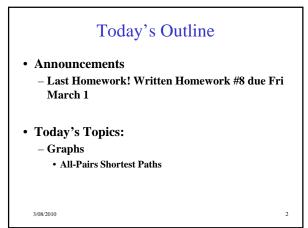
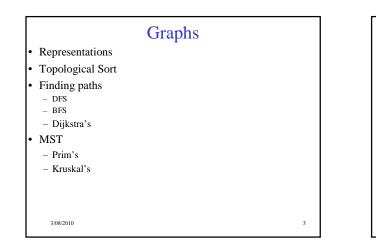
Graphs IV Chapter 9, 10.3 in Weiss

CSE 326 Data Structures Ruth Anderson





Single-Source Shortest Path

• Given a graph **G** = (V, E) and a single distinguished vertex **s**, find the shortest weighted path from **s** to every other vertex in **G**.

All-Pairs Shortest Path:

- Find the shortest paths between all pairs of vertices in the graph.
- How?

3/08/2010

Analysis

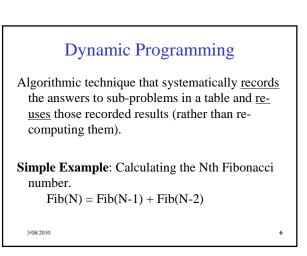
 Total running time for Dijkstra's: O(|V|² + |E|) (linear scan) O(|V| log |V| + |E| log |V|) (heaps)

What if we want to find the shortest path from each point to ALL other points?

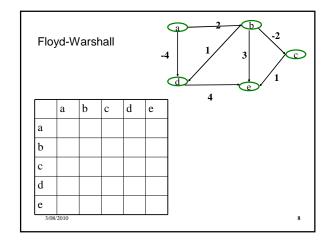
5

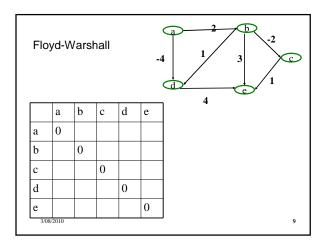
3/08/2010

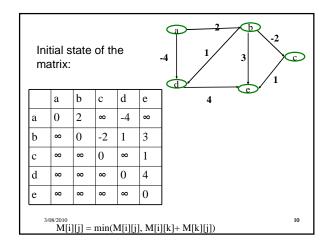
3/08/2010

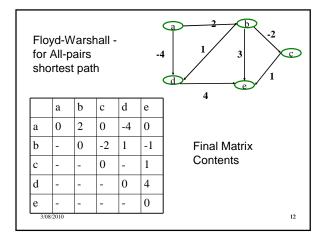


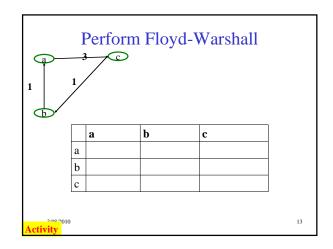
Floyd-Warshall for (int k = 1; k =< V; k++) for (int i = 1; i =< V; i++) for (int j = 1; j =< V; j++) if ((M[i][k]+ M[k][j]) < M[i][j]) M[i][j] = M[i][k]+ M[k][j] Invariant: After the kth iteration, the matrix includes the shortest paths for all pairs of vertices (i,j) containing only vertices 1..k as intermediate vertices 3082010</pre>











Transitive Closure

The transitive closure of a graph G=(V,E)Is the graph $G^* = (V, E^*)$ where

 $E^* = \{ (i,j) : \text{there is a } \underline{path} \text{ from vertex i to} \\ \text{vertex } j \text{ in } G \}$

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"All-pairs reachability"

3/08/2010