

CSE 322: Introduction to Formal Models in Computer Science  
Assignment #6  
November 16, 2005  
due: Wednesday, November 23

1. Let  $\Sigma = \{a, b, \#\}$ . Give a pushdown automaton for the language

$$\{u\#v \mid u, v \in \{a, b\}^* \text{ and } v^R \text{ is a substring of } u\}.$$

$v^R$  denotes the reversal of the string  $v$ . You should specify the transition function by giving the state diagram. You need not turn in a proof of correctness, though it would be good reassurance for yourself to do such a proof.

2. Give a pushdown automaton for the language

$$\{a^m b^n \mid n \leq m \leq 2n\}.$$

You should specify the transition function by giving the state diagram. You need not turn in a proof of correctness, though it would be good reassurance for yourself to do such a proof.

3. Use the procedure of Lemma 2.21 [1st Ed: Lemma 2.13] to convert the grammar  $G_3$  of Example 2.3 [1st Ed: Example 2.2] into an equivalent pushdown automaton  $M$ . You may use the shorthand allowing the automaton to push more than one symbol in a single step in your state diagram. Show an accepting computation of  $M$  on the input  $aababb$ , together with the corresponding derivation of this string in  $G_3$ .