

# CSE 322 Winter 2004

## Assignment #1

Due: Friday, January 16, 2004

**Reading assignment:** Read Sipser's book, sections 1.1 and 1.2; you should already have read Chapter 0.

### Problems:

1. We have only informally defined the reversal  $w^R$  of a string  $w$ . Formally, we can give the following inductive definition:

**Base case** If  $w = \epsilon$  then  $w^R = \epsilon$ .

**Inductive step** If  $w = va$  for  $v \in \Sigma^*$  and  $a \in \Sigma$  then  $w^R = av^R$ .

Prove by induction on the number of characters in  $y$  that for all strings  $x, y \in \Sigma^*$ ,  
 $(xy)^R = y^R x^R$ .

2. Sipser's book page 84, Exercise 1.3
3. Sipser's book page 84, Exercise 1.4. Parts (a), (b), (c), (d), (e), (f), (i), (l).  
As documentation for your DFAs, for each state write a very brief description of the set of strings that reach each state.
4. Do the same as Exercise 1.4 Part (d), but do it for those strings that have a 0 in the third from last position rather than in the third position.
5. For Example 1.4 in the text, write out the sequence of states that machine  $M_4$  goes through in computing on input string  $abaab$  and for input string  $bbaab$ .