CSEP 544

Lecture 9: Provenance, Views

Announcements

- Homework 5:
 - See schedule examples in today's email
 - Minor mistakes fixed yesterday (see email)
 - Homework due next Monday
- Reading assignment next week:
 Long paper + short paper = 1 review
 - Long paper + short paper = 1 review
- Final Exam
 - Take home exam Saturday-Sunday 3/15-16

Data Provenance

Data Provenance

Provenance inside the DBMS
 – Will discuss today

- Provenance outside of the DBMS
 - Much more messy; there is a standard, OPM (Open Provenance Model)

Provenance Annotations

- Some query produces an output table T(A,B,C)
- We store it over some period of time
- Later we ask: "where did this tuple come from?"
- The "provenance annotation" answers this.

| Α | В | С |
|----|----|----|
| a1 | b1 | c1 |
| a2 | b1 | c1 |
| a2 | b2 | c2 |
| a2 | b2 | c3 |

provenance1 provenance2 provenance3 provenance4

Provenance Annotations

- Start by annotating each tuple in the original database with a unique identifier; can be the Tuple Id (TID)
- Next, compute the provenance expression inductively, based on the query plan



Join Operator



Projection Operator



Union Operator



| Α | В | |
|----|----|-------|
| a1 | b1 | X1 |
| a2 | b2 | X2+Y1 |
| a3 | b3 | X3 |

Selection Operator



| Α | В | |
|----|----|----|
| a1 | b1 | X1 |
| a1 | b2 | X2 |

We could simply remove the tuples filtered out. But it's better to keep them around (we'll see why). What is their annotation?

Selection Operator



| Α | В | |
|----|----|--------|
| a1 | b1 | X1·1 |
| a1 | b2 | X2 · 1 |
| a2 | b1 | X3·0 |
| a2 | b2 | X4 · 0 |
| a2 | b3 | X5·0 |

We could simply remove the tuples filtered out. But it's better to keep them around (we'll see why). What is their annotation?

Simple Example 1

$\Pi_{AC}(R) \bowtie \Pi_{BC}(R) =$



| Α | В | С | |
|---|---|---|---|
| а | b | С | Х |
| d | b | е | Y |
| f | g | е | Ζ |

| Α | В | С | |
|---|---|---|-----|
| а | b | С | X·X |
| d | b | е | Υ·Υ |
| d | g | е | Υ·Ζ |
| f | b | е | Ζ·Υ |
| f | g | е | Ζ·Ζ |

Discuss in class what these annotations mean

Simple Example 2

 $\sigma_{C=e}(R) =$

R =



| Α | В | С | |
|---|---|---|--------------------------|
| а | b | С | $0 = \mathbf{X} \cdot 0$ |
| d | b | е | $Y = \mathbf{Y} \cdot 1$ |
| f | g | е | Z = Z · 1 |

Discuss in class what these annotations mean

Complex Example

$\sigma_{\mathsf{C=e}} \Pi_{\mathsf{AC}}(\ \Pi_{\mathsf{AC}}(\mathsf{R}) \bowtie \Pi_{\mathsf{BC}}(\mathsf{R}) \cup \Pi_{\mathsf{AB}}(\mathsf{R}) \bowtie \Pi_{\mathsf{BC}}(\mathsf{R})) =$

R =

| Α | В | С | |
|---|---|---|---|
| а | b | С | Х |
| d | b | е | Y |
| f | g | е | Z |

| Α | С | |
|---|---|--|
| а | С | $(X \cdot X + X \cdot X) \cdot 0 = 0 \cdot 2 \cdot \mathbf{X}^2 = 0$ |
| а | е | $X \cdot Y \cdot 1 = X \cdot Y$ |
| d | С | $Y \cdot X \cdot 0 = 0$ |
| d | е | $(\mathbf{Y} \cdot \mathbf{Y} + \mathbf{Y} \cdot \mathbf{Z} + \mathbf{Y} \cdot \mathbf{Y}) \cdot 1 = 2 \cdot \mathbf{Y}^2 + \mathbf{Y} \cdot \mathbf{Z}$ |
| f | е | $(Z \cdot Z + Z \cdot Y + Z \cdot Z) \cdot 1 = 2 \cdot Z^2 + Y \cdot Z$ |

Discuss in class what these annotations mean

K-Relations

Definition. A K-relation is a relation where each tuple is annotated with an element from the set K.

What we have described so far is an extension of the positive operations of the relational algebra to K-relations

We assumed that K has the operators +, ·

Identities on Provenance Expressions

The problem:

- We have defined provenance for a query plan P
- Given a query Q, we want the provenance to be independent of the plan
- Needed: if P1=P2, then provenance(P1) = Provenance(P2)

Example



Do these plans compute the same provenance for the output (a,b)?







Example



Do these two plans compute the same provenance expression for the output (a)?

Y

V(x) := S(x)V(x) := T(x)q(x) := R(x), V(x)









Identities on Provenance Expressions

Definition. A structure (K, +, ·, 0, 1) is called a commutative semiring if:

- 1. (K,+,0) is a commutative monoid:
 - a. + is associative: (x+y)+z=x+(y+z)
 - b. + is commutative: x+y=y+x
 - c. 0 is the identity for +: x+0=0+x=x
- 2. $(K, \cdot, 1)$ is a commutative monoid:
 - a. ... (similar identities)
- 3. distributes over +: $x \cdot (y+z) = x \cdot y + x \cdot z$

4. For all x: $x \cdot 0 = 0 \cdot x = 0$

Identities on Provenance Expressions

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- 3. distributes over +: $x \cdot (y+z) = x \cdot y + x \cdot z$
- 4. For all x: $x \cdot 0 = 0 \cdot x = 0$

<u>**Theorem</u></u>. The standard identities of the Bag algebra hold for K-relations iff (K, +, \cdot, 0, 1) is a commutative semiring.</u>**



$\sigma_{\mathsf{C=e}} \Pi_{\mathsf{AC}}(\ \Pi_{\mathsf{AC}}(\mathsf{R}) \bowtie \Pi_{\mathsf{BC}}(\mathsf{R}) \cup \Pi_{\mathsf{AB}}(\mathsf{R}) \bowtie \Pi_{\mathsf{BC}}(\mathsf{R})) =$



$$\begin{array}{c|cc}
A & C \\
a & c \\
0 \\
a & e \\
X \cdot Y \\
d & e \\
2 \cdot Y^2 + Y \cdot Z \\
f & e \\
2 \cdot Z^2 + Y \cdot Z \\
\end{array}$$

Q: Suppose we delete the tuple (d,b,e) from R. Which tuple(s) disappear from the result?

$\sigma_{\mathsf{C=e}} \Pi_{\mathsf{AC}}(\ \Pi_{\mathsf{AC}}(\mathsf{R}) \bowtie \Pi_{\mathsf{BC}}(\mathsf{R}) \cup \Pi_{\mathsf{AB}}(\mathsf{R}) \bowtie \Pi_{\mathsf{BC}}(\mathsf{R})) =$



Q: Suppose we delete the tuple (d,b,e) from R. Which tuple(s) disappear from the result?

A: Set Y=0

$\sigma_{\mathsf{C=e}} \Pi_{\mathsf{AC}}(\ \Pi_{\mathsf{AC}}(\mathsf{R}) \bowtie \Pi_{\mathsf{BC}}(\mathsf{R}) \cup \Pi_{\mathsf{AB}}(\mathsf{R}) \bowtie \Pi_{\mathsf{BC}}(\mathsf{R})) =$



$$\begin{array}{c|c} A & C \\ \hline a & c \\ 0 \\ \hline a & e \\ \hline d & e \\ f & e \\ 2 \cdot Y^2 + Y \cdot Z \\ \hline \end{array}$$

Q: Suppose each tuple in R occurs 3 times (bag semantics). How many times occurs each tuple in the answer?

$\sigma_{\mathsf{C=e}} \Pi_{\mathsf{AC}}(\ \Pi_{\mathsf{AC}}(\mathsf{R}) \bowtie \Pi_{\mathsf{BC}}(\mathsf{R}) \cup \Pi_{\mathsf{AB}}(\mathsf{R}) \bowtie \Pi_{\mathsf{BC}}(\mathsf{R})) =$



Q: Suppose each tuple in R occurs 3 times (bag semantics). How many times occurs each tuple in the answer?

A. Set X=Y=Z=3

Sets of Contributing Tuples

$\sigma_{\mathsf{C=e}} \Pi_{\mathsf{AC}}(\ \Pi_{\mathsf{AC}}(\mathsf{R}) \bowtie \Pi_{\mathsf{BC}}(\mathsf{R}) \cup \Pi_{\mathsf{AB}}(\mathsf{R}) \bowtie \Pi_{\mathsf{BC}}(\mathsf{R})) =$



Trace only the set of input tuples that contributed to an output tuple

This is also a semi-ring! Which one?

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Variants of Provenance

- Depending on the application we may want to tune the degree of detail that we keep in the provenance
- Historically, researchers have first proposed ad-hoc definitions of provenance (often called *lineage*)
- Later, all these were proven to be special cases of semi-rings



Lineage [CuiWidomWiener'00] Set of contributing tuples **Semiring:** $(Lin(X), +, \cup, \bot, \varnothing)$



Why-provenance [Buneman'08] Set of sets of witnesses **Semiring:** (Why(X), \cup , \bigcup , \emptyset , { \emptyset })



Why-provenance [Buneman'08] Set of sets of <u>minimal</u> witnesses **Semiring:** (PosBool(X), Λ , V, \top , \bot)



Trio lineage [Das Sarma'08] Bags of sets of witnesses **Semiring:** (Trio(X), +, \cdot , 0, 1)



Polynomials with boolean coefficients [Green'09] Sets of bags of contributing tuples **Semiring:** $(B[X], +, \cdot, 0, 1)$



Provenance polynomials [Green'07] Bags of bags of contributing tuples **Semiring:** $(N[X], +, \cdot, 0, 1)$

Discretionary Access Control [LaPadula]

- Public = P
- Confidential = C
- Secret = S
- Top Secret = T
- No Such Thing... = 0



| В | С | |
|---|-------------|----------|
| b | С | X=C |
| b | е | Y=P |
| g | е | Z=T |
| | B b b | BCbcbege |

| Α | С | |
|---|---|-------------------------------|
| а | С | $2 \cdot X^2 = ?$ |
| а | е | X·Y = ? |
| d | е | $2 \cdot Y^2 + Y \cdot Z = ?$ |
| f | е | $2 \cdot Z^2 + Y \cdot Z = ?$ |

Discretionary Access Control [LaPadula]

- Public = P
- Confidential = C
- Secret = S
- Top Secret = T
- No Such Thing... = 0

Alice has clearance S:

- Alice can read C data
- Alice cannot read T data
- Alice can write T data
- Alice cannot read C data



Discretionary Access Control [LaPadula]

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Q: Join record A labeled C with record B labeled S. What is the label of (A,B)?
Discretionary Access Control [LaPadula]

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- Alice can write T data
- Alice cannot read C data



Q: Join record A labeled C with record B labeled S. What is the label of (A,B)? A: S

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Alice has clearance S:

- Alice can read C data
- Alice cannot read T data
- Alice can write T data
- Alice cannot read C data

Why??

Q: Join record A labeled C with record B labeled S. What is the label of (A,B)? A: S

Q: Eliminate duplicates {A, A, A,A} labeled T, C, C, S. What is the label of A?

Discretionary Access Control [LaPadula]

- Public = P
- Confidential = C
- Secret = S
- Top Secret = T
- No Such Thing... = 0

Alice has clearance S:

- Alice can read C data
- Alice cannot read T data
- Alice can write T data
- Alice cannot read C data

Why??

Q: Join record A labeled C with record B labeled S. What is the label of (A,B)? A: S

Q: Eliminate duplicates {A, A, A,A} labeled T, C, C, S. What is the label of A? A: C



(A, min, max, 0, P), where A = P < C < S < T < 0

Discretionary Access Control [LaPadula]

- Public = P
- Confidential = C
- Secret = S
- Top Secret = T
- No Such Thing... = 0



| Α | С | |
|---|---|-------------------------------|
| а | С | $2 \cdot X^2 = \mathbf{C}$ |
| а | е | $X \cdot Y = C$ |
| d | е | $2 \cdot Y^2 + Y \cdot Z = C$ |
| f | е | $2 \cdot Z^2 + Y \cdot Z = T$ |

(A, min, max, 0, P), where A = P < C < S < T < 0

Semirings

| (B, ∧, ∨, ⊤, ⊥) | Set semantics |
|--|--|
| (ℕ, +, ⋅, 0, 1) | Bag semantics |
| (Ρ(Ω) , ∪, ∩, ∅, Ω) | Probabilistic events [FuhrRölleke 97] |
| (BoolExp(X), ∧, ∨, ⊤, ⊥) | Conditional tables (c-tables) [ImielinskiLipski 84] |
| (R ₊ ∞, min, +, 1, 0) | Tropical semiring (cost/distrust score/confidence need) |
| (A, min, max, 0, P) where A = P < C < S < T < 0 | Access control levels [PODS8] |

A provenance hierarchy



A provenance hierarchy













Using homomorphisms to relate models



Homomorphism?

h(x+y) = h(x)+h(y) h(xy)=h(x)h(y) h(0)=0 h(1)=1Moreover, for these homomorphisms h(x)=x

Views

Overview

Views are ubiquitous in data management:

 Used in SQL as names for predefined queries

 More generally, any derived data is a <u>view</u>

Views

- A view in SQL =
 - A table computed from other tables, s.t., whenever the base tables are updated, the view is updated too
- More generally:
 - A view is derived data that keeps track of changes in the original data
- Compare:
 - A function computes a value from other values, but does not keep track of changes to the inputs

StorePrice(store, price)

A Simple View

Create a view that returns for each store the prices of products purchased at that store

> CREATE VIEW StorePrice AS SELECT DISTINCT x.store, y.price FROM Purchase x, Product y WHERE x.product = y.pname

> > This is like a new table StorePrice(store,price)

Purchase(customer, product, store) StorePrice(store, price) We Use a View Like Any Table

- A "high end" store is a store that sell some products over 1000.
- For each customer, return all the high end stores that they visit.

SELECT DISTINCT u.name, u.store FROM Purchase u, StorePrice v WHERE u.store = v.store AND v.price > 1000

Types of Views

• <u>Virtual</u> views

- Used in databases
- Computed only on-demand slow at runtime
- Always up to date

<u>Materialized</u> views

- Used in data warehouses
- Pre-computed offline fast at runtime
- May have stale data (must recompute or update)
- Indexes are materialized views

StorePrice(store, price)

Query Modification

For each customer, find all the high end stores that they visit.

CREATE VIEW StorePrice AS SELECT DISTINCT x.store, y.price FROM Purchase x, Product y WHERE x.product = y.pname

SELECT DISTINCT u.name, u.store FROM Purchase u, StorePrice v WHERE u.store = v.store AND v.price > 1000

StorePrice(store, price)

Query Modification

For each customer, find all the high end stores that they visit.



StorePrice(store, price)

Query Modification

For each customer, find all the high end stores that they visit.

SELECT DISTINCT u.customer, u.store FROM Purchase u, Purchase x, Product y WHERE u.store = x.store AND y.price > 1000 AND x.product = y.pname Notice that Purchase occurs twice. Why?

Modified query:

Modified and unnested query:



SELECT DISTINCT u.customer, u.store FROM Purchase u, (SELECT DISTINCT x.store, y.price FROM Purchase x, Product y WHERE x.product = y.pname) v WHERE u.store = v.store AND v.price > 1000

Purchase(customer, product, store) Product(pname, price) **Further Virtual View Optimization**

Retrieve all stores whose name contains ACME

CREATE VIEW StorePrice AS SELECT DISTINCT x.store, y.price FROM Purchase x, Product y WHERE x.product = y.pname

SELECT DISTINCT v.store FROM StorePrice v WHERE v.store like '%ACME%'

Purchase(customer, product, store) StorePrice(store, price) Product(pname, price) Further Virtual View Optimization

Retrieve all stores whose name contains ACME

CREATE VIEW StorePrice AS SELECT DISTINCT x.store, y.price FROM Purchase x, Product y WHERE x.product = y.pname

Modified query:

SELECT DISTINCT v.store FROM StorePrice v WHERE v.store like '%ACME%'

SELECT DISTINCT v.store FROM (SELECT DISTINCT x.store, y.price FROM Purchase x, Product y WHERE x.product = y.pname) v WHERE v.store like '%ACME%'

Purchase(customer, product, store) Product(pname, price) Further Virtual View Optimization

Retrieve all stores whose name contains ACME

```
SELECT DISTINCT x.store
FROM Purchase x, Product y
WHERE x.product = y.pname
AND x.store like '%ACME%'
```

We can further optimize! How?

Modified query:

Modified and unnested query:



SELECT DISTINCT v.store FROM (SELECT DISTINCT x.store, y.price FROM Purchase x, Product y WHERE x.product = y.pname) v WHERE v.store like '%ACME%'

Purchase(customer, product, store) Product(pname, price) **Further Virtual View Optimization**

Retrieve all stores whose name contains ACME

```
SELECT DISTINCT x.store
FROM Purchase x, Product y
WHERE x.product = y.pname
—AND-x.store like '%ACME%'
```

Modified and unnested query:

Assuming Product.pname is a key <u>and</u> Purchase.product is a foreign key



Final Query

SELECT DISTINCT x.store FROM Purchase x WHERE x.store like '%ACME%'

Applications of Virtual Views

- Increased physical data independence. E.g.
 - Vertical data partitioning
 - Horizontal data partitioning
- Logical data independence. E.g.
 - Change schemas of base relations (i.e., stored tables)
- Security
 - View reveals only what the users are allowed to know

Physical Data Independence: Vertical Partitioning



Vertical Partitioning

CREATE VIEW Resumes AS SELECT T1.ssn, T1.name, T1.address, T2.resume, T3.picture FROM T1,T2,T3 WHERE T1.ssn=T2.ssn and T2.ssn=T3.ssn

Vertical Partitioning

SELECT address FROM Resumes WHERE name = 'Sue'

We want the system to query only table T1.

Will that happen?

Vertical Partitioning

- Hot trend in databases today for analytics
- Main idea:
 - Storage = Column(TID, value) pairs
 - Sort by TID \rightarrow enables reconstructing the table
 - Compress \rightarrow great compression, minimize I/O
 - Updates = VERY, VERY expensive
- Companies: <u>C-Store</u> and <u>Vertica</u>

Customers

| SSN | Name | City |
|--------|-------|----------|
| 234234 | Mary | Huston |
| 345345 | Sue | Seattle |
| 345343 | Joan | Seattle |
| 234234 | Ann | Portland |
| | Frank | Calgary |
| | Jean | Montreal |

CustomersInHuston

| SSN | Name | City |
|--------|------|--------|
| 234234 | Mary | Huston |
| | | |

CustomersInSeattle

| | SSN | Name | City | |
|-----------|--------|------|---------|---|
| | 345345 | Sue | Seattle | |
| \bigvee | 345343 | Joan | Seattle | ノ |

.

CREATE VIEW Customers AS CustomersInHuston UNION ALL CustomersInSeattle UNION ALL

SELECT name FROM Customers WHERE city = 'Seattle'

Which tables are queried by the system ?

SELECT name FROM Customers WHERE city = 'Seattle'

Now even humans can't tell which table contains customers in Seattle


Horizontal Partitioning

A hack around the problem:



Horizontal Partitioning





SELECT name FROM CustomersInSeattle

Denormalization

- Pre-compute a view that is the join of several tables
- The view is now a relation that is not in BCNF (why not?)

Purchase(customer, product, store) Product(<u>pname</u>, price)

> CREATE VIEW CustomerPurchase AS SELECT x.customer, x.store, y.pname, y.price FROM Purchase x, Product y WHERE x.product = y.pname

Fred is not allowed to see Balance

Views and Security

John is not allowed to see >0 balances

Customers:

| Name | Address | Balance |
|------|----------|---------|
| Mary | Huston | 450.99 |
| Sue | Seattle | -240 |
| Joan | Seattle | 333.25 |
| Ann | Portland | -520 |

| Name | Address | Balance |
|------|----------|---------|
| Mary | Huston | 450.99 |
| Sue | Seattle | -240 |
| Joan | Seattle | 333.25 |
| Ann | Portland | -520 |

CREATE VIEW PublicCustomers SELECT Name, Address FROM Customers CREATE VIEW BadCreditCustomers SELECT * FROM Customers WHERE Balance < 0

Data Integration Terminology



Which one needs query expansion, which one needs query answering using views ?

Horizontal Partitioning as LAV

SELECT name

FROM CustomersInSeattle

CREATE VIEW CustomersInSeattle AS (SELECT * FROM Customers WHERE city = 'Seattle') CREATE VIEW CustomersInHuston AS (SELECT * FROM Customers WHERE city = 'Huston')

SELECT name FROM Customers WHERE city = 'Seattle'

Indexes are Materialized Views

Product(<u>pid</u>, name, weight, price, ...)

CREATE INDEX W ON Product(weight) CREATE INDEX P ON Product(price)

Indexes as LAV:

CREATE VIEW W AS SELECT weight, pid FROM Product y CREATE VIEW P AS SELECT price, pid FROM Product y SELECT weight, price FROM Product WHERE weight > 10 and price < 100

"Covering indexes": query uses <u>only</u> the indexes

SELECT x.weight, y.price FROM W x, P y WHERE x.weight > 10 and y.price < 100 and x.pid = y.pid

Answering Queries Using Views

- We have several materialized views:
 - V1, V2, ..., Vn
- Given a query Q
 - Answer it by using views instead of base tables
- Variation: *Query rewriting using views*
 - Answer it by rewriting it to another query first
- Example: if the views are indexes, then we rewrite the query to use indexes

Rewriting Queries Using Views

Purchase(buyer, seller, product, store) Person(<u>pname</u>, city)

Have this materialized view: CREATE VIEW SeattleView AS SELECT y.buyer, y.seller, y.product, y.store FROM Person x, Purchase y WHERE x.city = 'Seattle' AND x.pname = y.buyer

Goal: rewrite this query in terms of the view

SELECTy.buyer, y.sellerYFROMPerson x, Purchase yWHEREx.city = 'Seattle'ANDx..pname = y.buyer ANDy.product='gizmo'

Rewriting Queries Using Views



Rewriting is not always possible





Technical Aspects

• View inlining, or query modification

 Query answering using views

- Updating views
- Incremental view update



Technical Aspects of Views

- Simplifying queries after the views have been in-lined
 - Query un-nesting
 - Query minimization
- Handling updates
 - Updating virtual views
 - Incremental update of materialized views



Updatable Views

- Have a virtual view V(A1, A2, ...) over tables R1, R2, ...
- User wants to update a tuple in V – Insert/modify/delete
- Can we translate this into updates to R1, R2, ... ?
- If yes: V = "an updateable view"
- If not: V = "a non-updateable view"





INSERT INTO AcmePurchase VALUES('Joe', 'Gizmo')

CREATE VIEW AcmePurchase AS SELECT customer, product FROM Purchase WHERE store = 'AcmeStore'

| Updateable | |
|------------|---|
| view | |
| | - |





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Also known as *view synchronization*

- Immediate synchronization = after each update
- Deferred synchronization
 - Lazy = at query time
 - Periodic
 - Forced = manual

Order(<u>cid, pid</u>, date) Product(<u>pid</u>, name, price)

> CREATE VIEW FullOrder AS SELECT x.cid,x.pid,x.date,y.name,y.price FROM Order x, Product y WHERE x.pid = y.pid

UPDATE Product SET price = price / 2 WHERE pid = '12345'



UPDATE FullOrder SET price = price / 2 WHERE pid = '12345'

No need to recompute the entire view !

Product(pid, name, category, price)

CREATE VIEW Categories AS SELECT DISTINCT category FROM Product



It doesn't work ! Why ? How can we fix it ?

Product(pid, name, category, price)

CREATE VIEW Categories AS SELECT category, count(*) as c FROM Product GROUP BY category

DELETE Product WHERE pid = '12345' UPDATE Categories SET c = c-1 WHERE category in (SELECT category FROM Product WHERE pid = '12345'); DELETE Categories WHERE c = 0