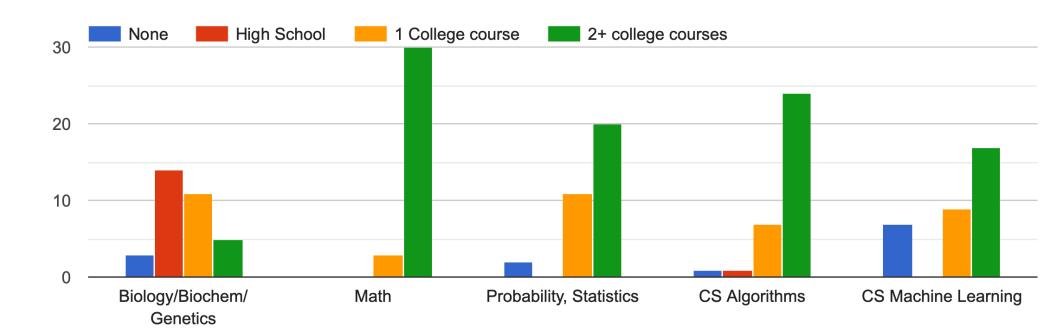
CSEP 527 Computational Biology Autumn 2020

Lectures 2-4
Sequence Alignment

20au Survey Results

Describe your experience in each of the following areas. ("None" is a ...



This week

Sequence alignment
Weekly "bio" interlude - DNA replication
More sequence alignment

What is an alignment?

Compare two strings to see how "similar" they are E.g., maximize the # of identical chars that line up

But we'll see more subtle measures

ATGTTAT vs ATCGTAC

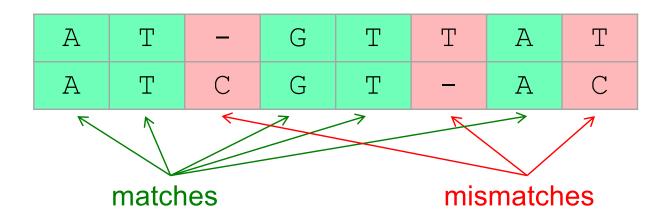
A	T	_	G	T	Т	A	T
А	Т	С	G	T	_	A	С

What is an alignment?

Compare two strings to see how "similar" they are E.g., maximize the # of identical chars that line up

But we'll see more subtle measures

ATGTTAT vs ATCGTAC



Sequence Alignment: Why

Biology

Among most widely used comp. tools in biology

DNA sequencing & assembly

New sequence always compared to data bases

Similar sequences often have similar origin and/or function

Recognizable similarity after 10⁸ –10⁹ yr

Other

spell check/correct, diff, svn/git/..., plagiarism, ...

BLAST Demo

http://www.ncbi.nlm.nih.gov/blast/

click "protein blast"

get seq from: http://www.uniprot.org/uniprot/P15172 i.e.:

>sp|P15172|MYOD1_HUMAN Myoblast determination protein 1 OS=Homo sapiens GN=MYOD1 PE=1 SV=3 MELLSPPLRDVDLTAPDGSLCSFATTDDFYDDPCFDSPDLRFFEDLDPRLMHVGALLKPE EHSHFPAAVHPAPGAREDEHVRAPSGHHQAGRCLLWACKACKRKTTNADRRKAATMRERR RLSKVNEAFETLKRCTSSNPNQRLPKVEILRNAIRYIEGLQALLRDQDAAPPGAAAAFYA PGPLPPGRGGEHYSGDSDASSPRSNCSDGMMDYSGPPSGARRRNCYEGAYYNEAPSEPRP GKSAAVSSLDCLSSIVERISTESPAAPALLLADVPSESPPRRQEAAAPSEGESSGDPTQS PDAAPQCPAGANPNPIYQVL

in blast window, paste "P15172" (or fasta above) in "query" box

adjust "alg parameters" to get top 1000 hits (or more)

click "BLAST" button.

scrolling to bottom of hits list & click may download all alignments, (otherwise it seems to download only 4 or 5 more when you scroll to bottom)

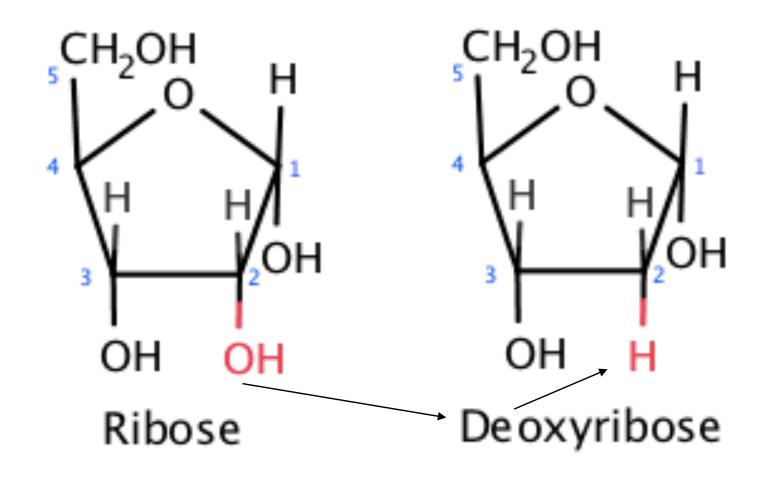
Also check out the "Graphic Summary", "Alignments", "Taxonomy" tabs, + "Distance tree of results"

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Lecture 3
Sequence Alignment

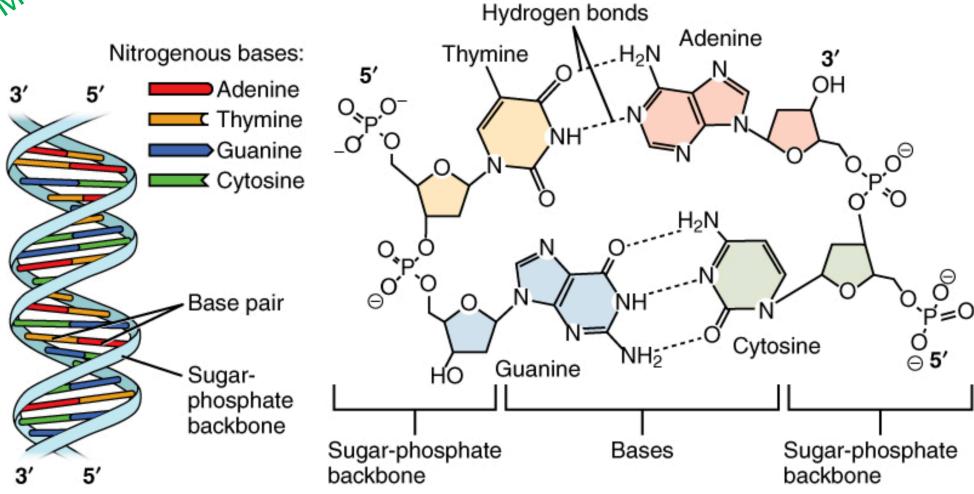
More on DWAIRNA

DNA, RNA, 3', 5', ...



More on DNAIRNA

Nucleotides

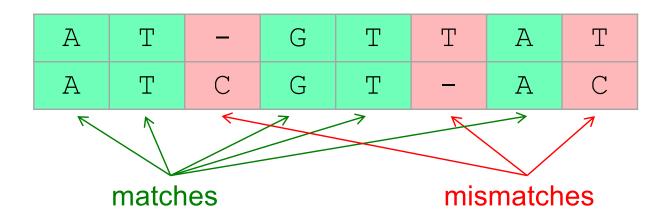


What is an alignment?

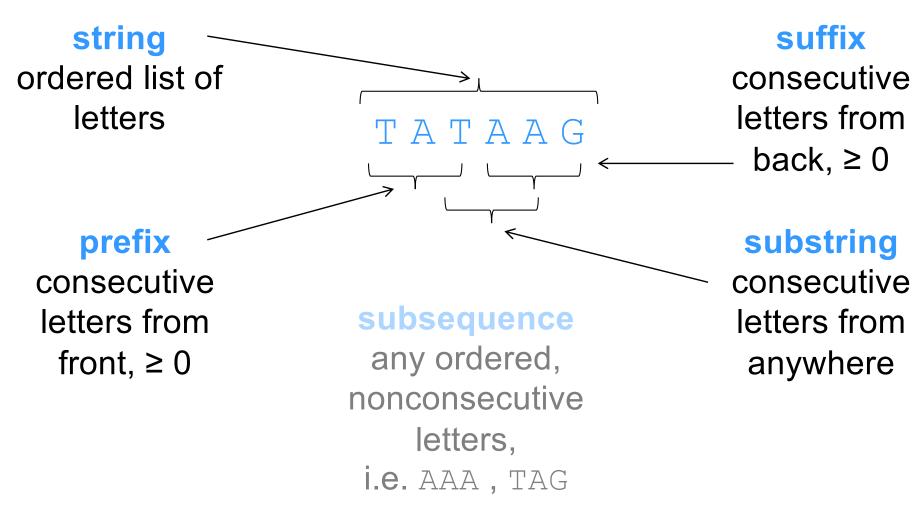
Compare two strings to see how "similar" they are E.g., maximize the # of identical chars that line up

But we'll see more subtle measures

ATGTTAT vs ATCGTAC



Terminology



Formal definition of an alignment

An alignment of strings S, T is a pair of strings S', T' with dash characters "-" inserted, so that

1.
$$|S'| = |T'|$$
, and ($|S| = \text{`length of S''}$)

Removing dashes leaves S, T

Consecutive dashes are called "a gap."

(NB: this is a defn for a general alignment, not necessarily optimal.)

Scoring an arbitrary alignment

Define a score for *pairs* of aligned chars, e.g.

$$\sigma(x, y) = \begin{cases} match & 2 \\ mismatch & -1 \end{cases}$$
 (Toy scores for examples in slides)

Apply that *per column*, then *add*.

Total Score = -2

More Realistic Scores: BLOSUM 62

(the " σ " scores)

	Α	R	N	D	C	Q	Ε	G	Н	Ι	L	K	M	F	P	S	Т	W	Υ	V
A	4	-1	-2	-2	0	-1	-1	0	-2	-1	-1	-1	-1	-2	-1	1	0	-3	-2	0
R	-1	5	0	-2	-3	1	0	-2	0	-3	-2	2	-1	-3	-2	-1	-1	-3	-2	-3
N	-2	0	6	1	-3	0	0	0	1	-3	-3	0	-2	-3	-2	1	0	-4	-2	-3
D	-2	-2	1	6	-3	0	2	-1	-1	-3	-4	-1	-3	-3	-1	0	-1	-4	-3	-3
C	0	-3	-3	-3	9	-3	-4	-3	-3	-1	-1	-3	-1	-2	-3	-1	-1	-2	-2	-1
Q	-1	1	0	0	-3	5	2	-2	0	-3	-2	1	0	-3	-1	0	-1	-2	-1	-2
Е	-1	0	0	2	-4	2	5	-2	0	-3	-3	1	-2	-3	-1	0	-1	-3	-2	-2
G	0	-2	0	-1	-3	-2	-2	6	-2	-4	-4	-2	-3	-3	-2	0	-2	-2	-3	-3
Н	-2	0	1	-1	-3	0	0	-2	8	-3	-3	-1	-2	-1	-2	-1	-2	-2	2	-3
Ι	-1	-3	-3	-3	-1	-3	-3	-4	-3	4	2	-3	1	0	-3	-2	-1	-3	-1	3
L	-1	-2	-3	-4	-1	-2	-3	-4	-3	2	4	-2	2	0	-3	-2	-1	-2	-1	1
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5	-1	-3	-1	0	-1	-3	-2	-2
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5	0	-2	-1	-1	-1	-1	1
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6	-4	-2	-2	1	3	-1
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7	-1	-1	-4	-3	-2
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4	1	-3	-2	-2
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5	-2	-2	0
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11	2	-3
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7	-1
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4

Optimal Alignment: A Simple Algorithm

for all subseqs A of S, B of T s.t. |A| = |B| **do** align A[i] with B[i], $1 \le i \le |A|$ align all other chars to spaces

compute its value retain the max

end

output the retained alignment

$$S = agct$$
 $A = ct$
 $T = wxyz$ $B = xz$
 $-agc-t$ $a-gc-t$
 $w--xyz$ $-w-xyz$

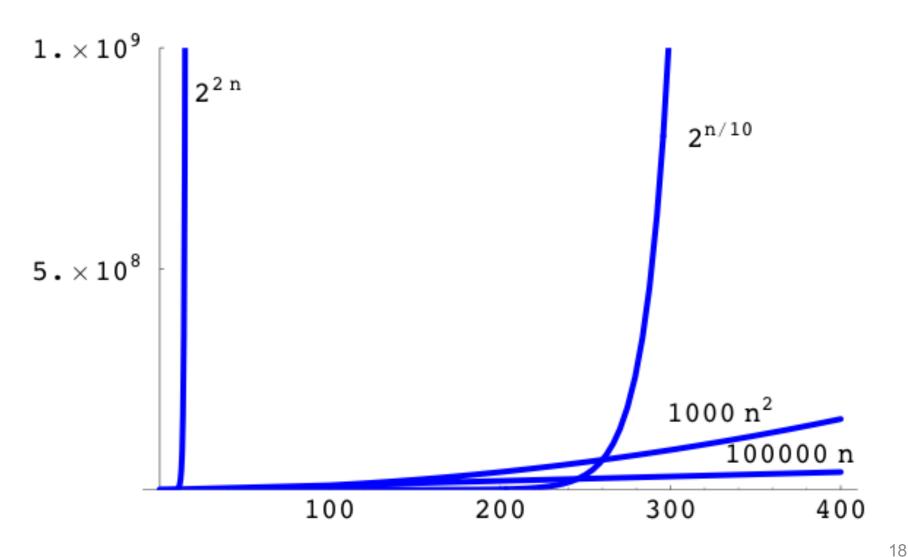
Analysis

Assume |S| = |T| = nCost of evaluating one alignment: $\geq n$

How many alignments are there:
$$\geq \binom{2n}{n}$$
 pick n chars of S,T together say k of them are in S match these k to the k *un*picked chars of T, rest to -

Total time:
$$\ge n \binom{2n}{n} > 2^{2n}$$
, for $n > 3$
E.g., for $n = 20$, time is $> 2^{40}$ operations

Polynomial vs Exponential Growth



Asymptotic Analysis

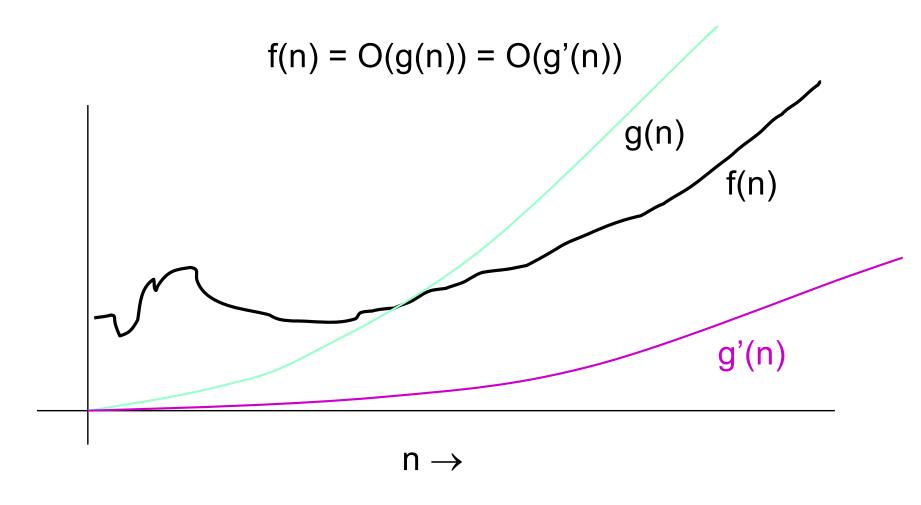
How does run time grow as a function of problem size?

```
n^2 or 100 n^2 + 100 n + 100 vs <math>2^{2n}
```

Defn: f(n) = O(g(n)) iff there is a constant c s.t. $|f(n)| \le cg(n)$ for all sufficiently large n.

100
$$n^2 + 100 n + 100 = O(n^2)$$
 [e.g. c = 101]
 $n^2 = O(2^{2n})$
 2^{2n} is *not* $O(n^2)$

Big-O Example



Utility of Asymptotics

"All things being equal," smaller asymptotic growth rate is better

All things are never equal

Even so, big-O bounds often let you quickly pick most promising candidates among competing algorithms

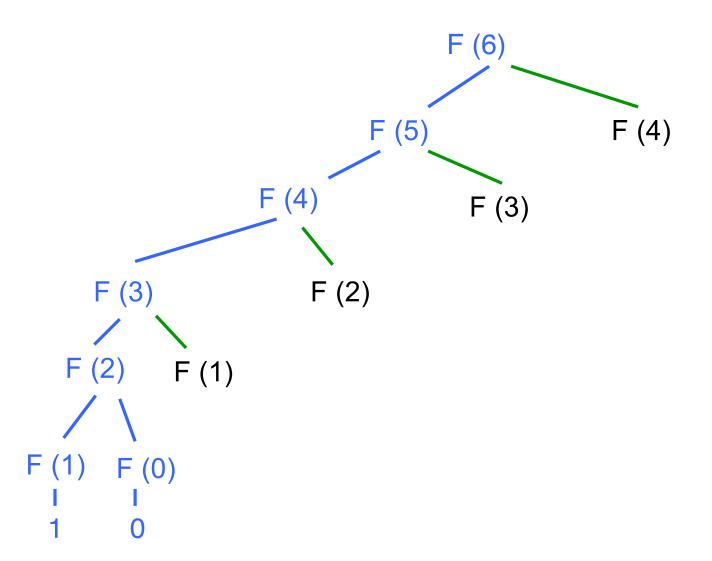
Poly time algs often practical; non-poly algs seldom are.

(Yes, there are exceptions.)

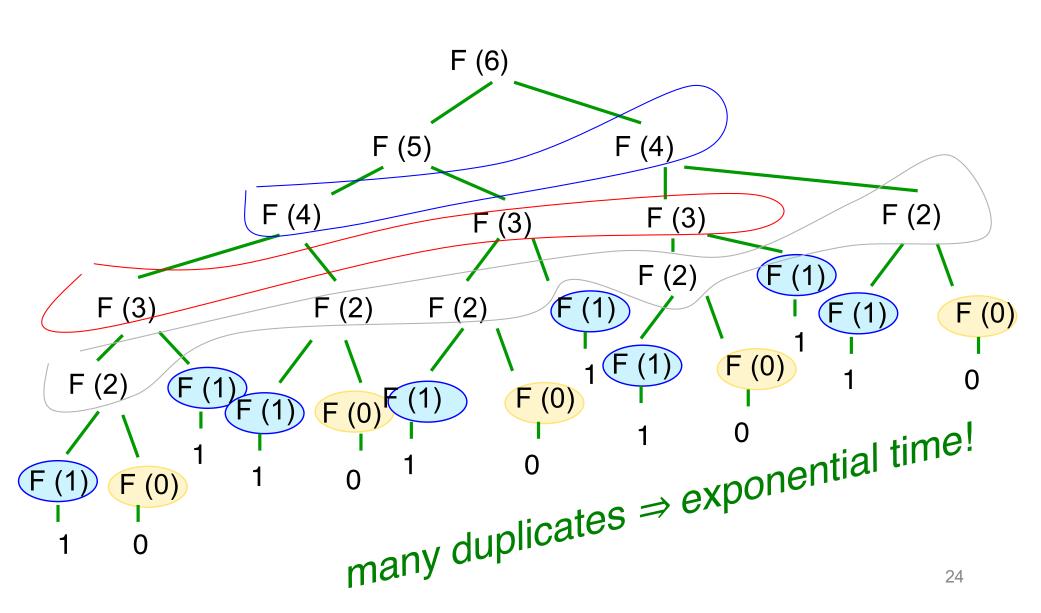
Fibonacci Numbers (recursion)

```
fibr(n) {
                                         Simple recursion,
 if (n <= 1) {
                                             but many
                                             repeated
   return n;
                                          subproblems!!
 } else {
   return fibr(n-1) + fibr(n-2);
                                         Time = \Omega(1.61^{\rm n})
```

Call tree - start



Full call tree



Fibonacci, II (dynamic programming)

```
int fibd[n];
fibd[0] = 0;
fibd[1] = 1;
for(i=2; i<=n; i++) {
 fibd[i] = fibd[i-1] + fibd[i-2];
return fibd[n];
```

Avoid repeated subproblems by tabulating their solutions

 \Rightarrow

Time = O(n)

(in this case)

When can we use Dynamic Programming?

1. Can we decompose into subproblems?

E.g., can we align smaller substrings (say, prefix/suffix in this case), then combine them somehow?

Do we have optimal substructure?

I.e., is optimal solution to a subproblem independent of context? E.g., is appending two optimal alignments also optimal? Perhaps, but some changes at the interface might be needed?

Optimal Substructure (In More Detail)

Optimal alignment *ends* in 1 of 3 ways: last chars of S & T aligned with each other last char of S aligned with dash in T last char of T aligned with dash in S (assume $\sigma(-, -) < 0$, so never align dash with dash)

In each case, the rest of S & T should be optimally aligned to each other

Optimal Alignment in O(n²) via "Dynamic Programming"

Input: S, T, |S| = n, |T| = m

Output: value of optimal alignment

Easier to solve a "harder" problem:

V(i,j) = value of optimal alignment of S[1], ..., S[i] with T[1], ..., T[j] for all $0 \le i \le n$, $0 \le j \le m$.

Base Cases

V(i,0): first i chars of S all match dashes

$$V(i,0) = \sum_{k=1}^{i} \sigma(S[k],-)$$

V(0,j): first j chars of T all match dashes

$$V(0,j) = \sum_{k=1}^{j} \sigma(-,T[k])$$

General Case

Opt align of S[1], ..., S[i] vs T[1], ..., T[j]:

$$\begin{bmatrix} \sim \sim \sim S[i] \\ \sim \sim \sim T[j] \end{bmatrix}, \quad \begin{bmatrix} \sim \sim \sim S[i] \\ \sim \sim \sim - \end{bmatrix}, \text{ or } \begin{bmatrix} \sim \sim \sim - \\ \sim \sim \sim T[j] \end{bmatrix}$$
Opt align of

$$S_1...S_{i-1}$$
 & $T_1...T_{j-1}$

Opt align of
$$S_1...S_{i-1} & \\ V(i,j) = \max \begin{cases} V(i-1,j-1) + \sigma(S[i],T[j]) \\ V(i-1,j) + \sigma(S[i],-) \\ V(i,j-1) + \sigma(-,T[j]) \end{cases}$$

for all $1 \le i \le n$, $1 \le j \le m$.

Calculating One Entry

$$V(i,j) = \max \begin{cases} V(i-1,j-1) + \sigma(S[i],T[j]) \\ V(i-1,j) + \sigma(S[i],-) \\ V(i,j-1) + \sigma(-,T[j]) \end{cases}$$

$$V(i-1,j-1) \qquad V(i-1,j)$$

$$V(i-1,j-1) \qquad V(i-1,j)$$

	j	0	1	2	3	4	5	
<u>i</u>			С	a	t	g	t	← T
0		0	-1	-2	-3	-4	-5	
1	a	-1						
2	С	-2		C	Sc			
3	g	-3						
4	С	-4						
5	t	-5						
6	g	-6						



	j	0	1	2	3	4	5	
<u>i</u>			С	a	t	g	t	← T
0		0	-1	-2	-3	-4	-5	
1	a	-1						
2	С	-2						
3	g	-3	- a	Sc	ore(-,a	n) = -1		
4	С	-4						
5	t	-5						
6	g	-6						



	j	0	1	2	3	4	5	
i			С	a	t	g	t	←T
0		0	-1	-2	-3	-4	-5	
1	a	-1						
2	С	-2	,					
3	9	3						
4	С	-4	_	- Sc	ore(-,c	(c) = -1		
5	t	-5	-1					
6	g	-6						



	j	0	1	2	3	4	5	
<u>i</u>			С	a	t	g	t	←T
0		0	-1	-2	-3	-4	-5	
1	a	-1	-1	1				
2	С	-2						
3	g	-3			_1			-2
4	С	-4				σ(a,	a)=+2	σ(-,a)=-1
5	t	-5				5 (2)	-)=-1	1 -3 ca-
6	g	-6			_1			-2 1 ca
	↑ S	<u>'</u>						ca ca ca a - a 35

Example

	j	0	1	2	3	4	5
i			С	a	t	g	t
0		0	-1	-2	-3	-4	-5
1	a	-1	-1	1			
2	С	-2	1				
3	g	-3					
4	С	-4					
5	t	-5					
6	g	-6					

 $\leftarrow T$

Time = O(mn)



Mismatch = -1Match = 2

Example

	j	0	1	2	3	4	5	
<u>i</u>			С	a	t	g	t	←
0		0	-1	-2	-3	-4	-5	
1	а	-1	-1	1	0	-1	-2	
2	С	-2	1	0	0	-1	-2	
3	9	-3	0	0	-1	2	1	
4	С	-4	-1	-1	-1	1	1	
5	t	-5	-2	-2	1	0	3	
6	g	-6	-3	-3	0	3	2	



alignments? C.f. slide 12 the

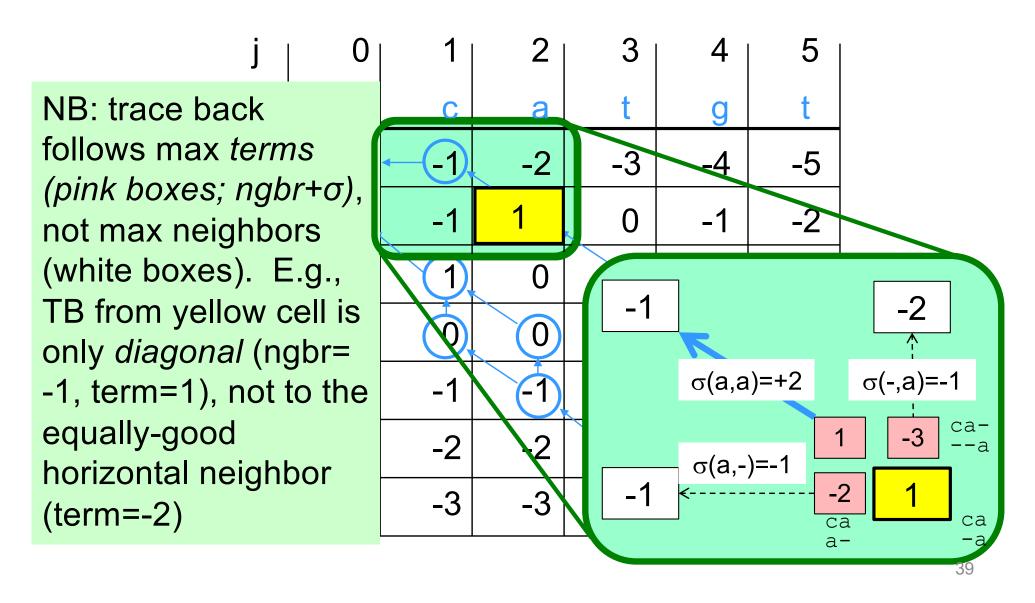
Finding Alignments: Trace Back

Arrows = (ties for) max in V(i,j); 3 LR-to-UL paths = 3 optimal alignments

	j	0	1	2	3	4	5	
<u>i</u>			С	a	t	g	t	←T
0		0	—————	-2	-3	-4	-5	
1	a	(1)	-1	1	0	-1	-2	
2	С	-2	(1)	0	0	-1	-2	
3	g	-3	0	0	-1	2	1	
4	С	-4	-1	-1	-1	1,	1	
5	t	-5	-2	-2	1,	0	3	
6	g	-6	-3	-3	0	3	_2	

Finding Alignments: Trace Back

Arrows = (ties for) max in V(i,j); 3 LR-to-UL paths = 3 optimal alignments



Complexity Notes

Time = O(mn), (value and alignment)

Space = O(mn)

Easy to get value in Time = O(mn) and Space = O(min(m,n))

Possible to get value and alignment in Time = O(mn) and Space = O(min(m,n)), but tricky (DEKM 2.6)

CSEP 527 Computational Biology Autumn 2020

Lecture 4
Sequence Alignment, Part II

Local Alignment & Gaps

Variations

Local Alignment

- Preceding gives *global* alignment, i.e. full length of both strings;
- Might well miss strong similarity of part of strings amidst dissimilar flanks

Gap Penalties

10 adjacent dashes cost 10 x one dash?

Many others

Similarly fast DP algs often possible

Local Alignment: Motivations

"Interesting" (evolutionarily conserved, functionally related) segments may be a small part of the whole

"Active site" of a protein

Scattered genes or exons amidst "junk", e.g. retroviral insertions, large deletions

Don't have whole sequence

Global alignment might miss them if flanking junk outweighs similar regions

Local Alignment

Optimal *local alignment* of strings S & T: Find substrings A of S and B of T having max value global alignment

$$S = abcxdex A = c x d e$$

$$T = xxxcde$$
 $B = c - d e value = 5 (toy σ)$

Local Alignment: "Obvious" Algorithm

for all substrings A of S and B of T: Align A & B via dynamic programming Retain pair with max value

end;

Output the retained pair

Time: O(n²) choices for A, O(m²) for B, O(nm) for DP, so O(n³m³) total.

[Best possible? Lots of redundant work...]

Local Alignment in O(nm) via Dynamic Programming

```
Input: S, T, |S| = n, |T| = m
Output: value of optimal local alignment
Better to solve a "harder" problem
for all 0 \le i \le n, 0 \le j \le m:
 V(i,j) = \max_{i} value of opt (global)
     alignment of a suffix of S[1], ..., S[i]
     with a suffix of T[1], ..., T[j]
 Report best i,j
```

Base Cases

Assume $\sigma(x,-) < 0$, $\sigma(-,x) < 0$ V(i,0): some suffix of first i chars of S; all match dashes in T; best suffix is empty V(i,0) = 0 V(0,j): similar V(0,j) = 0

General Case Recurrences

Opt suffix align S[1], ..., S[i] vs T[1], ..., T[j]:

$$\begin{bmatrix} \sim \sim \sim S[i] \\ \sim \sim \sim T[j] \end{bmatrix}, \begin{bmatrix} \sim \sim \sim S[i] \\ \sim \sim \sim T[j] \end{bmatrix}, \text{ or } \begin{bmatrix} \\ \\ \\ \\ \end{pmatrix}$$

Opt align of suffix of

$$V(i,j) = \max$$

$$V(i,j) = \max \begin{cases} V(i-1,j-1) + \sigma(S[i],T[j]) \\ V(i-1,j) + \sigma(S[i],-) \\ V(i,j-1) + \sigma(-,T[j]) \\ 0 \end{cases}, \text{ opt suffix alignment has:}$$

for all $1 \le i \le n$, $1 \le j \le m$.

alignment

Scoring Local Alignments

	j	0	1	2	3	4	5	6	
i			X	X	X	С	d	е	← T
0		0	0	0	0	0	0	0	
1	a	0							
2	b	0							
3	С	0							
4	X	0							
5	d	0							
6	е	0							
7	X	0							

Finding Local Alignments

Again, arrows follow max term (not max neighbor)

	J	0	1	2	3	4	5	6
i			X	X	X	С	d	е
0		0	0	0	0	0	0	0
1	a	0	0	0	0	0	0	0
2	b	0	0	0	0	0	0	0
3	С	0	0	0	0	2	1	0
4	X	0	2	2	2	<u> </u>	1	0
5	d	0	1	1	1	1	3	2
6	е	0	0	0	0	0	2	5
7	X	0	2	2	2	1	1	4

One

align-

ment

c-de

cxde

What's

other?

the

is:

Notes

Time and Space = O(mn)

Space O(min(m,n)) possible with time
O(mn), but finding alignment is trickier

Local alignment: "Smith-Waterman"

Global alignment: "Needleman-Wunsch"

Sequence Evolution

"Nothing in Biology Makes Sense Except in the Light of Evolution" – Theodosius Dobzhansky, 1973

Changes happen at random

Deleterious/neutral/advantageous changes unlikely/possibly/likely spread widely in a population

Changes are less likely to be tolerated in positions involved in many/close interactions, e.g.

enzyme binding pocket protein/protein interaction surface

. . .

Alignment With Gap Penalties

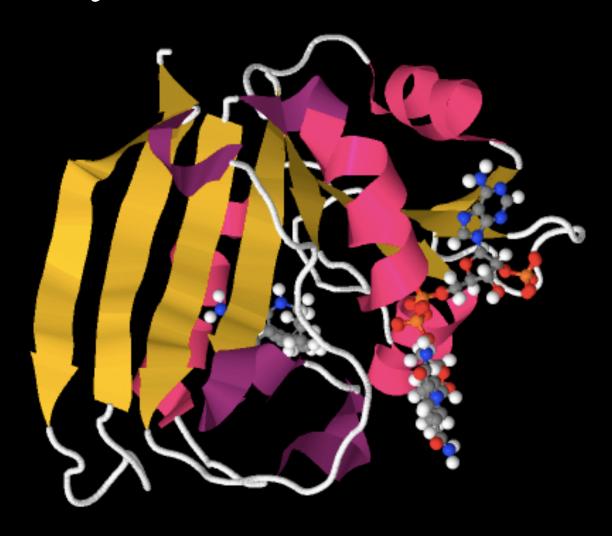
A Gap: maximal run of dashes in S' or T'

```
ag--ttc-t 2 gaps in S' a---ttcgt 1 gap in T'
```

Motivations, e.g.:

mutation might insert/delete several or even many residues at once some parts of proteins less critical matching mRNA (no introns) to genomic DNA (exons and introns)

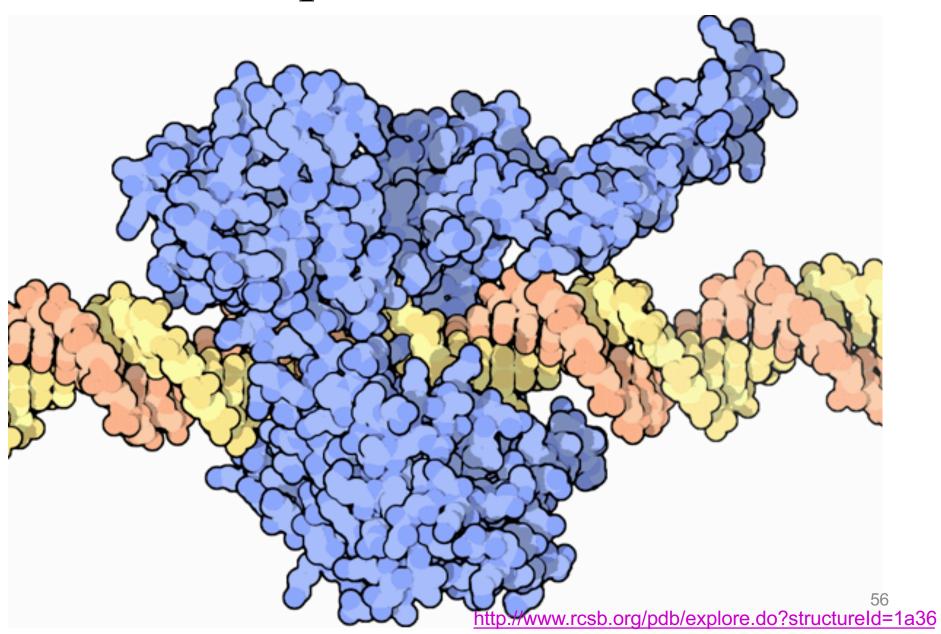
A Protein Structure: (Dihydrofolate Reductase)



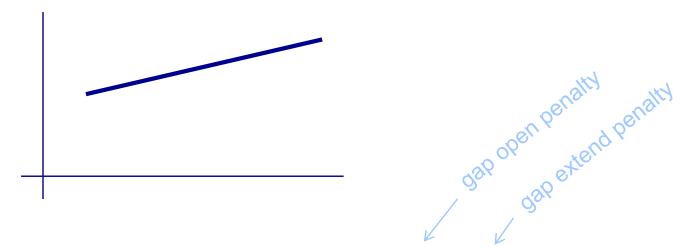
Alignment of 5 Dihydrofolate reductase proteins

```
P00375
             ----MVRPLNCIVAVSONMGIGKNGDLPWPPLRNEFKYFORMTTTSSVEGKONLVIMGRK
mouse
     P00374
             ----MVGSLNCIVAVSQNMGIGKNGDLPWPPLRNEFRYFQRMTTTSSVEGKQNLVIMGKK
human
     P00378
             ----VRSLNSIVAVCONMGIGKDGNLPWPPLRNEYKYFORMTSTSHVEGKONAVIMGKK
chicken
     P17719
             ----MLR-FNLIVAVCENFGIGIRGDLPWR-IKSELKYFSRTTKRTSDPTKQNAVVMGRK
     P07807
 veast
             MAGGKIPIVGIVACLOPEMGIGFRGGLPWR-LPSEMKYFROVTSLTKDPNKKNALIMGRK
                                    * * * * . * . * . * . .
     P00375
             TWFSIPEKNRPLKDRINIVLSRELKEP----PRGAHFLAKSLDDALRLIEQPELASKVDM
     P00374
             TWFSIPEKNRPLKGRINLVLSRELKEP----PQGAHFLSRSLDDALKLTEQPELANKVDM
     P00378
             TWFSIPEKNRPLKDRINIVLSRELKEA----PKGAHYLSKSLDDALALLDSPELKSKVDM
     P17719
             TYFGVPESKRPLPDRLNIVLSTTLQESDL--PKG-VLLCPNLETAMKILEE---QNEVEN
     P07807
             TWESIPPKFRPLPNRMNVIISRSFKDDFVHDKERSIVOSNSLANAIMNLESN-FKEHLER
             P00375
             VWIVGGSSVYQEAMNQPGHLRLFVTRIMQEFESDTFFPEIDLGKYKLLPEYPG-----
     P00374
             VWIVGGSSVYKEAMNHPGHLKLFVTRIMQDFESDTFFPEIDLEKYKLLPEYPG-----
     P00378
             VWIVGGTAVYKAAMEKPINHRLFVTRILHEFESDTFFPEIDYKDFKLLTEYPG-----
     P17719
             IWIVGGSGVYEEAMASPRCHRLYITKIMOKFDCDTFFPAIP-DSFREVAPDSD------
     P07807
             IYVIGGGEVYSQIFSITDHWLITKINPLDKNATPAMDTFLDAKKLEEVFSEQDPAQLKEF
             • • • • * *
                     CLUSTAL W (1.82) multiple
     P00375
             VLSEVQ-----EEKGIKYKFEVYEKKD---
             VLSDVQ-----EEKGIKYKFEVYEKND---
                                                      sequence alignment
     P00374
                                                      http://pir.georgetown.edu/cgi-
             VPADIQ-----EEDGIQYKFEVYQKSVLAQ
     P00378
                                                                 2/11/2013
                                                      bin/multialn.pl
             MPLGVQ-----EENGIKFEYKILEKHS---
     P17719
     P07807
             LPPKVELPETDCDORYSLEEKGYCFEFTLYNRK----
                                                                        55
                               ** *
```

Topoisomerase I



Affine Gap Penalties



Gap penalty = $g + e^*(gaplen-1)$, $g \ge e \ge 0$

Note: no longer suffices to know just the score of best subproblem(s) – state matters: do they end with '-' or not.

Global Alignment with Affine Gap Penalties

```
V(i,j) = value of opt alignment of S[1], ..., S[i] with T[1], ..., T[j]
G(i,j) = ..., s.t. last pair matches S[i] & T[j]
F(i,j) = ..., s.t. last pair matches S[i] & -
E(i,j) = ..., s.t. last pair matches - & T[j]
```

S	Т
x/ _	x/ _
Х	X
x	_
_	X

Time: O(mn) [calculate all, O(1) each]

Affine Gap Algorithm

Gap penalty = $g + e^*(gaplen-1)$, $g \ge e^* \ge 0$

$$V(i,0) = E(i,0) = V(0,i) = F(0,i) = -g-(i-1)*e$$

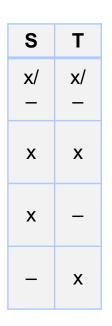
$$V(i,j) = max(G(i,j), F(i,j), E(i,j))$$

$$G(i,j) = V(i-1,j-1) + \sigma(S[i],T[j])$$

$$F(i,j) = max(F(i-1,j)-e, V(i-1,j)-g)$$

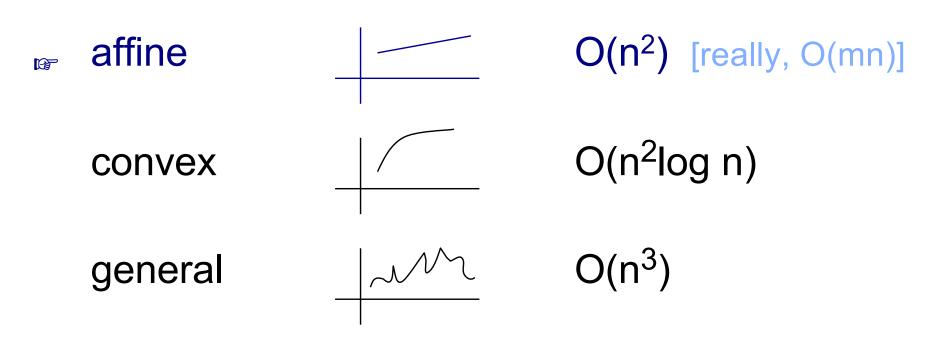
$$E(i,j) = max(E(i,j-1)-e, V(i,j-1)-g)$$

old gap new gap



Other Gap Penalties

Score = f(gap length)
Kinds, & best known alignment time



Summary: Alignment

- Functionally similar proteins/DNA often have recognizably similar sequences even after eons of divergent evolution
- Ability to find/compare/experiment with "same" sequence in other organisms is a huge win
- Surprisingly simple scoring works well in practice: score positions separately & add, usually w/ fancier affine gaps
- Simple dynamic programming algorithms can find *optimal* alignments under these assumptions in poly time (product of sequence lengths)
- This, and heuristic approximations to it like BLAST, are workhorse tools in molecular biology, and elsewhere.

Summary: Dynamic Programming

Keys to D.P. are to

- a) Identify the subproblems (usually repeated/overlapping)
- b) Solve them in a careful order so all small ones solved before they are needed by the bigger ones, and
- c) Build table with solutions to the smaller ones so bigger ones just need to do table lookups (no recursion, despite recursive formulation implicit in (a))
- d) Implicitly, optimal solution to whole problem devolves to optimal solutions to subproblems

A really important algorithm design paradigm

Significance of Alignment Scores

Is "42" a good score?

Compared to what?

Usual approach: compared to a specific "null model", such as "random sequences"

More on this later; a taste now, for use in next HW

Overall Alignment Significance, I Empirical p-values (via randomization)

You just searched with x, found "good" score for x:y Generate N random "y-like" sequences (say N = 10³ - 10⁶) Align x to each & score

If k of them have score than better or equal to that of x to y, then the (empirical) probability of a chance alignment as good as your observed x:y alignment is (k+1)/(N+1)

e.g., if 0 of 99 are better, you can say "estimated p ≤ .01"

How to gen "random y-like" seqs? Scores depend on:

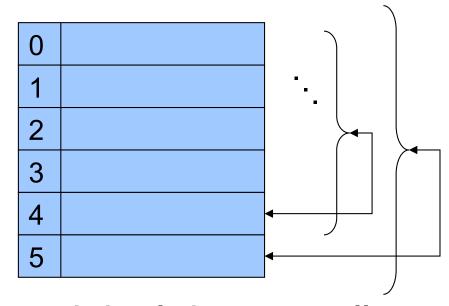
Length, so use same length as y

Sequence composition, so uniform 1/20 or 1/4 is a bad idea; even background p_i can be dangerous (if *y* unusual)

Better idea: permute y N times: exactly preserves len & composition

Generating Random Permutations

```
for (i = n-1; i > 0; i--){
    j = random(0..i);
    swap X[i] <-> X[j];
}
```



All n! permutations of the original data equally likely: A specific element will be last with prob 1/n; given that, another specific element will be next-to-last with prob 1/(n-1), ...; overall: 1/(n!)

C.f. http://en.wikipedia.org/wiki/Fisher-Yates_shuffle and (for subtle way to go wrong) http://www.codinghorror.com/blog/2007/12/the-danger-of-naivete.html