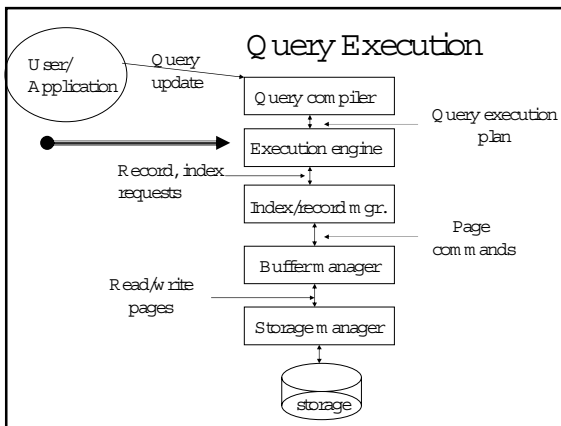


DBMS Internals Execution and Optimization

May 10th, 2004

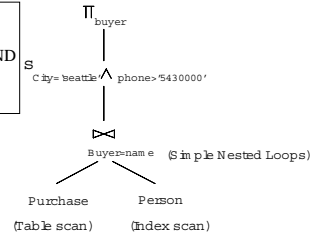
Agenda

- Questions on phase 2 of the project
- Today: DBMS internals part 2 –
 - Query execution
 - Query optimization
- Next week:
 - Thursday, not Monday.
 - Mostly Phil Bernstein on meta-data management.



Query Execution Plans

```
SELECT S.sname
FROM Purchase P, Person Q
WHERE P.buyer=Q.name AND
      Q.city='seattle' AND
      Q.phone > '5430000'
```



Query Plan:

- logical tree
- implementation choice at every node
- scheduling of operations.

Some operators are from relational algebra, and others (e.g., scan, group) are not.

The Leaves of the Plan: Scans

- Table scan: iterate through the records of the relation.
- Index scan: go to the index, from there get the records in the file (when would this be better?)
- Sorted scan: produce the relation in order. Implementation depends on relation size.

How do we combine Operations?

- The iterator model. Each operation is implemented by 3 functions:
 - Open: sets up the data structures and performs initializations
 - GetNext: returns the next tuple of the result.
 - Close: ends the operations. Cleans up the data structures.
- Enables pipelining!
- Contrast with data-driven materialize model.
- Sometimes it's the same (e.g., sorted scan).

Implementing Relational Operations

- We will consider how to implement:
 - Selection (σ) Selects a subset of rows from relation.
 - Projection (π) Deletes unwanted columns from relation.
 - Join (\bowtie) Allows us to combine two relations.
 - Set-difference Tuples in reh. 1, but not in reh. 2.
 - Union Tuples in reh. 1 and in reh. 2.
 - Aggregation (SUM, MIN, etc.) and GROUP BY

Schema for Examples

Purchase (buyer:string, seller:string, product:integer),

Person (name:string, city:string, phone:integer)

- Purchase:
 - Each tuple is 40 bytes long, 100 tuples per page, 1000 pages (i.e., 100,000 tuples, 4M B for the entire relation).
- Person:
 - Each tuple is 50 bytes long, 80 tuples per page, 500 pages (i.e., 40,000 tuples, 2M B for the entire relation).

Simple Selections

```
SELECT *
FROM Person R
WHERE R.phone < '543%'
```

- Of the form $\sigma_{R.attr \text{ op value}}(R)$
- With no index, unsorted: Must essentially scan the whole relation; cost is M (#pages in R).
- With an index on selection attribute: Use index to find qualifying data entries, then retrieve corresponding data records. (Hash index useful only for equality selections.)
- Result size estimation:
 - (Size of R) * reduction factor.
 - More on this later.

Using an Index for Selections

- Cost depends on #qualifying tuples, and clustering.
 - Cost of finding qualifying data entries (typically small) plus cost of retrieving records.
 - In example, assuming uniform distribution of phones, about 54% of tuples qualify (500 pages, 50000 tuples). With a clustered index, cost is little more than 500 I/Os; if unclustered, up to 50000 I/Os!
- Important refinement for unclustered indexes:
 1. Find sort the rid's of the qualifying data entries.
 2. Fetch rids in order. This ensures that each data page is looked at just once (though # of such pages likely to be higher than with clustering).

Two Approaches to General Selections

- First approach: Find the most selective access path, retrieve tuples using it, and apply any remaining terms that don't match the index:
 - Most selective access path: An index or file scan that we estimate will require the fewest page I/Os.
 - Consider `city= "seattle" AND phone< "543%"`:
 - A hash index on `city` can be used; then, `phone< "543%"` must be checked for each retrieved tuple.
 - Similarly, a b-tree index on `phone` could be used; `city= "seattle"` must then be checked.

Intersection of Rids

- Second approach
 - Get sets of rids of data records using each matching index.
 - Then intersect these sets of rids.
 - Retrieve the records and apply any remaining terms.

Implementing Projection

```
SELECT DISTINCT
  R.name,
  R.phone
FROM Person R
```

- Two parts:
 - (1) remove unwanted attributes,
 - (2) remove duplicates from the result.
- Refinements to duplicate removal:
 - If an index on a relation contains all wanted attributes, then we can do an index-only scan.
 - If the index contains a subset of the wanted attributes, you can remove duplicates locally.

Equality Joins With One Join Column

JOIN

```
SELECT *
FROM Person R, Purchase S
WHERE R.name=S.buyer
```

- $R \bowtie S$ is a common operation. The cross product is too large. Hence, performing $R \cdot S$ and then a selection is too inefficient.
- Assume: M pages in R , p_r tuples per page, N pages in S , p_s tuples per page.
 - In our examples, R is Person and S is Purchase.
- Cost metric: # of I/Os. We will ignore output costs.

Discussion

- How would you implement join?

Simple Nested Loops Join

For each tuple r in R do
 for each tuple s in S do
 if $r_1 == s_j$ then add $\langle r, s \rangle$ to result

- For each tuple in the outer relation R , we scan the entire inner relation S .
 - Cost: $M + (p_r * M) * N = 1000 + 100 * 1000 * 500$ I/Os: 140 hours!
- Page-oriented Nested Loops join: For each page of R , get each page of S , and write out matching pairs of tuples $\langle r, s \rangle$, where r is in R -page and S is in S -page.
 - Cost: $M + M * N = 1000 + 1000 * 500$ (1.4 hours)

Index Nested Loops Join

foreach tuple r in R do
 foreach tuple s in S where $r_1 == s_j$ do
 add $\langle r, s \rangle$ to result

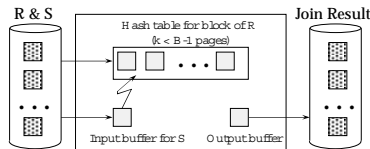
- If there is an index on the join column of one relation (say S), can make it the inner.
 - Cost: $M + (M * p_r) * \text{cost of finding matching } S \text{ tuples}$
- For each R tuple, cost of probing S index is about 1.2 for hash index, 2-4 for B+ tree. Cost of then finding S tuples depends on clustering.
 - Clustered index: 1 I/O (typical), unclustered: up to 1 I/O per matching S tuple.

Examples of Index Nested Loops

- Hash-index on name of Person (as inner):
 - Scan Purchase: 1000 page I/Os, 100*1000 tuples.
 - For each Person tuple: 1.2 I/Os to get data entry in index, plus 1 I/O to get (the exactly one) matching Person tuple. Total: 220,000 I/Os. (36 minutes)
- Hash-index on buyer of Purchase (as inner):
 - Scan Person: 500 page I/Os, 80*500 tuples.
 - For each Person tuple: 1.2 I/Os to find index page with data entries, plus cost of retrieving matching Purchase tuples. Assuming uniform distribution, 2.5 purchases per buyer (100,000 / 40,000). Cost of retrieving them is 1 or 2.5 I/Os depending on clustering.

Block Nested Loops Join

- Use one page as an input buffer for scanning the inner S , one page as the output buffer, and use all remaining pages to hold "block" of outer R .
 - For each matching tuple r in R -block, s in S -page, add $\langle r, s \rangle$ to result. Then read next R -block, scan S , etc.



Sort-Merge Join ($R \bowtie_{i,j} S$)

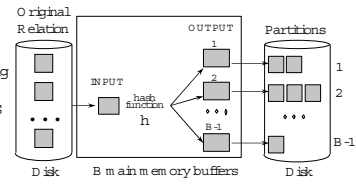
- Sort R and S on the join column n , then scan them to do a "merge" on the join column.
 - Advance scan of R until current R -tuple \geq current S tuple, then advance scan of S until current S -tuple \geq current R tuple; do this until current R tuple = current S tuple.
 - At this point, all R tuples with same value and all S tuples with same value match; output $\langle r, s \rangle$ for all pairs of such tuples.
 - Then resume scanning R and S .

Cost of Sort-Merge Join

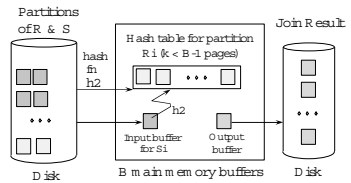
- R is scanned once; each S group is scanned once per matching R tuple.
- Cost: $M \log M + N \log N + (M + N)$
- But really, we can do it in $3(M + N)$ with some trickery.
 - The cost of scanning, $M + N$, could be $M * N$ (unlikely!)
- With 35, 100 or 300 buffer pages, both Person and Purchase can be sorted in 2 passes; total: 7500. (75 seconds).

Hash-Join

- Partition both relations using hash $fn h$: R tuples in partition i will only match S tuples in partition i .



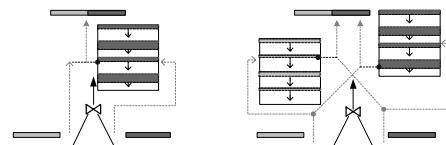
- Read in a partition of R , hash it using h_2 ($\ll h$). Scan matching partition of S , search for matches.



Cost of Hash-Join

- In partitioning phase, read + write both relations; $2(M + N)$. In matching phase, read both relations; $M + N$ I/Os.
- In our running example, this is a total of 4500 I/Os. (45 seconds!)
- Sort-Merge Join vs. Hash Join:
 - Given a minimum amount of memory both have a cost of $3(M + N)$ I/Os. Hash Join superior on this count if relation sizes differ greatly. Also, Hash Join shown to be highly parallelizable.
 - Sort-Merge less sensitive to data skew; result is sorted.

Double Pipelined Join (Tukwila)



Hash Join

- 8 Partially pipelined: no output until inner read
- 8 Asymmetric (inner vs. outer) — optimization requires source behavior/knowledge

Double Pipelined Hash Join

- 4 Outputs data immediately
- 4 Symmetric — requires less source knowledge to optimize

Query Optimization

Discussion

- How would you build a query optimizer?

Query Optimization Process (simplified a bit)

- Parse the SQL query into a logical tree:
 - identify distinct blocks (corresponding to nested sub-queries or views).
- Query rewrite phase:
 - apply algebraic transformations to yield a cheaper plan.
 - Merge blocks and move predicates between blocks.
- Optimize each block: join ordering.
- Complete the optimization: select scheduling (pipelining strategy).

Building Blocks

- Algebraic transformations (many and wacky).
- Statistical model: estimating costs and sizes.
- Finding the best join trees:
 - Bottom-up (dynamic programming): System-R
- Newer architectures:
 - Starburst: rewrite and then tree find
 - Volcano: all at once, top-down.

Key Lessons in Optimization

- There are many approaches and many details to consider in query optimization
 - Classic search/optimization problem!
 - Not completely solved yet!
- Main points to take away are:
 - Algebraic rules and their use in transformations of queries.
 - Deciding on join ordering: System-R style (Selinger style) optimization.
 - Estimating cost of plans and sizes of intermediate results.

Operations (revisited)

- Scan ([index], table, predicate):
 - Either index scan or table scan.
 - Try to push down sargable predicates.
- Selection (filter)
- Projection (always need to go to the data?)
- Joins: nested loop (indexed), sort-merge, hash, outer join.
- Grouping and aggregation (usually the last).

Algebraic Laws

- Commutative and Associative Laws
 - $R \cup S = S \cup R$, $R \cup (S \cap T) = (R \cup S) \cap T$
 - $R \cap S = S \cap R$, $R \cap (S \cup T) = (R \cap S) \cup T$
 - $R \times S = S \times R$, $R \times (S \times T) = (R \times S) \times T$
- Distributive Laws
 - $R \times (S \cup T) = (R \times S) \cup (R \times T)$

Algebraic Laws

- Laws involving selection:
 - $\sigma_{C \text{ AND } C'}(R) = \sigma_C(\sigma_{C'}(R)) = \sigma_C(R) \cap \sigma_{C'}(R)$
 - $\sigma_{C \text{ OR } C'}(R) = \sigma_C(R) \cup \sigma_{C'}(R)$
 - $\sigma_C(R \times S) = \sigma_C(R) \times S$
 - When C involves only attributes of R
 - $\sigma_C(R - S) = \sigma_C(R) - S$
 - $\sigma_C(R \cup S) = \sigma_C(R) \cup \sigma_C(S)$
 - $\sigma_C(R \cap S) = \sigma_C(R) \cap S$

Algebraic Laws

- Example: $R(A, B, C, D), S(E, F, G)$
 - $\sigma_{F=3}(\sigma_{D=E} S) = ?$
 - $\sigma_{A=5 \text{ AND } G=9}(\sigma_{D=E} S) = ?$

Algebraic Laws

- Laws involving projections
 - $P_M(R \times S) = P_N(P_P(R) \times P_Q(S))$
 - Where N, P, Q are appropriate subsets of attributes of M
 - $P_M(P_N(R)) = P_{M \cap N}(R)$
- Example $R(A, B, C, D), S(E, F, G)$
 - $P_{A, B, G}(\sigma_{D=E} S) = P_{?}(P_{?}(R) \times P_{?}(S))$

Query Rewrites: Sub-queries

```
SELECT EmpName
FROM Emp
WHERE EmpAge < 30
      AND EmpDept# IN
      (SELECT DeptDept#
       FROM Dept
       WHERE DeptLoc = "Seattle"
       AND EmpEmph# = DeptMgr)
```

The Un-Nested Query

```
SELECT EmpName
FROM Emp, Dept
WHERE EmpAge < 30
      AND EmpDept# = DeptDept#
      AND DeptLoc = "Seattle"
      AND EmpEmph# = DeptMgr
```

Converting Nested Queries

```
Select distinct x.name, x.maker
From productx
Where x.color= "blue"
AND x.price >= ALL (Select y.price
                    From producty
                    Where y.maker= x.maker
                    AND y.color= "blue")
```

Converting Nested Queries

Let's compute the complement first:

```
Select distinct x.name, x.maker
From productx
Where x.color= "blue"
AND x.price < SOME (Select y.price
                    From producty
                    Where y.maker= x.maker
                    AND y.color= "blue")
```

Converting Nested Queries

This one becomes a SFW query:

```
Select distinct x.name, x.maker
From productx, producty
Where x.color= "blue" AND x.maker= y.maker
AND y.color= "blue" AND x.price < y.price
```

This returns exactly the products we DON'T want, so...

Converting Nested Queries

```
(Select x.name, x.maker
From productx
Where x.color= "blue")
EXCEPT
(Select x.name, x.maker
From productx, producty
Where x.color= "blue" AND x.maker= y.maker
AND y.color= "blue" AND x.price < y.price)
```

Semi-Joins, Magic Sets

- You can't always un-nest sub-queries (it's tricky).
- But you can often use a semi-join to reduce the computation cost of the inner query.
- A magic set is a superset of the possible bindings in the result of the sub-query.
- Also called "side ways information passing".
- Great idea; reinvented every few years on a regular basis.

Rewrites: Magic Sets

```
Create View DepAvgSalAS
(Select E.did, Avg(E.sal) as avgSal
From Emp E
Group By E.did)

Select E.aid, E.sal
From Emp E, DeptD, DepAvgSalV
Where E.did=D.did AND D.did=V.did
And E.age < 30 and D.budget > 100k
And E.sal > V.avgSal
```

Rewrites: SIPS

```

Select E.aid, E.sal
From Emp E, Dept D, DeptAvgSal V
Where E.did=D.did AND D.did=V.did
  And E.age < 30 and D.budget > 100k
  And E.sal > V.avgSal
• DeptAvgSal needs to be evaluated only for departments
  where V.did IN
Select E.did
From Emp E, Dept D
Where E.did=D.did
  And E.age < 30 and D.budget > 100K
    
```

Supporting Views

1. Create View PartialResultAs
(Select E.aid, E.sal, E.did
From Emp E, Dept D
Where E.did=D.did
 And E.age < 30 and D.budget > 100K.)
2. Create View FilterAS
Select DISTINCT P.did FROM PartialResultP.
2. Create View LimitedAvgSalas
(Select F.did Avg(E.Sal) as avgSal
From Emp E, Filter F
Where E.did=F.did
Group By F.did)

And Finally...

Transformed query:

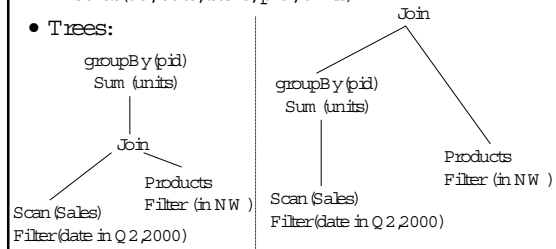
```

Select P.aid, P.sal
From PartialResultP, LimitedAvgSalV
Where P.did=V.did
  And P.sal > V.avgSal
    
```

Rewrites: Group By and Join

- Schema:
 - Product (pid, unitprice, ...)
 - Sales (tid, date, store, pid, units)

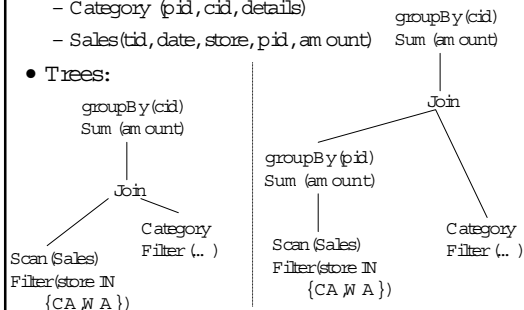
Trees:



Rewrites: Operation Introduction

- Schema: (pid determines cid)
 - Category (pid, cid, details)
 - Sales (tid, date, store, pid, amount)

Trees:



Schema for Some Examples

Sailors (*sid*: integer, *sname*: string, *rating*: integer, *age*: real)
Reserves (*sid*: integer, *bid*: integer, *day*: dates, *rname*: string)

- Reserves:
 - Each tuple is 40 bytes long, 100 tuples per page, 1000 pages (4000 tuples)
- Sailors:
 - Each tuple is 50 bytes long, 80 tuples per page, 500 pages (4000 tuples).

Query Rewriting: Predicate Pushdown

The earlier we process selections, less tuples we need to manipulate higher up in the tree.

Disadvantages?

Query Rewrites: Predicate Pushdown (through grouping)

```

Select bid, Max(age)
From Reserves R, Sailors S
Where R.sid=S.sid
GroupBy bid
Having Max(age) > 40

```

```

Select bid, Max(age)
From Reserves R, Sailors S
Where R.sid=S.sid and
      S.age > 40
GroupBy bid

```

- For each boat, find the maximum age of sailors who've reserved it.
- Advantage: the size of the join will be smaller.
- Requires transformation rules specific to the grouping/aggregation operators.
- Will it work if we replace Max by Min?

Query Rewrite: Predicate Moveraround

Sailing wizard dates: when did the youngest of each sailor level rent boats?

```

Select sid, date
From V1, V2
Where V1.rating = V2.rating and
      V1.age = V2.age

```

Create View V1 AS

```

Select rating, M in (age)
From Sailors S
Where S.age < 20
GroupBy rating

```

Create View V2 AS

```

Select sid, rating, age, date
From Sailors S, Reserves R
Where R.sid=S.sid

```

Query Rewrite: Predicate Moveraround

Sailing wizard dates: when did the youngest of each sailor level rent boats?

First, move predicates up the tree.

```

Select sid, date
From V1, V2
Where V1.rating = V2.rating and
      V1.age = V2.age, age < 20

```

Create View V1 AS

```

Select rating, M in (age)
From Sailors S
Where S.age < 20
GroupBy rating

```

Create View V2 AS

```

Select sid, rating, age, date
From Sailors S, Reserves R
Where R.sid=S.sid

```

Query Rewrite: Predicate Moveraround

Sailing wizard dates: when did the youngest of each sailor level rent boats?

First, move predicates up the tree.

```

Select sid, date
From V1, V2
Where V1.rating = V2.rating and
      V1.age = V2.age, and age < 20

```

Then, move them down.

Create View V1 AS

```

Select rating, M in (age)
From Sailors S
Where S.age < 20
GroupBy rating

```

Create View V2 AS

```

Select sid, rating, age, date
From Sailors S, Reserves R
Where R.sid=S.sid, and
      S.age < 20.

```

Query Rewrite Summary

- The optimizer can use any semantically correct rule to transform one query to another.
- Rules try to:
 - move constraints between blocks (because each will be optimized separately)
 - unnest blocks
- Especially important in decision support applications where queries are very complex.
- In a few minutes of thought, you'll come up with your own rewrite. Some queries, some rewrite, will benefit from it.
- Theorems?

Cost Estimation

- For each plan considered, must estimate cost:
 - Must estimate cost of each operation in plan tree.
 - Depends on input cardinalities.
 - Must estimate size of result for each operation in tree!
 - Use information about the input relations.
 - For selections and joins, assume independence of predicates.
- We'll discuss the System R cost estimation approach.
 - Very inexact, but works ok in practice.
 - More sophisticated techniques known now.

Statistics and Catalogs

- Need information about the relations and indexes involved. Catalogs typically contain at least:
 - # tuples (N Tuples) and # pages (N Pages) for each relation.
 - # distinct key values (N Keys) and N Pages for each index.
 - Index height, low/high key values (Low/High) for each tree index.
- Catalogs updated periodically.
 - Updating whenever data changes is too expensive; lots of approximation anyway, so slight inconsistency ok.
- More detailed information (e.g., histograms of the values in some field) are sometimes stored.

Size Estimation and Reduction

Factors

```
SELECT attribute list
FROM relation list
WHERE term1 AND ... AND termk
```

- Consider a query block:
- Maximum # tuples in result is the product of the cardinalities of relations in the FROM clause.
- Reduction factor (RF) associated with each term reflects the impact of the term in reducing result size. Result cardinality = Max # tuples * product of all RF's.
 - Implicit assumption that terms are independent!
 - Term $col = value$ has $RF = 1/NKeys(i)$, given index i on col .
 - Term $col1 = col2$ has $RF = 1/MAX(NKeys(i1), NKeys(i2))$
 - Term $col > value$ has $RF = (High(i) - value) / (High(i) - Low(i))$

Histograms

- Key to obtaining good cost and size estimates.
- Come in several flavors:
 - Equi-depth
 - Equi-width
- Which is better?
- Compressed histograms: special treatment of frequent values.

Histograms

- Statistics on data maintained by the RDBMS
- Makes size estimation much more accurate (hence, cost estimations are more accurate)

Histograms

Employee (ssn, name, salary, phone)

- Maintain a histogram on salary:

Salary:	0..20k	20k..40k	40k..60k	60k..80k	80k..100k	> 100k
Tuples	200	800	5000	12000	6500	500

- T (Employee) = 25000, but now we know the distribution

Histograms

Ranks(rankName, salary)

- Estimate the size of Employee \bowtie_{Salary} Ranks

Employee	0..20k	20k..40k	40k..60k	60k..80k	80k..100k	> 100k
	200	800	5000	12000	6500	500

Ranks	0..20k	20k..40k	40k..60k	60k..80k	80k..100k	> 100k
	8	20	40	80	100	2

Histograms

- Assume:
 - $V(\text{Employee, Salary}) = 200$
 - $V(\text{Ranks, Salary}) = 250$
- Then $T(\text{Employee} \bowtie_{\text{Salary}} \text{Ranks}) =$

$$= \sum_{i=1,6} T_i T_i' / 250$$

$$= (200 \times 8 + 800 \times 20 + 5000 \times 40 + 12000 \times 80 + 6500 \times 100 + 500 \times 2) / 250$$

$$= \dots$$

Plans for Single-Relation Queries (Prep for Join ordering)

- Task: create a query execution plan for a single Select-project-group-by block.
- Key idea: consider each possible access path to the relevant tuples of the relation. Choose the cheapest one.
- The different operations are essentially carried out together (e.g., if an index is used for a selection, projection is done for each retrieved tuple, and the resulting tuples are pipelined into the aggregate computation).

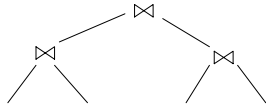
Example

```
SELECT S.sid
FROM Sailors S
WHERE S.rating=8
```

- If we have an index on rating:
 - $(1/N \text{Keys}(I)) * N \text{Tuples}(R) = (1/10) * 40000$ tuples retrieved.
 - Clustered index: $(1/N \text{Keys}(I)) * N \text{Pages}(I) = (1/10) * (50+500)$ pages are retrieved (= 55).
 - Unclustered index: $(1/N \text{Keys}(I)) * (N \text{Pages}(I) + N \text{Tuples}(R)) = (1/10) * (50+40000)$ pages are retrieved.
- If we have an index on sid:
 - Would have to retrieve all tuples/pages. With a clustered index, the cost is $50+500$.
- Doing a file scan: we retrieve all file pages (500).

Determining Join Ordering

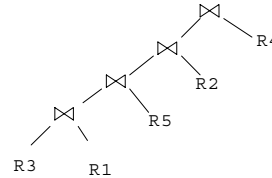
- $R_1 \bowtie R_2 \bowtie \dots \bowtie R_n$
- Join tree:



- A join tree represents a plan. An optimizer needs to inspect many (all?) join trees

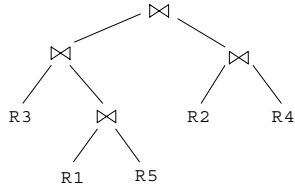
Types of Join Trees

- Left deep:



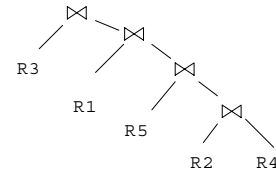
Types of Join Trees

- Bushy:



Types of Join Trees

- Right deep:



Problem

- Given: a query $R_1 \bowtie R_2 \bowtie \dots \bowtie R_n$
- Assume we have a function $cost()$ that gives us the cost of every join tree
- Find the best join tree for the query

Dynamic Programming

- Idea: for each subset of $\{R_1, \dots, R_n\}$, compute the best plan for that subset
- In increasing order of set cardinality:
 - Step 1: for $\{R_1\}, \{R_2\}, \dots, \{R_n\}$
 - Step 2: for $\{R_1, R_2\}, \{R_1, R_3\}, \dots, \{R_{n-1}, R_n\}$
 - ...
 - Step n: for $\{R_1, \dots, R_n\}$
- A subset of $\{R_1, \dots, R_n\}$ is also called a subquery

Dynamic Programming

- For each subquery $Q \subseteq \{R_1, \dots, R_n\}$ compute the following:
 - Size(Q)
 - A best plan for Q: Plan(Q)
 - The cost of that plan: Cost(Q)

Dynamic Programming

- Step 1: For each $\{R_i\}$ do:
 - Size($\{R_i\}$) = B(R_i)
 - Plan($\{R_i\}$) = R_i
 - Cost($\{R_i\}$) = (cost of scanning R_i)

Dynamic Programming

- Step i: For each $Q \in \{R_1, \dots, R_n\}$ of cardinality i do:
 - Compute $\text{Size}(Q)$ (later..)
 - For every pair of subqueries Q', Q''
s.t. $Q = Q' \cup Q''$
compute $\text{cost}(\text{Plan}(Q') \bowtie \text{Plan}(Q''))$
 - $\text{Cost}(Q)$ = the smallest such cost
 - $\text{Plan}(Q)$ = the corresponding plan

Dynamic Programming

- Return $\text{Plan}(\{R_1, \dots, R_n\})$

Dynamic Programming

- Summary: computes optimal plans for subqueries:
 - Step 1: $\{R_1\}, \{R_2\}, \dots, \{R_n\}$
 - Step 2: $\{R_1, R_2\}, \{R_1, R_3\}, \dots, \{R_{n-1}, R_n\}$
 - ...
 - Step n: $\{R_1, \dots, R_n\}$
- We used naïve size/cost estimations
- In practice:
 - more realistic size/cost estimations (next)
 - heuristics for reducing the Search Space
 - Restrict to left-linear trees
 - Restrict to trees "w/ out cartesian product"
 - need more than just one plan for each subquery:
 - "interesting orders"