

Claim 1

if NFA $S = (Q, \Sigma, S_0, \delta)$

with $K > 2$ states \exists

equivalent $S' = (Q', \Sigma, S'_0, \delta', \delta^f)$

with $K - 1$ states

pick state $K \notin S_0, \delta^f$

$Q' := Q - \{q_K\}$

S'

$r_{ij} := S(q_i, q_j)$

$r'_{ij} = r_{ij} \cup r_{ik} r_{kk} r_{kj}$

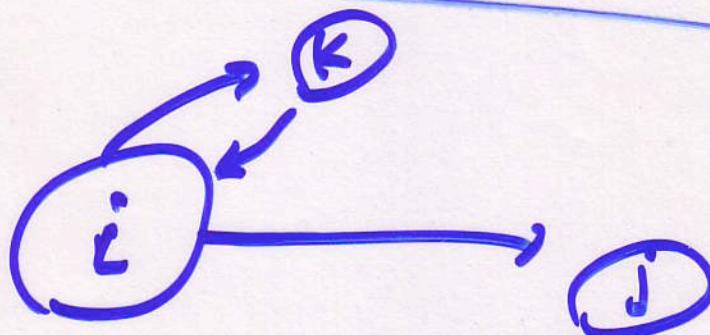
$\forall i, j \in Q'$

except $i \neq \text{final}$
 $j \neq \text{initial}$

Claim 2

$$L(r_{ij} \cup r_{ik}r_{kk^*}r_{kj})$$

$= \{x \mid \text{G could go from } i \text{ reading } x \text{ to } j \text{ without passing through any intermediate state except possibly } k\}$



Claim 3

G & G' are equivalent

Claim 4 \forall NFA \exists equiv. reg. expr.

Proof: NFA \rightarrow GNFA $\xrightarrow{\text{2-state}} \text{GNFA} \rightarrow \text{R.E.}$

by induction on k, using claim 1

Summary

- L is regular \Leftrightarrow
- $L = L(M)$ for some DFA M
 - $\hookrightarrow L = L(N) \dots$ NFA N
 - $\Rightarrow L = L(G) \dots$ GNFA/G
 - $\Leftrightarrow L = LCR \dots$ Reg. exp. R

Extended Regular Exp

~~cont~~ $((compl(r) \cup \cdot)^*)$

~~Write~~ Write a program that, when given a reg. language L decides whether $L = \emptyset$.
how?

$$(\emptyset \cdot \emptyset \cup \emptyset) \cdot a$$

$$T_{\text{Time}} \geq 2^{2^{2^{2^2}}} \quad \uparrow > \text{constant}$$

$$\begin{array}{c} 2 \\ 2^2 \\ 2^{2^2} \\ 2^{2^{2^2}} \\ 2^{2^{2^{2^2}}} \\ 2^{2^{2^{2^{2^2}}}} \end{array} \begin{array}{l} 16 \\ 65K \\ 2^{65} \\ \dots \\ 10^{20000} \end{array}$$

Imagine a computer the size of
a neutron ($\sim 10^{-15}$ meters diam.)
capable of 10^{15} operations per sec

Radii of visible universe

$\sim 10^{10}$ light-years

$\times \pi \times 10^7$ sec/yr

$\times 3 \times 10^8$ m/s (speed of light)

$\sim 10^{26}$ meters

Volume $\sim (10^{26})^3 = 10^{78} \text{ m}^3$

So packing visible universe with

these neutron-size computers

given $\sim \frac{10^{94}}{(10^{-15})^3} = 10^{123}$ processors

@ 10^{15} ops/sec $\times \pi \times 10^7$ sec/yr $\times 10^{10}$ yr

$\times 10^{123}$ processors $\sim 10^{155}$ ops

Since the dawn of time ...