# RNA Search and Motif Discovery

CSEP 590A Summer 2006

#### The Human Parts List, circa 2001

3 billion nucleotides, containing:

- •25,000 protein-coding genes (only ~1% of the DNA)
- •Messenger RNAs made from each
- •Plus a double-handful of other RNA genes

#### **Outline**

Whirlwind tour of ncRNA search & discovery

Covariance Model Review

Algorithms for Training

"Mutual Information"

Algorithms for searching

Rigorous & heuristic filtering

Motif discovery

Wrap up

Course Evals



#### Noncoding RNAs

Dramatic discoveries in last 5 years

100s of new families

Many roles: Regulation, transport, stability, catalysis, ...

1% of DNA codes for protein, but 30% of it is copied into RNA, i.e. ncRNA >> mRNA

# "RNA sequence analysis using covariance models"

Eddy & Durbin

Nucleic Acids Research, 1994
vol 22 #11, 2079-2088
(see also, Ch 10 of Durbin et al.)

#### What

A probabilistic model for RNA families

The "Covariance Model"

≈ A Stochastic Context-Free Grammar

A generalization of a profile HMM

Algorithms for Training

From aligned or unaligned sequences

Automates "comparative analysis"

Complements Nusinov/Zucker RNA folding

Algorithms for searching

#### Main Results

Very accurate search for tRNA
(Precursor to tRNAscanSE - current favorite)
Given sufficient data, model construction
comparable to, but not quite as good as,
human experts
Some quantitative info on importance of
pseudoknots and other tertiary features

#### Probabilistic Model Search

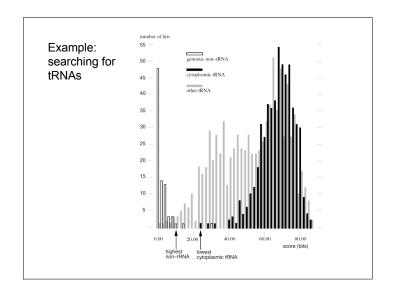
As with HMMs, given a sequence, you calculate likelihood ratio that the model could generate the sequence, vs a background model

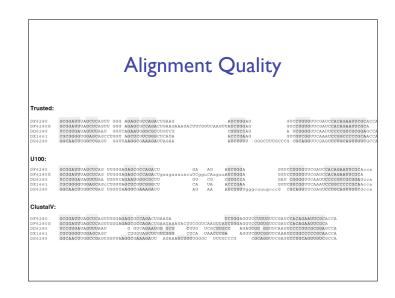
You set a score threshold

Anything above threshold → a "hit"

Scoring:

"Forward" / "Inside" algorithm - sum over all paths Viterbi approximation - find single best path (Bonus: alignment & structure prediction)





# Comparison to TRNASCAN

Fichant & Burks - best heuristic then 97.5% true positive 0.37 false positives per MB

CM A1415 (trained on trusted alignment)

> 99.98% true positives

<0.2 false positives per MB

Current method-of-choice is "tRNAscanSE", a CM-based scan with heuristic pre-filtering (including TRNASCAN?) for performance reasons.

#### **Profile Hmm Structure**

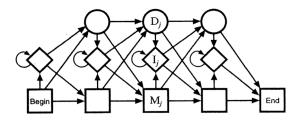


Figure 5.2 The transition structure of a profile HMM.

M<sub>j</sub>: Match states (20 emission probabilities)

Ij: Insert states (Background emission probabilities)

D<sub>j</sub>: Delete states (silent - no emission)

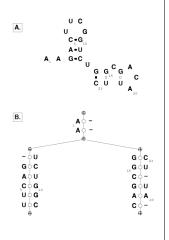
#### **CM** Structure

A: Sequence + structure

B: the CM "guide tree"

C: probabilities of letters/ pairs & of indels

Think of each branch being an HMM emitting both sides of a helix (but 3' side emitted in reverse order)

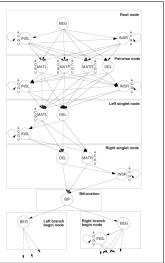


### Overall CM Architecture

One box ("node") per node of guide tree

BEG/MATL/INS/DEL just like an HMM

MATP & BIF are the key additions: MATP emits *pairs* of symbols, modeling basepairs; BIF allows multiple helices



## CM Viterbi Alignment

 $x_i = i^{th}$  letter of input

 $x_{ii}$  = substring i,...,j of input

 $T_{yz} = P(\text{transition } y \rightarrow z)$ 

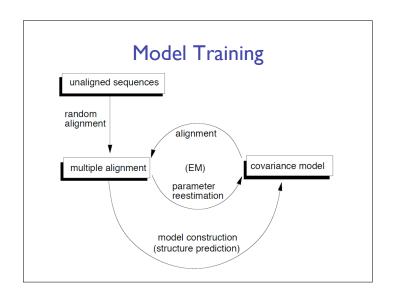
 $E_{x_i,x_i}^y = P(\text{emission of } x_i, x_j \text{ from state } y)$ 

 $S_{ii}^{y} = \max_{\pi} \log P(x_{ii} \text{ gen'd starting in state } y \text{ via path } \pi)$ 

$$S_{ij}^{y} = \max_{\pi} \log P(x_{ij} \text{ generated starting in state } y \text{ via path } \pi)$$

$$S_{ij}^{y} = \begin{cases} \max_{\pi} [S_{i+1,j-1}^{z} + \log T_{yz} + \log E_{x_{i},x_{j}}^{y}] & \text{match pair } \\ \max_{z} [S_{i+1,j}^{z} + \log T_{yz} + \log E_{x_{i}}^{y}] & \text{match/insert left } \\ \max_{z} [S_{i,j-1}^{z} + \log T_{yz} + \log E_{x_{j}}^{y}] & \text{match/insert right } \\ \max_{z} [S_{i,j}^{z} + \log T_{yz}] & \text{delete } \\ \max_{i < k \le j} [S_{i,k}^{y_{left}} + S_{k+1,j}^{y_{right}}] & \text{bifurcation} \end{cases}$$

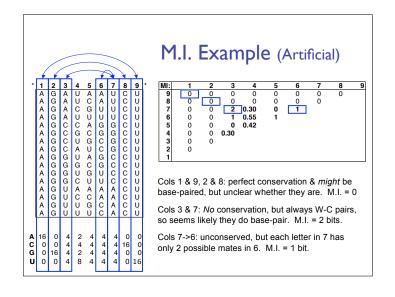
$$\text{Time O(qn^{3}), q states, seq len n}$$

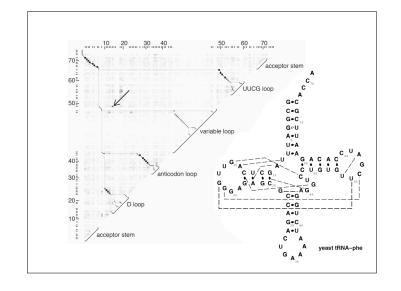


#### **Mutual Information**

$$M_{ij} = \sum_{xi,xj} f_{xi,xj} \log_2 \frac{f_{xi,xj}}{f_{xi}f_{xi}}; \quad 0 \le M_{ij} \le 2$$

Max when *no* seq conservation but perfect pairing MI = expected score gain from using a pair state Finding optimal MI, (i.e. opt pairing of cols) is hard(?) Finding optimal MI *without pseudoknots* can be done by dynamic programming





#### MI-Based Structure-Learning

Find best (max total MI) subset of column pairs among i...j, subject to absence of pseudo-knots

$$S_{i,j} = \max \begin{cases} S_{i,j-1} \\ \max_{i \leq k < j-4} S_{i,k-1} + M_{k,j} + S_{k+1,j-1} \end{cases}$$

"Just like Nussinov/Zucker folding"

BUT, need enough data---enough sequences at right phylogenetic distance

|       |                         |            | score  | alignment |
|-------|-------------------------|------------|--------|-----------|
| Model | training set            | iterations | (bits) | accuracy  |
| A1415 | all sequences (aligned) | 3          | 58.7   | 95%       |
| A100  | SIM100 (aligned)        | 3          | 57.3   | 94%       |
| A65   | SIM65 (aligned)         | 3          | 46.7   | 93%       |
| U100  | SIM100 (degapped)       | 23         | 56.7   | 90%       |
| U65   | SIM65 (degapped)        | 29         | 47.2   | 91%       |

Table 2: Training and multiple alignment results from models trained from the trusted alignments (A models) and models trained from no prior knowledge of tRNA (U models).

# Pseudoknots disallowed allowed $(\sum_{i=1}^n \max_j M_{i,j})/2$

|         | Aver | Min | May  | ClustalV | 1º info | 2º info   |
|---------|------|-----|------|----------|---------|-----------|
| Dataset |      |     |      | accuracy |         | (bits)    |
| TEST    |      |     | 1.00 |          | 43.7    | 30.0-32.3 |
| SIM100  |      |     | .986 |          | 39.7    | 30.5-32.7 |
| SIM65   |      |     | .685 |          | 31.8    | 28.6-30.7 |

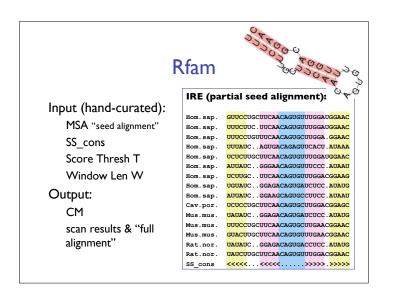
Table 1: Statistics of the training and test sets of 100 tRNA sequences each. The average identity in an alignment is the average pairwise identity of all aligned symbol pairs, with gap/symbol alignments counted as mismatches. Primary sequence information content is calculated according to [48]. Calculating pairwise mutual information content is an NP-complete problem of finding an optimum partition of columns into pairs. A lower bound is calculated by using the model construction procedure to find an optimal partition subject to a non-pseudoknotting restriction. An upper bound is calculated as sum of the single best pairwise covariation for each position, divided by two; this includes all pairwise tertiary interactions but overcounts because it does not guarantee a disjoint set of pairs. For the meaning of multiple alignment accuracy of ClustalV, see the text.

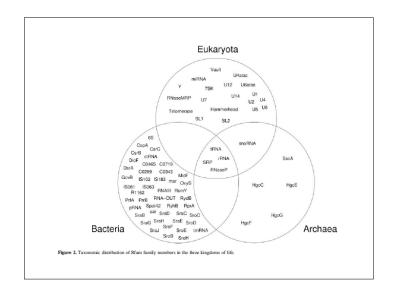
# Rfam – an RNA family DB

Griffiths-Jones, et al., NAR '03,'05

Biggest scientific computing user in Europe - 1000 cpu cluster for a month per release Rapidly growing:

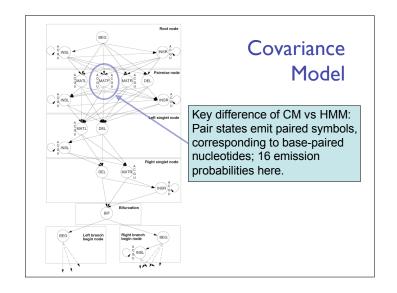
Rel 1.0, 1/03: 25 families, 55k instances Rel 7.0, 3/05: 503 families, >300k instances

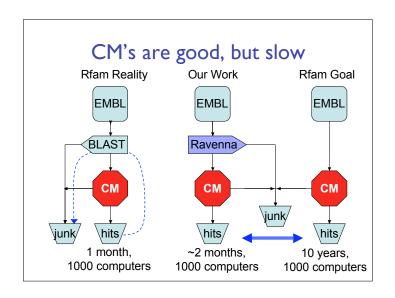


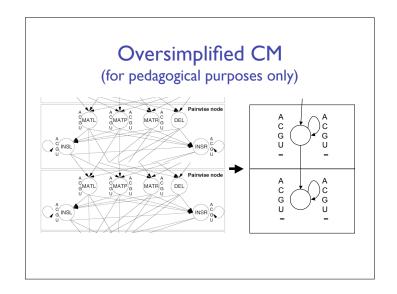


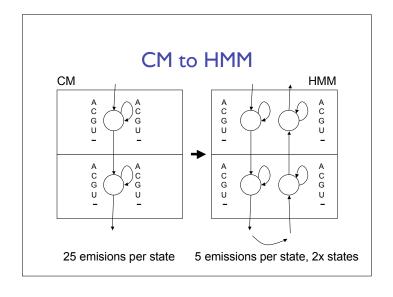
# Faster Genome Annotation of Non-coding RNAs Without Loss of Accuracy

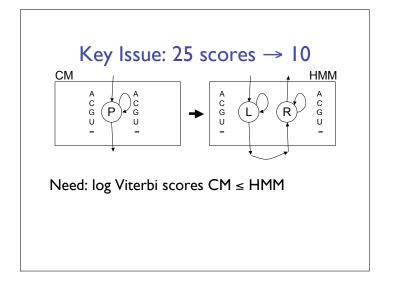
Zasha Weinberg & W.L. Ruzzo Recomb '04, ISMB '04, Bioinfo '06











### Viterbi/Forward Scoring

Path π defines transitions/emissions Score( $\pi$ ) = product of "probabilities" on  $\pi$ NB: ok if "probs" aren't, e.g.  $\Sigma \neq 1$ (e.g. in CM, emissions are odds ratios vs Oth-order background)

For any nucleotide sequence x:

Viterbi-score(x) =  $max{score(\pi) | \pi emits x}$ 

# Forward-score(x) = $\Sigma$ { score( $\pi$ ) | $\pi$ emits x}

# Rigorous Filtering

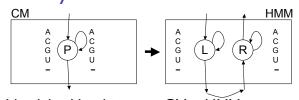
Any scores satisfying the linear inequalities give rigorous filtering

#### Proof:

CM Viterbi path score

- ≤ "corresponding" HMM path score
- ≤ Viterbi HMM path score (even if it does not correspond to any CM path)

# Key Issue: 25 scores $\rightarrow$ 10



#### Need: log Viterbi scores CM ≤ HMM

$$\begin{aligned} & P_{AA} \leq L_{A} + R_{A} & P_{CA} \leq L_{C} + R_{A} & ... \\ & P_{AC} \leq L_{A} + R_{C} & P_{CC} \leq L_{C} + R_{C} & ... \\ & P_{AG} \leq L_{A} + R_{G} & P_{CG} \leq L_{C} + R_{G} & ... \\ & P_{AU} \leq L_{A} + R_{U} & P_{CU} \leq L_{C} + R_{U} & ... \\ & P_{A-} \leq L_{A} + R_{-} & P_{C-} \leq L_{C} + R_{-} & ... \end{aligned}$$

#### Some scores filter better

$$P_{UA} = I \le L_U + R_A$$

$$P_{UG} = 4 \le L_U + R_G$$

Option I:  

$$L_U = R_A = R_G = 2$$

Option 2: 
$$L_{11} = 0$$
,  $R_{A} = 1$ ,  $R_{C} = 4$ 

Assuming ACGU 
$$\approx$$
 25%

Option I:

 $L_U = R_A = R_G = 2$ 
 $L_U + (R_A + R_G)/2 = 4$ 

Option 2: Opt 2: 
$$L_U = 0, R_A = 1, R_G = 4$$
  $C_U + (R_A + R_G)/2 = 2.5$ 

### **Optimizing filtering**

For any nucleotide sequence x:

Viterbi-score(x) = max{ score( $\pi$ ) |  $\pi$  emits x }

Forward-score(x) =  $\Sigma$ { score( $\pi$ ) |  $\pi$  emits x }

**Expected Forward Score** 

 $E(L_i, R_i) = \sum_{\text{all sequences } x} Forward\text{-score}(x) *Pr(x)$ 

NB: E is a function of L<sub>i</sub>, R<sub>i</sub> only

Under 0th-order background model

Optimization:

Minimize  $E(L_i, R_i)$  subject to score Lin.Ineq.s

This is heuristic ("forward $\downarrow \Rightarrow Viterbi \downarrow \Rightarrow filter \downarrow$ ")

But still rigorous because "subject to score Lin.Ineq.s"

### Calculating E(L<sub>i</sub>, R<sub>i</sub>)

 $E(L_i, R_i) = \sum_{x} Forward-score(x)*Pr(x)$ 

Forward-like: for every state, calculate expected score for all paths ending there, easily calculated from expected scores of predecessors & transition/emission probabilities/scores

# Minimizing $E(L_i, R_i)$

Calculate  $E(L_i, R_i)$  symbolically, in terms of emission scores, so we can do partial derivatives for numerical convex optimization algorithm

$$\frac{\partial E(L_1, L_2, ...)}{\partial L_i}$$

# Estimated Filtering Efficiency (139 Rfam 4.0 families)

| `                  |                         | ,                        |         |
|--------------------|-------------------------|--------------------------|---------|
| Filtering fraction | # families<br>(compact) | # families<br>(expanded) |         |
| < 10-4             | 105                     | 110                      | ~100x   |
| 10-4 - 10-2        | 8                       | 17                       | speedup |
| .0110              | 11                      | 3                        |         |
| .1025              | 2                       | 2                        |         |
| .2599              | 6                       | 4                        |         |
| .99 - 1.0          | 7                       | 3                        |         |

#### Results: New ncRNA's?

| Name                  | # found<br>BLAST<br>+ CM | # found<br>rigorous filter<br>+ CM | # new |
|-----------------------|--------------------------|------------------------------------|-------|
| Pyrococcus snoRNA     | 57                       | 180                                | 123   |
| Iron response element | 201                      | 322                                | 121   |
| Histone 3' element    | 1004                     | 1106                               | 102   |
| Purine riboswitch     | 69                       | 123                                | 54    |
| Retron msr            | 11                       | 59                                 | 48    |
| Hammerhead I          | 167                      | 193                                | 26    |
| Hammerhead III        | 251                      | 264                                | 13    |
| U4 snRNA              | 283                      | 290                                | 7     |
| S-box                 | 128                      | 131                                | 3     |
| U6 snRNA              | 1462                     | 1464                               | 2     |
| U5 snRNA              | 199                      | 200                                | 1     |
| U7 snRNA              | 312                      | 313                                | I     |

#### Results: With additional work

|                        | # with<br>BLAST+CM | # with rigorous filter series + CM | # new |  |  |
|------------------------|--------------------|------------------------------------|-------|--|--|
| Rfam tRNA              | 58609              | 63767                              | 5158  |  |  |
| Group II intron        | 5708               | 6039                               | 331   |  |  |
| tRNAscan-SE<br>(human) | 608                | 729                                | 121   |  |  |
| tmRNA                  | 226                | 247                                | 21    |  |  |
| Lysine riboswitch      | 60                 | 71                                 | 11    |  |  |
| And more               |                    |                                    |       |  |  |

#### "Additional work"

#### Profile HMM filters use no 2ary structure info

They work well because, tho structure can be critical to function, there is (usually) enough primary sequence conservation to exclude most of DB

But not on all families (and may get worse?)

#### Can we exploit some structure (quickly)?

Idea I: "sub-CM"

for some hairpins

Idea 2: extra HMM states remember mate

Idea 3: try lots of combinations of "some hairpins"

Idea 4: chain together several filters (select via Dijkstra)

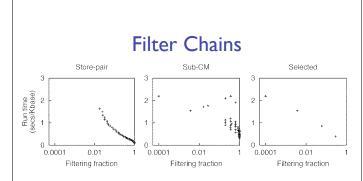


Fig. 2. Filter creation and selection. Filters for Rfam tRNA (RF00005) generated by the store-pair and sub-CM techniques and those selected for actual filtering are plotted by filtering fraction and run time. The CM runs at 3.5 secs/kbase. The four selected filters are run one after another, from highest to lowest fraction.

#### Heuristic Filters

Rigorous filters optimized for worst case Possible to trade improved speed for small loss in sensitivity?

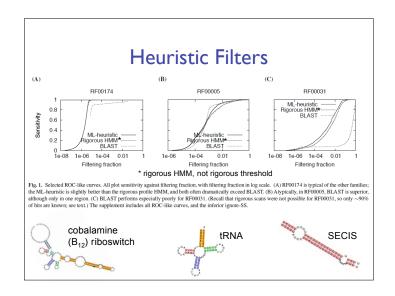
Yes – profile HMMs as before, but optimized for average case

"ML heuristic": train HMM from the infinite alignment generated by the CM

Often 10x faster, modest loss in sensitivity

### Cmfinder--A Covariance Model Based RNA Motif Finding Algorithm Bioinformatics, 2006, 22(4): 445-452

Zizhen Yao Zasha Weinberg Walter L. Ruzzo University of Washington, Seattle



## Searching for noncoding RNAs

CM's are great, but where do they come from?

An approach: comparative genomics

Search for motifs with common secondary structure in a set of functionally related sequences.

#### Challenges

Three related tasks

Locate the motif regions.

Align the motif instances.

Predict the consensus secondary structure.

Motif search space is huge!

Motif location space, alignment space, structure space.

#### **Approaches**

Align sequences, then look for common structure

Predict structures, then try to align them Do both together

# First approach Structural conservation ≠ Sequence conservation Alignment without structure information is unreliable CLUSTALW alignment of SECIS elements with flanking regions

Pitfall for sequence-alignment-

same-colored boxes should be aligned

## **Approaches**

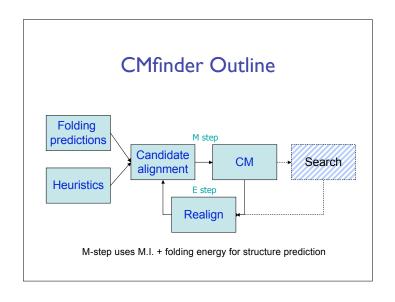
Align sequences, then look for common structure

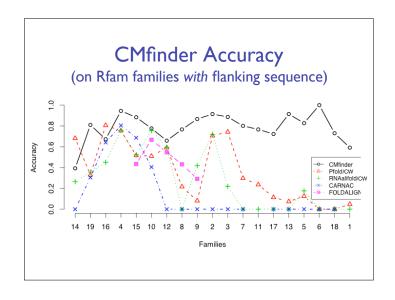
Predict structures, then try to align them single-seq struct prediction only ~ 60% accurate; exacerbated by flanking seq; no biologically-validated model for structural alignment

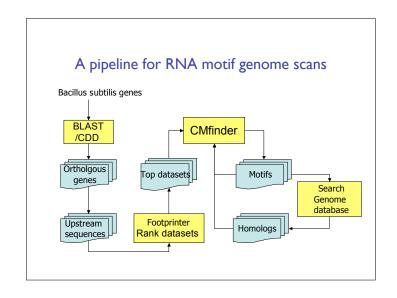
Do both together
Sankoff – good but slow
Heuristic

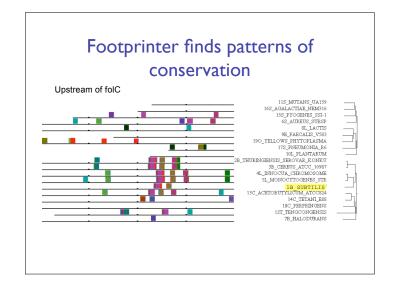
## Design Goals

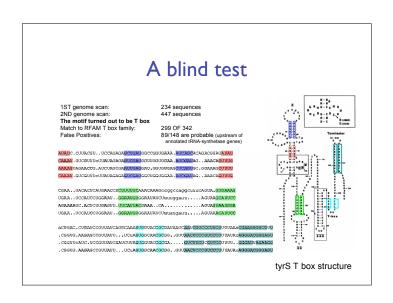
Find RNA motifs in unaligned sequences
Seq conservation exploited, but not required
Robust to inclusion of unrelated sequences
Robust to inclusion of flanking sequence
Reasonably fast and scalable
Produce a probabilistic model of the motif
that can be directly used for homolog search

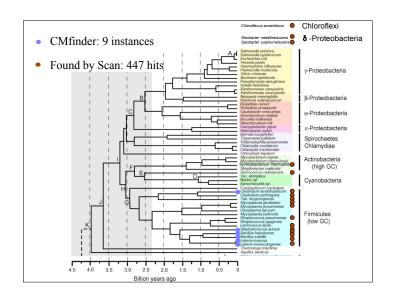


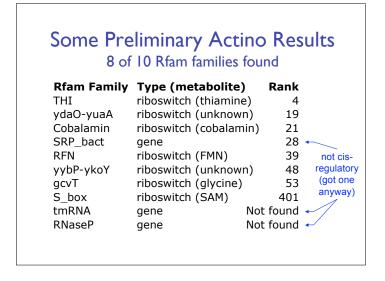


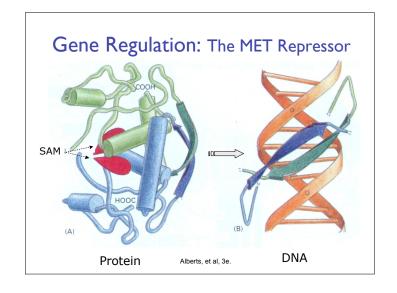


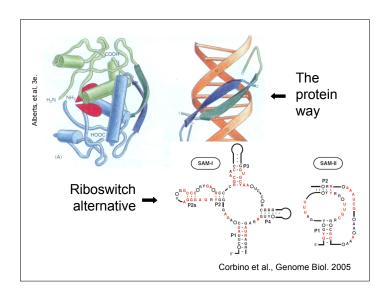












#### More Prelim Actino Results

Many others (not in Rfam) are likely real of top 50:

| known (Rfam, 23S)                        | 10 |
|--|----|
| probable (Tbox, CIRCE, LexA, parP, pyrR) | 7  |
| probable (ribosomal genes)               | 9  |
| potentially interesting                  | 12 |
| unknown or poor                          | 12 |

One bench-verified, 2 more in progress

#### Preliminary results of genome scan

Top 115 datasets (some are redundant)
13 T box, 22 riboswitches, 30 ribosomal genes
RNase P, tRNA, CIRCE elements and other DNA binding sites

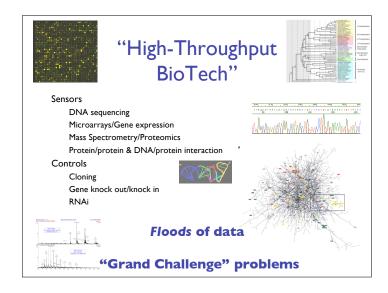
| Gene |    |     | RFAM      |     | #full | #TP | specificity |       |
|------|----|-----|-----------|-----|-------|-----|-------------|-------|
| metK | 13 | 150 | S_box     | 71  | 151   | 145 | 0.967       | 0.960 |
| ribB | 9  | 106 | RFN       | 48  | 114   | 97  | 0.915       | 0.851 |
| folC | 9  | 447 | T_box     | 67  | 342   | 299 | 0.669       | 0.874 |
| xpt  | 14 | 106 | Purine    | 37  | 100   | 97  | 0.915       | 0.970 |
| glmS | 16 | 33  | glmS      | 14  | 37    | 33  | 1.000       | 0.892 |
| thiA | 16 | 305 | THI       | 237 | 366   | 305 | 1.000       | 0.833 |
| ykoY | 10 | 34  | yybP-ykoY | 74  | 127   | 33  | 0.971       | 0.260 |

# Summary

ncRNA - apparently widespread, much interest Covariance Models - powerful but expensive tool for ncRNA motif representation, search, discovery Rigorous/Heuristic filtering - typically 100x speedup in search with no/little loss in accuracy CMfinder - CM-based motif discovery in unaligned sequences

#### Course Wrap Up

What is DNA? RNA?
How many Amino Acids are there?
Did human beings, as we know them, develop from earlier species of animals?
What are stem cells?
What did Viterbi invent?
What is dynamic programming?
What is a likelihood ratio test?
What is the EM algorithm?
How would you find the maximum of f(x) = ax³ + bx² + cx +d in the interval -10<x<25?



#### **CS** Points of Contact

#### Scientific visualization

Gene expression patterns

#### **Databases**

Integration of disparate, overlapping data sources

Distributed genome annotation in face of shifting underlying coordinates

#### AI/NLP/Text Mining

Information extraction from journal texts with inconsistent nomenclature, indirect interactions, incomplete/inaccurate models,...

#### Machine learning

System level synthesis of cell behavior from low-level heterogeneous data (DNA sequence, gene expression, protein interaction, mass spec,

#### Algorithms

• • •

## Frontiers & Opportunities

#### New data:

Proteomics, SNP, arrays CGH, comparative sequence information, methylation, chromatin structure, ncRNA, interactome

New methods:

graphical models? rigorous filtering?

Data integration

many, complex, noisy sources

# **Exciting Times**

Lots to do
Various skills needed
I hope I've given you a taste of it

## Frontiers & Opportunities

#### Open Problems:

splicing, alternative splicing
multiple sequence alignment (genome scale, w/ RNA etc.)
protein & RNA structure
interaction modeling
network models
RNA trafficing
ncRNA discovery

• • •

#### Thanks!