



CSE341: Programming Languages Lecture 24 Subtyping

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Last major topic: Subtyping

Build up key ideas from first principles

- In pseudocode because:
 - · No time for another language
 - · Simpler to first show subtyping without objects

Then:

- · How does subtyping relate to types for OOP?
 - Brief sketch only
- · What are the relative strengths of subtyping and generics?
- · How can subtyping and generics combine synergistically?

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A tiny language

- Can cover most core subtyping ideas by just considering records with mutable fields
- Will make up our own syntax
 - ML has records, but no subtyping or field-mutation
 - Racket and Ruby have no type system
 - Java uses class/interface names and rarely fits on a slide

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Records (half like ML, half like Java)

Record creation (field names and contents):

{f1=e1, f2=e2, ..., fn=en} Evaluate ei, make a record

Record field access:

e.f

Evaluate \mathbf{e} to record \mathbf{v} with an \mathbf{f} field, get contents of \mathbf{f} field

Record field update

e1.f = e2

Evaluate e1 to a record v1 and e2 to a value v2; Change v1's f field (which must exist) to v2; Return v2

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A Basic Type System

Record types: What fields a record has and type for each field

{f1:t1, f2:t2, ..., fn:tn}

Type-checking expressions:

- If e1 has type t1, ..., en has type tn,
 then {f1=e1, ..., fn=en} has type {f1:t1, ..., fn:tn}
- If e has a record type containing f: t, then e.f has type t
- If e1 has a record type containing f: t and e2 has type t,
 then e1.f = e2 has type t

This is safe

These evaluation rules and typing rules prevent ever trying to access a field of a record that does not exist

Example program that type-checks (in a made-up language):

```
fun distToOrigin (p:{x:real,y:real}) =
  Math.sqrt(p.x*p.x + p.y*p.y)

val pythag : {x:real,y:real} = {x=3.0, y=4.0}
val five : real = distToOrigin(pythag)
```

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Motivating subtyping

But according to our typing rules, this program does not type-check

- It does nothing wrong and seems worth supporting

```
fun distToOrigin (p:{x:real,y:real}) =
   Math.sqrt(p.x*p.x + p.y*p.y)

val c : {x:real,y:real,color:string} =
   {x=3.0, y=4.0, color="green"}

val five : real = distToOrigin(c)
```

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A good idea: allow extra fields

Natural idea: If an expression has type

```
{f1:t1, f2:t2, ..., fn:tn}
```

Then it can also have a type with some fields removed

This is what we need to type-check these function calls:

```
fun distToOrigin (p:{x:real,y:real}) = ...
fun makePurple (p:{color:string}) =
    p.color = "purple"

val c :{x:real,y:real,color:string} =
    {x=3.0, y=4.0, color="green"}

val _ = distToOrigin(c)
val _ = makePurple(c)
```

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Keeping subtyping separate

A programming language already has a lot of typing rules and we do not want to change them

 Example: The type of an actual function argument must equal the type of the function parameter

We can do this by adding "just two things to our language"

- Subtyping: Write t1 <: t2 for t1 is a subtype of t2</p>
- One new typing rule that uses subtyping:
 If e has type t1 and t1 <: t2,
 then e (also) has type t2

Now all we need to do is define t1 <: t2

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Subtyping is not a matter of opinion

- Misconception: If we are making a new language, we can have whatever typing and subtyping rules we want
- Not if you want to prevent what you claim to prevent [soundness]
 - Here: No accessing record fields that do not exist
- · Our typing rules were sound before we added subtyping
 - We should keep it that way
- Principle of substitutability: If t1 <: t2, then any value of type t1 must be usable in every way a t2 is
 - Here: Any value of subtype needs all fields any value of supertype has

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Four good rules

For our record types, these rules all meet the substitutability test:

- 1. "Width" subtyping: A supertype can have a subset of fields with the same types
- "Permutation" subtyping: A supertype can have the same set of fields with the same types in a different order
- 3. Transitivity: If t1 <: t2 and t2 <: t3, then t1 <: t3
- 4. Reflexivity: Every type is a subtype of itself
- (4) may seem unnecessary, but it composes well with other rules in a full language and "does no harm"

More record subtyping?

[Warning: I am misleading you ©]

Subtyping rules so far let us drop fields but not change their types

Example: A circle has a center field holding another record

```
fun circleY (c:{center:{x:real,y:real}, r:real}) =
    c.center.y

val sphere:{center:{x:real,y:real,z:real}, r:real} =
    {center={x=3.0,y=4.0,z=0.0}, r=1.0}

val _ = circleY(sphere)
```

```
For this to type-check, we need:
```

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Do not have this subtyping - could we?

- No way to get this yet: we can drop center, drop r, or permute order, but cannot "reach into a field type" to do subtyping
- So why not add another subtyping rule... "Depth" subtyping:
 If ta <: tb, then {f1:t1, ..., f:ta, ..., fn:tn} <:
 {f1:t1, ..., f:tb, ..., fn:tn}
- Depth subtyping (along with width on the field's type) lets our example type-check

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Stop!

- It is nice and all that our new subtyping rule lets our example type-check
- · But it is not worth it if it breaks soundness
 - Also allows programs that can access missing record fields
- Unfortunately, it breaks soundness ⊗

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Mutation strikes again

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Moral of the story

- In a language with records/objects with getters and setters, depth subtyping is unsound
 - Subtyping cannot change the type of fields
- · If fields are immutable, then depth subtyping is sound!
 - Yet another benefit of outlawing mutation!
 - Choose two of three: setters, depth subtyping, soundness
- · Remember: subtyping is not a matter of opinion

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Picking on Java (and C#)

Arrays should work just like records in terms of depth subtyping

- But in Java, if t1 <: t2, then t1[] <: t2[]
- So this code type-checks, surprisingly

```
class Point { ... }
class ColorPoint extends Point { ... }
...
void m1(Point[] pt_arr) {
  pt_arr[0] = new Point(3,4);
}
String m2(int x) {
  ColorPoint[] cpt_arr = new ColorPoint[x];
  for(int i=0; i < x; i++)
     cpt_arr[i] = new ColorPoint(0,0,"green");
  m1(cpt_arr); //!
  return cpt_arr[0].color; //!</pre>
```

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Why did they do this?

- More flexible type system allows more programs but prevents fewer errors
 - Seemed especially important before Java/C# had generics
- Good news: despite this "inappropriate" depth subtyping
 - e.color will never fail due to there being no color field
 - Array reads e1[e2] always return a (subtype of) t if e1 is a t[]
- · Bad news: to get the good news
 - e1[e2]=e3 can fail even if e1 has type t[] and e3 has type t
 - Array stores check the run-time class of e1's elements and do not allow storing a supertype
 - No type-system help to avoid such bugs / performance cost

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So what happens

- Causes code in m1 to throw an ArrayStoreException
 - Even though logical error is in m2
 - At least run-time checks occur only on array stores, not on field accesses like c.color

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null

- Array stores probably the most surprising choice for flexibility over static checking
- But null is the most common one in practice
 - null is not an object; it has no fields or methods
 - But Java and C# let it have any object type (backwards, huh?!)
 - So, in fact, we do *not* have the static guarantee that evaluating e in e.f or e.m (...) produces an object that has an f or m
 - The "or null" caveat leads to run-time checks and errors, as you have surely noticed
- Sometimes null is convenient (like ML's option types)
 - But also having "cannot be null" types would be nice

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Now functions

- Already know a caller can use subtyping for arguments passed
 - Or on the result
- · More interesting: When is one function type a subtype of another?
 - Important for higher-order functions: If a function expects an argument of type t1 -> t2, can you pass a t3 -> t4 instead?
 - Coming next: Important for understanding methods
 - (An object type is a lot like a record type where "method positions" are immutable and have function types)

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Example

No subtyping here yet:

- flip has exactly the type distMoved expects for f
- Can pass distMoved a record with extra fields for p, but that's old news

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Return-type subtyping

 Return type of flipGreen is {x:real,y:real,color:string}, but distMoved expects a return type of {x:real,y:real}

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- Nothing goes wrong: If ta <: tb, then t -> ta <: t-> tb
 - A function can return "more than it needs to"
 - Jargon: "Return types are covariant"

This is wrong

- Argument type of flipIfGreen is {x:real,y:real,color:string}, but it is called with a {x:real,y:real}
- Unsound! ta <: tb does NOT allow ta -> t <: tb -> t

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The other way works!

- Argument type of flipx_Y0 is {x:real}, but it is called with a
 {x:real,y:real}, which is fine
- If tb <: ta, then ta -> t <: tb -> t
 - A function can assume "less than it needs to" about arguments
 - Jargon: "Argument types are contravariant"

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Conclusion

- If t3 <: t1 and t2 <: t4, then t1 -> t2 <: t3 -> t4
 - Function subtyping contravariant in argument(s) and covariant in results
- · Also essential for understanding subtyping and methods in OOP
- · Most unintuitive concept in the course
 - Smart people often forget and convince themselves covariant arguments are okay
 - These people are always mistaken
 - At times, you or your boss or your friend may do this
 - Remember: A guy with a PhD in PL jumped up and down insisting that function/method subtyping is always contravariant in its argument -- covariant is unsound

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Can do both

• flipXMakeGreen has type

{x:real} -> {x:real,y:real,color:string}

Fine to pass a function of such a type as function of type
 {x:real,y:real} -> {x:real,y:real}

• If t3 <: t1 and t2 <: t4, then t1 -> t2 <: t3 -> t4

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