# CSEP 544: Lecture 02 

## Relational Query Languages and Database Design

## Homework 1

- Due next Tuesday, October 20, 11pm
- Please note update using SQL Azure - Use shared account (login in your email) - Database is already there, just run queries
- Create your own SQL Azure instance
- Extra credit in HW1
- Required for HW4


## Homework 3

I know it's far into the future, but...

- We will use Amazon Web Service
- You need to get a $\$ 100$ student's pass http://aws.amazon.com/grants
- Use your uw.edu email address


## Brief Review of $1^{\text {st }}$ Lecture

- Database = collection of related files
- Physical data independence
- SQL:
- Select-from-where
- Nested loop semantics
- Group by (you read the slides, right?)
- Advanced stuff: nested queries, outerjoins


## Big Data

What is it?

## Big Data

## What is it?

- Gartner report*
- High Volume
- High Variety
- High Velocity
* http://www.gartner.com/newsroom/id/1731916


## Big Data

What is it? Stonebraker:

- Big volumes, small analytics
- Big analytics, on big volumes
- Big velocity
- Big variety


## Big Data

- "Small analytics" = select/join/aggregate/groupby
- Discuss: column-oriented databases, shared-nothing, Hive/ Hadoop
- "Big analytics" = linear algebra (R, ScalaPack)
- Discuss: Sparse matrix multiplication = join/groupby
- High velocity = streaming data
- Discuss: Streaming SQL engines, e.g. Microsoft's Trill
- High variety $=$ heterogeneous data models (XML, documents)
- Discuss: ETL ("Extract Transform Load")


## Outline

- Relational Query Languages
- Relational algebra
- Recursion-free datalog with negation
- Relational calculus

Database Design

- Functional Dependencies and BCNF
- Suggested reading:

Three Query Language Formalisms https://courses.cs.washington.edu/ courses/cse344/12au/lectures/query-language-primer.pdf

## 1. Relational Algebra

- Used internally by the database engine to execute queries
- Book: chapter 4.2
- We will return to RA when we discuss query execution


## 1. Relational Algebra

The Basic Five operators:

- Union: $\cup$
- Difference: -
- Selection: $\sigma$
- Projection: П
- Join: $\ltimes$


## Running Example

Find all actors who acted both in 1910 and in 1940:

Q: SELECT DISTINCT a.fname, a.Iname
FROM Actor a, Casts c1, Movie m1, Casts c2, Movie m2 WHERE a.id = c1. pid AND c1. mid $=\mathrm{m} 1$.id

AND a.id $=$ c2.pid AND c2. $\mathrm{mid}=\mathrm{m} 2$.id
AND m1.year $=1910 \quad$ AND m2.year $=1940$;

## Two Perspectives

- Named Perspective:

Actor(id, fname, Iname)
Casts(pid,mid)
Movie(id,name,year)

- Unnamed Perspective:

Actor $=$ arity 3
Casts = arity 2
Movie $=$ arity 3

Named perspective needs renaming operator: $\rho$

## 1. Relational Algebra (Details)

- Selection: returns tuples that satisfy condition
- Named perspective:
- Unamed perspective:
$\sigma_{\text {year }}=1910^{\prime}$ (Movie)
$\sigma_{3=}{ }^{\prime} 1910^{\prime}$ (Movie)


## 1. Relational Algebra (Details)

- Selection: returns tuples that satisfy condition
- Named perspective:
- Unamed perspective:
$\sigma_{\text {year }}=1910^{\prime}$ (Movie)
$\sigma_{3}={ }^{\prime} 1910^{\prime}$ (Movie)
- Projection: returns only some attributes
- Named perspective:
- Unnamed perspective:
$\Pi_{\text {fname, Iname }}$ (Actor)
$\Pi_{2,3}$ (Actor)


## 1. Relational Algebra (Details)

- Selection: returns tuples that satisfy condition
- Named perspective:
- Unamed perspective:
$\sigma_{\text {year }=1910 \text { (Movie) }}$
$\sigma_{3}={ }^{\prime} 1910^{\prime}$ (Movie)
- Projection: returns only some attributes
- Named perspective:
- Unnamed perspective: $\quad \Pi_{2,3}$ (Actor)
- Join: joins two tables on a condition
- Named perspective:
- Unnamed perspectivie:

Casts $\bowtie_{\text {mid=id }}$ Movie
Casts $\bowtie_{2=1}$ Movie

## 1. Relational Algebra Example

Q: SELECT DISTINCT a.fname, a.Iname
FROM Actor a, Casts c1, Movie m1, Casts c2, Movie m2
WHERE a.id = c1.pid $\quad$ AND c1. $\mathrm{mid}=\mathrm{m} 1$.id
AND a.id $=\mathrm{c} 2$. pid $\quad$ AND c2. $\mathrm{mid}=\mathrm{m} 2 . \mathrm{id}$
AND m1. year $=1910$ AND m2 .year $=1940$;

Actor(id, fname, Iname) Casts(pid,mid)
Movie(id,name,year)

## Named perspective

$\prod_{\text {fname, Iname }}$
$\sigma_{\text {year1 }=\text { '1910' and year2='1940' }}$
Note how we renamed year to year1, year2


Casts

## 1. Relational Algebra Example

Q: SELECT DISTINCT a.fname, a.Iname
FROM Actor a, Casts c1, Movie m1, Casts c2, Movie m2
WHERE a.id = c1.pid $\quad$ AND c1. $\mathrm{mid}=\mathrm{m} 1$.id
AND a.id $=\mathrm{c} 2$.pid $\quad$ AND c2. $\mathrm{mid}=\mathrm{m} 2 . \mathrm{id}$

Actor(id, fname, Iname) Casts(pid,mid)
Movie(id,name,year)

## Unnamed perspective



## Joins and Cartesian Product

- Each tuple in R1 with each tuple in R2

$$
R 1 \times R 2
$$

- Rare in practice; mainly used to express joins


## Cartesian Product

 (aka Crosşeproduct)| Name | SSN |
| :--- | :--- |
| John | 999999999 |
| Tony | 777777777 |


| EmpSSN | DepName |
| :--- | :--- |
| 9999999999 | Emily |
| 777777777 | Joe |

## Employee $\times$ Dependent

| Name | SSN | EmpSSN | DepName |
| :--- | :--- | :--- | :--- |
| John | 999999999 | 999999999 | Emily |
| John | 999999999 | 777777777 | Joe |
| Tony | 777777777 | 999999999 | Emily |
| Tony | 777777777 | 7777777777 | Joe |
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## Natural Join

## $\mathrm{R} 1 \bowtie \mathrm{R} 2$

- Meaning: $R 1 \bowtie R 2=\Pi_{A}(\sigma(R 1 \times R 2))$
- Where:
- Selection $\sigma$ checks equality of all common attributes
- Projection eliminates duplicate common attributes


## Natural Join Example

R

| $A$ | $B$ |
| :---: | :---: |
| $X$ | $Y$ |
| $X$ | $Z$ |
| $Y$ | $Z$ |
| $Z$ | $V$ |

S

| $B$ | $C$ |
| :---: | :---: |
| $Z$ | $U$ |
| $V$ | $W$ |
| $Z$ | $V$ |

$\mathbf{R} \bowtie \mathbf{S}=$
$\Pi_{A B C}\left(\sigma_{R . B=S . B}(R \times S)\right)$

| A | B | C |
| :---: | :---: | :---: |
| $X$ | $Z$ | $U$ |
| $X$ | $Z$ | $V$ |
| $Y$ | $Z$ | $U$ |
| $Y$ | $Z$ | $V$ |
| $Z$ | $V$ | $W$ |

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## Natural Join Example 2

AnonPatient $P$

| age | zip | disease |
| :--- | :--- | :--- |
| 54 | 98125 | heart |
| 20 | 98120 | flu |

Voters V

| name | age | zip |
| :--- | :--- | :--- |
| p1 | 54 | 98125 |
| p2 | 20 | 98120 |

$P \bowtie V$

| age | zip | disease | name |
| :--- | :--- | :--- | :--- |
| 54 | 98125 | heart | $p 1$ |
| 20 | 98120 | flu | $p 2$ |

## Natural Join

- Given schemas $R(A, B, C, D), S(A, C, E)$, what is the schema of $R \bowtie S$ ?
- Given $R(A, B, C), S(D, E)$, what is $R \bowtie S$ ?
- Given $R(A, B), S(A, B)$, what is $R \bowtie S$ ?


## Theta Join

- A join that involves a predicate

$$
R 1 \bowtie_{\theta} R 2=\sigma_{\theta}(R 1 \times R 2)
$$

- Here $\theta$ can be any condition
- For our voters/disease example:
$P \bowtie_{\text {P.zip }}=V$. zip and P.age $<$ V.age +5 and P.age $>$ V.age -5


## Equijoin

- A theta join where $\theta$ is an equality

$$
R 1 \bowtie_{A=B} R 2=\sigma_{A=B}(R 1 \times R 2)
$$

- This is by far the most used variant of join in practice


## Equijoin Example

AnonPatient $P$

| age | zip | disease |
| :--- | :--- | :--- |
| 54 | 98125 | heart |
| 20 | 98120 | flu |

$P \bowtie_{\text {P.age=}=\text { V.age }} \quad V$

| P.age | P.zip | disease | name | V.age | V.zip |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 54 | 98125 | heart | p 1 | 54 | 98125 |
| 20 | 98120 | flu | p 2 | 20 | 98120 |

Note:
Optional, drop the redundant age

## Join Summary

- Theta-join: $R \bowtie_{\theta} S=\sigma_{\theta}(R \times S)$
- Join of $R$ and $S$ with a join condition $\theta$
- Cross-product followed by selection $\theta$
- Equijoin: $\mathrm{R}_{\bowtie}{ }_{\theta} \mathrm{S}=\pi_{\mathrm{A}}\left(\sigma_{\theta}(\mathrm{R} \times \mathrm{S})\right)$
- Join condition $\theta$ consists only of equalities
- Projection $\pi_{\mathrm{A}}$ drops all redundant attributes
- Natural join: $R_{\bowtie} S=\pi_{A}\left(\sigma_{\theta}(R \times S)\right)$
- Equijoin
- Equality on all fields with same name in R and in S


## So Which Join Is It?

- When we write $R \bowtie S$ we usually mean an equijoin, but we often omit the equality predicate when it is clear from the context


## More Joins

- Outer join
- Include tuples with no matches in the output
- Use NULL values for missing attributes
- Variants
- Left outer join
- Right outer join
- Full outer join


## Outer Join Example

AnonPatient $P$

| age | zip | disease |
| :--- | :--- | :--- |
| 54 | 98125 | heart |
| 20 | 98120 | flu |
| 33 | 98120 | lung |

AnnonJob J

| job | age | zip |
| :--- | :--- | :--- |
| lawyer | 54 | 98125 |
| cashier | 20 | 98120 |


| age | zip | disease | job |
| :--- | :--- | :--- | :--- |
| 54 | 98125 | heart | lawyer |
| 20 | 98120 | flu | cashier |
| 33 | 98120 | lung | null |

## Some Examples

## Supplier(sno, sname, scity,sstate) Part(pno, pname, psize, pcolor) Supply(sno, pno,qty,price)

Q2: Name of supplier of parts with size greater than 10
$\pi_{\text {sname }}\left(\right.$ Supplier $\bowtie$ Supply $\bowtie\left(\sigma_{\text {psize>10 }}\right.$ (Part))
Q3: Name of supplier of red parts or parts with size greater than 10
$\pi_{\text {sname }}\left(\right.$ Supplier $\bowtie$ Supply $\bowtie\left(\sigma_{\text {psize>10 }}(\right.$ Part $) \cup \sigma_{\text {pcolor='red' }}($ Part $)$ ) )

## Outline

- Relational Query Languages
- Relational algebra
- Recursion-free datalog with negation
- Relational calculus

Database Design

- Functional Dependencies and BCNF


## 2. Datalog

- Very friendly notation for queries
- Designed in the 80's for recursive queries
- Confined to academia, until the Big Data explosion. Commercial systems today: LogicBlox, Yedalog (google)
- This lecture: recursion-free datalog with negation. Later lecture: recursion


## 2. Datalog

## How to try out datalog quickly: <br> - Download DLV from http://www.dbai.tuwien.ac.at/proj/dlv/

- Run DLV on this file:

```
parent(william, john).
parent(john, james).
parent(james, bill).
parent(sue, bill).
parent(james, carol).
parent(sue, carol).
male(john).
male(james).
female(sue).
male(bill).
female(carol).
grandparent(X, Y) :- parent(X, Z), parent(Z, Y).
father(X, Y) :- parent(X, Y), male(X).
mother(X, Y) :- parent(X, Y), female(X).
brother(X, Y) :- parent(P, X), parent(P, Y), male(X), X != Y.
sister(X, Y) :- parent(P, X), parent(P, Y), female(X), X != Y.
```


## 2. Datalog: Facts and Rules

Facts
Actor(344759, 'Douglas', 'Fowley').
Casts(344759, 29851).
Casts(355713, 29000).
Movie(7909, 'A Night in Armour', 1910).
Movie(29000, 'Arizona', 1940).
Movie(29445, 'Ave Maria', 1940).

Rules
Q1(y) :- Movie( $x, y, z$ ), $z={ }^{\prime} 1940$ '.

Q2(f, I) :- $\operatorname{Actor}(\mathrm{z}, \mathrm{f}, \mathrm{I}), \operatorname{Casts}(\mathrm{z}, \mathrm{x})$, Movie(x,y,'1940').

$$
\begin{aligned}
& \text { Q3(f,I) :- Actor(z,f,I), Casts(z,x1), Movie(x1,y1,1910), } \\
& \text { Casts(z,x2), Movie(x2,y2,1940) }
\end{aligned}
$$

Facts = tuples in the database Rules = queries

Extensional Database Predicates = EDB Intensional Database Predicates $=$ IDB

## 2. Datalog: Terminology

head
body

f, I = head variables
$x, y, z=$ existential variables

## 2. Datalog program

Find all actors with Bacon number $\leq 2$

```
B0(x) :- Actor(x,'Kevin', 'Bacon')
B1(x) :- Actor(x,f,l), Casts(x,z), Casts(y,z), B0(y)
B2(x) :- Actor(x,f,l), Casts(x,z), Casts(y,z), B1(y)
Q4(x) :- B1(x)
Q4(x) :- B2(x)
```

Note: Q4 is the union of B1 and B2

## 2. Datalog with negation

Find all actors with Bacon number $\geq 2$

```
B0(x) :- Actor(x,'Kevin', 'Bacon')
B1(x) :- Actor(x,f,l), Casts(x,z), Casts(y,z), B0(y)
Q6(x) :- Actor(x,f,I), not B1(x), not B0(x)
```


## 2. Safe Datalog Rules

Here are unsafe datalog rules. What's "unsafe" about them ?
U1 (x,y) :- Movie(x,z,1994), y>1910
U2(x) :- Movie(x,z,1994), not Casts(u,x)

A datalog rule is safe if every variable appears in some positive relational atom

## 2. Datalog v.s. SQL

- Non-recursive datalog with negation is very close to SQL; with some practice, you should be able to translate between them back and forth without difficulty; see example in the paper


## Outline

- Relational Query Languages
- Relational algebra
- Recursion-free datalog with negation
- Relational calculus

Database Design

- Functional Dependencies and BCNF


## 3. Relational Calculus

- Also known as predicate calculus, or first order logic
- The most expressive formalism for queries: easy to write complex queries
- TRC = Tuple RC = named perspective
- DRC = Domain RC = unnamed perspective


## 3. Relational Calculus

Predicate P:

$$
P::=\text { atom }|P \wedge P| P \vee P|P \Rightarrow P| \operatorname{not}(P)|\forall x . P| \exists x . P
$$

Query Q:

$$
Q\left(x_{1}, \ldots, x_{k}\right)=P
$$

Example: find the first/last names of actors who acted in 1940

$$
Q(f, I)=\exists x . \text { ヨy. ヨz. (Actor(z,f,I) } \wedge \operatorname{Casts}(z, x) \wedge \operatorname{Movie}(x, y, 1940))
$$

What does this query return?

$$
Q(f, I)=\exists z .(\operatorname{Actor}(z, f, I) \wedge \forall x .(\operatorname{Casts}(z, x) \Rightarrow \exists y . M o v i e(x, y, 1940)))
$$

## 3. Relational Calculus:

Likes(drinker, beer)

## Example

Frequents(drinker, bar)
Serves(bar, beer)
Find drinkers that frequent some bar that serves some beer they like.

$$
Q(x)=\exists y . \exists z \text {. Frequents }(x, y) \wedge \text { Serves }(y, z) \wedge \text { Likes }(x, z)
$$

## 3. Relational Calculus:

Likes(drinker, beer)

## Example

Frequents(drinker, bar)
Serves(bar, beer)
Find drinkers that frequent some bar that serves some beer they like.

$$
Q(x)=\exists y . \exists z \text {. Frequents }(x, y) \wedge \text { Serves }(y, z) \wedge \text { Likes }(x, z)
$$

Find drinkers that frequent only bars that serves some beer they like.

## 3. Relational Calculus:

Likes(drinker, beer)

## Example

Frequents(drinker, bar)
Serves(bar, beer)
Find drinkers that frequent some bar that serves some beer they like.

$$
Q(x)=\exists y . \exists z . \text { Frequents }(x, y) \wedge \text { Serves }(y, z) \wedge \text { Likes }(x, z)
$$

Find drinkers that frequent only bars that serves some beer they like.

$$
\mathrm{Q}(\mathrm{x})=\forall \mathrm{y} . \text { Frequents }(\mathrm{x}, \mathrm{y}) \Rightarrow(\exists \mathrm{z} \text {. Serves }(\mathrm{y}, \mathrm{z}) \wedge \text { Likes }(\mathrm{x}, \mathrm{z}))
$$

Find drinkers that frequent some bar that serves only beers they like.

## 3. Relational Calculus:

Likes(drinker, beer) Example
Frequents(drinker, bar)
Serves(bar, beer)
Find drinkers that frequent some bar that serves some beer they like.

$$
Q(x)=\exists y . \exists z \text {. Frequents }(x, y) \wedge \text { Serves }(y, z) \wedge \text { Likes }(x, z)
$$

Find drinkers that frequent only bars that serves some beer they like.

$$
Q(x)=\forall y . \text { Frequents }(x, y) \Rightarrow(\exists z . \operatorname{Serves}(y, z) \wedge \operatorname{Likes}(x, z))
$$

Find drinkers that frequent some bar that serves only beers they like.

$$
Q(x)=\exists y . \text { Frequents }(x, y) \wedge \forall z .(\text { Serves }(y, z) \Rightarrow \text { Likes }(x, z))
$$

Find drinkers that frequent only bars that serves only beer they like.

## 3. Relational Calculus:

Likes(drinker, beer) Example
Frequents(drinker, bar)
Serves(bar, beer)
Find drinkers that frequent some bar that serves some beer they like.

$$
\mathrm{Q}(\mathrm{x})=\exists \mathrm{y} . \exists \mathrm{z} \text {. Frequents }(\mathrm{x}, \mathrm{y}) \wedge \text { Serves }(\mathrm{y}, \mathrm{z}) \wedge \text { Likes }(\mathrm{x}, \mathrm{z})
$$

Find drinkers that frequent only bars that serves some beer they like.

$$
Q(x)=\forall y . \text { Frequents }(x, y) \Rightarrow(\exists z . \operatorname{Serves}(y, z) \wedge \operatorname{Likes}(x, z))
$$

Find drinkers that frequent some bar that serves only beers they like.

$$
Q(x)=\exists y . \text { Frequents }(x, y) \wedge \forall z .(\operatorname{Serves}(y, z) \Rightarrow \text { Likes }(x, z))
$$

Find drinkers that frequent only bars that serves only beer they like.

$$
\mathrm{Q}(\mathrm{x})=\forall \mathrm{y} \text {. Frequents }(\mathrm{x}, \mathrm{y}) \Rightarrow \forall \mathrm{z} .(\operatorname{Serves}(\mathrm{y}, \mathrm{z}) \Rightarrow \text { Likes }(\mathrm{x}, \mathrm{z}))
$$

## 3. Domain Independent Relational Calculus

- As in datalog, one can write "unsafe" RC queries; they are also called domain dependent
- See examples in the Three Query Languages paper
- Moral: make sure your RC queries are always domain independent


## 3. Relational Calculus

Take home message:

- Need to write a complex SQL query:
- First, write it in RC
- Next, translate it to datalog (see next)
- Finally, write it in SQL

As you gain experience, take shortcuts

# 3. From RC to Non-recursive Datalog w/ negation 

Query: Find drinkers that like some beer so much that they frequent all bars that serve it
$Q(x)=\exists y . \operatorname{Likes}(x, y) \wedge \forall z$. $\operatorname{Serves}(z, y) \Rightarrow$ Frequents $(x, z))$

# 3. From RC to Non-recursive Datalog w/ negation 

Query: Find drinkers that like some beer so much that they frequent all bars that serve it
$Q(x)=\exists y . \operatorname{Likes}(x, y) \wedge \forall z .($ Serves $(z, y) \Rightarrow$ Frequents $(x, z))$

Step 1: Replace $\forall$ with $\exists$ using de Morgan's Laws

$$
Q(x)=\exists y . \text { Likes }(x, y) \wedge \neg \exists z .(S e r v e s(z, y) \wedge \neg F r e q u e n t s(x, z))
$$

## 3. From RC to Non-recursive Datalog w/ negation

Query: Find drinkers that like some beer so much that they frequent all bars that serve it
$Q(x)=\exists y . \operatorname{Likes}(x, y) \wedge \forall z .(\operatorname{Serves}(z, y) \Rightarrow$ Frequents $(x, z))$

Step 1: Replace $\forall$ with $\exists$ using de Morgan’s Laws

$$
\mathrm{Q}(\mathrm{x})=\exists \mathrm{y} \text {. Likes }(\mathrm{x}, \mathrm{y}) \wedge \neg \exists \mathrm{z} \text {.(Serves( } \mathrm{z}, \mathrm{y}) \wedge \neg \text { Frequents }(\mathrm{x}, \mathrm{z}))
$$

Step 2: Make all subqueries domain independent
$\mathrm{Q}(\mathrm{x})=\exists \mathrm{y} . \operatorname{Likes}(\mathrm{x}, \mathrm{y}) \wedge \neg \exists \mathrm{z}$.(Likes(x,y) $\wedge$ Serves(z,y) $\wedge \neg$ Frequents $(\mathrm{x}, \mathrm{z}))$

## 3. From RC to Non-recursive Datalog w/ negation

$$
\mathrm{Q}(\mathrm{x})=\exists \mathrm{y} . \operatorname{Likes}(\mathrm{x}, \mathrm{y}) \wedge \neg \exists \mathrm{z} .(\operatorname{Likes}(\mathrm{x}, \mathrm{y}) \wedge \text { Serves }(\mathrm{z}, \mathrm{y}) \wedge \neg \text { Frequents }(\mathrm{x}, \mathrm{z}))
$$

$$
H(x, y)
$$

Step 3: Create a datalog rule for each subexpression; (shortcut: only for subexpressions under $ᄀ$ )

```
H(x,y) :- Likes(x,y),Serves(y,z), not Frequents(x,z)
Q(x) :- Likes(x,y), not H(x,y)
```


## 3. From RC to Non-recursive Datalog w/ negation

$\begin{array}{ll}H(x, y) & :-\operatorname{Likes}(x, y), \operatorname{Serves}(y, z), \text { not Frequents }(x, z) \\ Q(x) & :-\operatorname{Likes}(x, y), \text { not } H(x, y)\end{array}$
Step 4: Write it in SQL
SELECT DISTINCT L.drinker FROM Likes L
WHERE not exists
(SELECT * FROM Likes L2, Serves S
WHERE L2.drinker=L.drinker and L2.beer=L.beer and L2.beer=S.beer and not exists (SELECT * FROM Frequents F WHERE F.drinker=L2.drinker and F.bar=S.bar))

## 3. From RC to Non-recursive Datalog w/ negation

$H(x, y) \quad:-$ Likes $(x, y), S e r v e s(y, z)$, not Frequents $(x, z)$
$\mathrm{Q}(\mathrm{x}) \quad:-$ Likes $(\mathrm{x}, \mathrm{y})$, not $\mathrm{H}(\mathrm{x}, \mathrm{y})$

Improve the SQL query by using an unsafe datalog rule
SELECT DISTINCT L.drinker FROM Likes L
WHERE not exists
(SELECT * FROM Serves S
WHERE L.beer=S.beer and not exists (SELECT * FROM Frequents F WHERE F.drinker=L.drinker and F.bar=S.bar))

## Summary of Translation

- $\mathrm{RC} \rightarrow$ recursion-free datalog $w /$ negation
- Subtle: as we saw; more details in the paper
- Recursion-free datalog w/ negation $\rightarrow$ RA
- Easy: see paper
- RA $\rightarrow$ RC
- Easy: see paper


## Summary

- All three have same expressive power:
- RA
- Non-recursive datalog w/ neg. (= "core" SQL)
-RC
- Write complex queries in RC first, then translate to SQL


## Outline

- Relational Query Languages
- Database Design:
- On your own: slides and/or Chapters 2, 3
- In class: What goes around
- Functional Dependencies and BCNF


## Database Design

## Database Design Process

Conceptual Model:


Relational Model:
Tables + constraints
And also functional dep. Normalization:
Eliminates anomalies Conceptual Schema

Physical storage details
Physical Schema


## Entity / Relationship Diagrams

- Entity set = a class
- An entity = an object
- Attribute

Product

## city

- Relationship


## makes

## Product

## Company

## Person




## Keys in E/R Diagrams

- Every entity set must have a key



## What is a Relation ?

- A mathematical definition:
- if $A, B$ are sets, then a relation $R$ is a subset of $A \times B$
- $A=\{1,2,3\}, B=\{a, b, c, d\}$,

$$
\begin{aligned}
& A \times B=\{(1, a),(1, b), \ldots,(3, d)\} \\
& R=\{(1, a),(1, c),(3, b)\}
\end{aligned}
$$



- makes is a subset of Product $\times$ Company:



## Multiplicity of E/R Relations

- one-one:
- many-one

- many-many



## Notation in Class v.s. the Book

## In class:

Product makes

## Company

In the book:

Product makes

## Multi-way Relationships

How do we model a purchase relationship between buyers, products and stores?


Can still model as a mathematical set (Q. how ?)
A. As a set of triples $\subseteq$ Person $\times$ Product $\times$ Store

## Arrows in Multiway Relationships

Q: What does the arrow mean?


A: A given person buys a given product from at most one store
[Arrow pointing to E means that if we select one entity from each of the other entity sets in the relationship, those entities are related to at most one entity in E]

## Arrows in Multiway Relationships

Q: What does the arrow mean?


A: A given person buys a given product from at most one store AND every store sells to every person at most one product

## Arrows in Multiway Relationships

Q: How do we say that every person shops at at most one store?


A: Cannot. This is the best approximation.
(Why only approximation?)

## Converting Multi-way Relationships to Binary



## Converting Multi-way Relationships to Binary



## Design Principles

## What's wrong?



Moral: be faithful to the specifications of the app!

## Design Principles: What's Wrong?



Moral: pick the right kind of entities.

## Design Principles: What's Wrong?



Moral: don't complicate life more than it already is.

# From E/R Diagrams to Relational Schema 

- Entity set $\rightarrow$ relation
- Relationship $\rightarrow$ relation


## Entity Set to Relation



Product(prod-ID, category, price)

| prod-ID | category | price |
| :--- | :--- | :--- |
| Gizmo55 | Camera | 99.99 |
| Pokemn19 | Toy | 29.99 |

## Create Table (SQL)

CREATE TABLE Product ( prod-ID CHAR(30) PRIMARY KEY, category VARCHAR(20), price double)

## N-N Relationships to Relations



Represent that in relations!

## N-N Relationships to Relations



## Create Table (SQL)

CREATE TABLE Shipment( name CHAR(30) REFERENCES Shipping-Co,
prod-ID CHAR(30),
cust-ID VARCHAR(20),
date DATETIME,
PRIMARY KEY (name, prod-ID, cust-ID), FOREIGN KEY (prod-ID, cust-ID) REFERENCES Orders

## $\mathrm{N}-1$ Relationships to Relations



Represent this in relations!

## N-1 Relationships to Relations



Remember: no separate relations for many-one relationship

## Multi-way Relationships to Relations



Purchase(prod-ID, cust-ssn, store-name)

## Modeling Subclasses

Some objects in a class may be special define a new class better: define a subclass


So --- we define subclasses in E/R

## Subclasses



## Understanding Subclasses

Think in terms of records:
Product

SoftwareProduct

EducationalProduct
field1
field2
field4
field5

## Subclasses to Relations



Other ways to convert are possible

## Product

| Name | Price | Category |
| :---: | :---: | :---: |
| Gizmo | 99 | gadget |
| Camera | 49 | photo |
| Toy | 39 | gadget |

Sw.Product | Name | platforms |
| :---: | :---: |
| Gizmo | unix |

Ed.Product

| Name | Age <br> Group |
| :---: | :---: |
| Gizmo | toddler |
| Toy | retired |

# Modeling Union Types With Subclasses 

## FurniturePiece

## Person

## Company

Say: each piece of furniture is owned either by a person or by a company

## Modeling Union Types With Subclasses

Say: each piece of furniture is owned either by a person or by a company
Solution 1. Acceptable but imperfect (What's wrong ?)


## Modeling Union Types With Subclasses

## Solution 2: better, more laborious



## Weak Entity Sets

Entity sets are weak when their key comes from other classes to which they are related.


Team(sport, number, universityName) University(name)

## What Are the Keys of R?



## Constraints in E/R Diagrams

-Finding constraints is part of the modeling process.
-Commonly used constraints:

- Keys: social security number uniquely identifies a person.
- Single-value constraints: a person can have only one father.
- Referential integrity constraints: if you work for a company, it - must exist in the database.
- Other constraints: peoples' ages are between 0 and 150.


## Keys in E/R Diagrams

## Underline:


keys in E/R diagrams


# Single Value Constraints 



## Referential Integrity Constraints

## Product makes

Company

Each product made by at most one company. Some products made by no company

## Product

## makes

Company
Each product made by exactly one company.
Note: For weak entity sets $\longrightarrow$ should be replaced by $\longrightarrow$ (sec 4.4.2)

## Other Constraints



Q: What does this mean?
A: A Company entity cannot be connected by relationship to more than 99 Product entities

Note: For "at least one", you can use " $\geq 1$ " in a many-many relationship

## Database Design Summary

- Conceptual modeling = design the database schema
- Usually done with Entity-Relationship diagrams
- It is a form of documentation the database schema; it is not executable code
- Straightforward conversion to SQL tables
- Big problem in the real world: the SQL tables are updated, the $E / R$ documentation is not maintained
- Schema refinement using normal forms
- Functional dependencies, normalization


## Outline

- Relational Query Languages
- Database Design:
- On your own: slides and/or Chapters 2, 3
- In class: What goes around
- Functional Dependencies and BCNF


## Data Models

- M. Stonebraker and J. Hellerstein. What Goes Around Comes Around. In "Readings in Database Systems" (aka the Red Book). 4th ed.


## "Data Model"

- Apps need to model real-world data
- Typically includes entities and relationships between them
- Entities: e.g. students, courses, products, clients
- Relationships: e.g. course registrations, product purchases
- Data model enables a user to define the data using high-level constructs without worrying about many low-level details of how data will be stored on disk


## Levels of Abstraction



## What goes around...

- Structured data
- What is this? Examples?
- Semistructured data
- What is this?
- Examples?
- Unstructured data
- What is this? Examples?


## What goes around...

- Structured data
- All data conforms to a schema. Ex: business data
- Semistructured data
- Some structure in the data but implicit and irregular
- Ex: resume, ads
- Unstructured data
- No structure in data. Ex: text, sound, video, images
- In our class: structured data \& relational DBMSs


## Early Proposal 1: IMS

- What is it ?


## Early Proposal 1: IMS

- Hierarchical data model
- Record
- Type: collection of named fields with data types (+)
- Instance: must match type definition (+)
- Each instance must have a key (+)
- Record types must be arranged in a tree (-)
- IMS database is collection of instances of record types organized in a tree


## IMS Example



Two Hierarchical Organizations
Figure 2

## DL/1

- How does a programmer retrieve data in IMS ?


## DL/1

- Each record has a hierarchical sequence key (HSK)
- Records are totally ordered: depth-first and left-to-right
- HSK defines semantics of commands:
- get_next
- get_next_within_parent
- DL/1 is a record-at-a-time language
- Programmer constructs an algorithm for solving the query
- Programmer must worry about query optimization


## Data storage

- How is the data physically stored in IMS ?


## Data storage

- Root records
- Stored sequentially (sorted on key)
- Indexed in a B-tree using the key of the record
- Hashed using the key of the record
- Dependent records
- Physically sequential
- Various forms of pointers
- Selected organizations restrict DL/1 commands
- No updates allowed with sequential organization
- No "get-next" for hashed organization


## Data Independence

- What is it?


## Data Independence

- Physical data independence: Applications are insulated from changes in physical storage details
- Logical data independence: Applications are insulated from changes to logical structure of the data


## IMS Limitations

- Tree-structured data model
- Redundant data
- Existence depends on parent
- Record-at-a-time user interface
- Very limited physical independence
- Phys. organization limits possible operations
- Application programs break if organization changes
- Provides some logical independence
- DL/1 program runs on logical database
- Difficult to achieve good logical data independence with a tree model


## Early Proposal 2: CODASYL - What is it ?

## Early Proposal 2: CODASYL

- Networked data model
- Record types with keys (+)
- Organized in a network
- More flexible than hierarchy (+)
- A record can have multiple parents (-)
- Arcs between records are named
- At least one entry point to the network
- Record-at-a-time DML (-)


## CODASYL Example



A CODASYL Network
Figure 5

## CODASYL Limitations

- No physical data independence
- No logical data independence
- Very complex:
- Programs must "navigate the hyperspace"
- Load and recover as one gigantic object


## Relational Model Overview

- Proposed by Ted Codd in 1970
- Motivation: better logical and physical data independence


# Relational Model Overview 

- Defines logical data model
- No physical data model
- Set-at-a-time query language


## Great Debate

- Pro relational
- What where the arguments ?
- Against relational
- What where the arguments ?
- How was it settled?


## Great Debate

- Pro relational
- CODASYL is too complex
- CODASYL does not provide sufficient data independence
- Record-at-a-time languages are too hard to optimize
- Trees/networks not flexible enough for common cases
- Against relational
- COBOL programmers cannot understand relational languages
- Impossible to represent the relational model efficiently
- CODASYL can represent tables
- Ultimately settled by the market place


## Other Data Models

- Entity-Relationship: 1970's
- Successful in logical database design (this lecture + hw2)
- Extended Relational: 1980's
- Semantic: late 1970's and 1980's
- Object-oriented: late 1980's and early 1990's
- Impedance mismatch: relational dbs $\longleftrightarrow$ OO languages
- Interesting but ultimately failed (several reasons, see paper)
- Object-relational: late 1980's and early 1990's
- User-defined types, ops, functions, and access methods
- Semi-structured: late 1990's to the present
- XML, JSon, Protobuf


## Outline

- Relational Query Languages
- Database Design:
- On your own: slides and/or Chapters 2, 3
- In class: What goes around
- Functional Dependencies and BCNF


## Relational Schema Design

| Name | SSN | PhoneNumber | City |
| :--- | :--- | :--- | :--- |
| Fred | $123-45-6789$ | $206-555-1234$ | Seattle |
| Fred | $123-45-6789$ | $206-555-6543$ | Seattle |
| Joe | $987-65-4321$ | $908-555-2121$ | Westfield |

One person may have multiple phones, but lives in only one city

Primary key is thus (SSN,PhoneNumber)

What is the problem with this schema?

## Relational Schema Design

| Name | $\underline{\text { SSN }}$ | PhoneNumber | City |
| :--- | :--- | :--- | :--- |
| Fred | $123-45-6789$ | $206-555-1234$ | Seattle |
| Fred | $123-45-6789$ | $206-555-6543$ | Seattle |
| Joe | $987-65-4321$ | $908-555-2121$ | Westfield |

## Anomalies:

Redundancy = repeat data
Update anomalies = what if Fred moves to "Bellevue"?
Deletion anomalies = what if Joe deletes his phone number?

## Relation Decomposition

## Break the relation into two:

|  | Name | SSN | PhoneNumber | City |
| :---: | :---: | :---: | :---: | :---: |
|  | Fred | 123-45-6789 | 206-555-1234 | Seattle |
|  | Fred | 123-45-6789 | 206-555-6543 | Seattle |
|  | Joe | 987-65-4321 | 908-555-2121 | Westfield |
| Name | SSN | City | SSN | PhoneNumber |
| Fred | 123-45-6789 | Seattle | 123-45-6789 | 206-555-1234 |
| Joe | 987-65-4321 | Westfield | 123-45-6789 | 206-555-6543 |
| Anomalies have gone: |  |  | 987-65-4321 | 908-555-2121 |

No more repeated data
Easy to move Fred to "Bellevue" (how ?)
Easy to delete all Joe's phone numbers (how ?)

## Relational Schema Design (or Logical Design)

How do we do this systematically?

Start with some relational schema

Find out its functional dependencies (FDs)

Use FDs to normalize the relational schema

## Functional Dependencies (FDs)

## Definition

If two tuples agree on the attributes

$$
A_{1}, A_{2}, \ldots, A_{n}
$$

then they must also agree on the attributes

$$
B_{1}, B_{2}, \ldots, B_{m}
$$

Formally:

## $A_{1} \ldots A_{n}$ determines $B_{1} . . B_{m}$

$$
A_{1}, A_{2}, \ldots, A_{n} \rightarrow B_{1}, B_{2}, \ldots, B_{m}
$$

## Functional Dependencies (FDs)

Definition $A_{1}, \ldots, A_{m} \rightarrow B_{1}, \ldots, B_{n}$ holds in $R$ if: $\forall t, t^{\prime} \in R$,
(t. $A_{1}=t^{\prime} . A_{1} \wedge \ldots \wedge t . A_{m}=t^{\prime} . A_{m} \Rightarrow t . B_{1}=t^{\prime} . B_{1} \wedge \ldots \wedge t . B_{n}=$
$\left.t^{\prime} . B_{n}\right)$

if $t$, $\mathrm{t}^{\prime}$ agree here then t , $\mathrm{t}^{\prime}$ agree here

## Example

An FD holds, or does not hold on an instance:

| EmpID | Name | Phone | Position |
| :--- | :--- | :--- | :--- |
| E0045 | Smith | 1234 | Clerk |
| E3542 | Mike | 9876 | Salesrep |
| E1111 | Smith | 9876 | Salesrep |
| E9999 | Mary | 1234 | Lawyer |

EmpID $\rightarrow$ Name, Phone, Position
Position $\rightarrow$ Phone
but not Phone $\rightarrow$ Position

## Example

| EmpID | Name | Phone | Position |
| :--- | :--- | :--- | :--- |
| E0045 | Smith | 1234 | Clerk |
| E3542 | Mike | $9876 \leftarrow$ | Salesrep |
| E1111 | Smith | $9876 \leftarrow$ | Salesrep |
| E9999 | Mary | 1234 | Lawyer |

Position $\rightarrow$ Phone

## Example

| EmpID | Name | Phone | Position |
| :--- | :--- | :--- | :--- |
| E0045 | Smith | $1234 \rightarrow$ | Clerk |
| E3542 | Mike | 9876 | Salesrep |
| E1111 | Smith | 9876 | Salesrep |
| E9999 | Mary | $1234 \rightarrow$ | Lawyer |

But not Phone $\rightarrow$ Position

## Example name $\rightarrow$ color

 category $\rightarrow$ department color, category $\rightarrow$ price| name | category | color | department | price |
| :---: | :---: | :---: | :---: | :---: |
| Gizmo | Gadget | Green | Toys | 49 |
| Tweaker | Gadget | Green | Toys | 99 |

Do all the FDs hold on this instance?

## Example name $\rightarrow$ color

 category $\rightarrow$ department color, category $\rightarrow$ price| name | category | color | department | price |
| :---: | :---: | :---: | :---: | :---: |
| Gizmo | Gadget | Green | Toys | 49 |
| Tweaker | Gadget | Black | Toys | 99 |
| Gizmo | Stationary | Green | Office-supp. | 59 |

## Terminology

FD holds or does not hold on an instance

If we can be sure that every instance of $R$ will be one in which a given FD is true, then we say that $R$ satisfies the FD

If we say that $R$ satisfies an FD F, we are stating a constraint on $R$

## An Interesting Observation

name $\rightarrow$ color<br>category $\rightarrow$ department color, category $\rightarrow$ price

Then this FD also holds: name, category $\rightarrow$ price

If we find out from application domain that a relation satisfies some FDs, it doesn't mean that we found all the FDs that it satisfies!
There could be more FDs implied by the ones we have.

## Closure of a set of Attributes

Given a set of attributes $A_{1}, \ldots, A_{n}$

The closure, $\left\{A_{1}, \ldots, A_{n}\right\}^{+}=$the set of attributes $B$

$$
\text { s.t. } A_{1}, \ldots, A_{n} \rightarrow B
$$

Example: 1. name $\rightarrow$ color
2. category $\rightarrow$ department
3. color, category $\rightarrow$ price
name ${ }^{+}=$\{name, color\}
\{name, category $\}^{+}=\{$name, category, color, department, price\}
color $^{+}=$\{color $\}$

## Closure Algorithm

$$
X=\{A 1, \ldots, A n\} .
$$

Repeat until X doesn't change do: if $B_{1}, \ldots, B_{n} \rightarrow C$ is a FD and $B_{1}, \ldots, B_{n}$ are all in $X$
then add C to X .

## Example:

1. name $\rightarrow$ color
2. category $\rightarrow$ department
3. color, category $\rightarrow$ price
$\{\text { name, category }\}^{+}=$ \{

## Closure Algorithm

$X=\{A 1, \ldots, A n\}$.

Repeat until $X$ doesn't change do:
if $B_{1}, \ldots, B_{n} \rightarrow C$ is a FD and $B_{1}, \ldots, B_{n}$ are all in $X$
then add C to X .

## Example:

1. name $\rightarrow$ color
2. category $\rightarrow$ department
3. color, category $\rightarrow$ price
\{name, category ${ }^{+}=$
\{ name, category, color, department, price \}

## Closure Algorithm

$X=\{A 1, \ldots, A n\}$.

Repeat until $X$ doesn't change do:
if $B_{1}, \ldots, B_{n} \rightarrow C$ is a FD and $B_{1}, \ldots, B_{n}$ are all in $X$
then add C to X .

## Example:

1. name $\rightarrow$ color
2. category $\rightarrow$ department
3. color, category $\rightarrow$ price
\{name, category $\}^{+}=$
\{ name, category, color, department, price \}
Hence: name, category $\rightarrow$ color, department, price

## Example

In class:
R(A,B,C,D,E,F)

$$
\begin{array}{lll}
\mathrm{A}, \mathrm{~B} & \rightarrow \mathrm{C} \\
\mathrm{~A}, \mathrm{D} & \rightarrow & \mathrm{E} \\
\mathrm{~B} & \rightarrow & \mathrm{D} \\
\mathrm{~A}, \mathrm{~F} & \rightarrow & \mathrm{~B}
\end{array}
$$

Compute $\{\mathrm{A}, \mathrm{B}\}^{+} \quad \mathrm{X}=\{\mathrm{A}, \mathrm{B}$, \}

Compute $\{\mathrm{A}, \mathrm{F}\}^{+} \quad \mathrm{X}=\{\mathrm{A}, \mathrm{F}$, \}

## Example

In class:
R(A,B,C,D,E,F)

$$
\begin{array}{lll}
\mathrm{A}, \mathrm{~B} & \rightarrow \mathrm{C} \\
\mathrm{~A}, \mathrm{D} & \rightarrow & \mathrm{E} \\
\mathrm{~B} & \rightarrow & \mathrm{D} \\
\mathrm{~A}, \mathrm{~F} & \rightarrow & \mathrm{~B} \\
\hline
\end{array}
$$

Compute $\{\mathrm{A}, \mathrm{B}\}^{+} \quad \mathrm{X}=\{\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D}, \mathrm{E}\}$

Compute $\{A, F\}^{+} \quad X=\{A, F$, \}

## Example

In class:
R(A,B,C,D,E,F)

$$
\begin{array}{lll}
\mathrm{A}, \mathrm{~B} & \rightarrow \mathrm{C} \\
\mathrm{~A}, \mathrm{D} & \rightarrow & \mathrm{E} \\
\mathrm{~B} & \rightarrow & \mathrm{D} \\
\mathrm{~A}, \mathrm{~F} & \rightarrow & \mathrm{~B} \\
\hline
\end{array}
$$

Compute $\{\mathrm{A}, \mathrm{B}\}^{+} \quad \mathrm{X}=\{\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D}, \mathrm{E}\}$

Compute $\{\mathrm{A}, \mathrm{F}\}^{+} \quad \mathrm{X}=\{\mathrm{A}, \mathrm{F}, \mathrm{B}, \mathrm{C}, \mathrm{D}, \mathrm{E}\}$

## Example

In class:
R(A,B,C,D,E,F)

$$
\begin{array}{lll}
\mathrm{A}, \mathrm{~B} & \rightarrow & \mathrm{C} \\
\mathrm{~A}, \mathrm{D} & \rightarrow & \mathrm{E} \\
\mathrm{~B} & \rightarrow & \mathrm{D} \\
\mathrm{~A}, \mathrm{~F} & \rightarrow & \mathrm{~B}
\end{array}
$$

Compute $\{\mathrm{A}, \mathrm{B}\}^{+} \quad \mathrm{X}=\{\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D}, \mathrm{E}\}$

Compute $\{\mathrm{A}, \mathrm{F}\}^{+} \quad \mathrm{X}=\{\mathrm{A}, \mathrm{F}, \mathrm{B}, \mathrm{C}, \mathrm{D}, \mathrm{E}\}$

## Practice at Home

Find all FD's implied by:

$$
\begin{array}{lll}
\mathrm{A}, \mathrm{~B} & \rightarrow & \mathrm{C} \\
\mathrm{~A}, \mathrm{D} & \rightarrow & \mathrm{~B} \\
\mathrm{~B} & \rightarrow & \mathrm{D}
\end{array}
$$

## Practice at Home

Find all FD's implied by:

$$
\begin{array}{lll}
\mathrm{A}, \mathrm{~B} & \rightarrow \mathrm{C} \\
\mathrm{~A}, \mathrm{D} & \rightarrow & \mathrm{~B} \\
\mathrm{~B} & \rightarrow & \mathrm{D}
\end{array}
$$

Step 1: Compute $\mathrm{X}^{+}$, for every X :

$$
\begin{aligned}
& \mathrm{A}+=\mathrm{A}, \mathrm{~B}+=\mathrm{BD}, \mathrm{C}+=\mathrm{C}, \mathrm{D}+=\mathrm{D} \\
& \mathrm{AB}+=\mathrm{ABCD}, \mathrm{AC}+=\mathrm{AC}, \mathrm{AD}+=\mathrm{ABCD}, \\
& \mathrm{BC}+=\mathrm{BCD}, \mathrm{BD}+=\mathrm{BD}, \mathrm{CD}+=\mathrm{CD} \\
& \mathrm{ABC}+=\mathrm{ABD}+=\mathrm{ACD}+=\mathrm{ABCD} \text { (no need to compute- why ?) } \\
& \mathrm{BCD}^{+}=\mathrm{BCD}, \mathrm{ABCD}+=\mathrm{ABCD}
\end{aligned}
$$

## Practice at Home

Find all FD's implied by:

$$
\begin{array}{lll}
\mathrm{A}, \mathrm{~B} & \rightarrow \mathrm{C} \\
\mathrm{~A}, \mathrm{D} & \rightarrow & \mathrm{~B} \\
\mathrm{~B} & \rightarrow & \mathrm{D}
\end{array}
$$

Step 1: Compute $\mathrm{X}^{+}$, for every X :

$$
\begin{aligned}
& A+=A, \quad B+=B D, \quad C+=C, \quad D+=D \\
& A B+=A B C D, A C+=A C, A D+=A B C D, \\
& B C+=B C D, B D+=B D, C D+=C D
\end{aligned}
$$

$\mathrm{ABC}+=\mathrm{ABD}+=\mathrm{ACD}+=\mathrm{ABCD}$ (no need to compute- why ?)
$B C D+$ BCD, $\quad A B C D+=A B C D$
Step 2: Enumerate all FD's $X \rightarrow Y$, s.t. $Y \subseteq X^{+}$and $X \cap Y=\varnothing$ : $\mathrm{AB} \rightarrow \mathrm{CD}, \mathrm{AD} \rightarrow \mathrm{BC}, \mathrm{ABC} \rightarrow \mathrm{D}, \mathrm{ABD} \rightarrow \mathrm{C}, \mathrm{ACD} \rightarrow \mathrm{B}$

## Keys

- A superkey is a set of attributes $A_{1}, \ldots, A_{n}$ s.t. for any other attribute $B$, we have $A_{1}, \ldots, A_{n} \rightarrow B$
- A key is a minimal superkey
- A superkey and for which no subset is a superkey


## Computing (Super)Keys

- For all sets X , compute $\mathrm{X}^{+}$
- If $\mathrm{X}^{+}=$[all attributes], then X is a superkey
- Try only the minimal X's to get the keys


## Example

# Product(name, price, category, color) 

## name, category $\rightarrow$ price category $\rightarrow$ color

What is the key?

## Example

## Product(name, price, category, color)

## name, category $\rightarrow$ price category $\rightarrow$ color

What is the key?
(name, category) + = \{ name, category, price, color \}
Hence (name, category) is a key

## Key or Keys ?

Can we have more than one key?

Given $R(A, B, C)$ define FD's s.t. there are two or more keys

## Key or Keys?

Can we have more than one key?

Given $R(A, B, C)$ define $F D$ 's s.t. there are two or more keys

$$
\begin{aligned}
& \mathrm{A} \rightarrow \mathrm{~B} \\
& \mathrm{~B} \rightarrow \mathrm{C} \\
& \mathrm{C} \rightarrow \mathrm{~A}
\end{aligned}
$$

$$
\begin{aligned}
& \mathrm{AB} \rightarrow \mathrm{C} \\
& \mathrm{BC} \rightarrow \mathrm{~A}
\end{aligned}
$$


$A \rightarrow B C$
$B \rightarrow A C$
what are the keys here?

## Eliminating Anomalies

| Name | SSN | PhoneNumber | City |
| :--- | :--- | :--- | :--- |
| Fred | $123-45-6789$ | $206-555-1234$ | Seattle |
| Fred | $123-45-6789$ | $206-555-6543$ | Seattle |
| Joe | $987-65-4321$ | $908-555-2121$ | Westfield |
| Joe | $987-65-4321$ | $908-555-1234$ | Westfield |

SSN $\rightarrow$ Name, City What is the key?

Suggest a rule for decomposing the table to eliminate anomalies

## Eliminating Anomalies

Main idea:

- $X \rightarrow A$ is OK if $X$ is a (super)key
- $X \rightarrow A$ is not OK otherwise
- Need to decompose the table, but how?


## Boyce-Codd Normal Form

There are no "bad" FDs:

Definition. A relation R is in BCNF if:
Whenever $X \rightarrow B$ is a non-trivial dependency, then $X$ is a superkey.

Equivalently: Definition. A relation R is in BCNF if: $\forall X$, either $X^{+}=X \quad$ or $X^{+}=$[all attributes]

## BCNF Decomposition Algorithm

Normalize(R)
find $X$ s.t.: $X \neq X^{+} \neq$[all attributes]
if (not found) then " $R$ is in BCNF"
let $Y=X^{+}-X ; \quad Z=[$ all attributes $]-X^{+}$ decompose $R$ into R1 $(X \cup Y)$ and R2 $(X \cup Z)$ Normalize(R1); Normalize(R2);


## Example

| Name | SSN | PhoneNumber | City |
| :--- | :--- | :--- | :--- |
| Fred | $123-45-6789$ | $206-555-1234$ | Seattle |
| Fred | $123-45-6789$ | $206-555-6543$ | Seattle |
| Joe | $987-65-4321$ | $908-555-2121$ | Westfield |
| Joe | $987-65-4321$ | $908-555-1234$ | Westfield |

## SSN $\rightarrow$ Name, City

The only key is: \{SSN, PhoneNumber\} Hence SSN $\rightarrow$ Name, City is a "bad" dependency


In other words:
SSN+ = Name, City and is neither SSN nor All Attributes

## Example BCNF Decomposition

| Name | SSN | City |
| :--- | :--- | :--- |
| Fred | $123-45-6789$ | Seattle |
| Joe | $987-65-4321$ | Westfield |

SSN $\rightarrow$ Name, City

| SSN | PhoneNumber |
| :--- | :--- |
| $123-45-6789$ | $206-555-1234$ |
| $123-45-6789$ | $206-555-6543$ |
| $987-65-4321$ | $908-555-2121$ |
| $987-65-4321$ | $908-555-1234$ |

Let's check anomalies:
Redundancy?
Update?
Delete?

Find X s.t.: $\mathrm{X} \neq \mathrm{X}^{+} \neq[$all attributes $]$

## Example BCNF Decomposition

Person(name, SSN, age, hairColor, phoneNumber) SSN $\rightarrow$ name, age age $\rightarrow$ hairColor

Find X s.t.: $\mathrm{X} \neq \mathrm{X}^{+} \neq[$all attributes $]$

## Example BCNF Decomposition

Person(name, SSN, age, hairColor, phoneNumber) SSN $\rightarrow$ name, age age $\rightarrow$ hairColor
Iteration 1: Person: SSN+ = SSN, name, age, hairColor Decompose into: P(SSN, name, age, hairColor) Phone(SSN, phoneNumber)


Find X s.t.: $\mathrm{X} \neq \mathrm{X}^{+} \neq$[all attributes]

## Example BCNF Decomposition

Person(name, SSN, age, hairColor, phoneNumber)

SSN $\rightarrow$ name, age age $\rightarrow$ hairColor

What are the keys?

Iteration 1: Person: SSN+ = SSN, name, age, hairColor Decompose into: P(SSN, name, age, hairColor) Phone(SSN, phoneNumber)

Iteration 2: P : age+ = age, hairColor
Decompose: People(SSN, name, age)
Hair(age, hairColor)
Phone(SSN, phoneNumber)

Find X s.t.: $\mathrm{X} \neq \mathrm{X}^{+} \neq$[all attributes]

## Example BCNF Decomposition

Person(name, SSN, age, hairColor, phoneNumber)
SSN $\rightarrow$ name, age age $\rightarrow$ hairColor

## Note the keys!

Iteration 1: Person: SSN+ = SSN, name, age, hairColor Decompose into: P(SSN, name, age, hairColor)

Phone(SSN, phoneNumber)

Iteration 2: P : age+ = age, hairColor
Decompose: People(SSN, name, age)
Hair(age, hairColor)
Phone(SSN, phoneNumber)
$R(A, B, C, D)$

## Practice at Home

$$
\begin{aligned}
& A \rightarrow B \\
& B \rightarrow C
\end{aligned}
$$

## R(A,B,C,D) <br> $A^{+}=A B C \neq A B C D$

## Practice at Home

$$
\begin{aligned}
& A \rightarrow B \\
& B \rightarrow C
\end{aligned}
$$



What happens if in R we first pick $\mathrm{B}^{+}$? Or $\mathrm{AB}^{+}$?

## Schema Refinements = Normal Forms

- 1st Normal Form = all tables are flat
- 2nd Normal Form = obsolete
- Boyce Codd Normal Form = today
- 3rd Normal Form = see book

