

NFA

$$L \left(\begin{array}{c} \text{state} \xrightarrow{a, b, \dots} \text{state} \\ \text{state} \xrightarrow{\epsilon} \text{state} \end{array} \right) = \Sigma^*$$

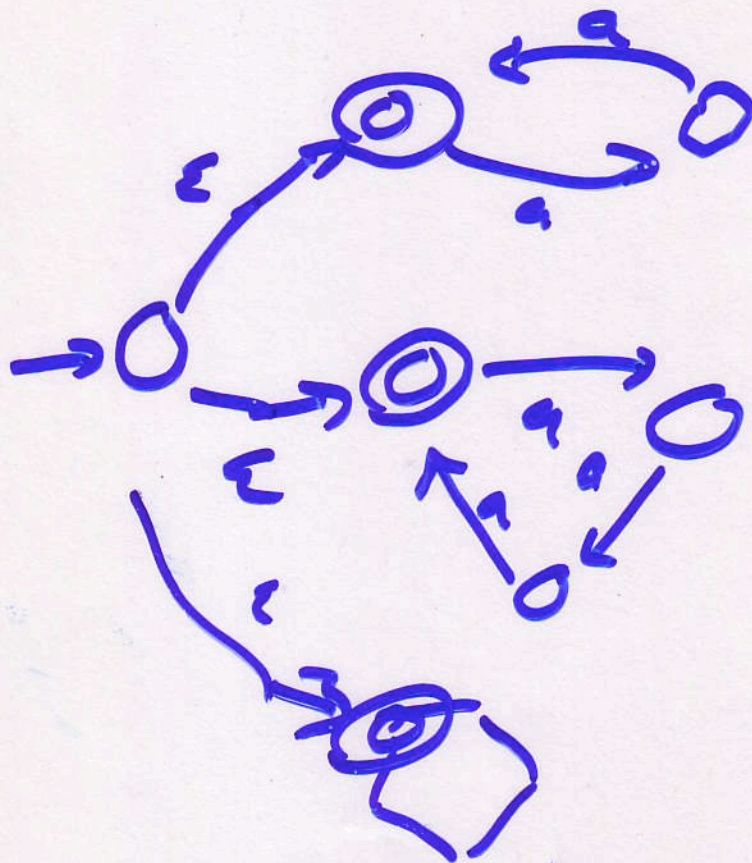
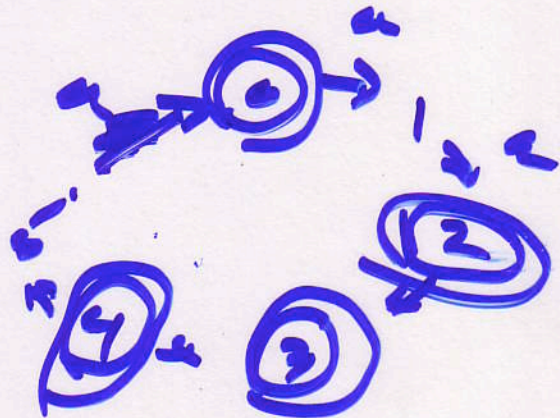
or 5

$$L = \{ a^n \mid n \text{ is a multiple of } 2 \text{ or } 3 \}$$

$$\Sigma = \{ a \}$$

$$L = L_2 \cup L_3 \cup L_5$$

$$L_2 = \{ a^n \mid 2 \mid n \}$$



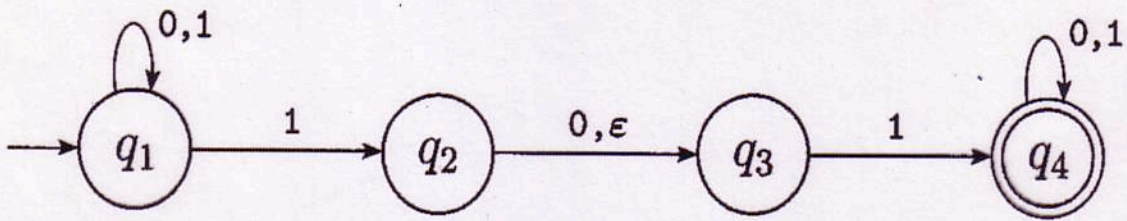


FIGURE 1.27

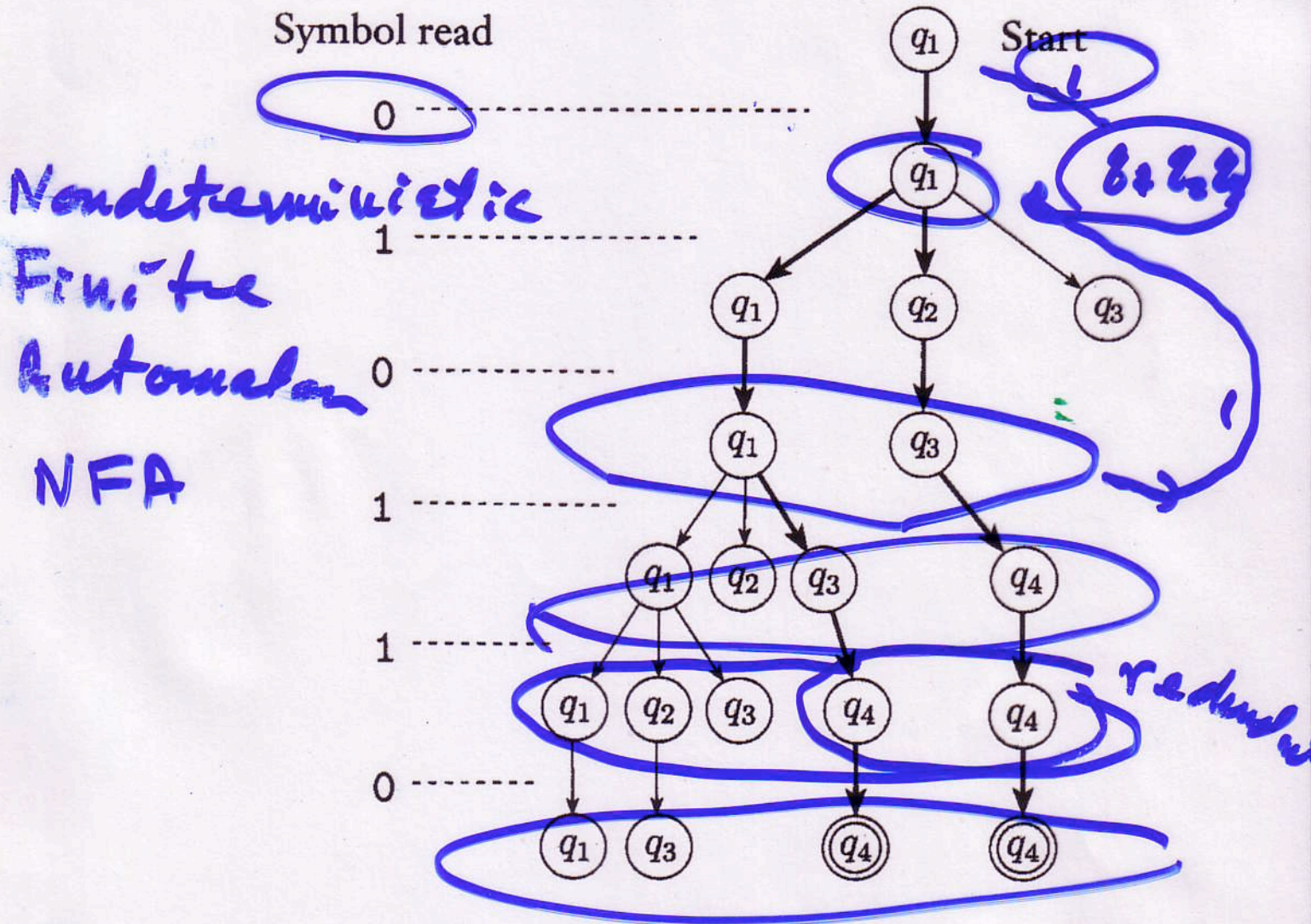
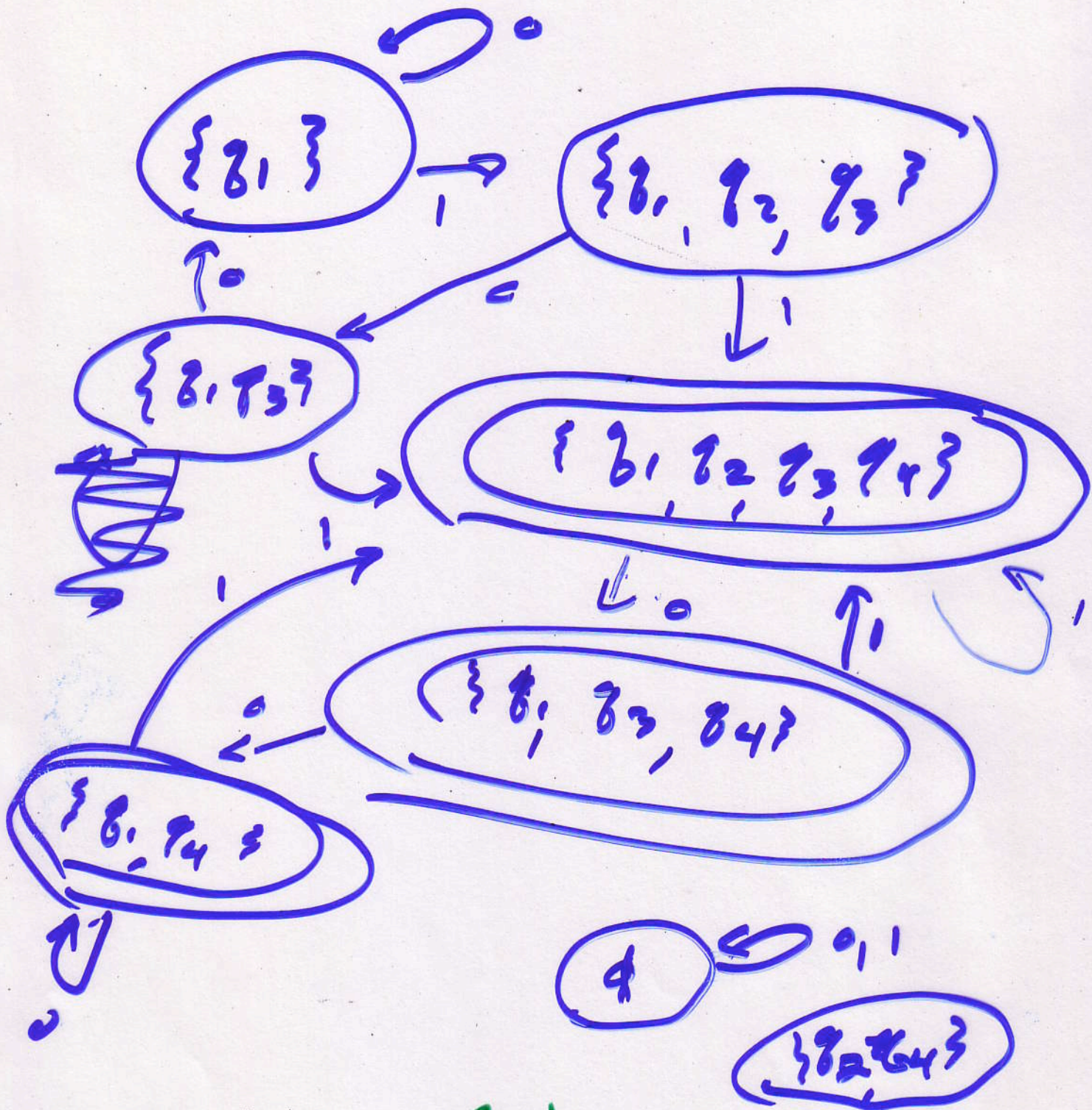


FIGURE 1.29



and 8 more: $2^4 = 16$

M_1 is equivalent to M_2 if

$$L(M_1) = L(M_2)$$

Thm 1.39 \forall nfa N \exists an equivalent DFA M .

$$N = (Q, \Sigma, \delta, q_0, F)$$

$$M = (Q', \Sigma, \delta', q_0', F')$$

no ϵ -moves

$$Q' = 2^Q$$

with ϵ

$$q_0' = \{q_0\}$$

$$q_0' = E(\{q_0\})$$

$$F' = \{R \subseteq Q \mid R \cap F \neq \emptyset\}$$

$$\forall a \in \Sigma, \forall R \subseteq Q$$

$$\delta'(R, a) = \bigcup_{r \in R} \delta(r, a)$$

$$\forall R \subseteq Q$$

$$E(R) = \{q \mid q \text{ reachable from}$$

some $r \in R$ by

one or more ϵ -moves