

Overview

- ◆ Last lecture
 - Introduction to finite-state machines
 - ▣ Moore versus Mealy machines
 - ▣ Synchronous Mealy machines
 - ▣ Example: A parity checker
- ◆ Today
 - Example: A sequence detector FSM
 - Example: A vending machine FSM

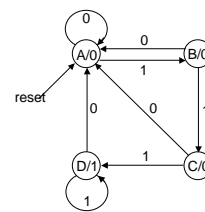
FSM design

- ◆ FSM-design procedure
 1. State diagram and state-transition table
 2. State minimization
 3. State assignment (or state encoding)
 4. Minimize next-state logic
 5. Implement the design

Example: Sequence detector

- ◆ Design a circuit to detect 3 or more 1's in a bit string
 - Assume Moore machine
 - Assume D flip-flops
 - Assume flip-flops have a reset

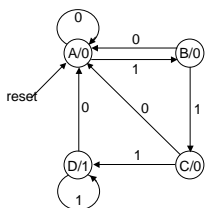
1. State diagram and state-transition table



reset	current state	input	next state	current output
1	-	-	A	0
0	A	0	A	0
0	A	1	B	0
0	B	0	A	0
0	B	1	C	0
0	C	0	A	0
0	C	1	D	0
0	D	0	A	1
0	D	1	D	1

2. State minimization & 3. State encoding

- ◆ State diagram is already minimized
- ◆ Try a binary encoding



reset	current state	input	next state	current output
1	-	-	00	0
0	00	0	00	0
0	00	1	01	0
0	01	0	00	0
0	01	1	10	0
0	10	0	00	0
0	10	1	11	0
0	11	0	00	1
0	11	1	11	1

4. Minimize next-state logic

MSB+		M	
0	1	0	1
0	0	0	0
0	1	1	1

$$MSB+ = L \cdot in + M \cdot in$$

LSB+		M	
0	1	0	1
0	0	0	0
1	0	1	1

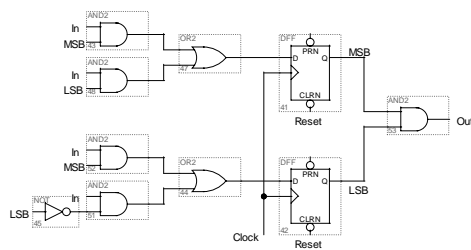
$$LSB+ = L' \cdot in + M \cdot in$$

OUT+		M	
0	1	0	1
0	0	1	0
0	0	1	0

$$Out+ = ML$$

Notation
 M := MSB
 L := LSB
 In := Input

5. Implement the design

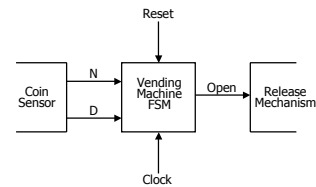


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Design example: A vending machine

- ◆ Release item after receiving 15 cents
 - Single coin slot for dimes and nickels
 - ◆ Sensor specifies coin type
 - Machine does not give change

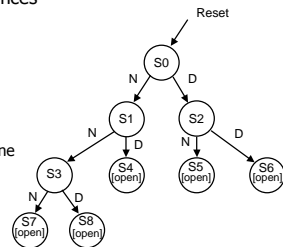


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1a. State diagram

- ◆ Consider input sequences
 - 3 nickels
 - 2 nickels, dime
 - nickel, dime
 - dime, nickel
 - two dimes
- ◆ Draw state diagram
 - Assume Moore machine
 - Inputs: N, D, reset
 - Output: Open



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1b. Symbolic state-transition table

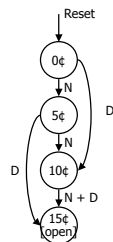
present state	inputs		next state	present output
	D	N		
0¢	0	0	0¢	0
	0	1	5¢	0
	1	0	10¢	0
	1	1	—	—
5¢	0	0	5¢	0
	0	1	10¢	0
	1	0	15¢	0
	1	1	—	—
10¢	0	0	10¢	0
	0	1	15¢	0
	1	0	15¢	0
	1	1	—	—
15¢	—	—	15¢	1

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2. State minimization

- ◆ Reuse states where possible
 - Notice we can use the deposited coin values for states
 - State is the same if we input 2 nickels or 1 dime



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3. State encoding

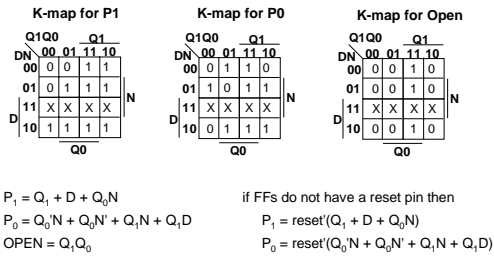
- ◆ Encode states uniquely
 - 4 states:
 - ◆ 2 bits minimum
 - ◆ 4 bits maximum
 - Look for optimal encoding
 - Assume D flip-flops

present state	inputs		next state	present output
Q0 Q1	D	N	P1 P0	
0 0	0	0	0 0	0
	0	1	0 1	0
	1	0	1 0	0
	1	1	—	—
0 1	0	0	0 1	0
	0	1	1 0	0
	1	0	1 1	0
	1	1	—	—
1 0	0	0	1 0	0
	0	1	1 1	0
	1	0	1 1	0
	1	1	—	—
1 1	—	—	1 1	1

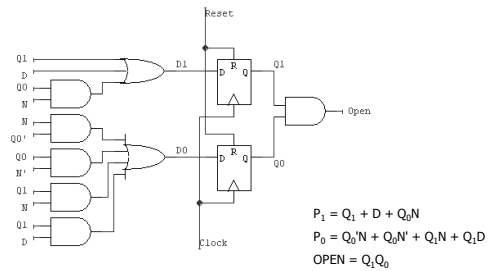
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4. Minimize the logic

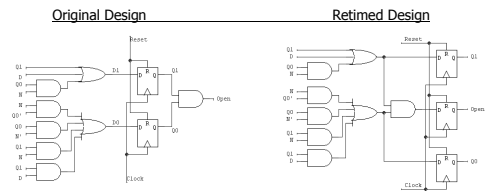


5. Implement the design



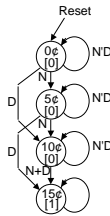
Retime design

- ◆ OPEN is delayed by AND gate after Q_1 and Q_0
 - Can remove this delay by retiming
 - ✦ Move output logic (AND gate) to eliminate delay
 - $OPEN = Q_1Q_0 = (Q_1 + D + Q_0N)(Q_0N + Q_0N' + Q_1N + Q_1D)$



Moore versus Mealy vending machine

Moore machine



Mealy machine

