplest circuits with feedback

- Two inverters form a static memory cell
 - will hold value as long as it has power applied



- How to get a new value into the memory cell?
 - selectively break feedback path
 - load new value into cell

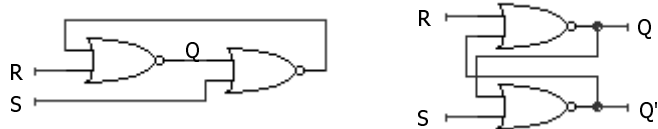


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Memory with cross-coupled gates

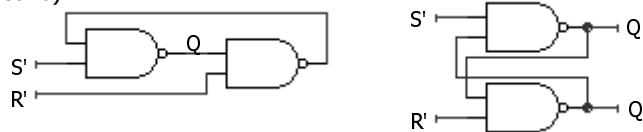
■ Cross-coupled NOR gates

- similar to inverter pair, with capability to force output to 0 (reset=1) or 1 (set=1)



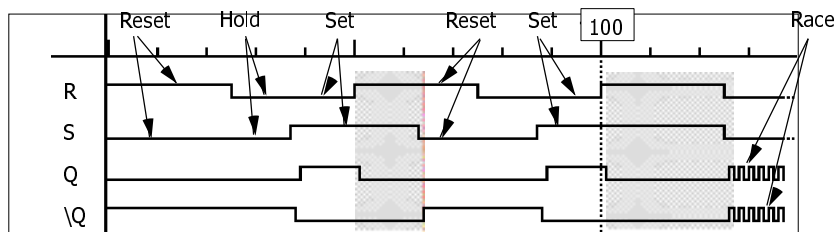
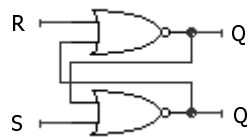
■ Cross-coupled NAND gates

- similar to inverter pair, with capability to force output to 0 (reset=0) or 1 (set=0)



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Timing behavior



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State behavior or R-S latch

■ Truth table of R-S latch behavior

S	R	Q
0	0	hold
0	1	0
1	0	1
1	1	unstable

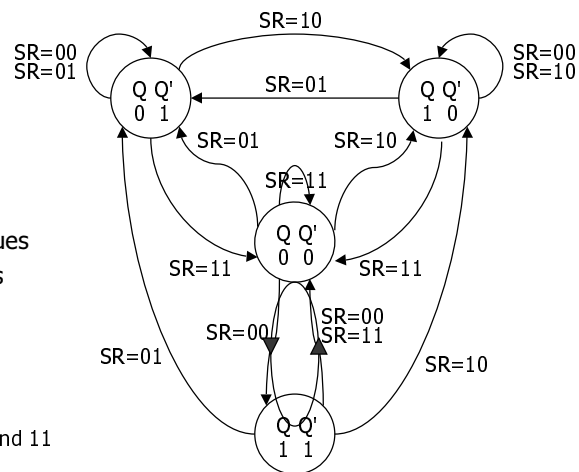


Theoretical R-S latch behavior

■ State diagram

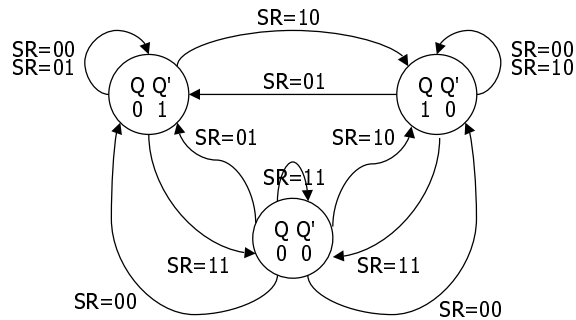
- states: possible values
- transitions: changes based on inputs

possible oscillation between states 00 and 11



Observed R-S latch behavior

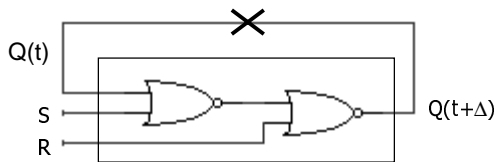
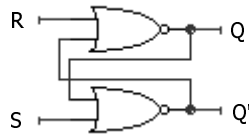
- Very difficult to observe R-S latch in the 1-1 state
 - ▮ one of R or S usually changes first
- Ambiguously returns to state 0-1 or 1-0
 - ▮ a so-called "race condition"
 - ▮ or non-deterministic transition



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R-S latch analysis

- Break feedback path



S	R	Q(t)	Q(t+Δ)	
0	0	0	0	hold
0	0	1	1	
0	1	0	0	reset
0	1	1	0	
1	0	0	1	set
1	0	1	1	
1	1	0	X	not allowed
1	1	1	X	

		S	
		0	1
Q(t)	0	0	X
	1	0	X

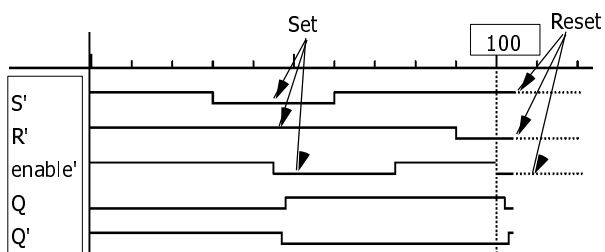
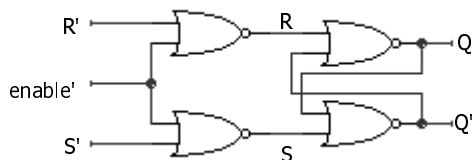
R

characteristic equation
 $Q(t+\Delta) = S + R' Q(t)$

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Gated R-S latch

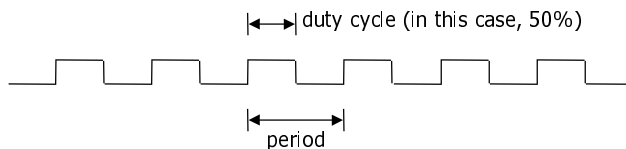
- Control when R and S inputs matter
 - otherwise, the slightest glitch on R or S while enable is low could cause change in value stored



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Clocks

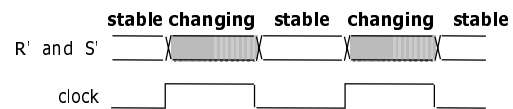
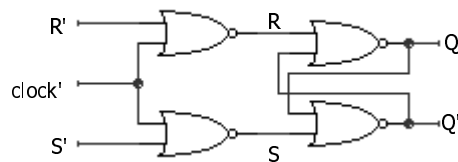
- Used to keep time
 - wait long enough for inputs (R' and S') to settle
 - then allow to have effect on value stored
- Clocks are regular periodic signals
 - period (time between ticks)
 - duty-cycle (time clock is high between ticks - expressed as % of period)



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Clocks (cont'd)

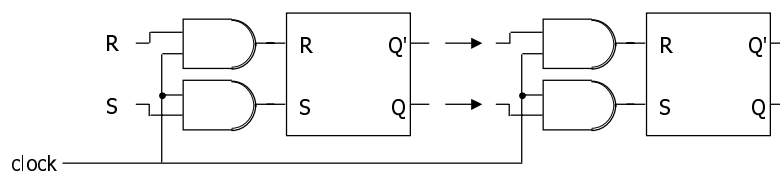
- Controlling an R-S latch with a clock
 - can't let R and S change while clock is active (allowing R and S to pass)
 - only have half of clock period for signal changes to propagate
 - signals must be stable for the other half of clock period



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Cascading latches

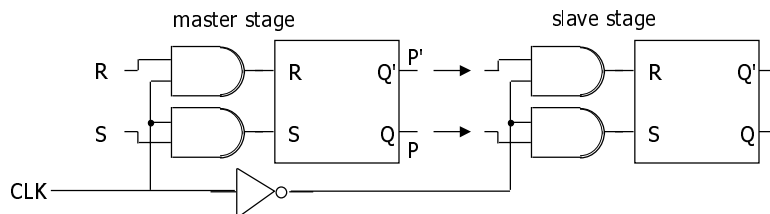
- Connect output of one latch to input of another
- How to stop changes from racing through chain?
 - need to be able to control flow of data from one latch to the next
 - move one latch per clock period
 - have to worry about logic between latches (arrows) that is too fast



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Master-slave structure

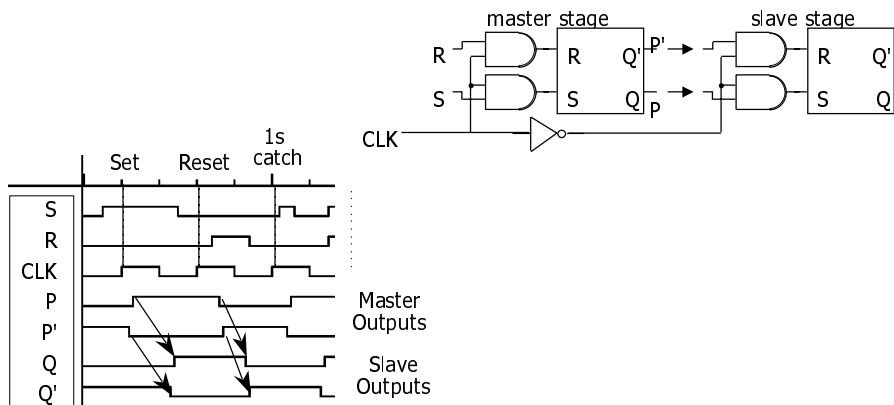
- Break flow by alternating clocks (like an air-lock)
 - use positive clock to latch inputs into one R-S latch
 - use negative clock to change outputs with another R-S latch
- View pair as one basic unit
 - master-slave flip-flop
 - twice as much logic
 - output changes a few gate delays after the falling edge of clock but does not affect any cascaded flip-flops



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The 1s catching problem

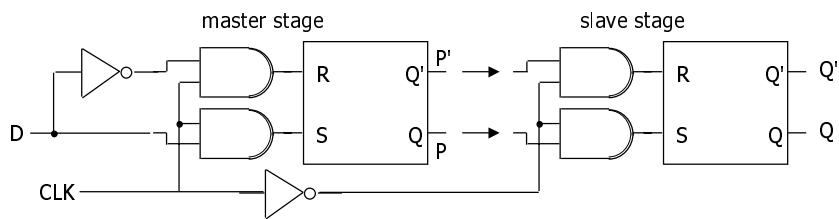
- In first R-S stage of master-slave FF
 - 0-1-0 glitch on R or S while clock is high is "caught" by master stage
 - leads to constraints on logic to be hazard-free



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D flip-flop

- Make S and R complements of each other
 - eliminates 1s catching problem
 - can't just hold previous value (must have new value ready every clock period)
 - value of D just before clock goes low is what is stored in flip-flop
 - can make R-S flip-flop by adding logic to make $D = S + R'Q$

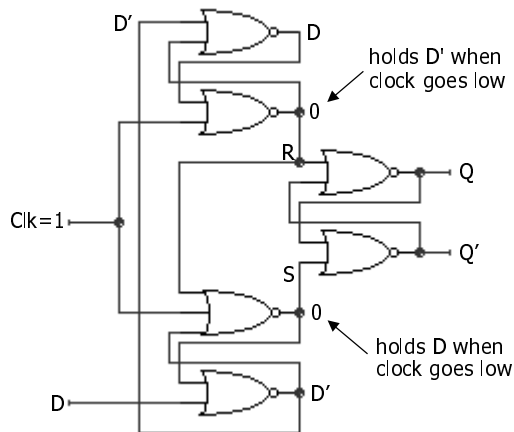


10 gates

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Edge-triggered flip-flops

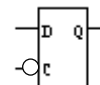
- More efficient solution: only 6 gates
 - sensitive to inputs only near edge of clock signal (not while high)



negative edge-triggered D flip-flop (D-FF)

4-5 gate delays

must respect setup and hold time constraints to successfully capture input

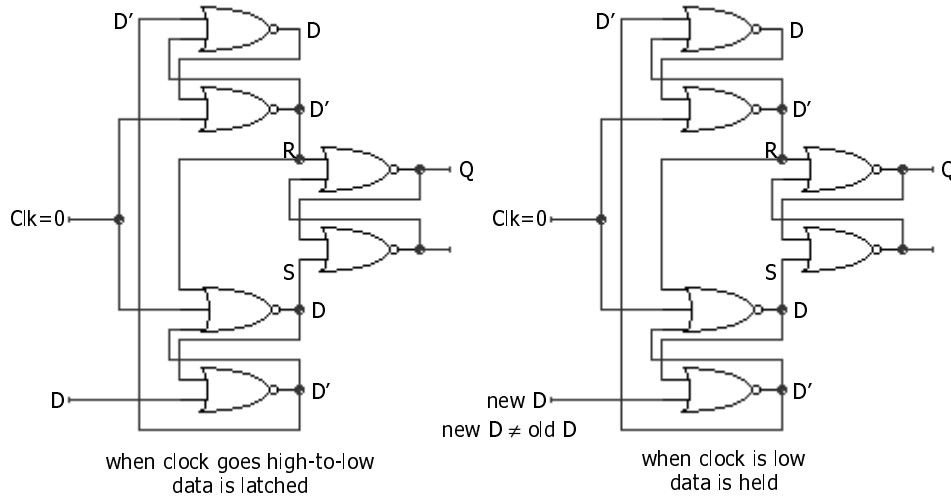


characteristic equation
 $Q(t+1) = D$

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Edge-triggered flip-flops (cont'd)

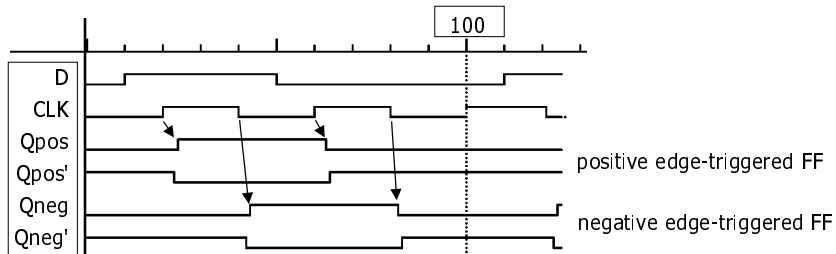
■ Step-by-step analysis



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Edge-triggered flip-flops (cont'd)

- Positive edge-triggered
 - inputs sampled on rising edge; outputs change after rising edge
- Negative edge-triggered flip-flops
 - inputs sampled on falling edge; outputs change after falling edge



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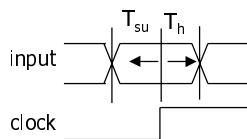
Timing methodologies

- Rules for interconnecting components and clocks
 - ▮ guarantee proper operation of system when strictly followed
- Approach depends on building blocks used for memory elements
 - ▮ we'll focus on systems with edge-triggered flip-flops
 - ▮ found in programmable logic devices
 - ▮ many custom integrated circuits focus on level-sensitive latches
- Basic rules for correct timing:
 - ▮ (1) correct inputs, with respect to time, are provided to the flip-flops
 - ▮ (2) no flip-flop changes state more than once per clocking event

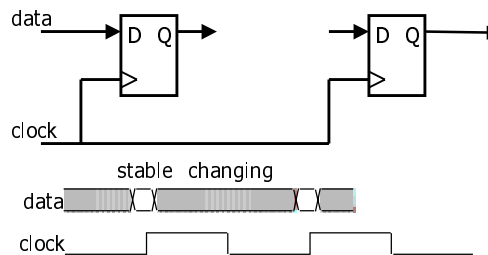
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Timing methodologies (cont'd)

- Definition of terms
 - ▮ clock: periodic event, causes state of memory element to change
can be rising edge or falling edge or high level or low level
 - ▮ setup time: minimum time before the clocking event by which the input must be stable (T_{su})
 - ▮ hold time: minimum time after the clocking event until which the input must remain stable (T_h)

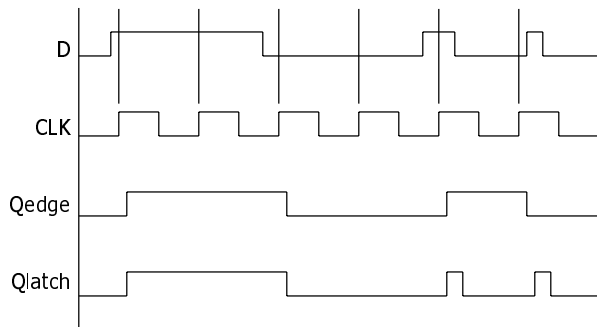
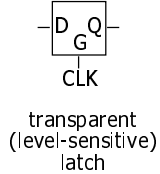
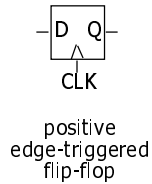


there is a timing "window" around the clocking event during which the input must remain stable and unchanged in order to be recognized



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Comparison of latches and flip-flops



behavior is the same unless input changes
while the clock is high

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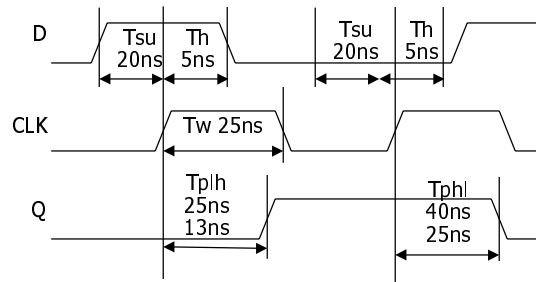
Comparison of latches and flip-flops (cont'd)

Type	When inputs are sampled	When output is valid
unlocked latch	always	propagation delay from input change
level-sensitive latch	clock high (T_{su}/T_{th} around falling edge of clock)	propagation delay from input change or clock edge (whichever is later)
master-slave flip-flop	clock high (T_{su}/T_{th} around falling edge of clock)	propagation delay from falling edge of clock
negative edge-triggered flip-flop	clock hi-to-lo transition (T_{su}/T_{th} around falling edge of clock)	propagation delay from falling edge of clock

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Typical timing specifications

- Positive edge-triggered D flip-flop
 - setup and hold times
 - minimum clock width
 - propagation delays (low to high, high to low, max and typical)

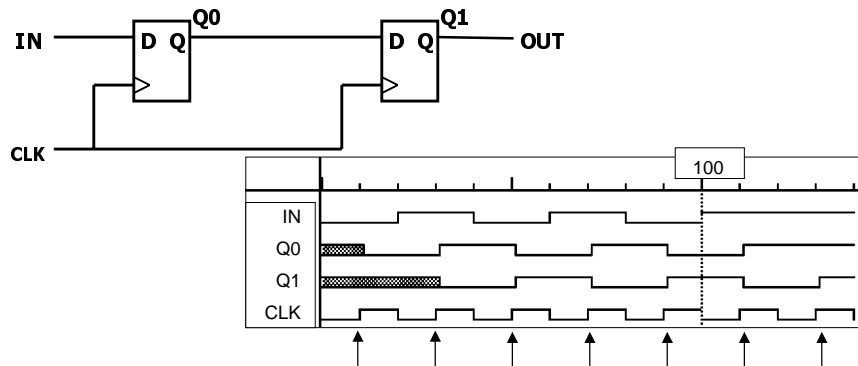


all measurements are made from the clocking event that is, the rising edge of the clock

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Cascading edge-triggered flip-flops

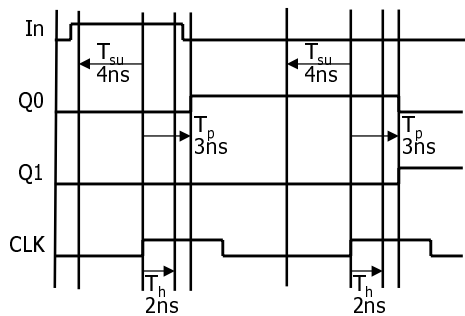
- Shift register
 - new value goes into first stage
 - while previous value of first stage goes into second stage
 - consider setup/hold/propagation delays (prop must be > hold)



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Cascading edge-triggered flip-flops (cont'd)

- Why this works
 - propagation delays exceed hold times
 - clock width constraint exceeds setup time
 - this guarantees following stage will latch current value before it changes to new value



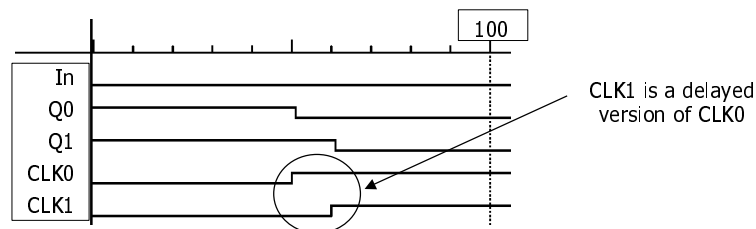
timing constraints
guarantee proper
operation of
cascaded components

assumes infinitely fast
distribution of the clock

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Clock skew

- The problem
 - correct behavior assumes next state of all storage elements determined by all storage elements at the same time
 - this is difficult in high-performance systems because time for clock to arrive at flip-flop is comparable to delays through logic
 - effect of skew on cascaded flip-flops:



original state: IN = 0, Q0 = 1, Q1 = 1
due to skew, next state becomes: Q0 = 0, Q1 = 0, and not Q0 = 0, Q1 = 1

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Summary of latches and flip-flops

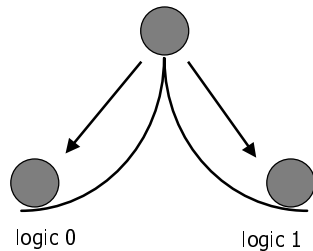
- Development of D-FF
 - ┆ level-sensitive used in custom integrated circuits
 - ┆ can be made with 4 switches
 - ┆ edge-triggered used in programmable logic devices
 - ┆ good choice for data storage register
- Historically J-K FF was popular but now never used
 - ┆ similar to R-S but with 1-1 being used to toggle output (complement state)
 - ┆ good in days of TTL/SSI (more complex input function: $D = JQ' + K'Q$)
 - ┆ not a good choice for PALs/PLAs as it requires 2 inputs
 - ┆ can always be implemented using D-FF
- Preset and clear inputs are highly desirable on flip-flops
 - ┆ used at start-up or to reset system to a known state

Metastability and asynchronous inputs

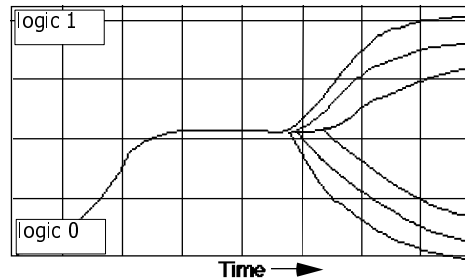
- Clocked synchronous circuits
 - ┆ inputs, state, and outputs sampled or changed in relation to a common reference signal (called the clock)
 - ┆ e.g., master/slave, edge-triggered
- Asynchronous circuits
 - ┆ inputs, state, and outputs sampled or changed independently of a common reference signal (glitches/hazards a major concern)
 - ┆ e.g., R-S latch
- Asynchronous inputs to synchronous circuits
 - ┆ inputs can change at any time, will not meet setup/hold times
 - ┆ dangerous, synchronous inputs are greatly preferred
 - ┆ cannot be avoided (e.g., reset signal, memory wait, user input)

Synchronization failure

- Occurs when FF input changes close to clock edge
 - the FF may enter a metastable state – neither a logic 0 nor 1 –
 - it may stay in this state an indefinite amount of time
 - this is not likely in practice but has some probability



small, but non-zero probability that the FF output will get stuck in an in-between state

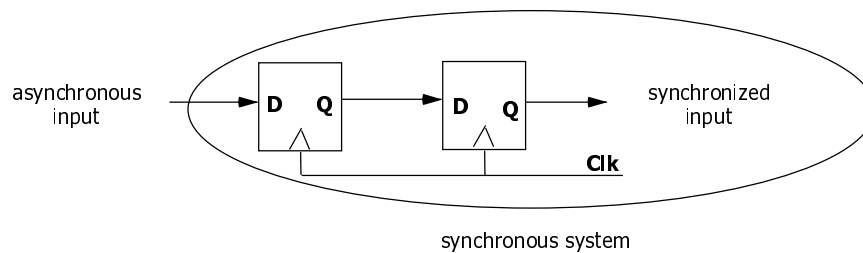


oscilloscope traces demonstrating synchronizer failure and eventual decay to steady state

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Dealing with synchronization failure

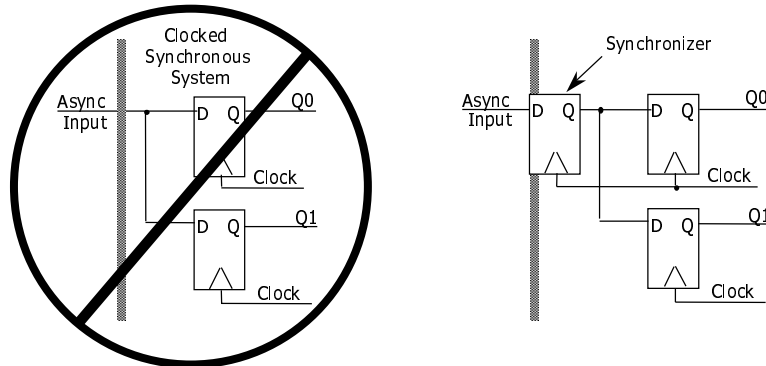
- Probability of failure can never be reduced to 0, but it can be reduced
 - (1) slow down the system clock
this gives the synchronizer more time to decay into a steady state; synchronizer failure becomes a big problem for very high speed systems
 - (2) use fastest possible logic technology in the synchronizer
this makes for a very sharp "peak" upon which to balance
 - (3) cascade two synchronizers
this effectively synchronizes twice (both would have to fail)



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Handling asynchronous inputs

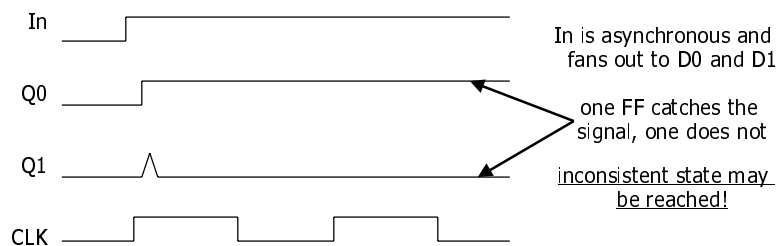
- Never allow asynchronous inputs to fan-out to more than one flip-flop
 - synchronize as soon as possible and then treat as synchronous signal



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Handling asynchronous inputs (cont'd)

- What can go wrong?
 - input changes too close to clock edge (violating setup time constraint)



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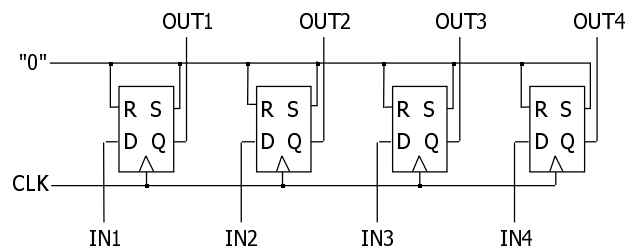
Flip-flop features

- Reset (set state to 0) – R
 - ▮ synchronous: $D_{new} = R' \cdot D_{old}$ (when next clock edge arrives)
 - ▮ asynchronous: doesn't wait for clock, quick but dangerous
- Preset or set (set state to 1) – S (or sometimes P)
 - ▮ synchronous: $D_{new} = D_{old} + S$ (when next clock edge arrives)
 - ▮ asynchronous: doesn't wait for clock, quick but dangerous
- Both reset and preset
 - ▮ $D_{new} = R' \cdot D_{old} + S$ (set-dominant)
 - ▮ $D_{new} = R' \cdot D_{old} + R'S$ (reset-dominant)
- Selective input capability (input enable or load) – LD or EN
 - ▮ multiplexor at input: $D_{new} = LD' \cdot Q + LD \cdot D_{old}$
 - ▮ load may or may not override reset/set (usually R/S have priority)
- Complementary outputs – Q and Q'

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Registers

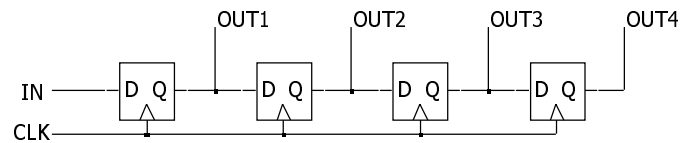
- Collections of flip-flops with similar controls and logic
 - ▮ stored values somehow related (for example, form binary value)
 - ▮ share clock, reset, and set lines
 - ▮ similar logic at each stage
- Examples
 - ▮ shift registers
 - ▮ counters



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Shift register

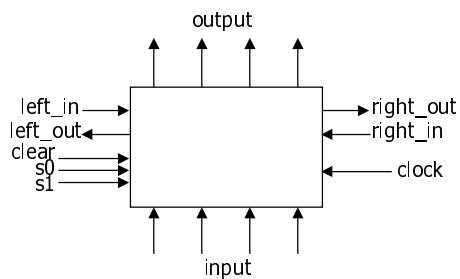
- Holds samples of input
 - store last 4 input values in sequence
 - 4-bit shift register:



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Universal shift register

- Holds 4 values
 - serial or parallel inputs
 - serial or parallel outputs
 - permits shift left or right
 - shift in new values from left or right



clear sets the register contents and output to 0

s1 and s0 determine the shift function

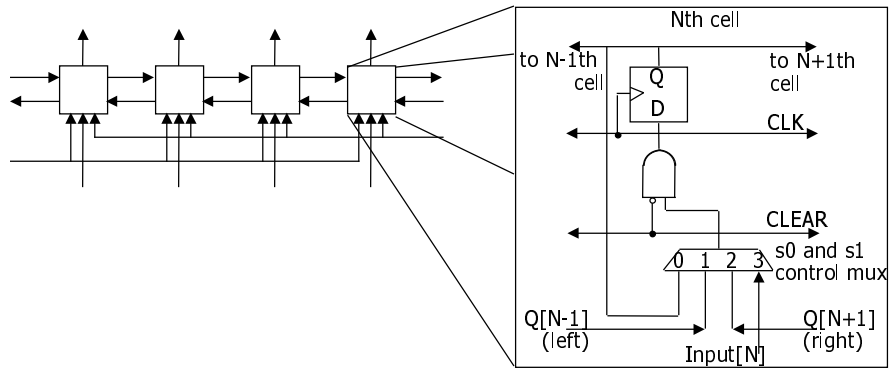
s0	s1	function
0	0	hold state
0	1	shift right
1	0	shift left
1	1	load new input

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Design of universal shift register

- Consider one of the four flip-flops
 - new value at next clock cycle:

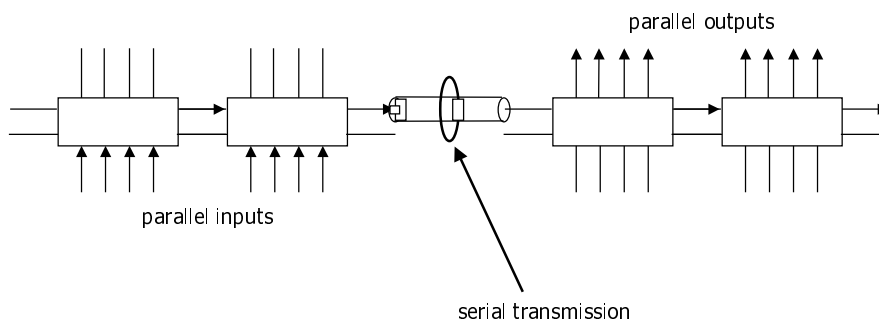
clear	s0	s1	new value
1	-	-	0
0	0	0	output
0	0	1	output value of FF to left (shift right)
0	1	0	output value of FF to right (shift left)
0	1	1	input



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Shift register application

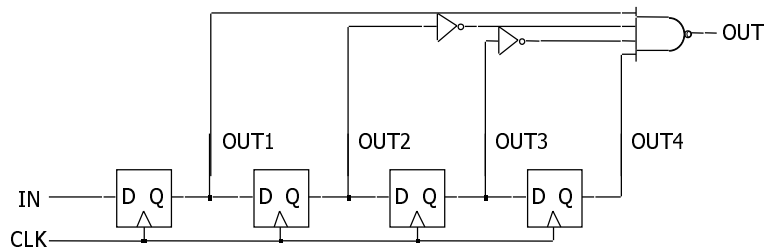
- Parallel-to-serial conversion for serial transmission



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Pattern recognizer

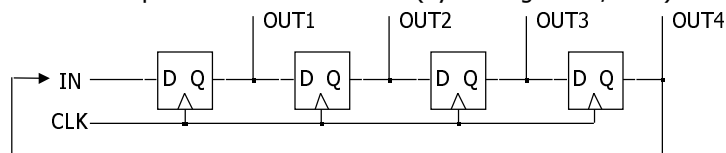
- Combinational function of input samples
 - in this case, recognizing the pattern 1001 on the single input signal



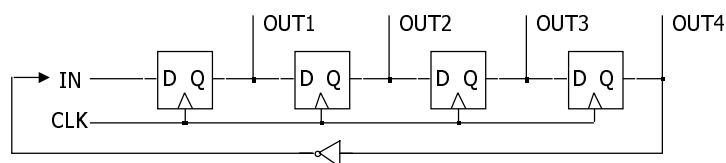
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Counters

- Sequences through a fixed set of patterns
 - in this case, 1000, 0100, 0010, 0001
 - if one of the patterns is its initial state (by loading or set/reset)



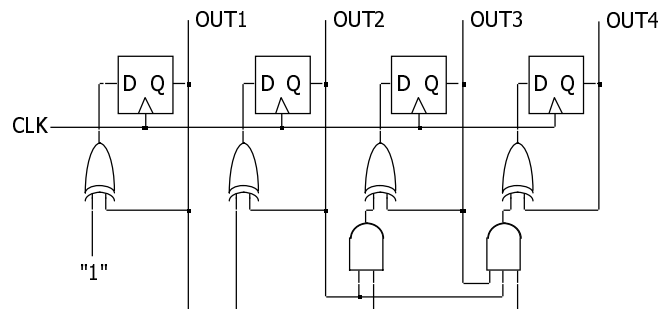
- Mobius (or Johnson) counter
 - in this case, 1000, 1100, 1110, 1111, 0111, 0011, 0001, 0000



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Binary counter

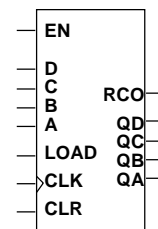
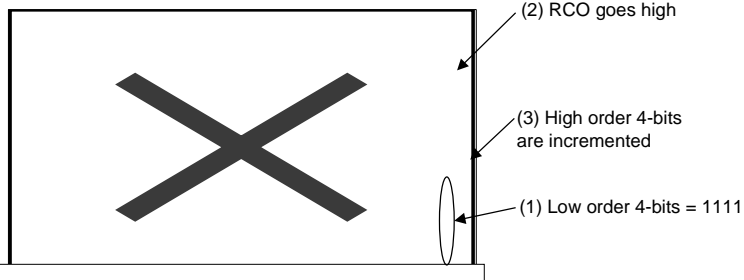
- Logic between registers (not just multiplexer)
 - XOR decides when bit should be toggled
 - always for low-order bit,
 - only when first bit is true for second bit,
 - and so on



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Four-bit binary synchronous up-counter

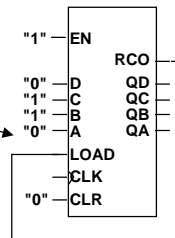
- Standard component with many applications
 - positive edge-triggered FFs w/ synchronous load and clear inputs
 - parallel load data from D, C, B, A
 - enable inputs: must be asserted to enable counting
 - RCO: ripple-carry out used for cascading counters
 - high when counter is in its highest state 1111
 - implemented using an AND gate



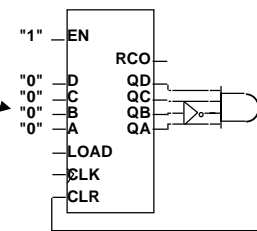
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Offset counters

- Starting offset counters – use of synchronous load
 - ▮ e.g., 0110, 0111, 1000, 1001, 1010, 1011, 1100, 1101, 1111, 0110, . . .



- Ending offset counter – comparator for ending value
 - ▮ e.g., 0000, 0001, 0010, . . ., 1100, 1101, 0000



- Combinations of the above (start and stop value)

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Sequential logic summary

- Fundamental building block of circuits with state
 - ▮ latch and flip-flop
 - ▮ R-S latch, R-S master/slave, D master/slave, edge-triggered D flip-flop
- Timing methodologies
 - ▮ use of clocks
 - ▮ cascaded FFs work because propagation delays exceed hold times
 - ▮ beware of clock skew
- Asynchronous inputs and their dangers
 - ▮ synchronizer failure: what it is and how to minimize its impact
- Basic registers
 - ▮ shift registers
 - ▮ pattern detectors
 - ▮ counters

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