

Hierarchical Modeling

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Reading

Required:

- ◆ Angel, sections 8.1 – 8.6, 8.8

Optional:

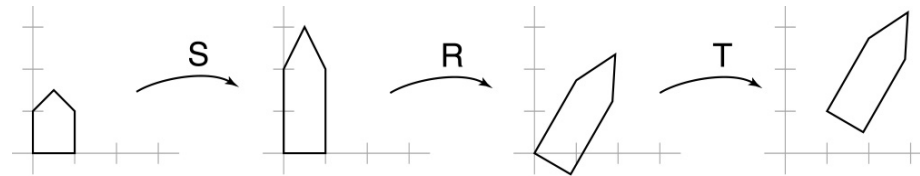
- ◆ *OpenGL Programming Guide*, chapter 3

Symbols and instances

Most graphics APIs support a few geometric **primitives**:

- ◆ spheres
- ◆ cubes
- ◆ cylinders

These symbols are **instanced** using an **instance transformation**.



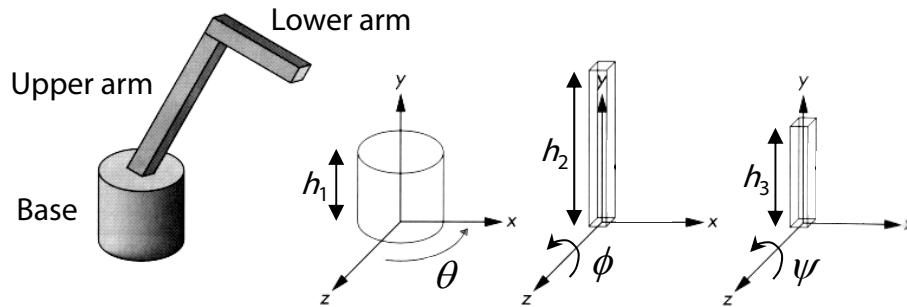
Q: What is the matrix for the instance transformation above?

$$\cancel{M = SRT}$$
$$M = TRS$$

3D Example: A robot arm

Let's build a robot arm out of a cylinder and two cuboids, with the following 3 degrees of freedom:

- ◆ Base rotates about its vertical axis by θ
- ◆ Upper arm rotates in its xy -plane by ϕ
- ◆ Lower arm rotates in its xy -plane by ψ



[Angel, 2011]

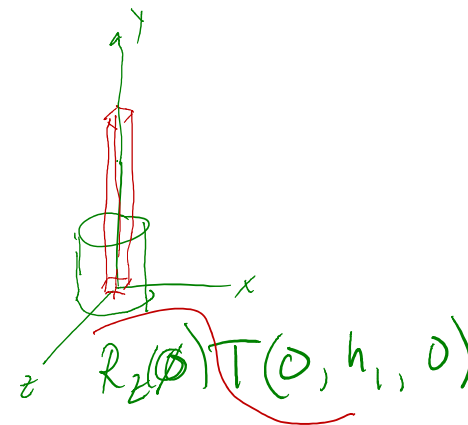
(Note that the angles are set to zero in the figures on the right; i.e., the parts are shown in their "default" positions.)

Suppose we have transformations $R_x(\cdot)$, $R_y(\cdot)$, $R_z(\cdot)$, $T(\cdot, \cdot, \cdot)$.

Q: What matrix do we use to transform the base?

Q: What matrix product for the upper arm?

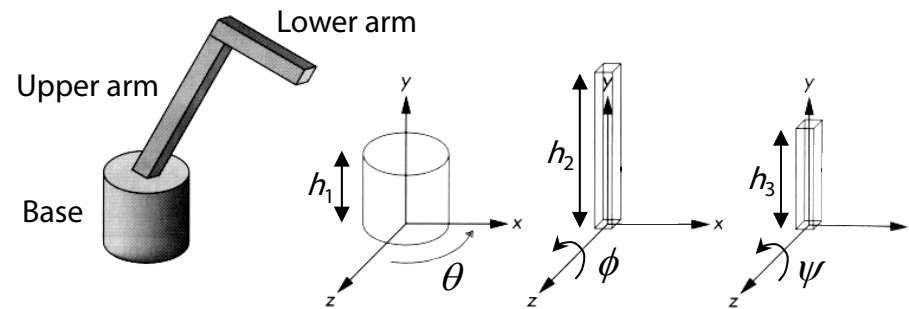
Q: What matrix product for the lower arm?



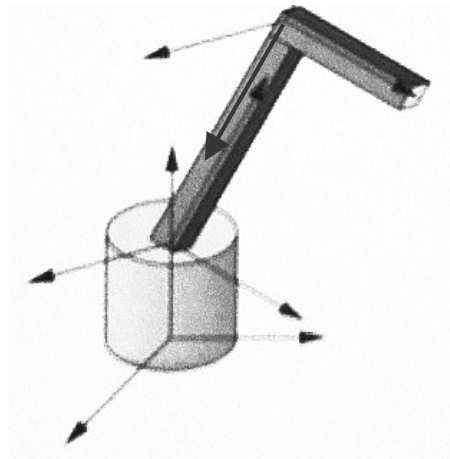
$$\underbrace{R_y(\theta)}_{\text{base}} \underbrace{T(0, h_1, 0)}_{\text{upper arm}} \underbrace{R_z(\phi) T(0, h_2, 0) R_z(\psi)}_{\text{lower arm}}$$

3D Example: A robot arm

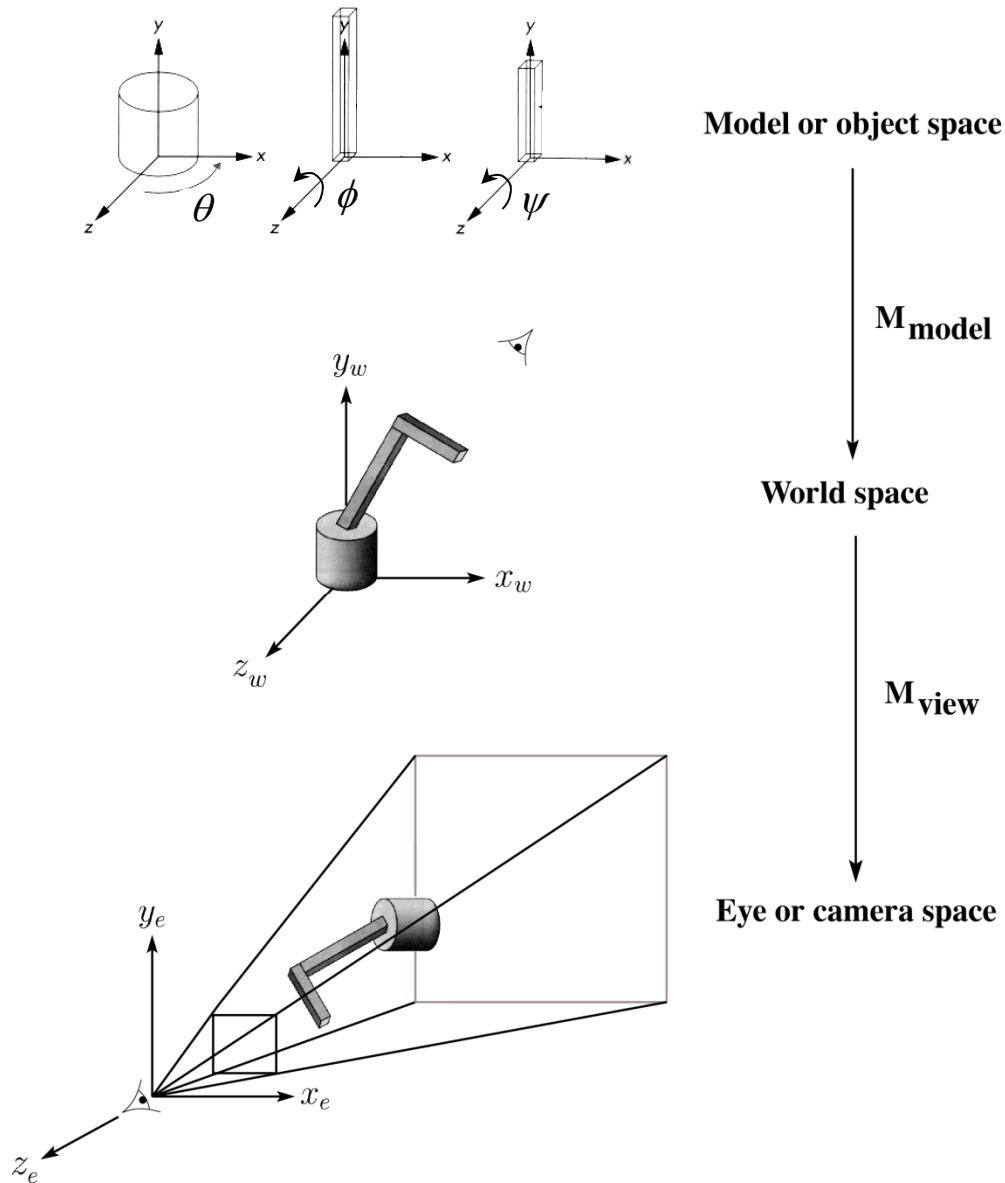
An alternative interpretation is that we are taking the original coordinate frames...



...and translating and rotating them into place:



From parts to model to viewer



Robot arm implementation

The robot arm can be displayed by keeping a global matrix and computing it at each step:

```
Matrix M, M_model, M_view;
```

```
main()
```

```
{  
    . . .  
    M_view = compute_view_transform();  
    robot_arm();  
    . . .  
}
```

```
robot_arm()
```

```
{  
    M_model = R_y(theta);  
    M = M_view*M_model;  
    base();  
    M_model = R_y(theta)*T(0,h1,0)*R_z(phi);  
    M = M_view*M_model;  
    upper_arm();  
    M_model = R_y(theta)*T(0,h1,0)  
                *R_z(phi)*T(0,h2,0)*R_z(psi);  
    M = M_view*M_model;  
    lower_arm();  
}
```

Do the matrix computations seem wasteful?



Robot arm implementation, better

Instead of recalculating the global matrix each time, we can just update it *in place* by concatenating matrices on the right:

```
Matrix M_modelview;

main()
{
    . . .
    M_modelview = compute_view_transform();
    robot_arm();
    . . .
}

robot_arm()
{
    M_modelview *= R_y(theta);
    base();
    M_modelview *= T(0,h1,0)*R_z(phi);
    upper_arm();
    M_modelview *= T(0,h2,0)*R_z(psi);
    lower_arm();
}
```


Robot arm implementation, OpenGL

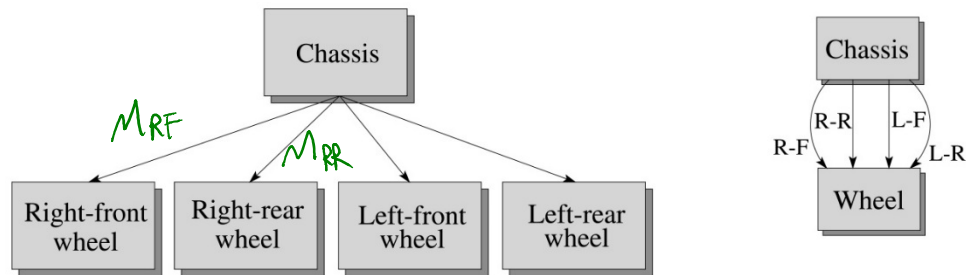
OpenGL maintains a global state matrix called the **model-view matrix**, which is updated by concatenating matrices on the *right*.

```
main()
{
    . . .
    glMatrixMode( GL_MODELVIEW );
    Matrix M = compute_view_xform();
    glLoadMatrixf( M );
    robot_arm();
    . . .
}

robot_arm()
{
    glRotatef( theta, 0.0, 1.0, 0.0 );
    base();
    glTranslatef( 0.0, h1, 0.0 );
    glRotatef( phi, 0.0, 0.0, 1.0 );
    lower_arm();
    glTranslatef( 0.0, h2, 0.0 );
    glRotatef( psi, 0.0, 0.0, 1.0 );
    upper_arm();
}
```

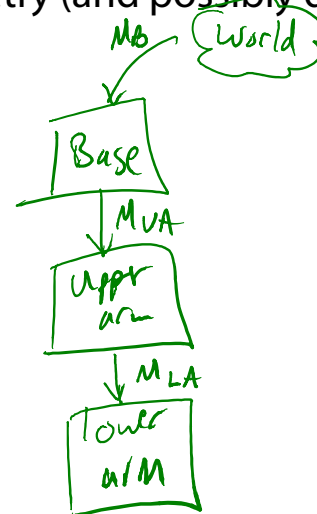
Hierarchical modeling

Hierarchical models can be composed of instances using trees or DAGs:

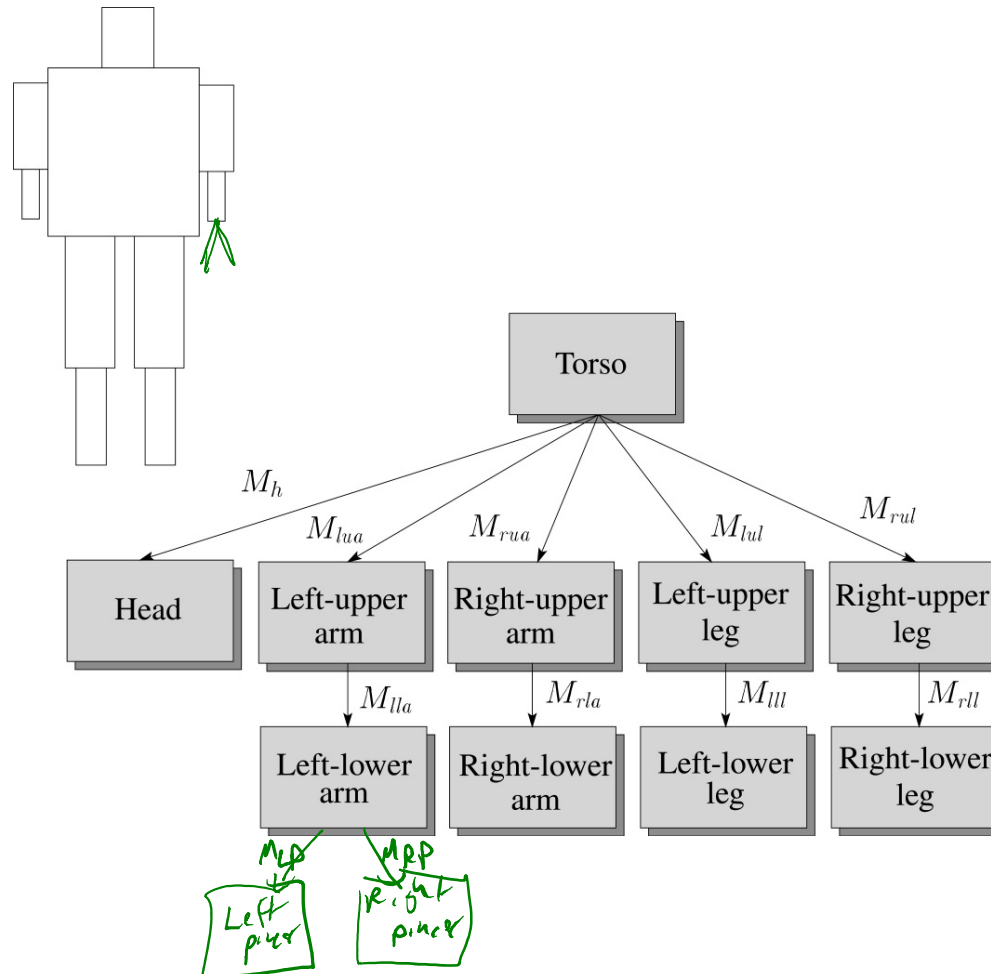


- ◆ edges contain geometric transformations
- ◆ nodes contain geometry (and possibly drawing attributes)

How might we draw the tree for the robot arm?



A complex example: human figure



Q: What's the most sensible way to traverse this tree?

Depth first w/ stack

Human figure implementation, OpenGL

```
figure()
{
    torso();
    glPushMatrix();
        glTranslate( ... );
        glRotate( ... );
        head();
    glPopMatrix();
    glPushMatrix();
        glTranslate( ... );
        glRotate( ... );
        left_upper_arm();
        glPushMatrix();
            glTranslate( ... );
            glRotate( ... );
            left_lower_arm();
        glPopMatrix();
    glPopMatrix();
    . . .
}
```

Animation

The above examples are called **articulated models**:

- ◆ rigid parts
- ◆ connected by joints

They can be animated by specifying the joint angles (or other display parameters) as functions of time.

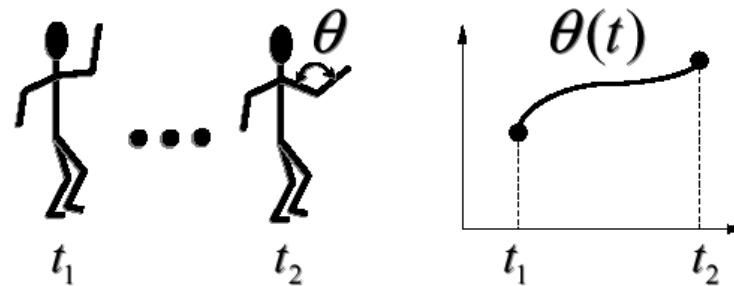
Key-frame animation

The most common method for character animation in production is **key-frame animation**.

- ◆ Each joint specified at various **key frames** (not necessarily the same as other joints)
- ◆ System does interpolation or **in-betweening**

Doing this well requires:

- ◆ A way of smoothly interpolating key frames: **splines**
- ◆ A good interactive system
- ◆ A lot of skill on the part of the animator

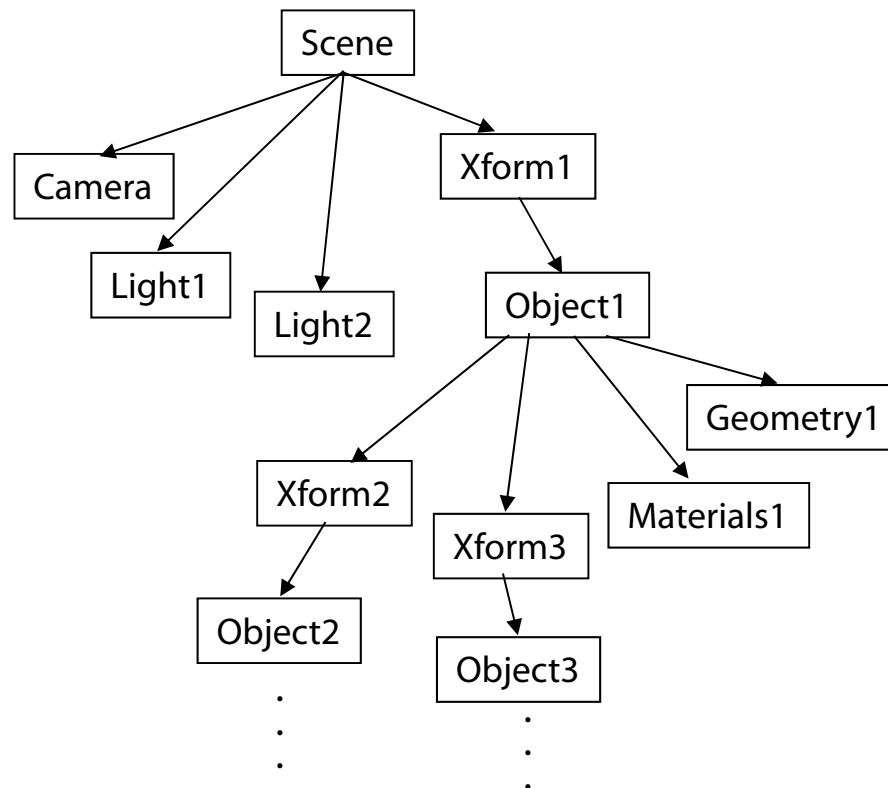


Scene graphs

The idea of hierarchical modeling can be extended to an entire scene, encompassing:

- ◆ many different objects
- ◆ lights
- ◆ camera position

This is called a **scene tree** or **scene graph**.



Summary

Here's what you should take home from this lecture:

- ◆ All the **boldfaced terms**.
- ◆ How primitives can be instantiated and composed to create hierarchical models using geometric transforms.
- ◆ How the notion of a model tree or DAG can be extended to entire scenes.
- ◆ How OpenGL transformations can be used in hierarchical modeling.
- ◆ How keyframe animation works.