Anti-aliasing and Monte Carlo Path Tracing

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Reading

Required:

Marschner and Shirley, Section 13.4 (online handout)

Further reading:

- Pharr, Jakob, and Humphreys, Physically Based Ray Tracing: From Theory to Implementation, Chapter 13
- A. Glassner. An Introduction to Ray Tracing. Academic Press, 1989.
- Robert L. Cook, Thomas Porter, Loren Carpenter. "Distributed Ray Tracing." Computer Graphics (Proceedings of SIGGRAPH 84). 18 (3). pp. 137-145. 1984.
- James T. Kajiya. "The Rendering Equation." Computer Graphics (Proceedings of SIGGRAPH 86). 20 (4). pp. 143-150. 1986.

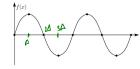
Aliasing

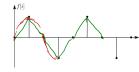
Ray tracing is a form of sampling and can suffer from annoying visual artifacts...

Consider a continuous function f(x). Now sample it at intervals Δ to give $f[i] = \text{quantize}[f(i \Delta)]$.

Q: How well does f[i] approximate f(x)?

Consider sampling a sinusoid:

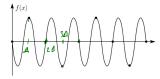




In this case, the sinusoid is reasonably well approximated by the samples.

Aliasing (con't)

Now consider sampling a higher frequency sinusoid





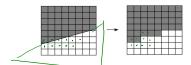
We get the exact same samples, so we seem to be approximating the first lower frequency sinusoid again.

We say that, after sampling, the higher frequency sinusoid has taken on a new "alias", i.e., changed its identity to be a lower frequency sinusoid.

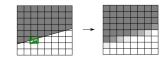
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Aliasing and anti-aliasing in rendering

One of the most common rendering artifacts is the "jaggies". Consider rendering a white polygon against a black background:



We would instead like to get a smoother transition:



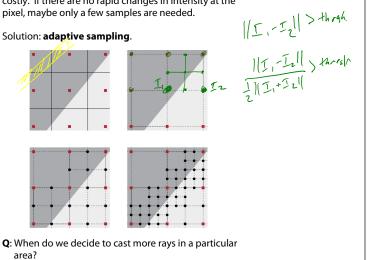
Anti-aliasing is the process of removing high frequencies before they cause aliasing.

In a renderer, computing the average color within a pixel is a good way to anti-alias. How exactly do we compute the average color?

Antialiasing by adaptive sampling

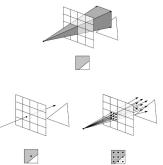
Casting many rays per pixel can be unnecessarily costly. If there are no rapid changes in intensity at the pixel, maybe only a few samples are needed.

Solution: adaptive sampling.



Antialiasing in a ray tracer

We would like to compute the average intensity in the neighborhood of each pixel.

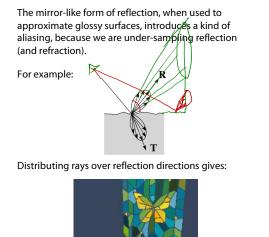


When casting one ray per pixel, we are likely to have aliasing artifacts.

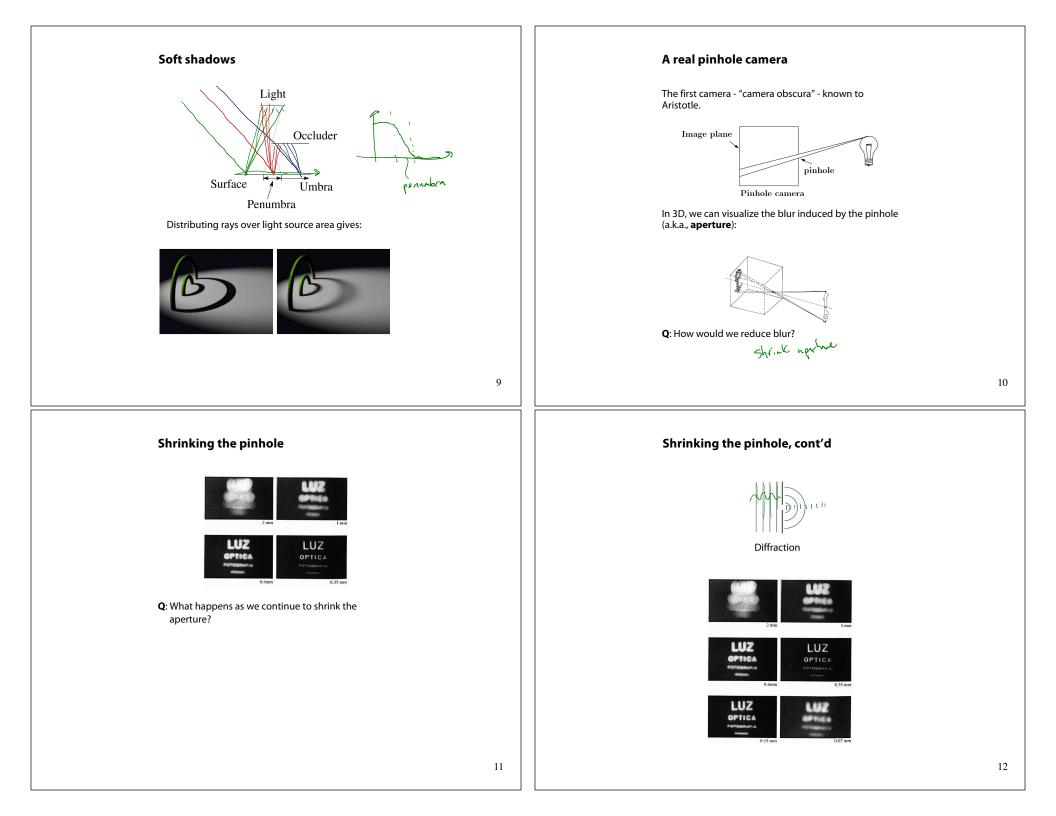
To improve matters, we can cast more than one ray per pixel and average the result.

A.k.a., super-sampling and averaging down.

Gloss and translucency



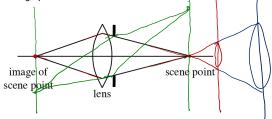




Lenses to focus light

A lens can capture a sharp image of an object *without* using a tiny aperture, allowing for shorter exposure times.

It does this by refracting (focusing) a cone of rays emanating from a scene point down to a single image point:



For a given image *plane*, there is a parallel object plane that is kept in focus.

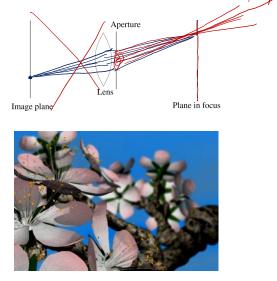
The wider the aperture, the more light collected, allowing for shorter exposure times, but there is a trade-off...

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Depth of field (cont'd)

To simulate depth of field, we can model the refraction of light through a lens. Objects close to the in-focus plane are sharp, and the rest is blurry.



Depth of field

A significant limitation (or perhaps desirable artistic effect O) of lenses is the fact that points that are not in the object plane appear out of focus.

The **depth of field** of a camera is a measure of how far from the object plane points can be before appearing "too blurry."

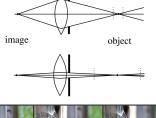




Image credit: http://www.cambridgeincolour.com/tutorials/depth-of-field.htm

Depth of field (cont'd)

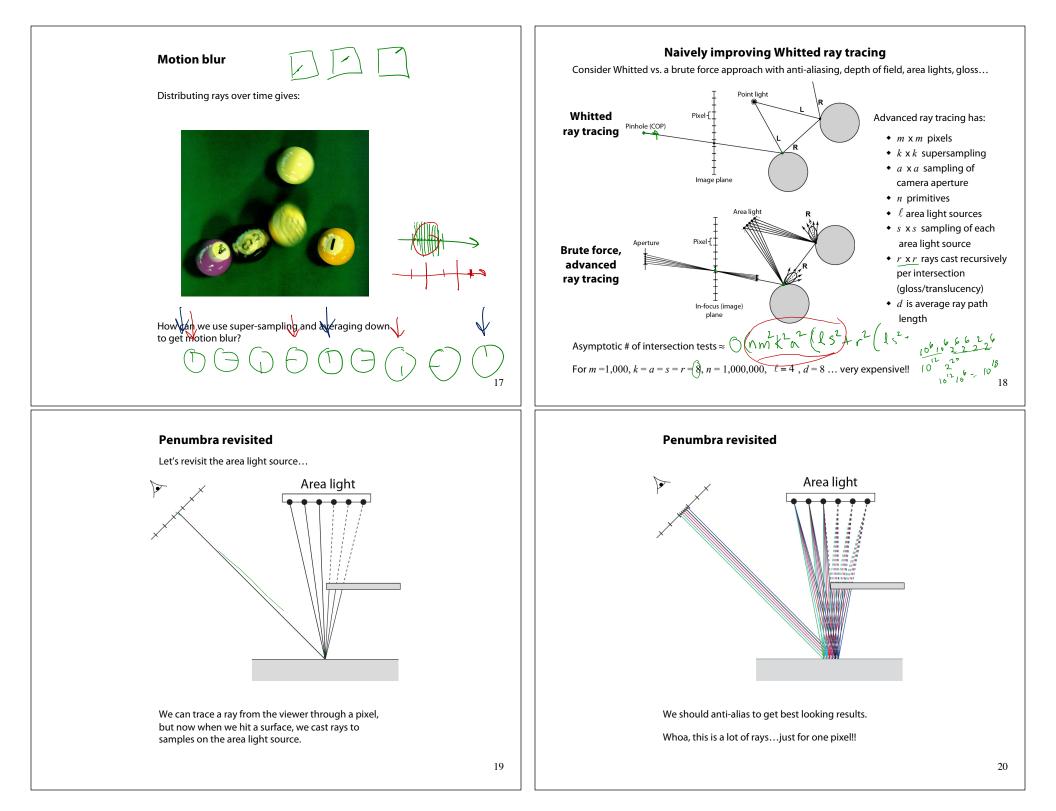
Neat idea: we can think of this as a generalization of the graphics pinhole model:

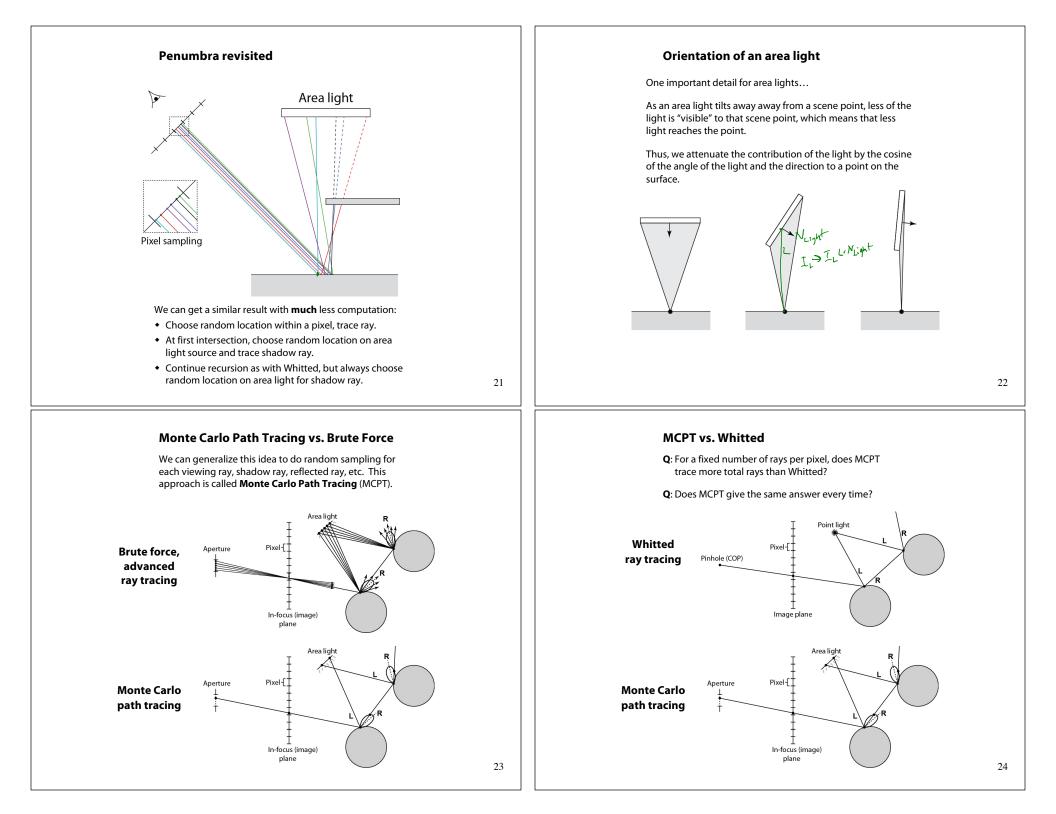


Image plane

But now:

- Put the image plane at the depth you want to be in focus.
- Treat the aperture as multiple COPs (samples across the aperture).
- For each pixel, trace multiple viewing primary rays for each COP and average the results Aperture





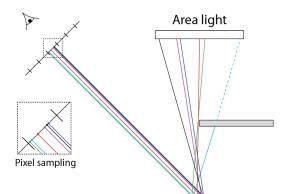
Ray tracing as integration

Ray tracing amounts to estimating a multidimensional integral at each pixel. The integration is over:

- the pixel area
- the aperture
- each light source
- all diffuse/glossy reflections (recursively)

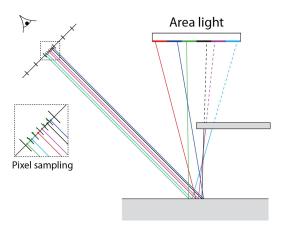
MCPT images are often noisy. We can reduce noise by being smarter about which rays we cast...

Penumbra revisited: clumped samples



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Penumbra: stratified sampling

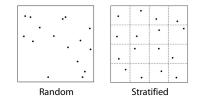


Stratified sampling gives a better distribution of samples:

- Break pixel and light source into regions.
- Choose random locations within each region.
- Trace rays through/to those jittered locations.

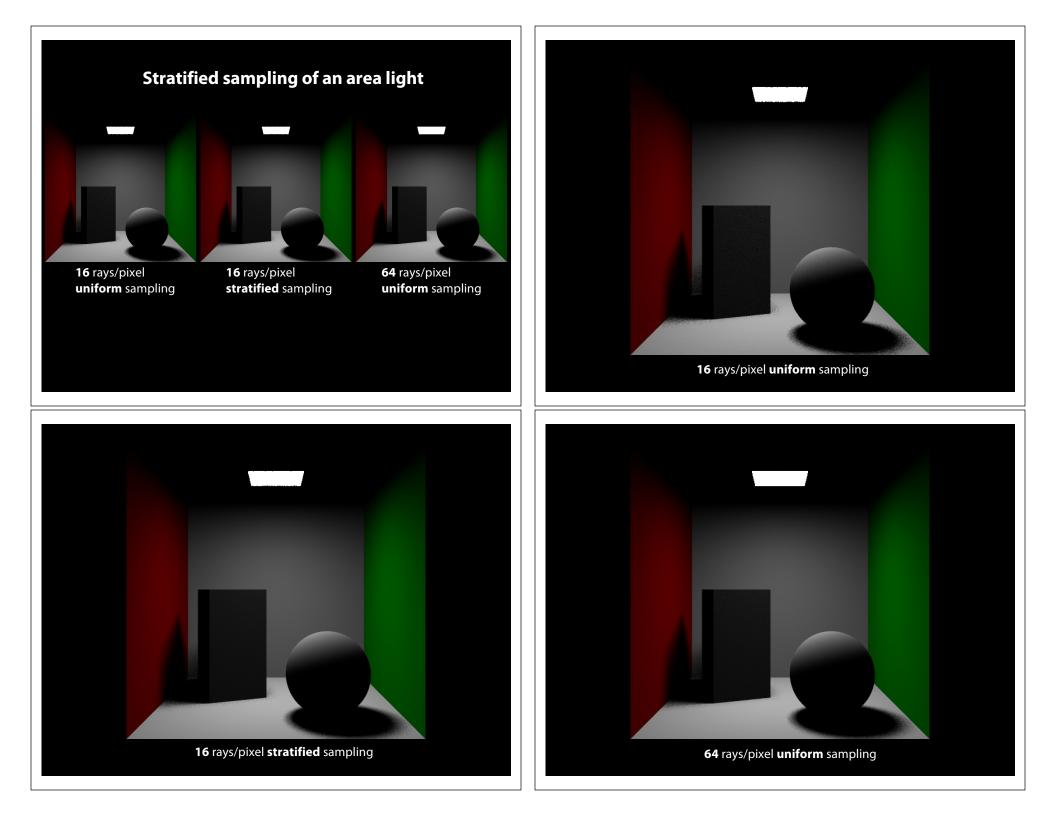
Stratified sampling of a 2D pixel

Here we see pure uniform vs. stratified sampling over a 2D pixel (here 16 rays/pixel):



The stratified pattern on the right is also sometimes called a **jittered** sampling pattern.

Similar grids can be constructed over the camera aperture, light sources, and diffuse/glossy reflection directions.

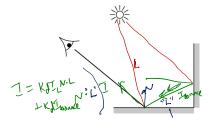


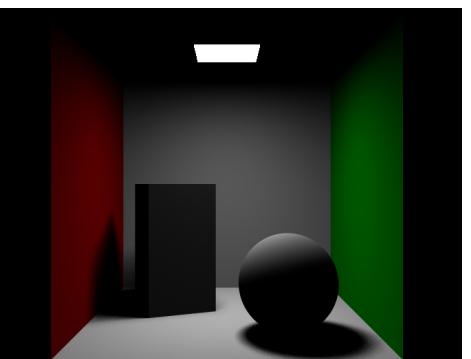
Integration over reflection

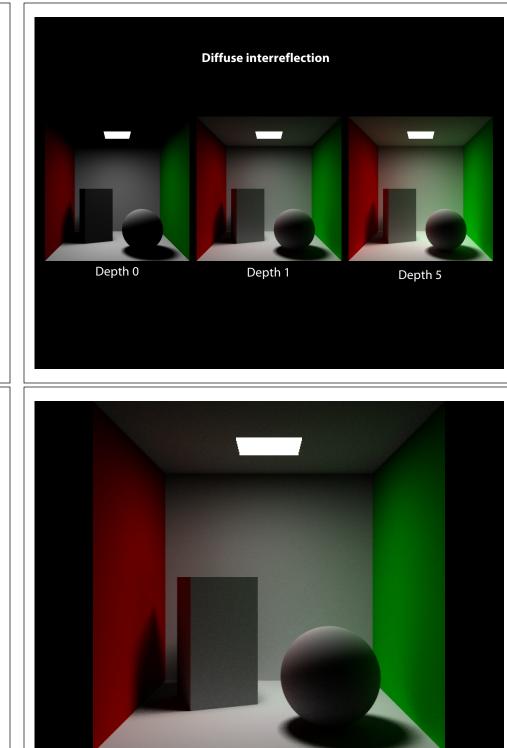
As described earlier, we can also reflect rays in directions away from ideal reflection.

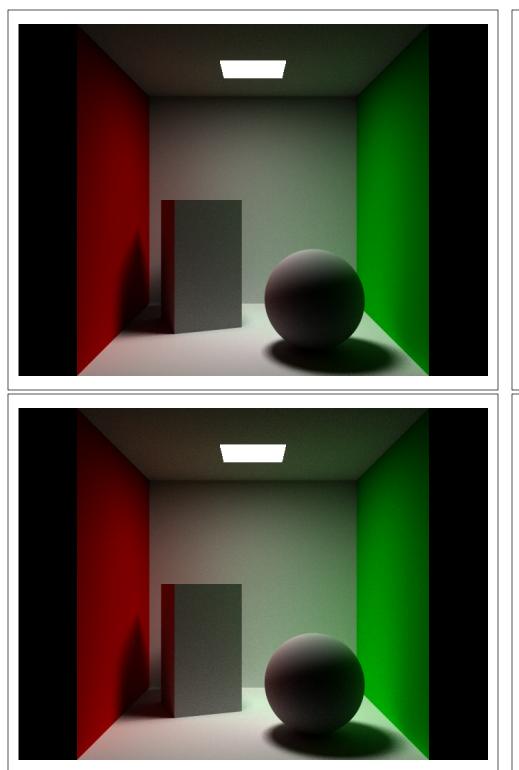
An extreme case is diffuse reflection. The idea is that we:

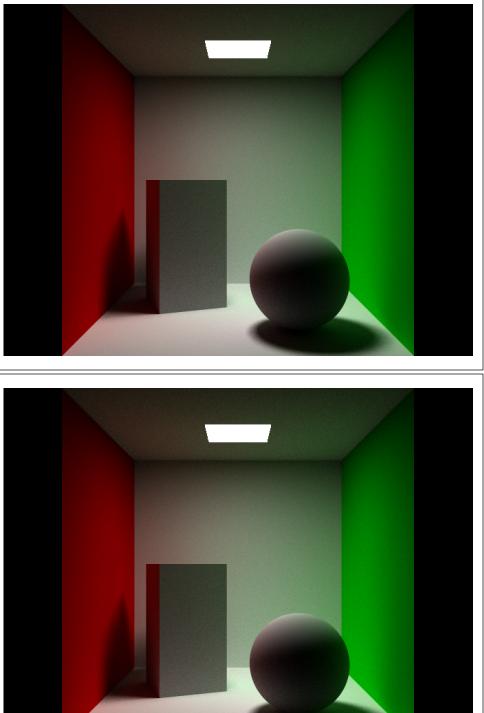
- 1. Hit a surface.
- 2. Choose a random direction for reflection.
- 3. Treat the returning ray value as a directional light.
- 4. Shade with that returned indirect light, as well as with direct lighting.
- 5. Return the result.







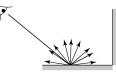




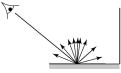
Importance sampling

Originally, we said we would choose a random direction for diffuse reflection. Whatever comes back, we will weight it by $\cos\theta$, where θ is the angle between the normal and the reflection direction.

Let's look at a bunch of uniformly random directions. Are they equally important?

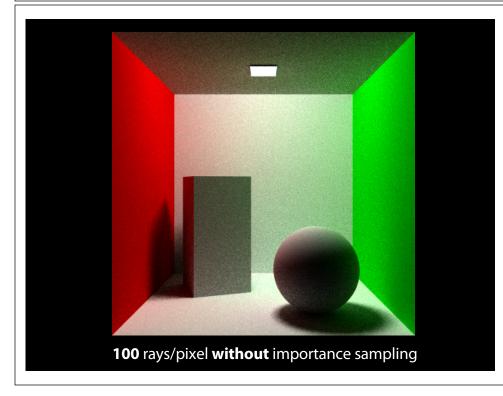


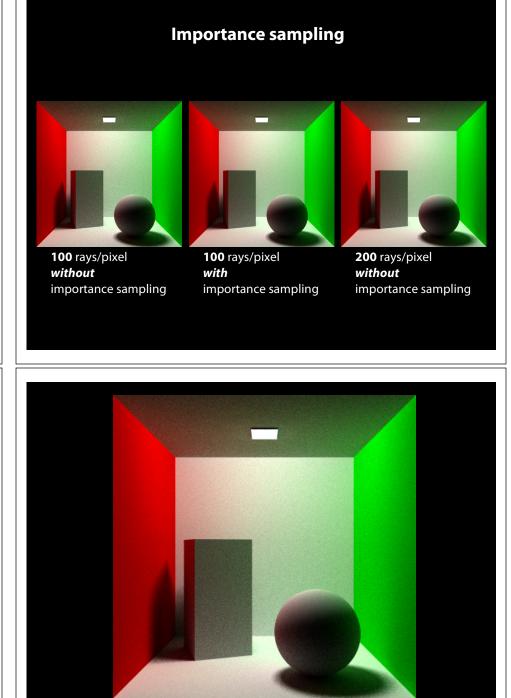
Instead, we could choose to reflect more rays in directions where $\cos\theta$ is greater, and fewer where it is smaller:



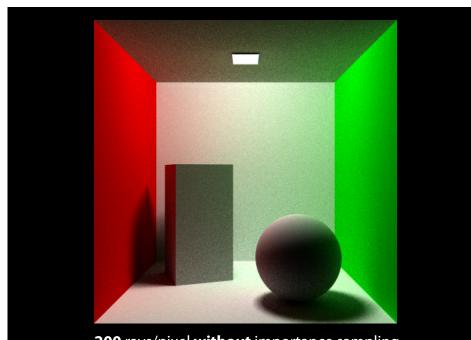
This is called importance sampling. In fact, if we choose the reflection direction q from a probability distribution function $p(\theta) \sim \cos(\theta)$, then we don't actually have to weight the rays at all!

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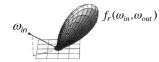
100 rays/pixel **with** importance sampling



200 rays/pixel without importance sampling

Integration over reflection

Integration over diffuse/glossy reflections is at the heart of rendering. Recall that the BRDF tells us how incoming light will scatter into outgoing directions:



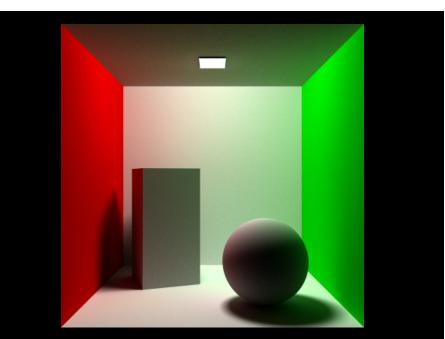
By reciprocity, we can replace ω_{in} on the left side above with ω_{out} , and treat the function $f_r(\omega_{in}, \omega_{out})$ as the "sensitivity" to different incoming directions.

To compute the total light for an outgoing direction, we integrate all incoming directions:

$$I(\omega_{out}) = \int_{H} I(\omega_{in}) f_r(\omega_{in}, \omega_{out}) (\omega_{in} \cdot \mathbf{N}) d\omega_{in}$$

To integrate in with MCPT, when considering reflection recursion, we could just:

- Cast a ray in a (uniformly) random direction
- Weight the result by $f_r(\omega_{in}, \omega_{out})(\omega_{in} \cdot \mathbf{N})$



900 rays/pixel with importance sampling

Importance sampling of reflection For a given BRDF:



again the surface reflection equation is:

$$I(\omega_{out}) = \int_{H} I(\omega_{in}) f_r(\omega_{in}, \omega_{out}) (\omega_{in} \cdot \mathbf{N}) d\omega_{in}$$

With importance sampling:

- Cast a ray in a direction drawn from a distribution $p(\omega_{in})$ that is large where the BRDF is large.
- Weight the ray by: $f_r(\omega_{in}, \omega_{out})(\omega_{in} \cdot \mathbf{N}) / p(\omega_{in})$

Ideally, the distribution is proportional to the BRDF:

 $p(\omega_{in}) \sim f_r(\omega_{in}, \omega_{out})(\omega_{in} \cdot \mathbf{N})$



Area light, glossy and diffuse reflection, depth of field (1024 rays/pixel)

Summary

What to take home from this lecture:

- The meanings of all the boldfaced terms.
- An intuition for what aliasing is.
- How to reduce aliasing artifacts in a ray tracer
- The limitations of Whitted ray tracing (no glossy surfaces, etc.)
- The main idea behind Monte Carlo path tracing and what effects it can simulate (glossy surfaces, etc.)

MCPT for beginners

If you want to try out MCPT, it is not as hard as you might think.

Try it with simple sampling strategies:

- Choose one of the effects you really like, add more if you have time.
- Skip stratification.
- If you do diffuse, don't do importance to begin with, just weight by the shading equation (normal dot with reflected ray direction).
- If you do glossy, you do need some kind of importance sampling.
 - Try simple perturbations around the reflection direction; the more random perturbation you allow, the blurrier the reflections.
 - The amount of perturbation is ideally determined by the specular exponent for Phong shading (bigger exponent means less perturbation).
- Throw a lot of rays per pixel!