

# CSEP 517

# Natural Language Processing

## Parsing (Trees)

Luke Zettlemoyer - University of Washington

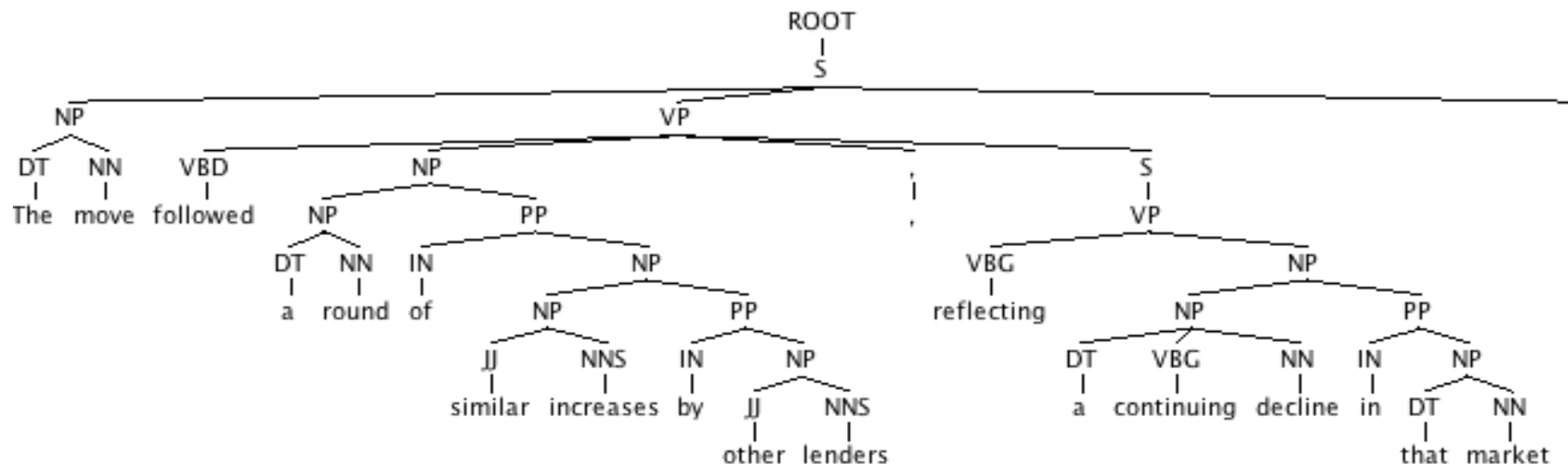
[Slides from Yejin Choi, Dan Klein, Michael Collins, and Ray Mooney]

# Topics

---

- Parse Trees
- (Probabilistic) Context Free Grammars
  - Supervised learning
  - Parsing: most likely tree, marginal distributions
- Treebank Parsing (English, edited text)

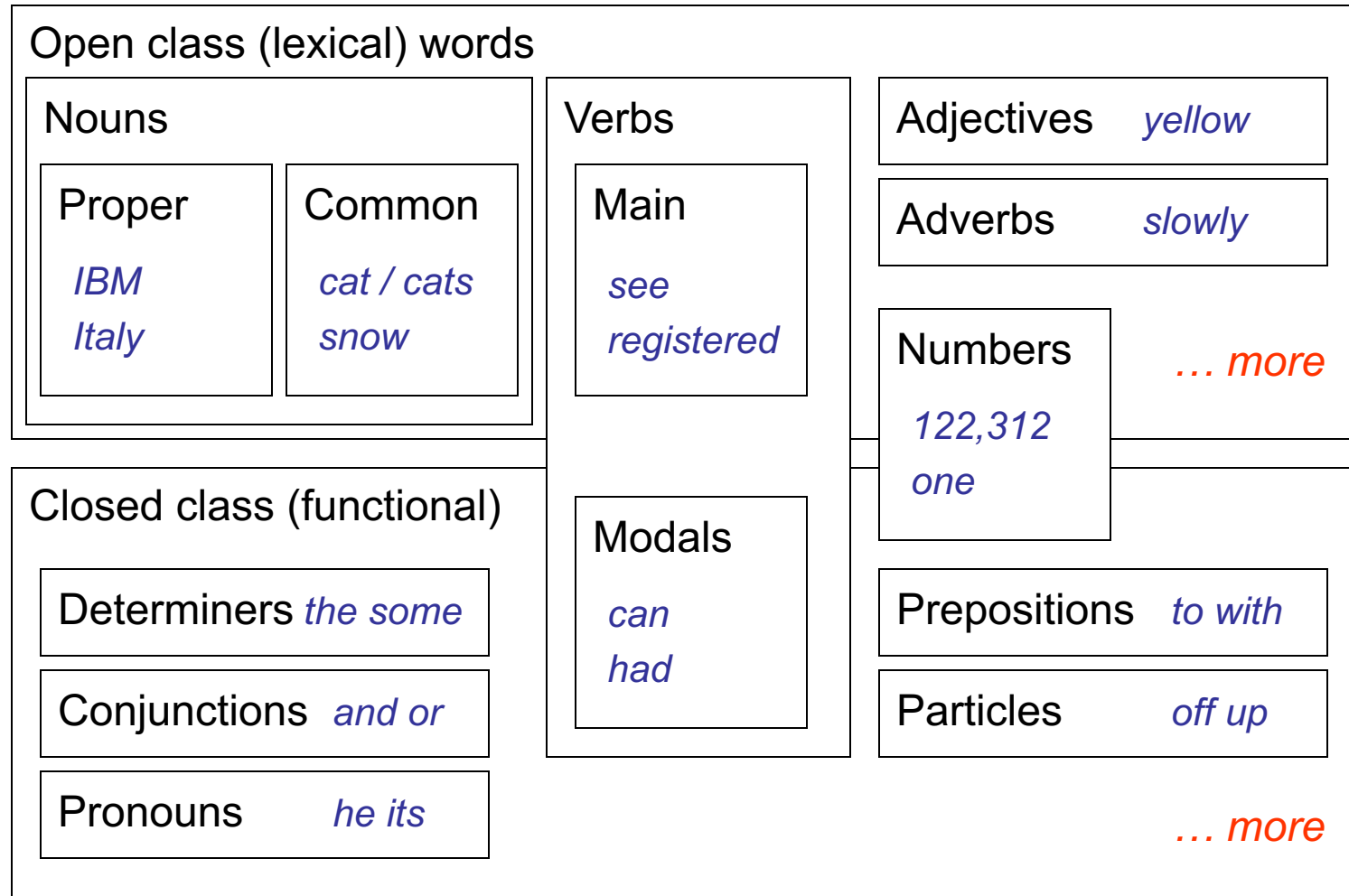
# Parse Trees



The move followed a round of similar increases  
by other lenders, reflecting a continuing decline  
in that market

# Parts-of-Speech (English)

- One basic kind of linguistic structure: syntactic word classes



# Penn Treebank Non-terminals

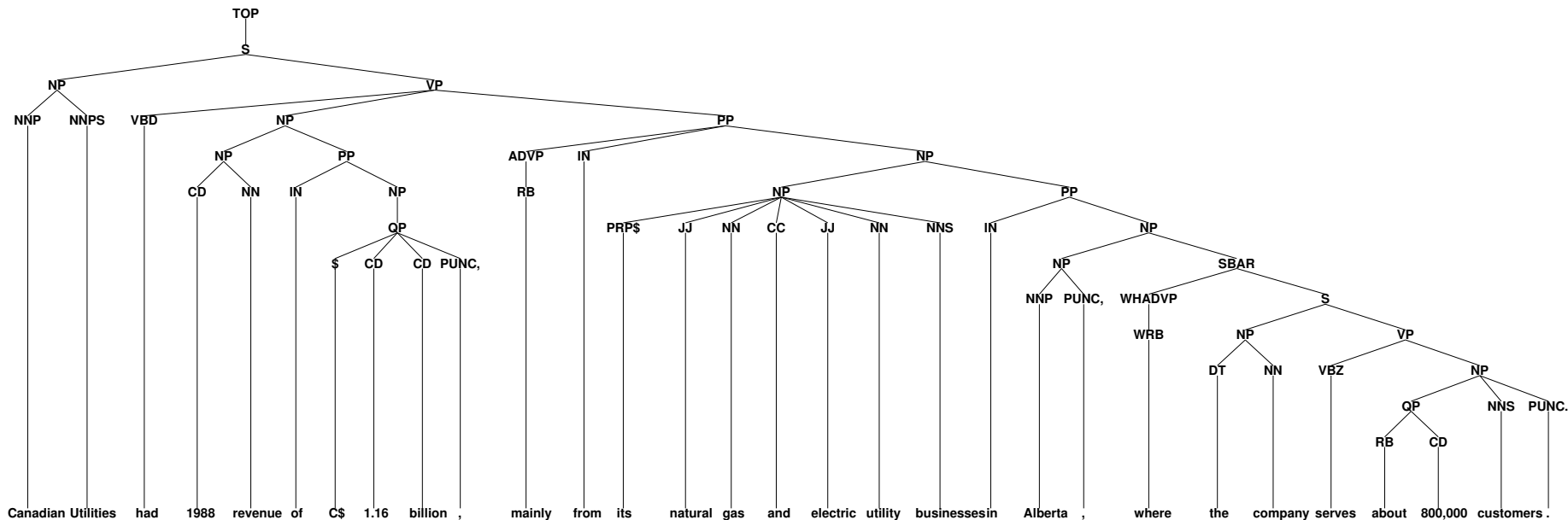
Table 1.2. The Penn Treebank syntactic tagset

ADJP	Adjective phrase
ADVP	Adverb phrase
NP	Noun phrase
PP	Prepositional phrase
S	Simple declarative clause
SBAR	Subordinate clause
SBARQ	Direct question introduced by <i>wh</i> -element
SINV	Declarative sentence with subject-aux inversion
SQ	Yes/no questions and subconstituent of SBARQ excluding <i>wh</i> -element
VP	Verb phrase
WHADVP	Wh-adverb phrase
WHNP	Wh-noun phrase
WHPP	Wh-prepositional phrase
X	Constituent of unknown or uncertain category
*	“Understood” subject of infinitive or imperative
0	Zero variant of <i>that</i> in subordinate clauses
T	Trace of <i>wh</i> -Constituent

# The Penn Treebank: Size

- ▶ Penn WSJ Treebank = 50,000 sentences with associated trees
- ▶ Usual set-up: 40,000 training sentences, 2400 test sentences

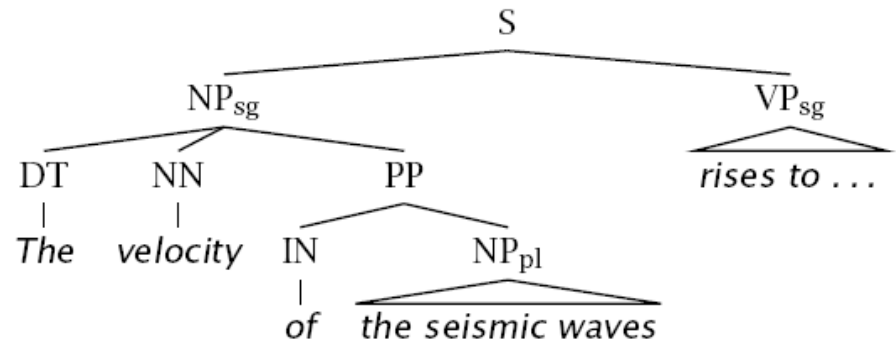
## An example tree:



# Phrase Structure Parsing

---

- Phrase structure parsing organizes syntax into constituents or brackets
- In general, this involves nested trees
- Linguists can, and do, argue about details
- Lots of ambiguity
- Not the only kind of syntax...



new art critics write reviews with computers

# Constituency Tests

- How do we know what nodes go in the tree?

- Classic constituency tests:

- Substitution by proform

- he, she, it, they, ...

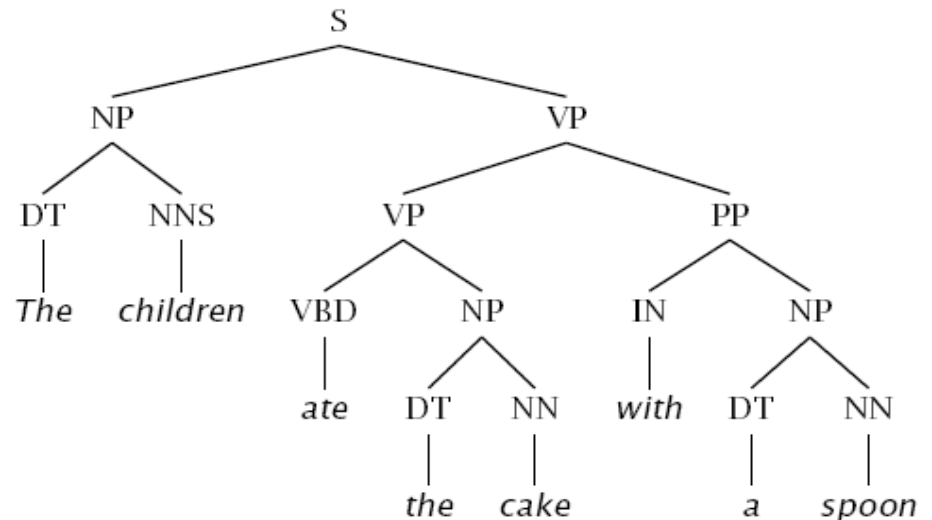
- Question / answer

- Deletion

- Movement / dislocation

- Conjunction / coordination

- Cross-linguistic arguments, too





# Conflicting Tests

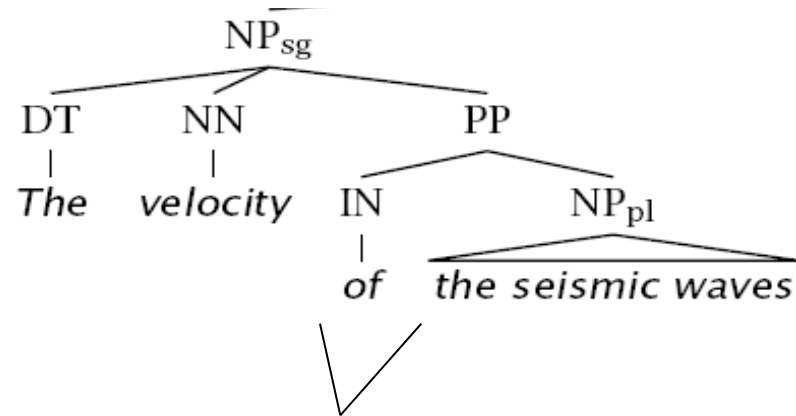
- Constituency isn't always clear

- Units of transfer:

- think about ~ penser à
    - talk about ~ hablar de

- Phonological reduction:

- I will go → I'll go
  - I want to go → I wanna go
  - a le centre → au centre



La    vitesse    des ondes sismiques

- Coordination

- He went to and came from the store.

# Classical NLP: Parsing in 70s/80s

---

- Write symbolic or logical rules:

## Grammar (CFG)

ROOT  $\rightarrow$  S

S  $\rightarrow$  NP VP

NP  $\rightarrow$  DT NN

NP  $\rightarrow$  NN NNS

NP  $\rightarrow$  NP PP

VP  $\rightarrow$  VBP NP

VP  $\rightarrow$  VBP NP PP

PP  $\rightarrow$  IN NP

## Lexicon

NN  $\rightarrow$  interest

NNS  $\rightarrow$  raises

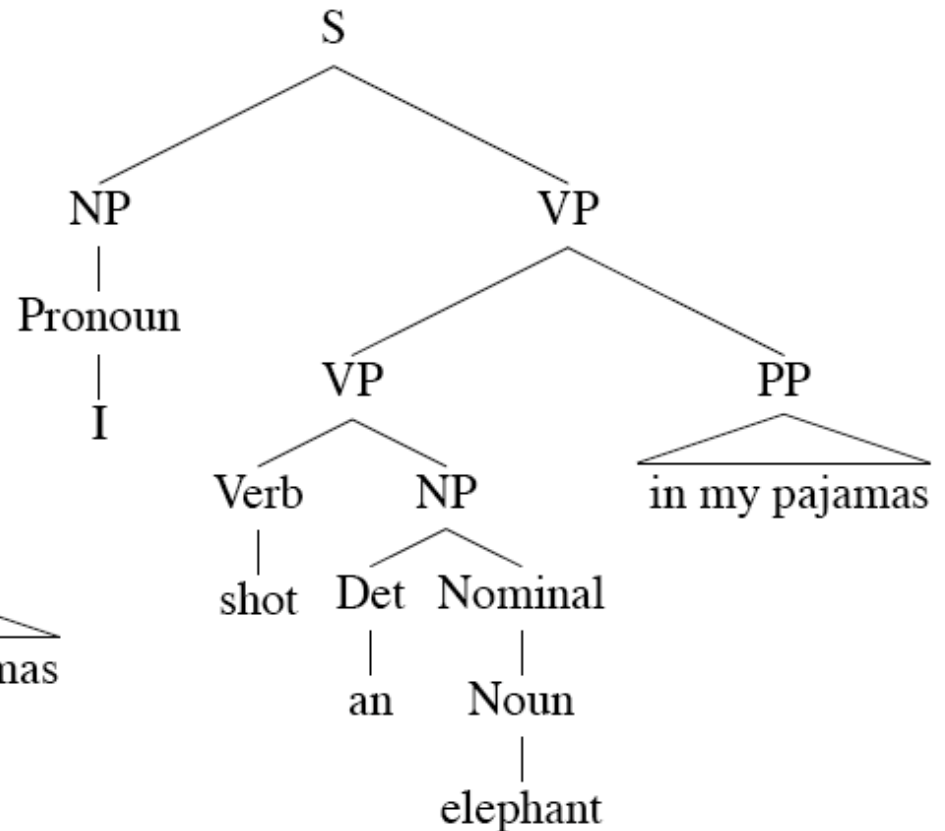
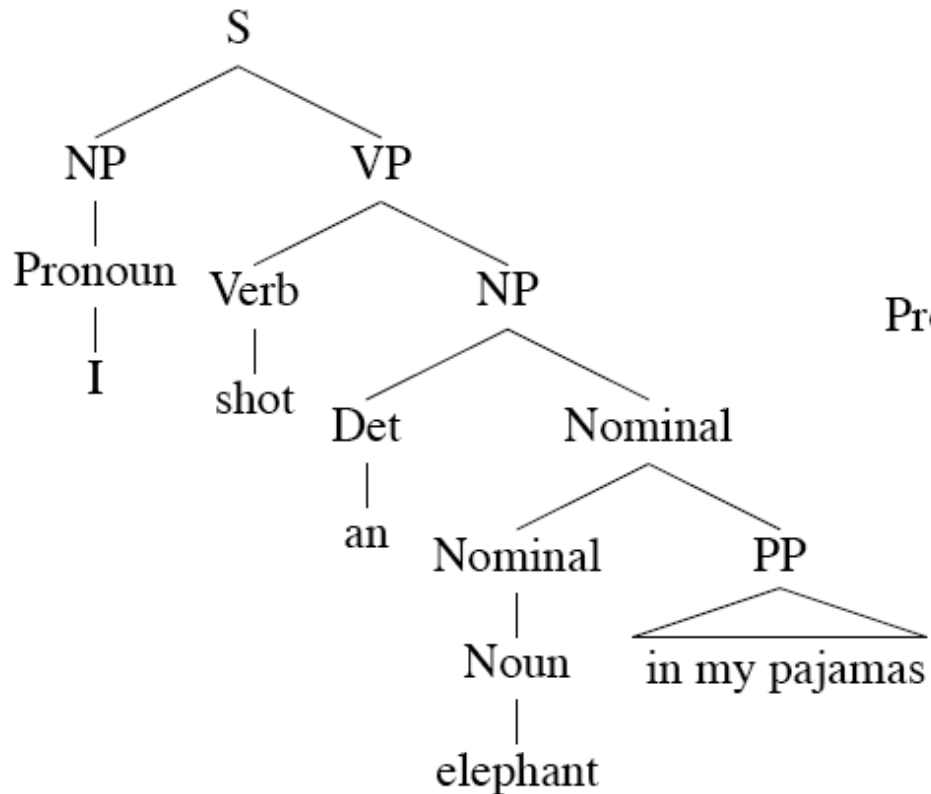
VBP  $\rightarrow$  interest

VBZ  $\rightarrow$  raises

...

- Use deduction systems to prove parses from words
  - Simple 10-rule grammar: 592 parses
  - Real-size grammar: many millions of parses
- This scaled very badly, but was a popular approach in the 70's and 80's before corpora were available.
- Didn't yield broad-coverage tools.

I shot [an elephant] [in my pajamas]



Examples from J&M

# Attachment Ambiguity

---

- I cleaned the dishes from dinner
- I cleaned the dishes with detergent
- I cleaned the dishes in my pajamas
- I cleaned the dishes in the sink

The board approved [its acquisition] [by Royal Trustco Ltd.]  
[of Toronto]  
[for \$27 a share]  
[at its monthly meeting].

```
graph LR; A1[ ] --> B[its acquisition]; A2[ ] --> B; A3[ ] --> B; A4[ ] --> B; A1 --- C1[by Royal Trustco Ltd.]; A2 --- C2[of Toronto]; A3 --- C3[for $27 a share]; A4 --- C4[at its monthly meeting.];
```

# Syntactic Ambiguities I

---

- **Prepositional phrases:**  
They cooked the beans in the pot on the stove with handles.
- **Particle vs. preposition:**  
The puppy tore up the staircase.
- **Complement structures**  
The tourists objected to the guide that they couldn't hear.  
She knows you like the back of her hand.
- **Gerund vs. participial adjective**  
Visiting relatives can be boring.  
Changing schedules frequently confused passengers.

# Syntactic Ambiguities II

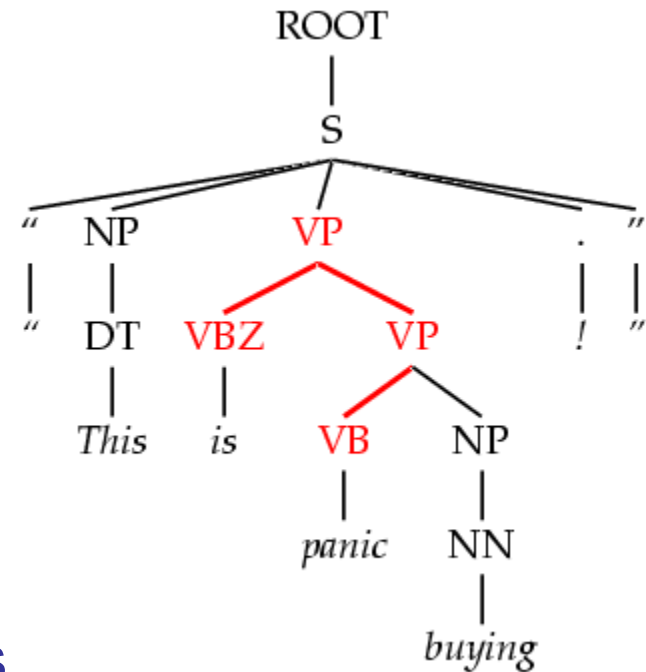
---

- **Modifier scope within NPs**  
impractical design requirements  
plastic cup holder
- **Multiple gap constructions**  
The chicken is ready to eat.  
The contractors are rich enough to sue.
- **Coordination scope:**  
Small rats and mice can squeeze into holes or cracks in the wall.

# Dark Ambiguities

- **Dark ambiguities:** most analyses are shockingly bad (meaning, they don't have an interpretation you can get your mind around)

This analysis corresponds  
to the correct parse of  
“This will panic buyers ! ”



- **Unknown words and new usages**
- **Solution:** We need mechanisms to focus attention on the best ones, probabilistic techniques do this

# Context-Free Grammars

---

- A context-free grammar is a tuple  $\langle N, \Sigma, S, R \rangle$ 
  - $N$  : the set of non-terminals
    - Phrasal categories: S, NP, VP, ADJP, etc.
    - Parts-of-speech (pre-terminals): NN, JJ, DT, VB
  - $\Sigma$  : the set of terminals (the words)
  - $S$  : the start symbol
    - Often written as ROOT or TOP
    - Not usually the sentence non-terminal S
  - $R$  : the set of rules
    - Of the form  $X \rightarrow Y_1 Y_2 \dots Y_n$ , with  $X \in N$ ,  $n \geq 0$ ,  $Y_i \in (N \cup \Sigma)$
    - Examples:  $S \rightarrow NP VP$ ,  $VP \rightarrow VP CC VP$
    - Also called rewrites, productions, or local trees



# Example Grammar

$N = \{S, NP, VP, PP, DT, Vi, Vt, NN, IN\}$

$S = S$

$\Sigma = \{\text{sleeps, saw, man, woman, telescope, the, with, in}\}$

$R =$

S	$\Rightarrow$	NP	VP
VP	$\Rightarrow$	Vi	
VP	$\Rightarrow$	Vt	NP
VP	$\Rightarrow$	VP	PP
NP	$\Rightarrow$	DT	NN
NP	$\Rightarrow$	NP	PP
PP	$\Rightarrow$	IN	NP

Vi	$\Rightarrow$	sleeps
Vt	$\Rightarrow$	saw
NN	$\Rightarrow$	man
NN	$\Rightarrow$	woman
NN	$\Rightarrow$	telescope
DT	$\Rightarrow$	the
IN	$\Rightarrow$	with
IN	$\Rightarrow$	in

S=sentence, VP=verb phrase, NP=noun phrase, PP=prepositional phrase,  
DT=determiner, Vi=intransitive verb, Vt=transitive verb, NN=noun, IN=preposition

$R =$

S	$\Rightarrow$	NP	VP
VP	$\Rightarrow$	Vi	
VP	$\Rightarrow$	Vt	NP
VP	$\Rightarrow$	VP	PP
NP	$\Rightarrow$	DT	NN
NP	$\Rightarrow$	NP	PP
PP	$\Rightarrow$	IN	NP

Vi	$\Rightarrow$	sleeps
Vt	$\Rightarrow$	saw

NN	$\Rightarrow$	man
NN	$\Rightarrow$	woman
NN	$\Rightarrow$	telescope

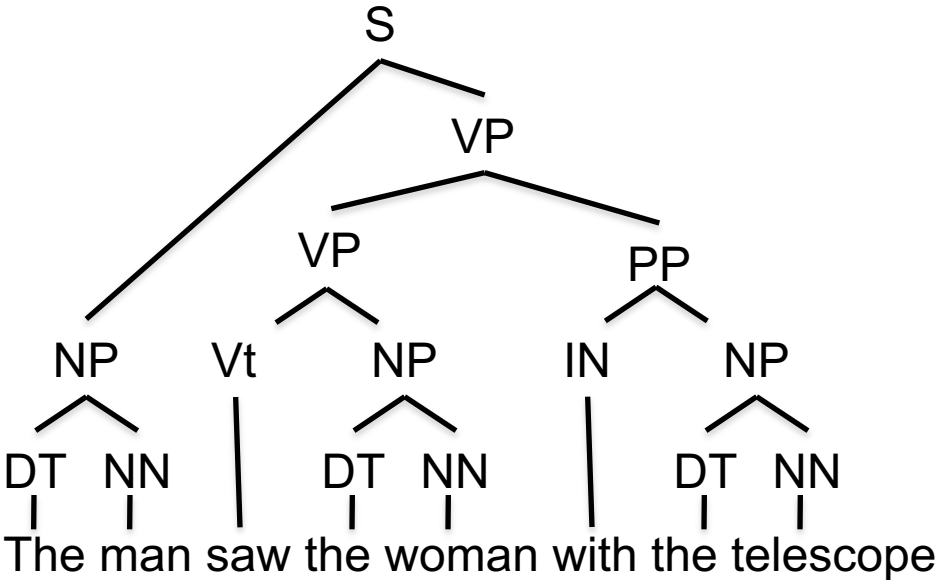
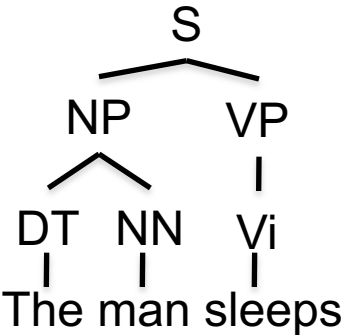
  

DT	$\Rightarrow$	the
----	---------------	-----

IN	$\Rightarrow$	with
IN	$\Rightarrow$	in

# Example Parses



S=sentence, VP=verb phrase, NP=noun phrase, PP=prepositional phrase,  
 DT=determiner, Vi=intransitive verb, Vt=transitive verb, NN=noun, IN=preposition

# Probabilistic Context-Free Grammars

---

- A context-free grammar is a tuple  $\langle N, \Sigma, S, R \rangle$ 
  - $N$  : the set of non-terminals
    - Phrasal categories: S, NP, VP, ADJP, etc.
    - Parts-of-speech (pre-terminals): NN, JJ, DT, VB, etc.
  - $\Sigma$  : the set of terminals (the words)
  - $S$  : the start symbol
    - Often written as ROOT or TOP
    - Not usually the sentence non-terminal S
  - $R$  : the set of rules
    - Of the form  $X \rightarrow Y_1 Y_2 \dots Y_n$ , with  $X \in N$ ,  $n \geq 0$ ,  $Y_i \in (N \cup \Sigma)$ 
      - Examples:  $S \rightarrow NP VP$ ,  $VP \rightarrow VP CC VP$
- A PCFG adds a distribution  $q$ :
  - Probability  $q(r)$  for each  $r \in R$ , such that for all  $X \in N$ :

$$\sum_{\alpha \rightarrow \beta \in R: \alpha = X} q(\alpha \rightarrow \beta) = 1$$

# PCFG Example

S	$\Rightarrow$	NP	VP	1.0
VP	$\Rightarrow$	Vi		0.4
VP	$\Rightarrow$	Vt	NP	0.4
VP	$\Rightarrow$	VP	PP	0.2
NP	$\Rightarrow$	DT	NN	0.3
NP	$\Rightarrow$	NP	PP	0.7
PP	$\Rightarrow$	P	NP	1.0

Vi	$\Rightarrow$	sleeps	1.0
Vt	$\Rightarrow$	saw	1.0
NN	$\Rightarrow$	man	0.7
NN	$\Rightarrow$	woman	0.2
NN	$\Rightarrow$	telescope	0.1
DT	$\Rightarrow$	the	1.0
IN	$\Rightarrow$	with	0.5
IN	$\Rightarrow$	in	0.5

- Probability of a tree  $t$  with rules

$$\alpha_1 \rightarrow \beta_1, \alpha_2 \rightarrow \beta_2, \dots, \alpha_n \rightarrow \beta_n$$

is

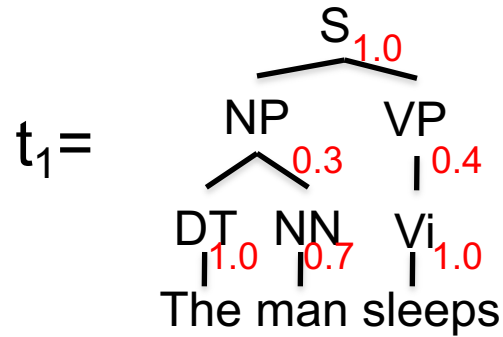
$$p(t) = \prod_{i=1}^n q(\alpha_i \rightarrow \beta_i)$$

where  $q(\alpha \rightarrow \beta)$  is the probability for rule  $\alpha \rightarrow \beta$ .

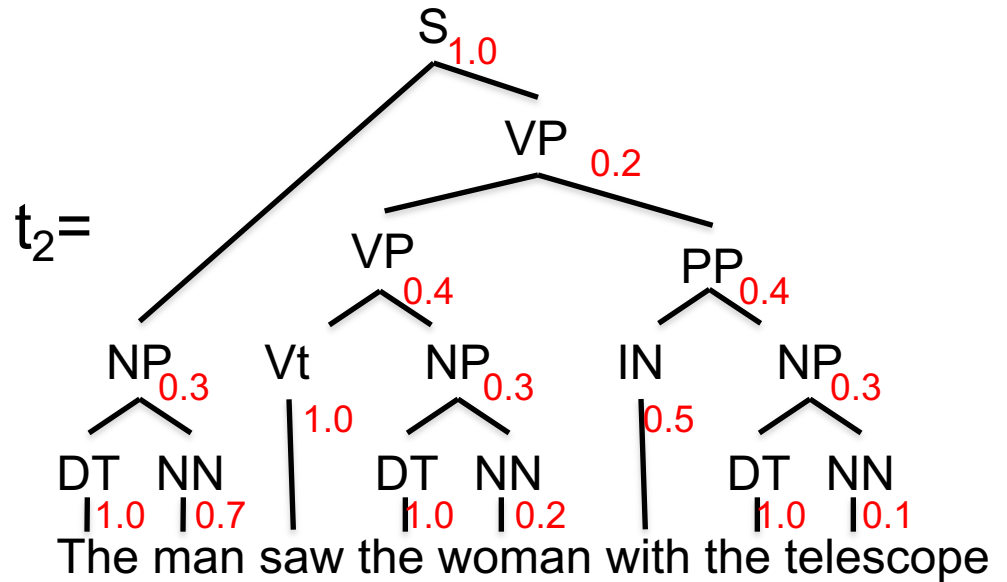
# PCFG Example

S	$\Rightarrow$	NP VP	1.0
VP	$\Rightarrow$	Vi	0.4
VP	$\Rightarrow$	Vt NP	0.4
VP	$\Rightarrow$	VP PP	0.2
NP	$\Rightarrow$	DT NN	0.3
NP	$\Rightarrow$	NP PP	0.7
PP	$\Rightarrow$	P NP	1.0

Vi	$\Rightarrow$	sleeps	1.0
Vt	$\Rightarrow$	saw	1.0
NN	$\Rightarrow$	man	0.7
NN	$\Rightarrow$	woman	0.2
NN	$\Rightarrow$	telescope	0.1
DT	$\Rightarrow$	the	1.0
IN	$\Rightarrow$	with	0.5
IN	$\Rightarrow$	in	0.5



$$p(t_1) = 1.0 * 0.3 * 1.0 * 0.7 * 0.4 * 1.0$$



$$p(t_s) = 1.8 * 0.3 * 1.0 * 0.7 * 0.2 * 0.4 * 1.0 * 0.3 * 1.0 * 0.2 * 0.4 * 0.5 * 0.3 * 1.0 * 0.1$$

# PCFGs: Learning and Inference

---

## ■ Model

- The probability of a tree  $t$  with  $n$  rules  $\alpha_i \rightarrow \beta_i$ ,  $i = 1..n$

$$p(t) = \prod_{i=1}^n q(\alpha_i \rightarrow \beta_i)$$

## ■ Learning

- Read the rules off of labeled sentences, use ML estimates for probabilities

$$q_{ML}(\alpha \rightarrow \beta) = \frac{\text{Count}(\alpha \rightarrow \beta)}{\text{Count}(\alpha)}$$

- and use all of our standard smoothing tricks!

## ■ Inference

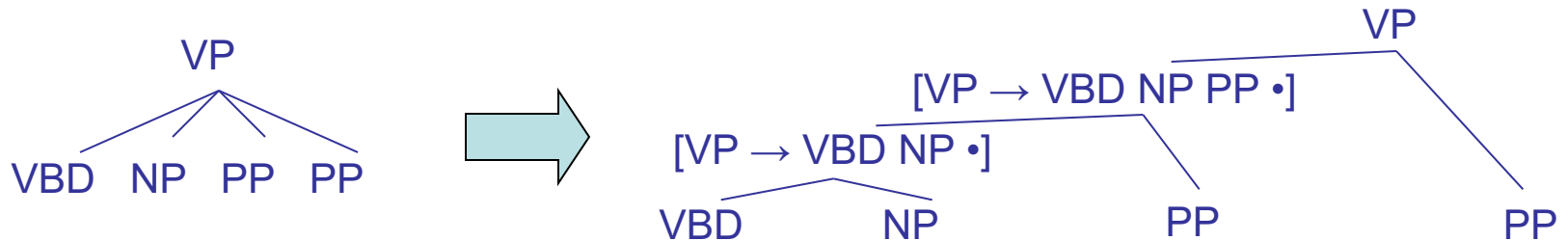
- For input sentence  $s$ , define  $T(s)$  to be the set of trees whose *yield* is  $s$  (whole leaves, read left to right, match the words in  $s$ )

$$t^*(s) = \arg \max_{t \in T(s)} p(t)$$

# Chomsky Normal Form

- Chomsky normal form:

- All rules of the form  $X \rightarrow YZ$  or  $X \rightarrow w$
- In principle, this is no limitation on the space of (P)CFGs
  - N-ary rules introduce new non-terminals



- Unaries / empties are “promoted”
- In practice it’s kind of a pain:
  - Reconstructing n-aries is easy
  - Reconstructing unaries is trickier
  - The straightforward transformations don’t preserve tree scores
- Makes parsing algorithms simpler!

# Original Grammar

S → NP VP                      0.8  
S → Aux NP VP                0.1

**S → VP                      0.1**

NP → Pronoun                0.2

NP → Proper-Noun            0.2

NP → Det Nominal            0.6  
Nominal → Noun              0.3

Nominal → Nominal Noun    0.2  
Nominal → Nominal PP       0.5

**VP → Verb                    0.2**

VP → Verb NP                0.5  
VP → VP PP                  0.3  
PP → Prep NP                1.0

## Lexicon:

Noun → book | flight | meal | money  
          0.1     0.5     0.2     0.2

**Verb → book | include | prefer**  
          **0.5     0.2     0.3**

# CNF Conversion Example

Det → the | a | that | this  
          0.6 0.2 0.1 0.1

Pronoun → I | he | she | me  
              0.5 0.1 0.1 0.3

Proper-Noun → Houston | NWA  
                          0.8     0.2

Aux → does  
          1.0

Prep → from | to | on | near | through  
          0.25 0.25 0.1 0.2 0.2



# Original Grammar

# Chomsky Normal Form

$S \rightarrow NP VP$	0.8
$S \rightarrow Aux NP VP$	0.1
$S \rightarrow VP$	0.1

$S \rightarrow NP VP$	0.8
$S \rightarrow X1 VP$	0.1
$X1 \rightarrow Aux NP$	1.0

$NP \rightarrow Pronoun$	0.2
--------------------------	-----

$NP \rightarrow Proper-Noun$	0.2
------------------------------	-----

$NP \rightarrow Det Nominal$	0.6
$Nominal \rightarrow Noun$	0.3

$Nominal \rightarrow Nominal Noun$	0.2
$Nominal \rightarrow Nominal PP$	0.5
$VP \rightarrow Verb$	0.2

$VP \rightarrow Verb NP$	0.5
$VP \rightarrow VP PP$	0.3
$PP \rightarrow Prep NP$	1.0

Lexicon (See previous slide for full list) :

Noun  $\rightarrow$  book | flight | meal | money  
           0.1    0.5    0.2    0.2

Verb  $\rightarrow$  book | include | prefer  
           0.5    0.2    0.3

# Original Grammar

# Chomsky Normal Form

S → NP VP 0.8

S → Aux NP VP 0.1

**S → VP 0.1**

NP → Pronoun 0.2

NP → Proper-Noun 0.2

NP → Det Nominal 0.6

Nominal → Noun 0.3

Nominal → Nominal Noun 0.2

Nominal → Nominal PP 0.5

**VP → Verb 0.2**

**VP → Verb NP 0.5**

**VP → VP PP 0.3**

PP → Prep NP 1.0

S → NP VP 0.8

S → X1 VP 0.1

X1 → Aux NP 1.0

S → book | include | prefer

S → Verb NP

S → VP PP

**Lexicon** (See previous slide for full list) :

Noun → book | flight | meal | money

0.1 0.5 0.2 0.2

**Verb → book | include | prefer**

**0.5 0.2 0.3**

# Original Grammar

# Chomsky Normal Form

S → NP VP	0.8	S → NP VP	0.8
S → Aux NP VP	0.1	S → X1 VP	0.1
<b>S → VP</b>	<b>0.1</b>	X1 → Aux NP	1.0
		S → book   include   prefer	
		0.01 0.004 0.006	
		S → Verb NP	0.05
		S → VP PP	0.03
NP → Pronoun	0.2	NP → I   he   she   me	
		0.1 0.02 0.02 0.06	
NP → Proper-Noun	0.2	NP → Houston   NWA	
		0.16 .04	
NP → Det Nominal	0.6	NP → Det Nominal	0.6
Nominal → Noun	0.3	Nominal → book   flight   meal   money	
		0.03 0.15 0.06 0.06	
Nominal → Nominal Noun	0.2	Nominal → Nominal Noun	0.2
Nominal → Nominal PP	0.5	Nominal → Nominal PP	0.5
<b>VP → Verb</b>	<b>0.2</b>	VP → book   include   prefer	
		0.1 0.04 0.06	
<b>VP → Verb NP</b>	<b>0.5</b>	VP → Verb NP	0.5
<b>VP → VP PP</b>	<b>0.3</b>	VP → VP PP	0.3
PP → Prep NP	1.0	PP → Prep NP	1.0

**Lexicon** (See previous slide for full list) :

Noun → book | flight | meal | money

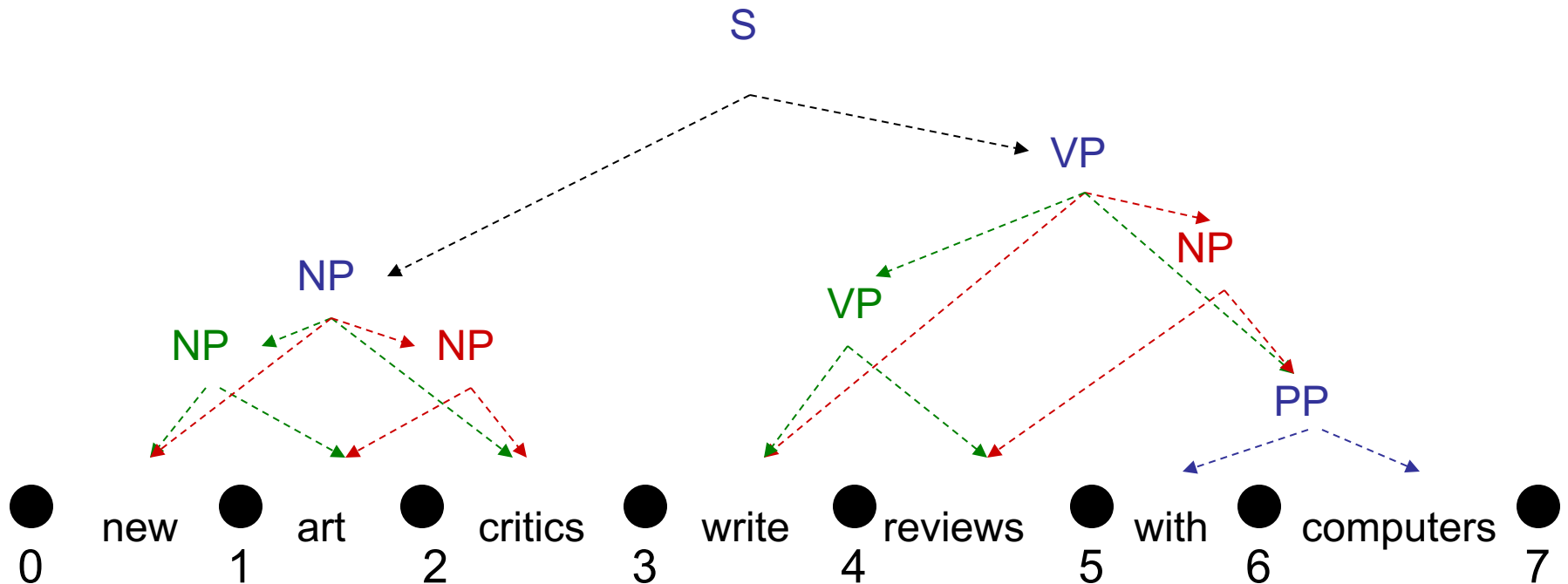
0.1 0.5 0.2 0.2

**Verb → book | include | prefer**

**0.5 0.2 0.3**

# The Parsing Problem

---



# A Recursive Parser

---

```
bestScore(i, j, X)
  if (j == i)
    return q(X->s[i])
  else
    return maxk, X->YZ q(X->YZ) *
      bestScore(i, k, Y) *
      bestScore(k+1, j, Z)
```

- Will this parser work?
- Why or why not?
- Memory/time requirements?
- Q: Remind you of anything? Can we adapt this to other models / inference tasks?

# Dynamic Programming

---

- **We will store:** score of the max parse of  $x_i$  to  $x_j$  with root non-terminal  $X$

$$\pi(i, j, X)$$

- **So we can compute the most likely parse:**

$$\pi(1, n, S) = \max_{t \in \mathcal{T}_G(s)} p(t)$$

- **Via the recursion:**

$$\pi(i, j, X) = \max_{\substack{X \rightarrow YZ \in R, \\ s \in \{i \dots (j-1)\}}} (q(X \rightarrow YZ) \times \pi(i, s, Y) \times \pi(s+1, j, Z))$$

- **With base case:**

$$\pi(i, i, X) = \begin{cases} q(X \rightarrow x_i) & \text{if } X \rightarrow x_i \in R \\ 0 & \text{otherwise} \end{cases}$$

# The CKY Algorithm

- **Input:** a sentence  $s = x_1 \dots x_n$  and a PCFG =  $\langle N, \Sigma, S, R, q \rangle$
- **Initialization:** For  $i = 1 \dots n$  and all  $X$  in  $N$

$$\pi(i, i, X) = \begin{cases} q(X \rightarrow x_i) & \text{if } X \rightarrow x_i \in R \\ 0 & \text{otherwise} \end{cases}$$

- For  $l = 1 \dots (n-1)$  [iterate all phrase lengths]
  - For  $i = 1 \dots (n-l)$  and  $j = i+l$  [iterate all phrases of length  $l$ ]
    - For all  $X$  in  $N$  [iterate all non-terminals]

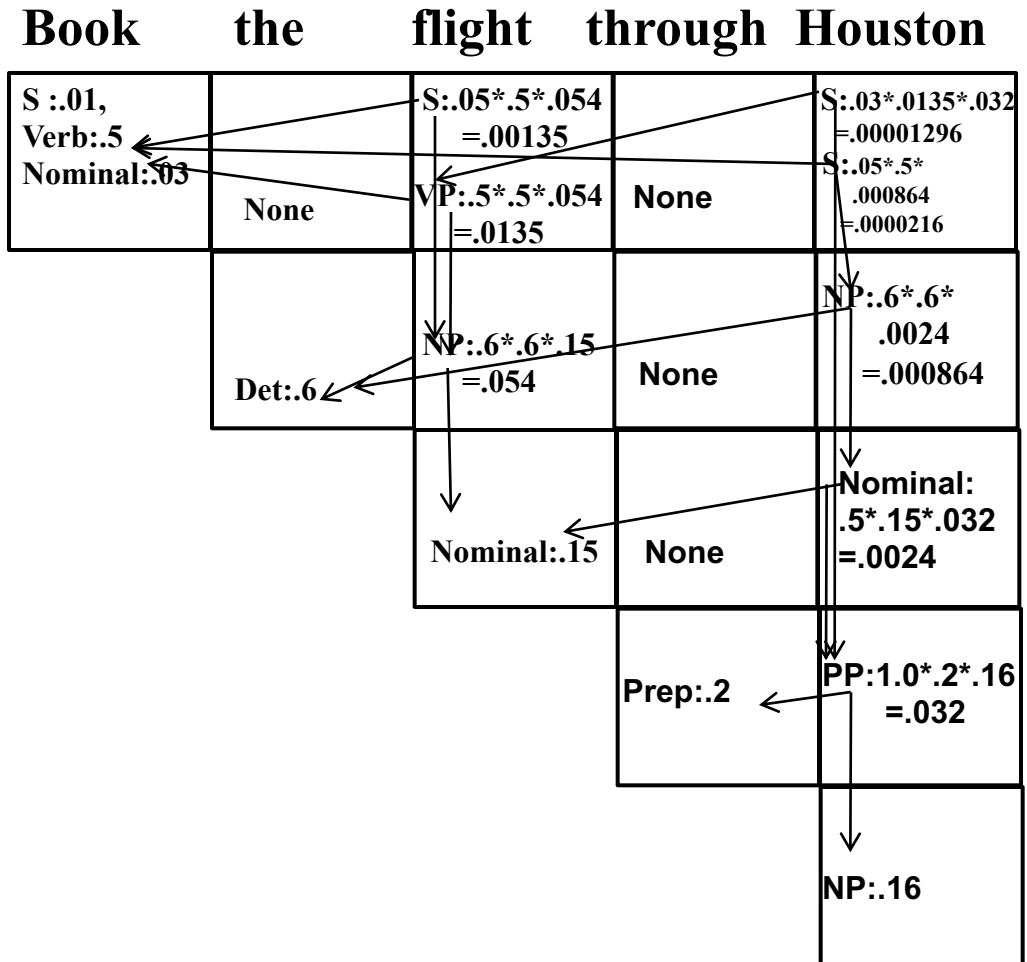
$$\pi(i, j, X) = \max_{\substack{X \rightarrow YZ \in R, \\ s \in \{i \dots (j-1)\}}} (q(X \rightarrow YZ) \times \pi(i, s, Y) \times \pi(s+1, j, Z))$$

- also, store back pointers

$$bp(i, j, X) = \arg \max_{\substack{X \rightarrow YZ \in R, \\ s \in \{i \dots (j-1)\}}} (q(X \rightarrow YZ) \times \pi(i, s, Y) \times \pi(s+1, j, Z))$$

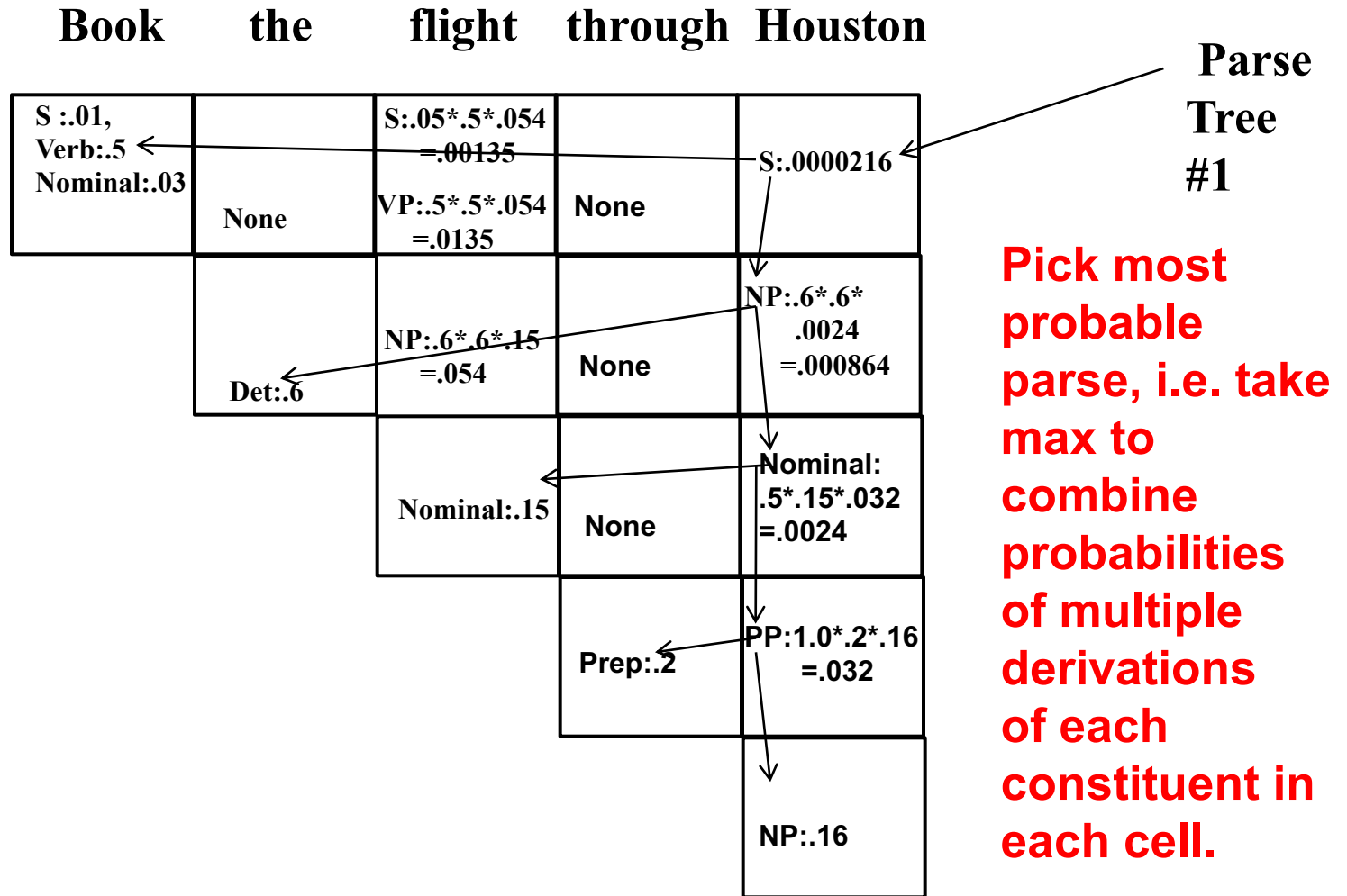
# Probabilistic CKY Parser

**S** → **NP VP** 0.8  
**S** → **X1 VP** 0.1  
**X1** → **Aux NP** 1.0  
**S** → **book | include | prefer**  
           0.01 0.004 0.006  
**S** → **Verb NP** 0.05  
**S** → **VP PP** 0.03  
**NP** → **I | he | she | me**  
           0.1 0.02 0.02 0.06  
**NP** → **Houston | NWA**  
           0.16 0.04  
**Det** → **the | a | an**  
           0.6 0.1 0.05  
**NP** → **Det Nominal** 0.6  
**Nominal** → **book | flight | meal | money**  
           0.03 0.15 0.06 0.06  
**Nominal** → **Nominal Nominal** 0.2  
**Nominal** → **Nominal PP** 0.5  
**Verb** → **book | include | prefer**  
           0.5 0.04 0.06  
**VP** → **Verb NP** 0.5  
**VP** → **VP PP** 0.3  
**Prep** → **through | to | from**  
           0.2 0.3 0.3  
**PP** → **Prep NP** 1.0

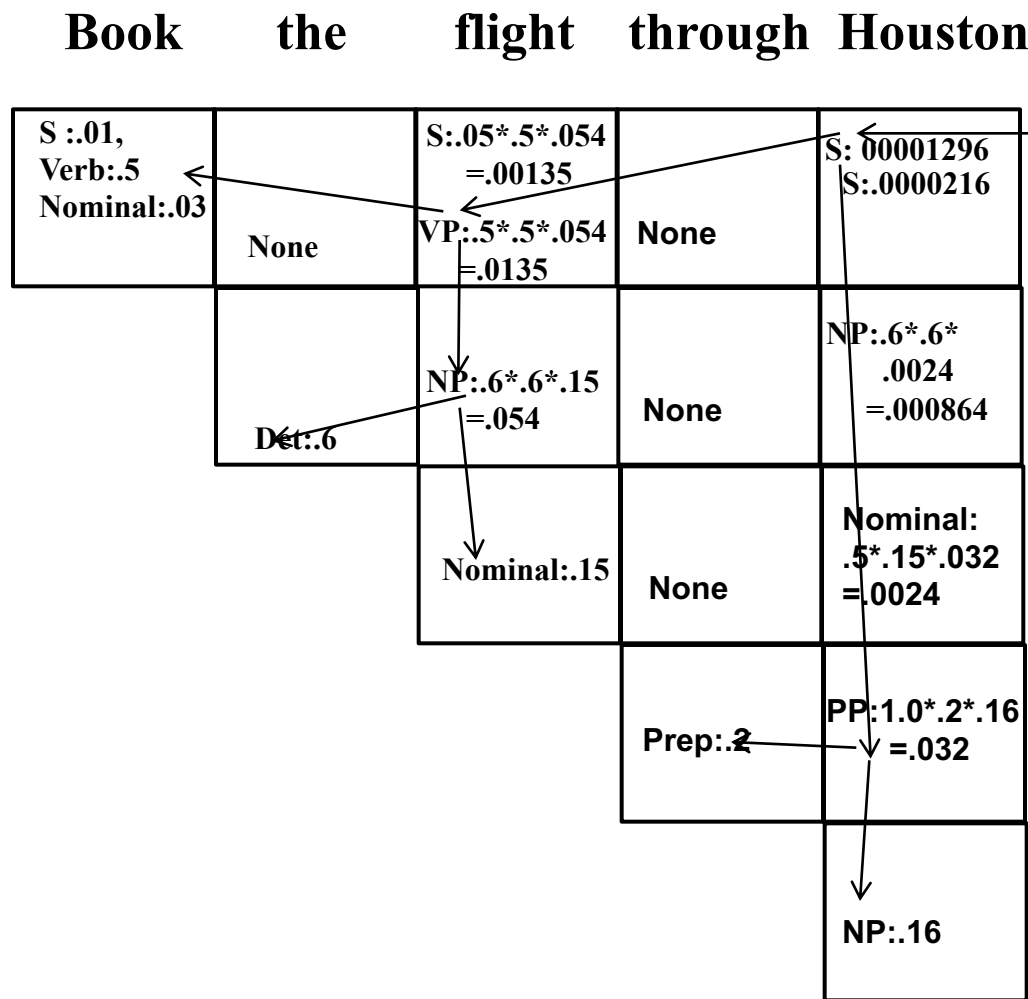




# Probabilistic CKY Parser



# Probabilistic CKY Parser



**Pick most probable parse, i.e. take max to combine probabilities of multiple derivations of each constituent in each cell.**

# Memory

---

- How much memory does this require?
  - Have to store the score cache
  - Cache size:  $|\text{symbols}| * n^2$  doubles
- Pruning: Beam Search
  - $\text{score}[X][i][j]$  can get too large (when?)
  - Can keep beams (truncated maps  $\text{score}[i][j]$ ) which only store the best K scores for the span  $[i,j]$
- Pruning: Coarse-to-Fine
  - Use a smaller grammar to rule out most  $X[i,j]$
  - Much more on this later...

# Time: Theory

---

- How much time will it take to parse?

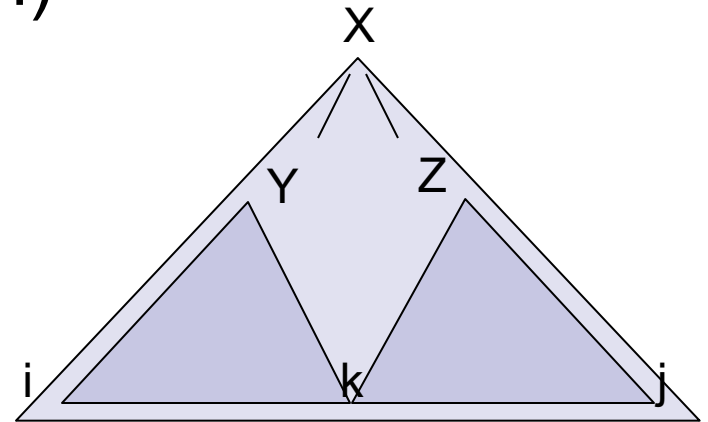
- For each diff ( $:= j - i$ ) ( $\leq n$ )

- For each  $i$  ( $\leq n$ )

- For each rule  $X \rightarrow Y Z$

- For each split point  $k$

- Do constant work

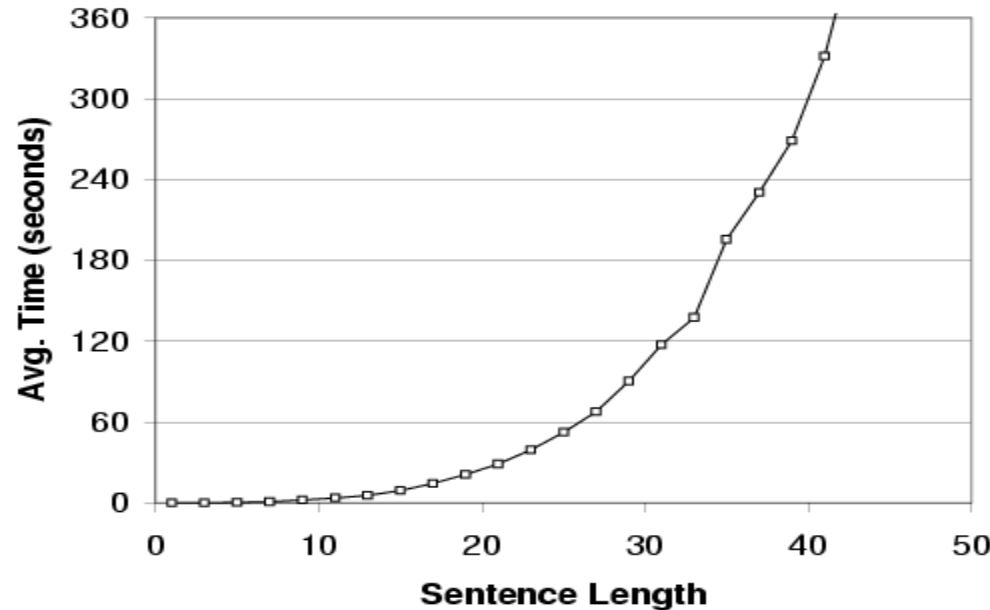


- Total time:  $|\text{rules}| * n^3$

- Something like 5 sec for an unoptimized parse of a 20-word sentences

# Time: Practice

- Parsing with the vanilla treebank grammar:



~ 20K Rules

(not an  
optimized  
parser!)

Observed  
exponent:

3.6

- Why's it worse in practice?

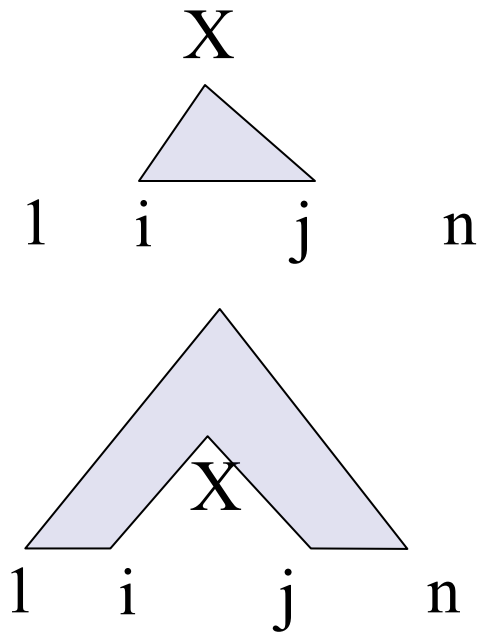
- Longer sentences “unlock” more of the grammar
- All kinds of systems issues don't scale

# Other Dynamic Programs

---

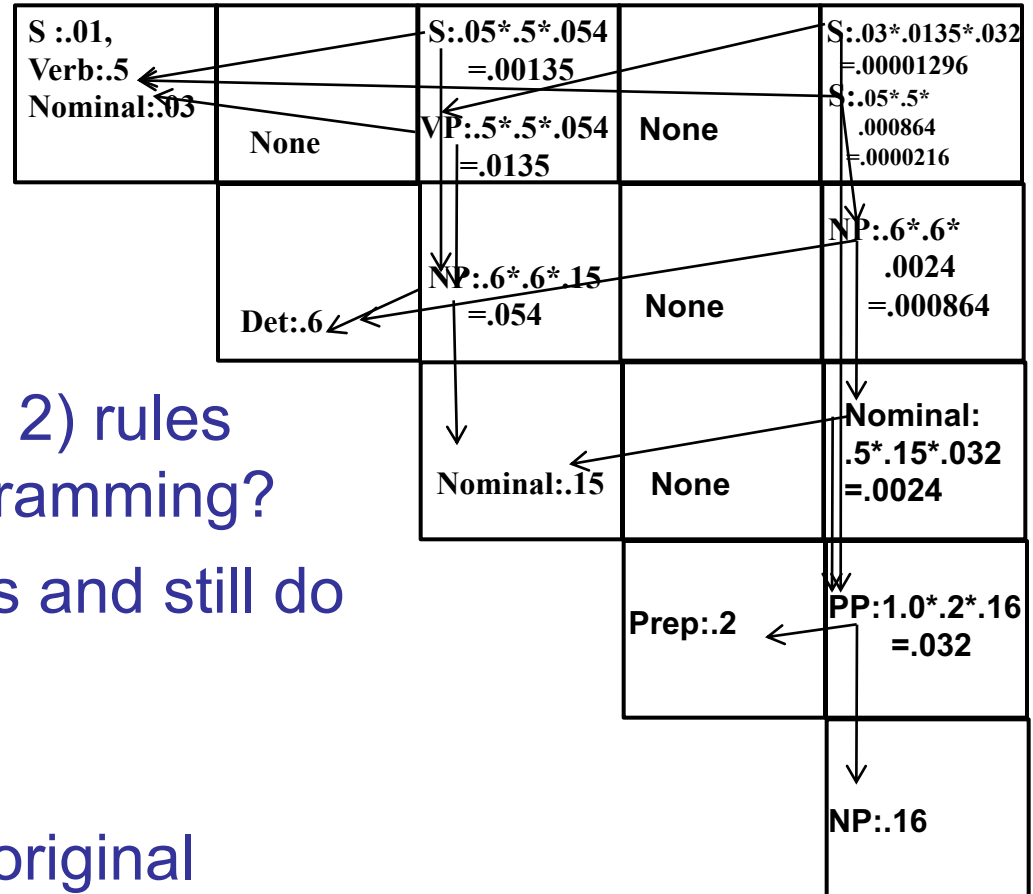
Can also compute other quantities:

- *Best Inside*: score of the max parse of  $w_i$  to  $w_j$  with root non-terminal  $X$
- *Best Outside*: score of the max parse of  $w_0$  to  $w_n$  with a gap from  $w_i$  to  $w_j$  rooted with non-terminal  $X$ 
  - see notes for derivation, it is a bit more complicated
- Sum Inside/Outside: Do sums instead of maxes



# Why Chomsky Normal Form?

**Book the flight through Houston**



Inference:

- Can we keep N-ary ( $N > 2$ ) rules and still do dynamic programming?
- Can we keep unary rules and still do dynamic programming?

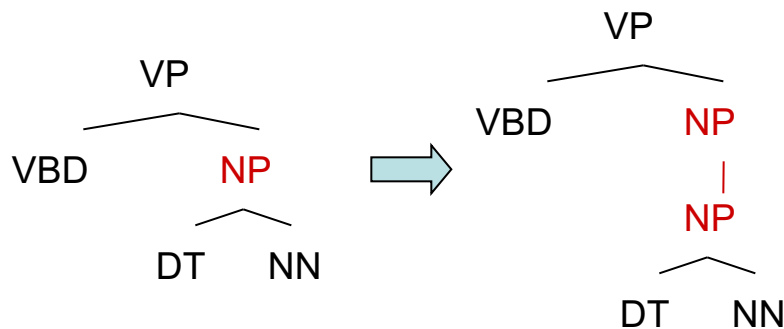
Learning:

- Can we reconstruct the original trees?

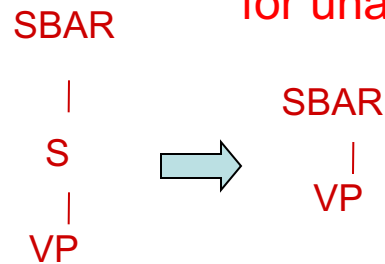
# CNF + Unary Closure

We need unaries to be non-cyclic

- Calculate closure  $\text{Close}(R)$  for unary rules in  $R$ 
  - Add  $X \rightarrow Y$  if there exists a rule chain  $X \rightarrow Z_1, Z_1 \rightarrow Z_2, \dots, Z_k \rightarrow Y$  with  $q(X \rightarrow Y) = q(X \rightarrow Z_1) * q(Z_1 \rightarrow Z_2) * \dots * q(Z_k \rightarrow Y)$
  - If no unary rule exist for  $X$ , add  $X \rightarrow X$  with  $q(X \rightarrow X) = 1$  for all  $X$  in  $N$



WARNING: Watch out for unary cycles!



- Rather than zero or more unaries, always exactly one
- Alternate unary and binary layers
- What about  $X \rightarrow Y$  with different unary paths (and scores)?



# The CKY Algorithm

- **Input:** a sentence  $s = x_1 \dots x_n$  and a PCFG =  $\langle N, \Sigma, S, R, q \rangle$
- **Initialization:** For  $i = 1 \dots n$  and all  $X$  in  $N$

$$\pi(i, i, X) = \begin{cases} q(X \rightarrow x_i) & \text{if } X \rightarrow x_i \in R \\ 0 & \text{otherwise} \end{cases}$$

- For  $l = 1 \dots (n-1)$  [iterate all phrase lengths]
  - For  $i = 1 \dots (n-l)$  and  $j = i+l$  [iterate all phrases of length  $l$ ]
    - For all  $X$  in  $N$  [iterate all non-terminals]

$$\pi(i, j, X) = \max_{\substack{X \rightarrow YZ \in R, \\ s \in \{i \dots (j-1)\}}} (q(X \rightarrow YZ) \times \pi(i, s, Y) \times \pi(s+1, j, Z))$$

- also, store back pointers

$$bp(i, j, X) = \arg \max_{\substack{X \rightarrow YZ \in R, \\ s \in \{i \dots (j-1)\}}} (q(X \rightarrow YZ) \times \pi(i, s, Y) \times \pi(s+1, j, Z))$$

# CKY with Unary Closure

- **Input:** a sentence  $s = x_1 \dots x_n$  and a PCFG =  $\langle N, \Sigma, S, R, q \rangle$
- **Initialization:** For  $i = 1 \dots n$ :

- Step 1: for all  $X$  in  $N$ :  

$$\pi(i, i, X) = \begin{cases} q(X \rightarrow x_i) & \text{if } X \rightarrow x_i \in R \\ 0 & \text{otherwise} \end{cases}$$

- Step 2: for all  $X$  in  $N$ :  

$$\pi_U(i, i, X) = \max_{X \rightarrow Y \in \text{Close}(R)} (q(X \rightarrow Y) \times \pi(i, i, Y))$$

- For  $l = 1 \dots (n-1)$  [iterate all phrase lengths]
  - For  $i = 1 \dots (n-l)$  and  $j = i+l$  [iterate all phrases of length  $l$ ]

- Step 1: (Binary)
    - For all  $X$  in  $N$  [iterate all non-terminals]

$$\pi_B(i, j, X) = \max_{X \rightarrow YZ \in R, s \in \{i \dots (j-1)\}} (q(X \rightarrow YZ) \times \pi_U(i, s, Y) \times \pi_U(s+1, j, Z))$$

- Step 2: (Unary)
    - For all  $X$  in  $N$  [iterate all non-terminals]

$$\pi_U(i, j, X) = \max_{X \rightarrow Y \in \text{Close}(R)} (q(X \rightarrow Y) \times \pi_B(i, j, Y))$$

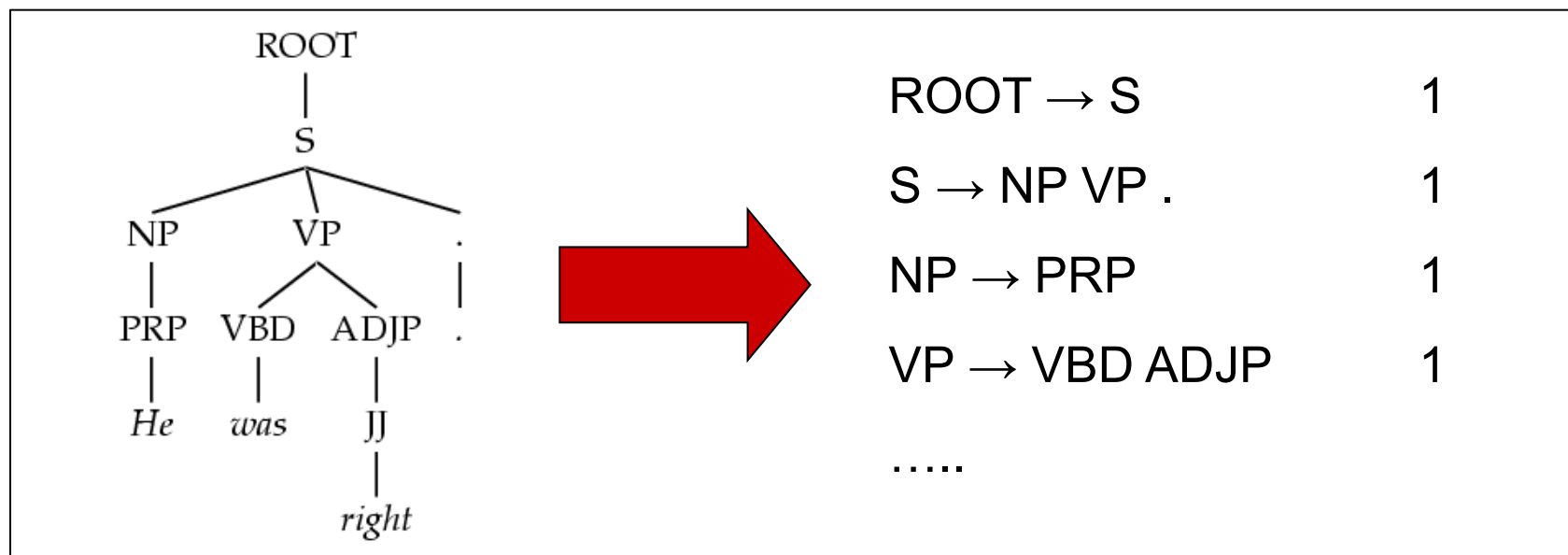
# Treebank Sentences

---

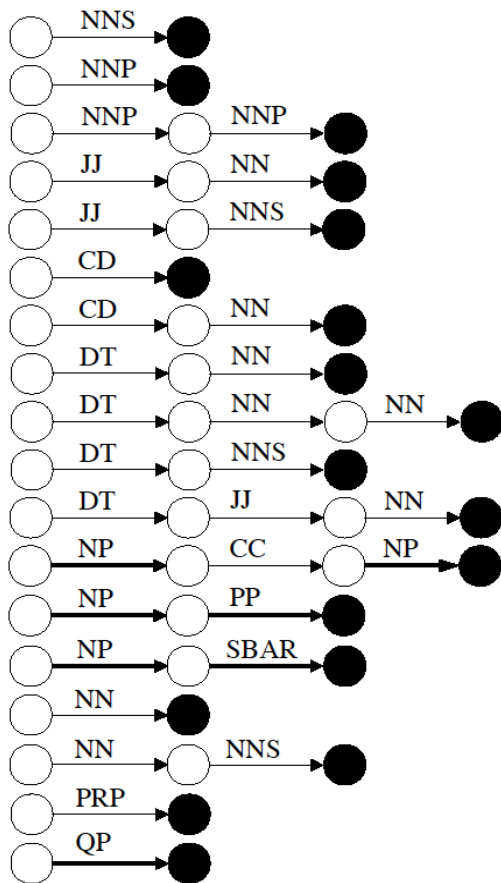
```
( (S (NP-SBJ The move)
    (VP followed
      (NP (NP a round)
        (PP of
          (NP (NP similar increases)
            (PP by
              (NP other lenders))
            (PP against
              (NP Arizona real estate loans))))))
    ,
    (S-ADV (NP-SBJ *)
      (VP reflecting
        (NP (NP a continuing decline)
          (PP-LOC in
            (NP that market))))))
  .))
```

# Treebank Grammars

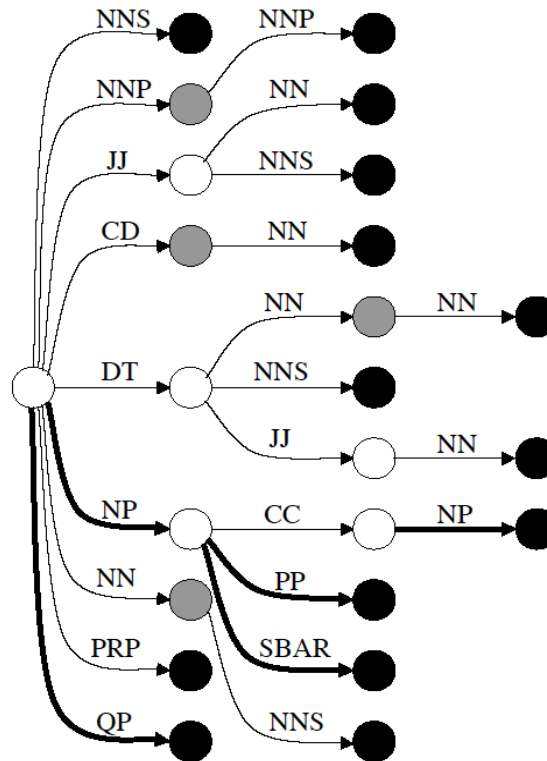
- Need a PCFG for broad coverage parsing.
- Can take a grammar right off the trees (doesn't work well):



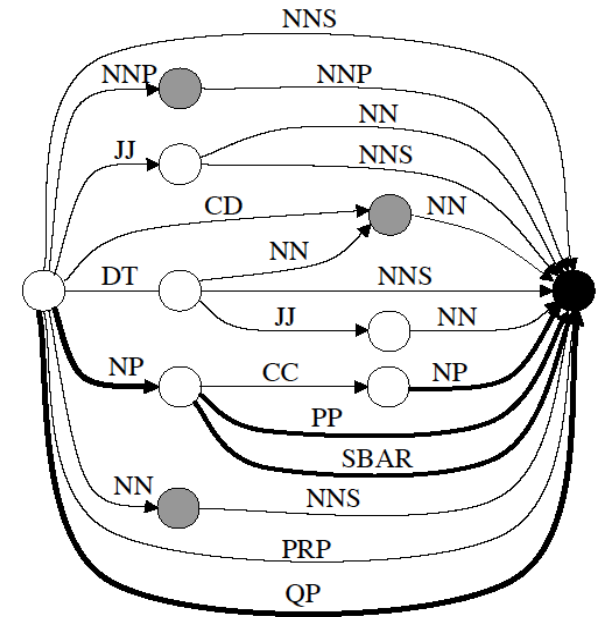
- Better results by enriching the grammar (e.g., lexicalization).
- Can also get reasonable parsers without lexicalization.



## LIST



# TRIE



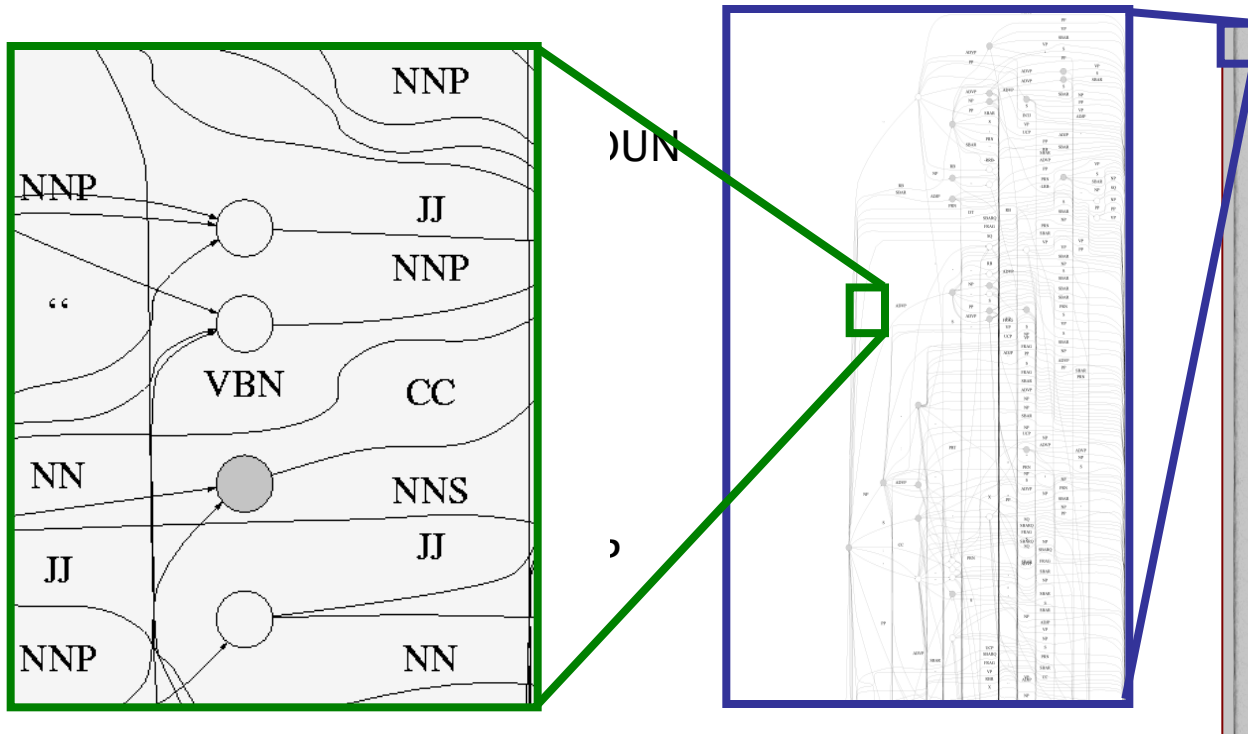
## Min FSA

Grammar encodings: Non-black states are active, non-white states are accepting, and bold transitions are phrasal. FSAs for a subset of the rules for the category NP.

# Treebank Grammar Scale

- Treebank grammars can be enormous
  - As FSAs, the raw grammar has ~10K states, excluding the lexicon
  - Better parsers usually make the grammars larger, not smaller

NP:



# Typical Experimental Setup

---

- Corpus: Penn Treebank, WSJ



Training: sections 02-21

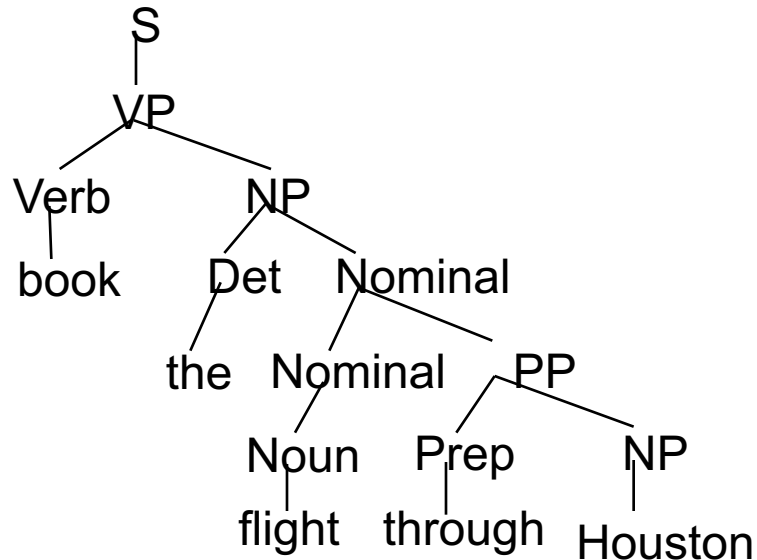
Development: section 22 (here, first 20 files)

Test: section 23

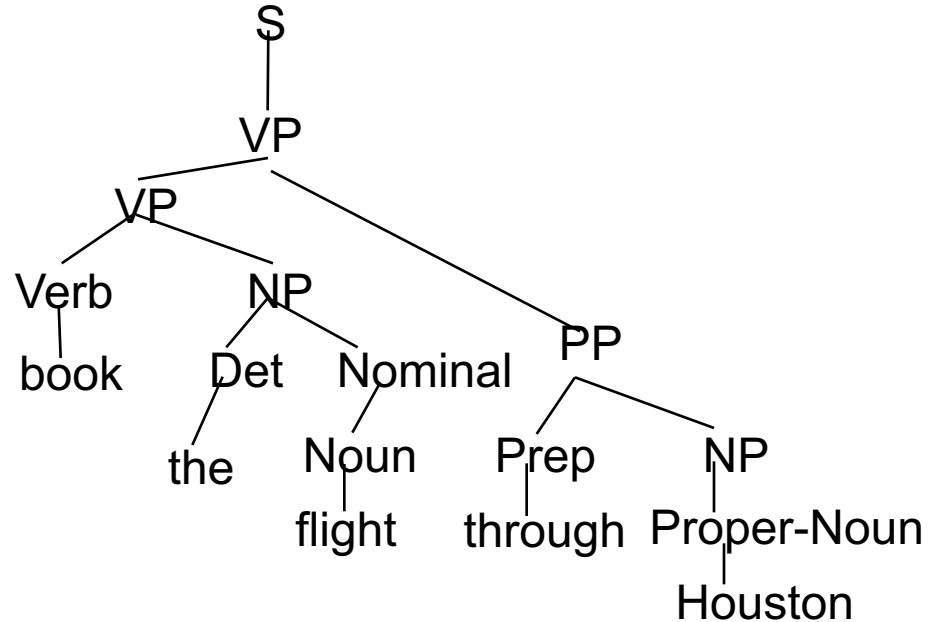
- Accuracy – F1: harmonic mean of per-node labeled precision and recall.
- Here: also size – number of symbols in grammar.
  - Passive / complete symbols: NP, NP<sup>S</sup>
  - Active / incomplete symbols: NP → NP CC •

# How to Evaluate?

**Correct Tree T**



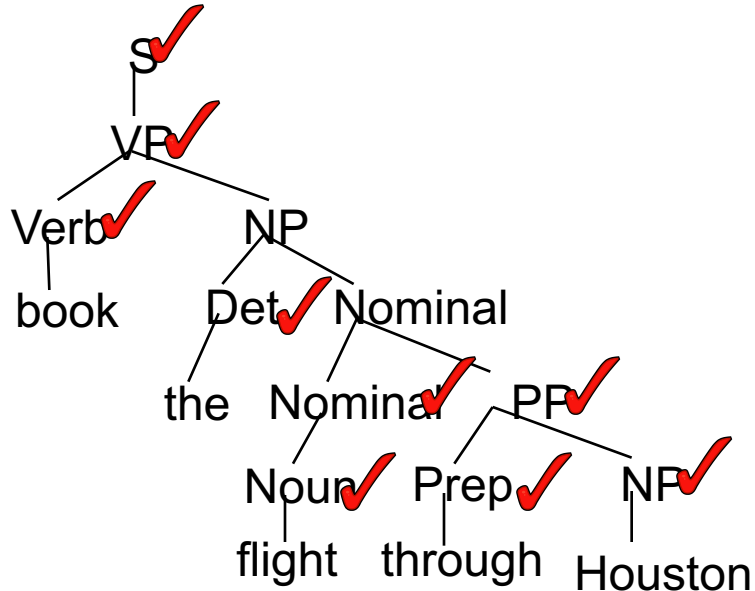
**Computed Tree P**





# PARSEVAL Example

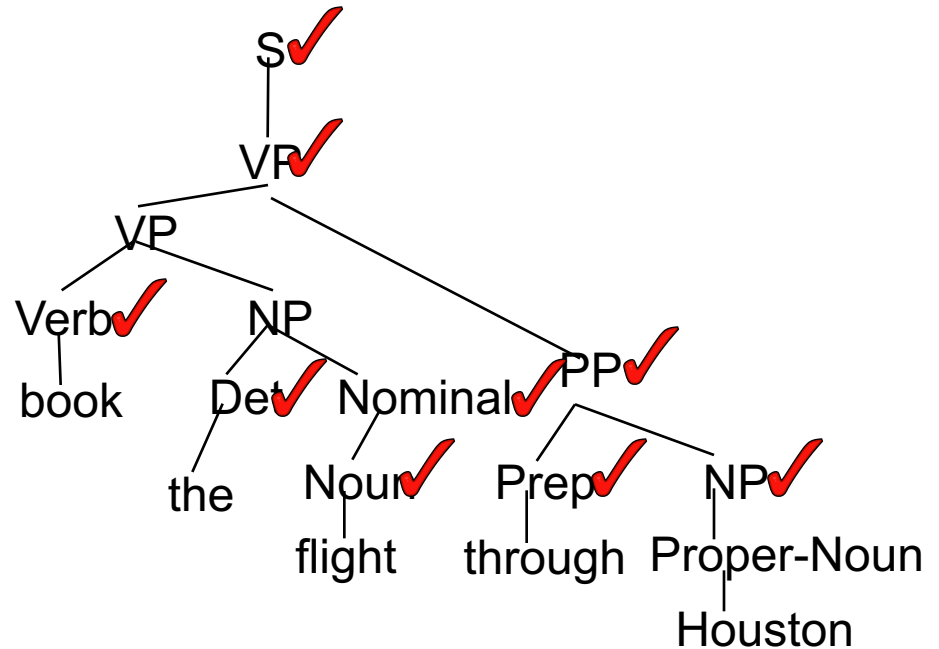
**Correct Tree T**



# Constituents: 11

# Correct Constituents: 10

**Computed Tree P**



# Constituents: 12

Recall =  $10/11 = 90.9\%$     Precision =  $10/12 = 83.3\%$      $F_1 = 87.4\%$

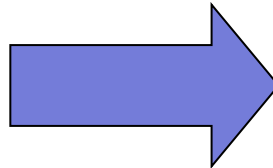
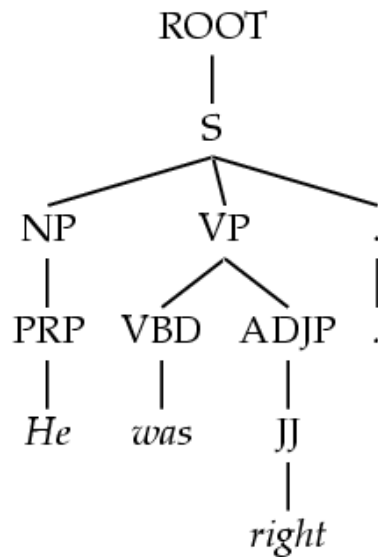
# Evaluation Metric

---

- PARSEVAL metrics measure the fraction of the constituents that match between the computed and human parse trees. If  $P$  is the system's parse tree and  $T$  is the human parse tree (the “gold standard”):
  - $\text{Recall} = (\# \text{ correct constituents in } P) / (\# \text{ constituents in } T)$
  - $\text{Precision} = (\# \text{ correct constituents in } P) / (\# \text{ constituents in } P)$
- Labeled Precision and labeled recall require getting the non-terminal label on the constituent node correct to count as correct.
- F1 is the harmonic mean of precision and recall.
  - $F1 = (2 * \text{Precision} * \text{Recall}) / (\text{Precision} + \text{Recall})$

# Performance with Vanilla PCFGs

- Use PCFGs for broad coverage parsing [Charniak 96]
- Take the grammar right off the trees



ROOT  $\rightarrow$  S 1

S  $\rightarrow$  NP VP . 1

NP  $\rightarrow$  PRP 1

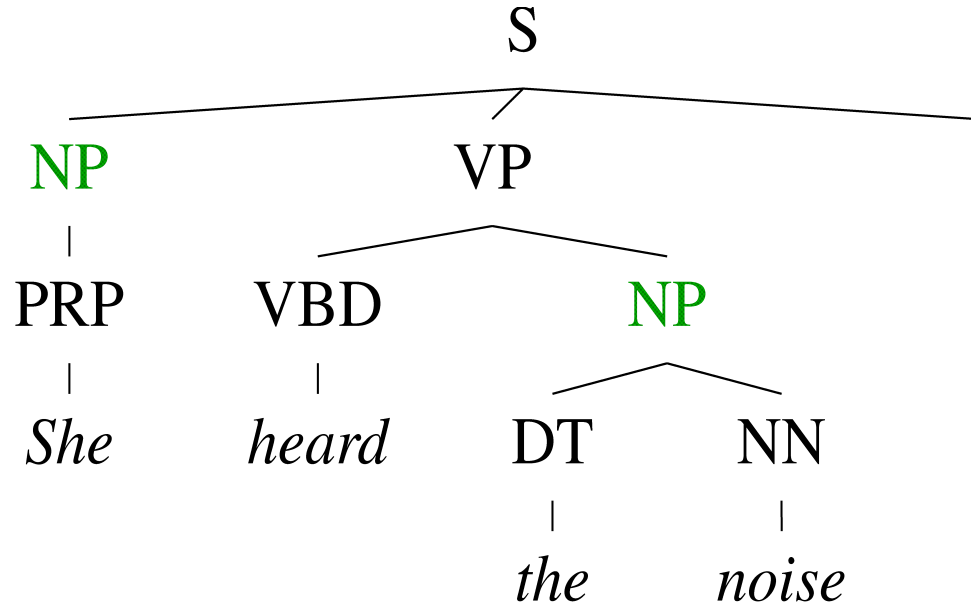
VP  $\rightarrow$  VBD ADJP 1

.....

Model	F1
Baseline	72.0

# Conditional Independence?

---



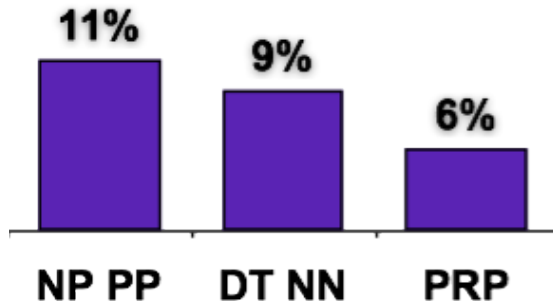
- Not every NP expansion can fill every NP slot
  - A grammar with symbols like “NP” won’t be context-free
  - Statistically, conditional independence too strong

# Non-Independence

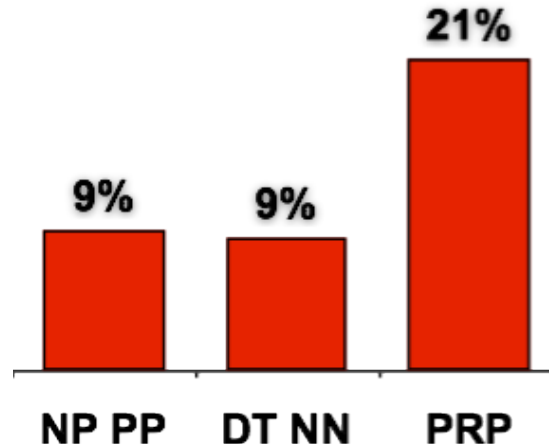
---

- Independence assumptions are often too strong.

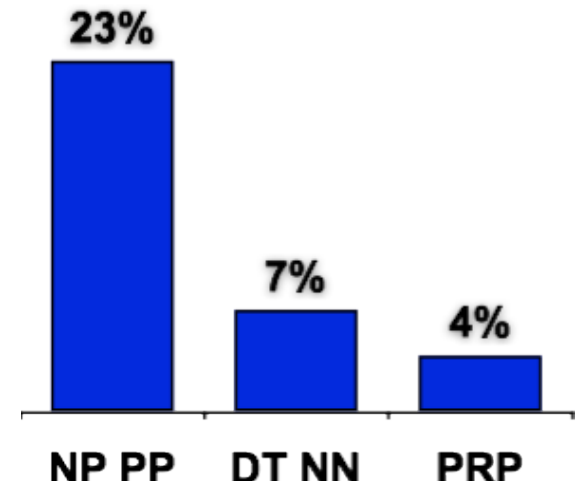
All NPs



NPs under S

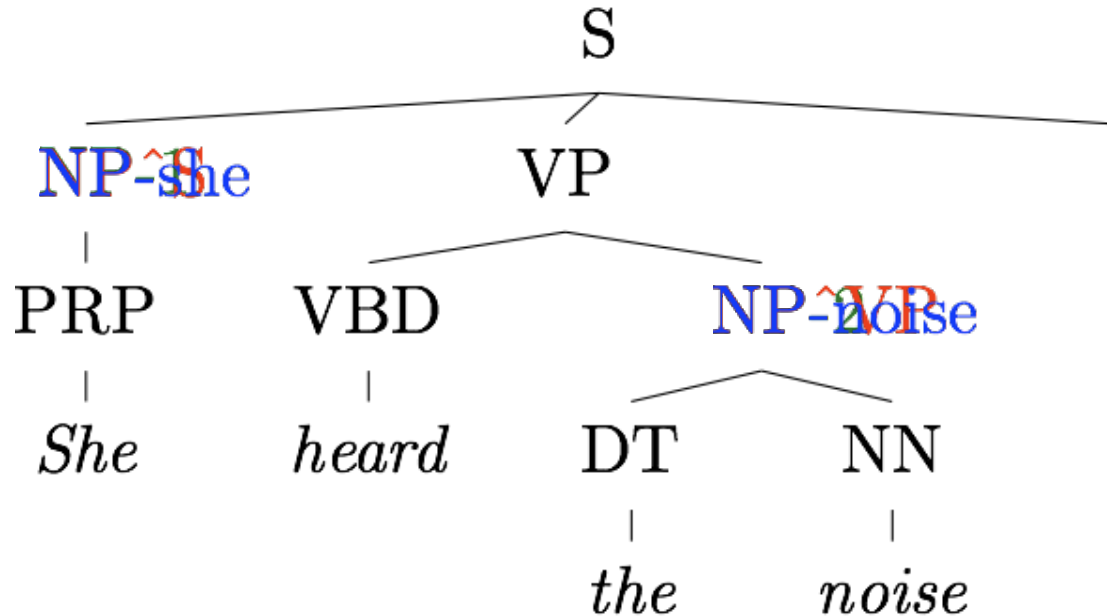


NPs under VP



- Example: the expansion of an NP is highly dependent on the parent of the NP (i.e., subjects vs. objects).
- Also: the subject and object expansions are correlated!

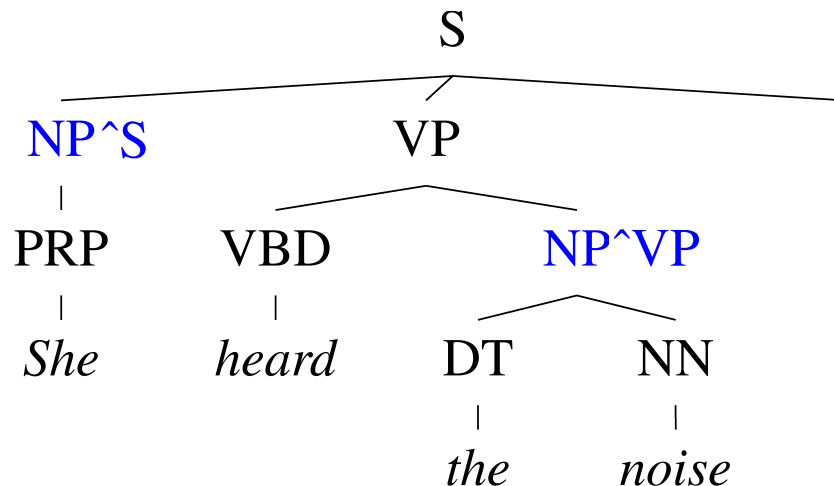
# Grammar Refinement



- Structure Annotation [Johnson '98, Klein&Manning '03]
- Lexicalization [Collins '99, Charniak '00]
- Latent Variables [Matsuzaki et al. '05, Petrov et al. '06]

# The Game of Designing a Grammar

---

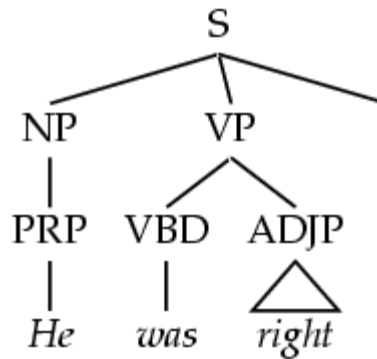


- Annotation refines base treebank symbols to improve statistical fit of the grammar
- Structural annotation

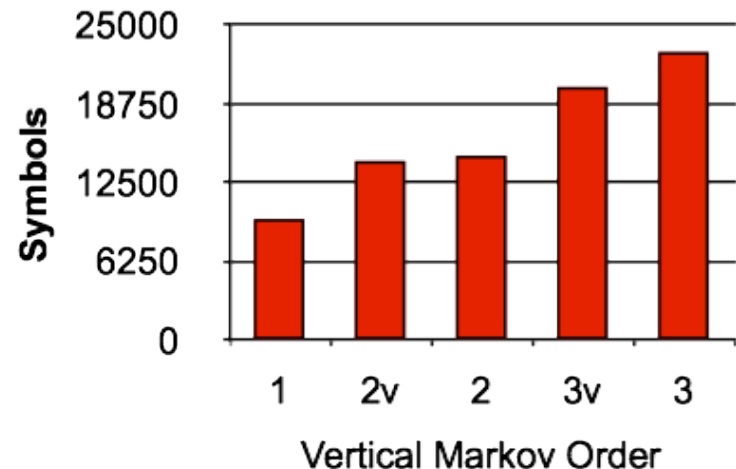
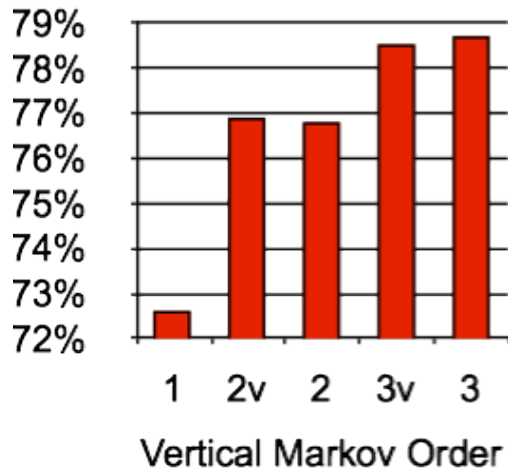
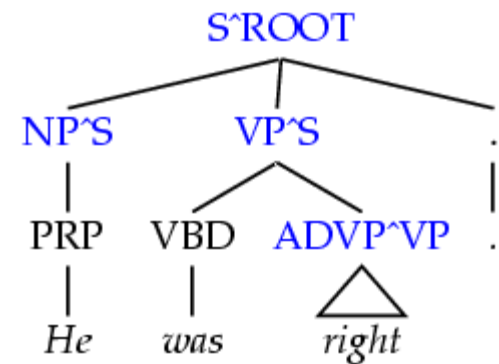
# Vertical Markovization

- Vertical Markov order: rewrites depend on past  $k$  ancestor nodes.  
(cf. parent annotation)

Order 1

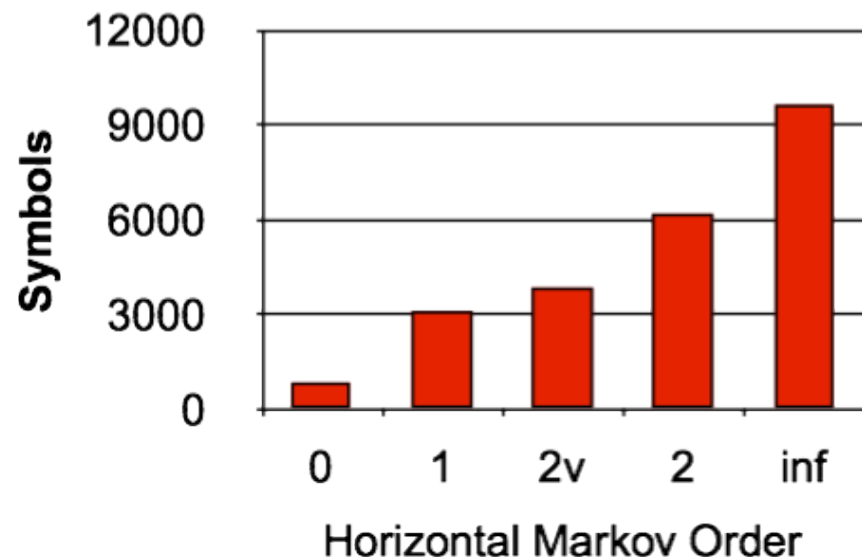
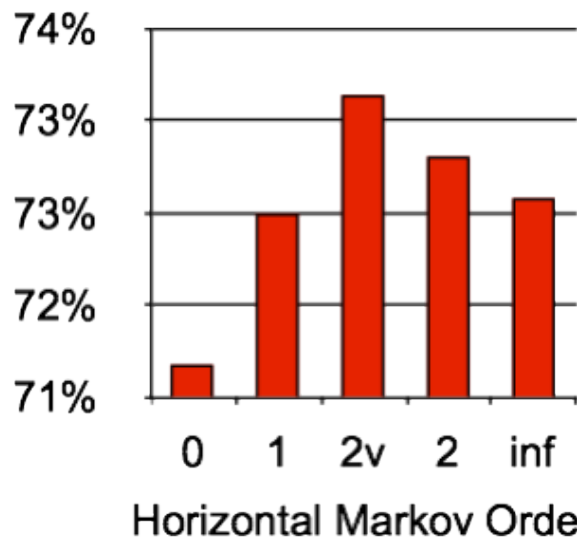
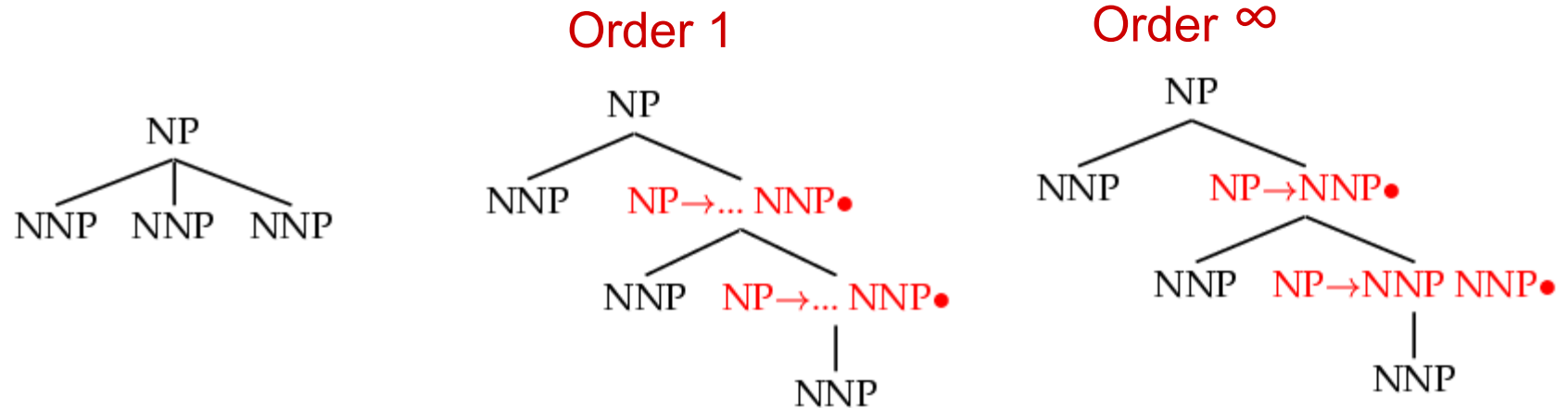


Order 2

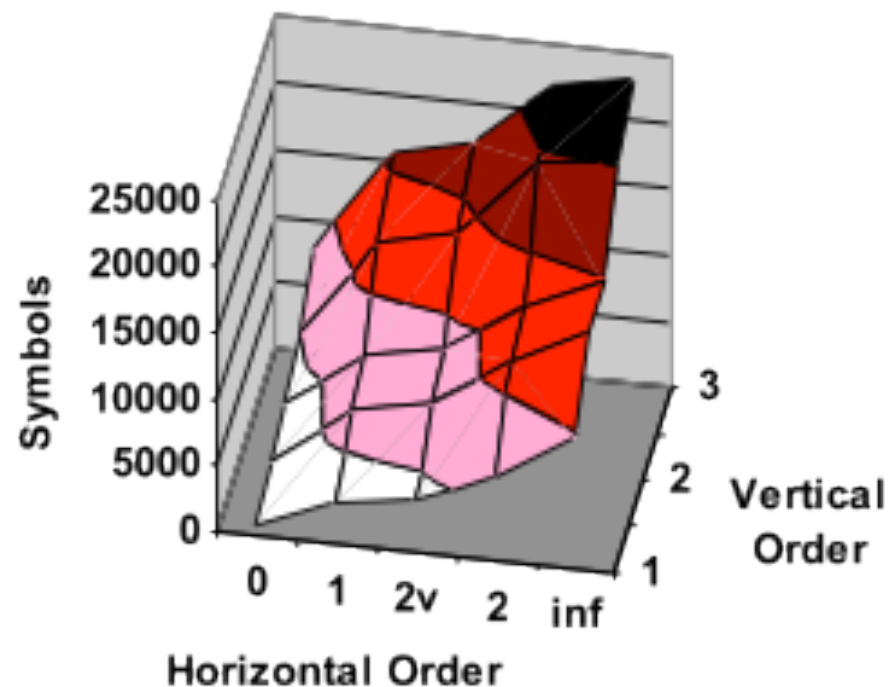
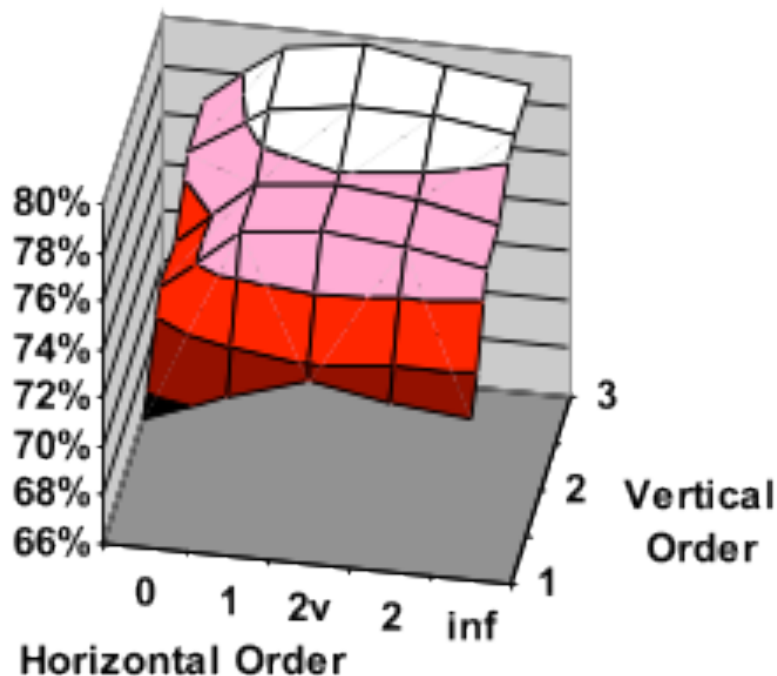




# Horizontal Markovization



# Vertical and Horizontal



- Raw treebank:  $v=1, h=\infty$
- Johnson 98:  $v=2, h=\infty$
- Collins 99:  $v=2, h=2$
- Best F1:  $v=3, h=2v$

Model	F1	Size
$v=h=2v$	77.8	7.5K

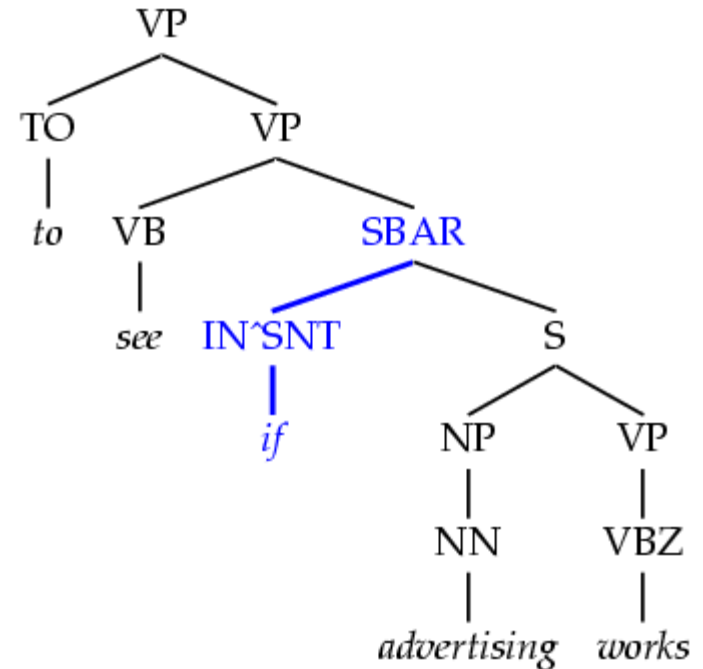
# Unlexicalized PCFG Grammar Size

Vertical Order		Horizontal Markov Order				
		$h = 0$	$h = 1$	$h \leq 2$	$h = 2$	$h = \infty$
$v = 1$	No annotation	71.27 (854)	72.5 (3119)	73.46 (3863)	72.96 (6207)	72.62 (9657)
$v \leq 2$	Sel. Parents	74.75 (2285)	77.42 (6564)	77.77 (7619)	77.50 (11398)	76.91 (14247)
$v = 2$	All Parents	74.68 (2984)	77.42 (7312)	77.81 (8367)	77.50 (12132)	76.81 (14666)
$v \leq 3$	Sel. GParents	76.50 (4943)	78.59 (12374)	79.07 (13627)	78.97 (19545)	78.54 (20123)
$v = 3$	All GParents	76.74 (7797)	79.18 (15740)	79.74 (16994)	79.07 (22886)	78.72 (22002)

Figure 2: Markovizations:  $F_1$  and grammar size.

# Tag Splits

- Problem: Treebank tags are too coarse.
- Example: Sentential, PP, and other prepositions are all marked IN.
- Partial Solution:
  - Subdivide the IN tag.



Annotation	F1	Size
<b>v=h=2v</b>	<b>78.3</b>	<b>8.0K</b>
SPLIT-IN	80.3	8.1K

# Other Tag Splits

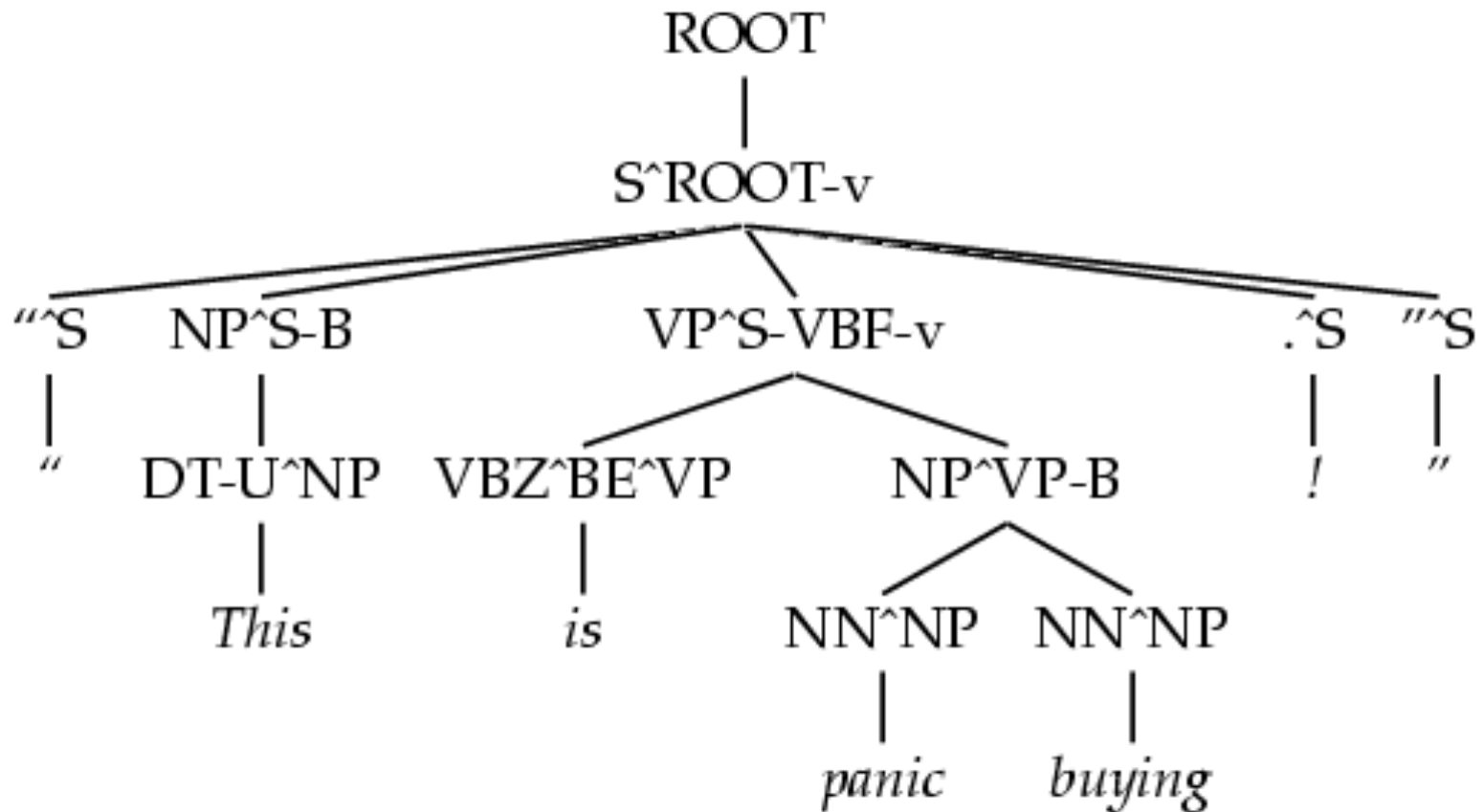
---

- UNARY-DT: mark demonstratives as DT<sup>U</sup> (“the X” vs. “those”)
- UNARY-RB: mark phrasal adverbs as RB<sup>U</sup> (“quickly” vs. “very”)
- TAG-PA: mark tags with non-canonical parents (“not” is an RB<sup>VP</sup>)
- SPLIT-AUX: mark auxiliary verbs with –AUX [cf. Charniak 97]
- SPLIT-CC: separate “but” and “&” from other conjunctions
- SPLIT-%: “%” gets its own tag.

F1	Size
80.4	8.1K
80.5	8.1K
81.2	8.5K
81.6	9.0K
81.7	9.1K
81.8	9.3K

# A Fully Annotated (Unlex) Tree

---



# Some Test Set Results

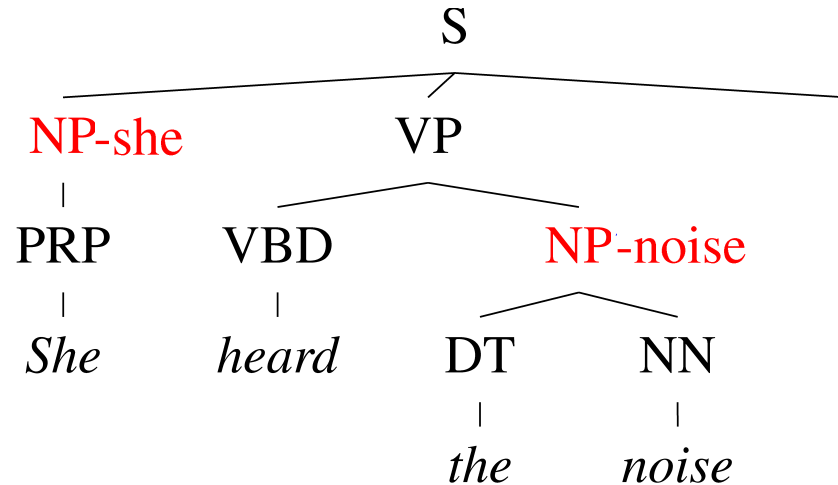
---

Parser	LP	LR	F1
Magerman 95	84.9	84.6	84.7
Collins 96	86.3	85.8	86.0
Unlexicalized	86.9	85.7	86.3
Charniak 97	87.4	87.5	87.4
Collins 99	88.7	88.6	88.6

- Beats “first generation” lexicalized parsers.
- Lots of room to improve – more complex models next.

# The Game of Designing a Grammar

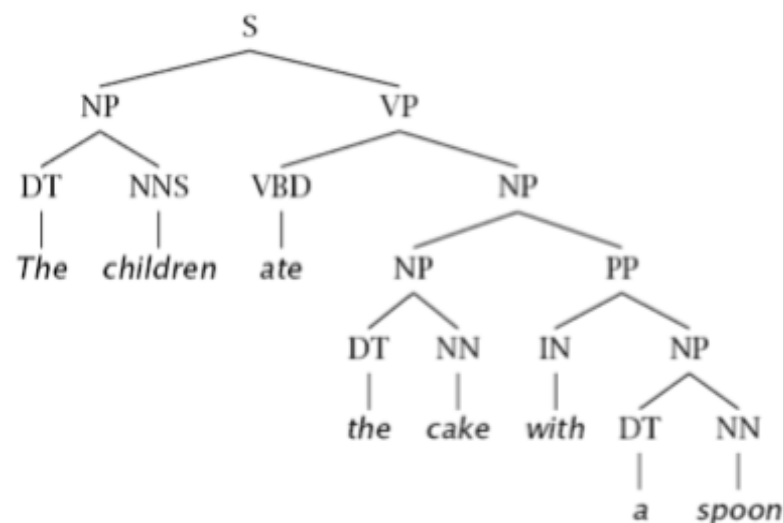
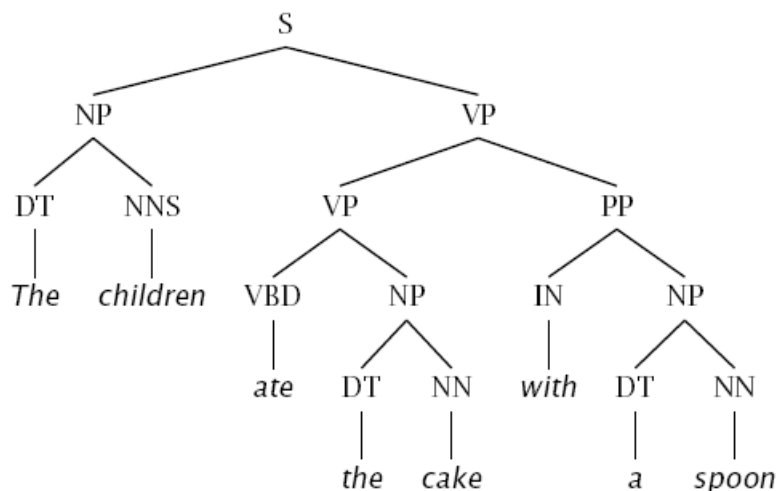
---



- Annotation refines base treebank symbols to improve statistical fit of the grammar
- Structural annotation [Johnson ' 98, Klein and Manning 03]
- Head lexicalization [Collins ' 99, Charniak ' 00]



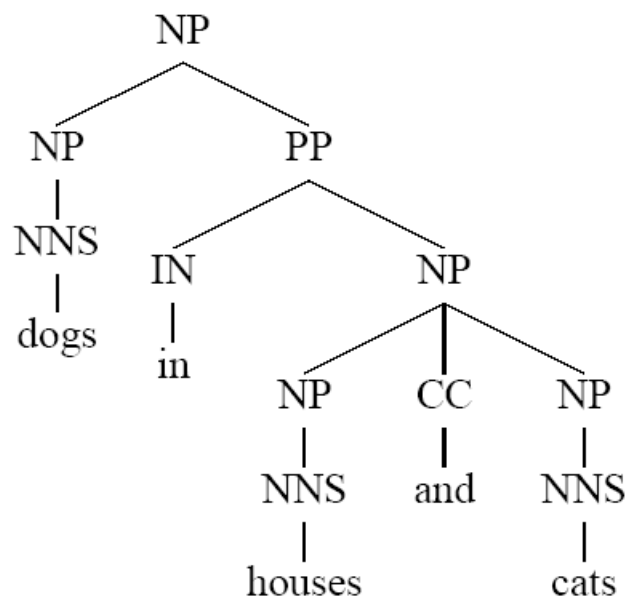
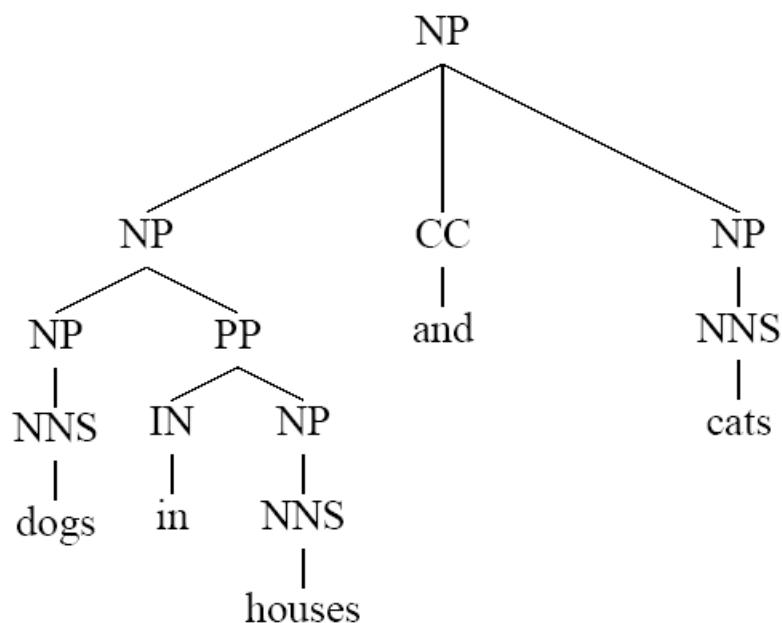
# Problems with PCFGs



- If we do no annotation, these trees differ only in one rule:
  - $VP \rightarrow VP PP$
  - $NP \rightarrow NP PP$
- Parse will go one way or the other, regardless of words
- We addressed this in one way with unlexicalized grammars (how?)
- Lexicalization allows us to be sensitive to specific words

# Problems with PCFGs

---



- What's different between basic PCFG scores here?
- What (lexical) correlations need to be scored?

# Lexicalize Trees!



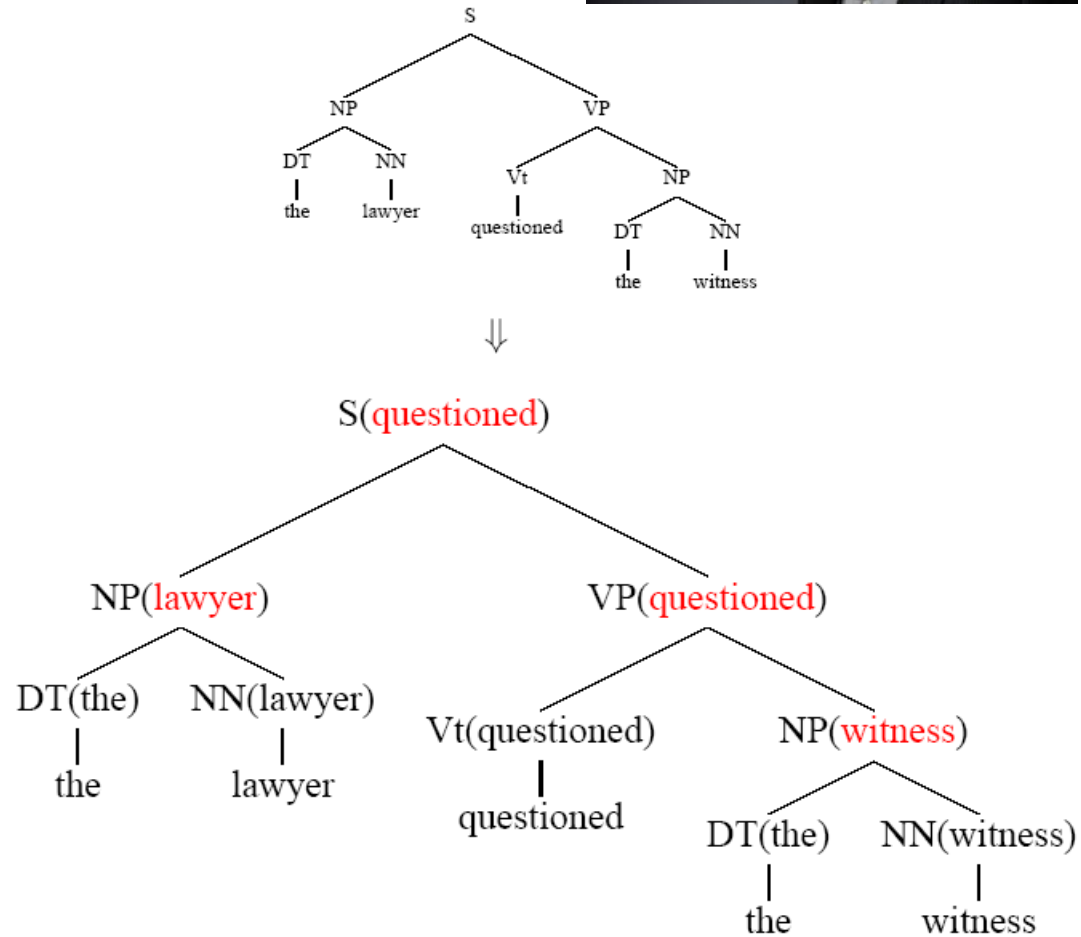
- Add “headwords” to each phrasal node
  - Headship not in (most) treebanks
  - Usually use (handwritten) head rules, e.g.:

- NP:

- Take leftmost NP
- Take rightmost N\*
- Take rightmost JJ
- Take right child

- VP:

- Take leftmost VB\*
- Take leftmost VP
- Take left child



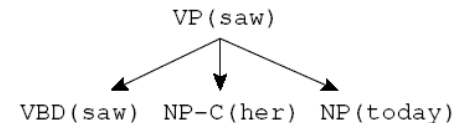
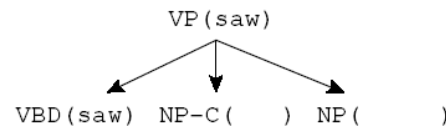
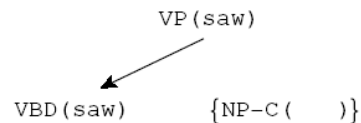
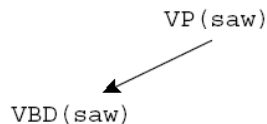
# Lexicalized PCFGs?

---

- Problem: we now have to estimate probabilities like

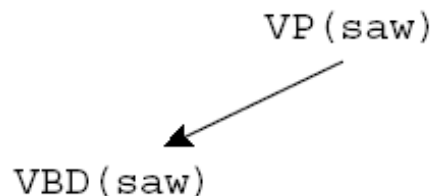
$VP(saw) \rightarrow VBD(saw) \ NP-C(her) \ NP(today)$

- Never going to get these atomically off of a treebank
- Solution: break up derivation into smaller steps

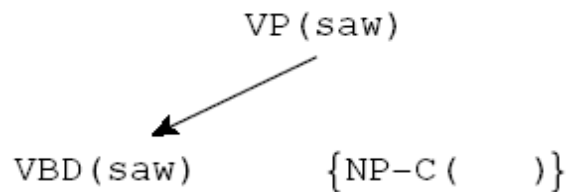


# Lexical Derivation Steps

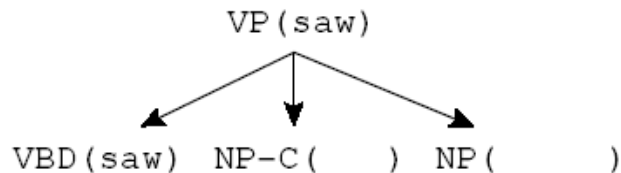
- **Main idea:** define a linguistically-motivated Markov process for generating children given the parent



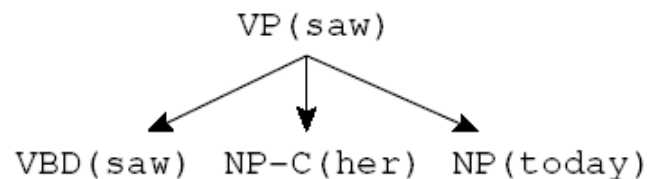
Step 1: Choose a head tag and word



Step 2: Choose a complement bag

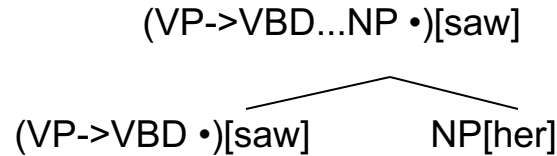


Step 3: Generate children (incl. adjuncts)



Step 4: Recursively derive children

# Lexicalized CKY



**bestScore**(i, j, **X**, **h**)

if (j = i+1)

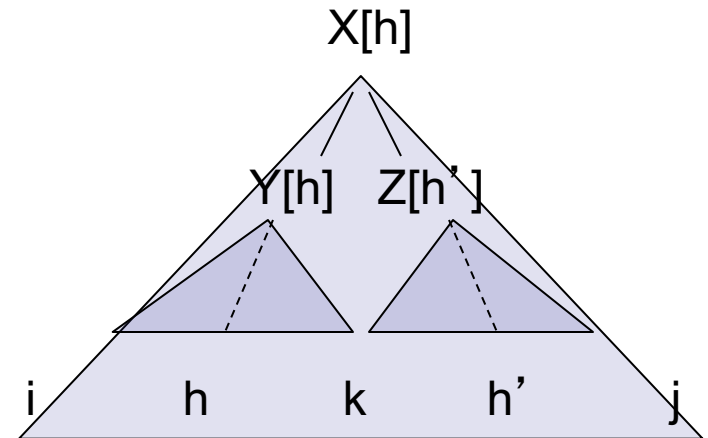
return **tagScore**(X, s[i])

else

return

```

max   max   score(X[h]->Y[h] Z[h']) *
k, h',    bestScore(i, k, Y, h) *
X->YZ     bestScore(k+1, j, Z, h')
           score(X[h]->Y[h'] Z[h]) *
           max
           k, h',    bestScore(i, k, Y, h') *
           X->YZ     bestScore(k+1, j, Z, h)
    
```

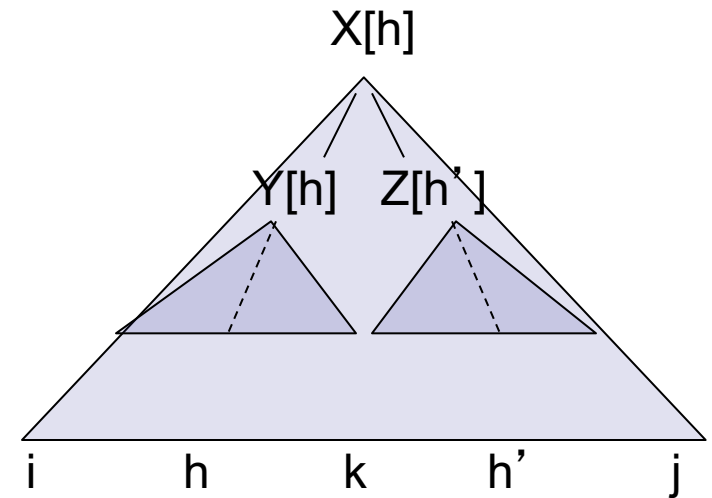


still cubic time?



# Pruning with Beams

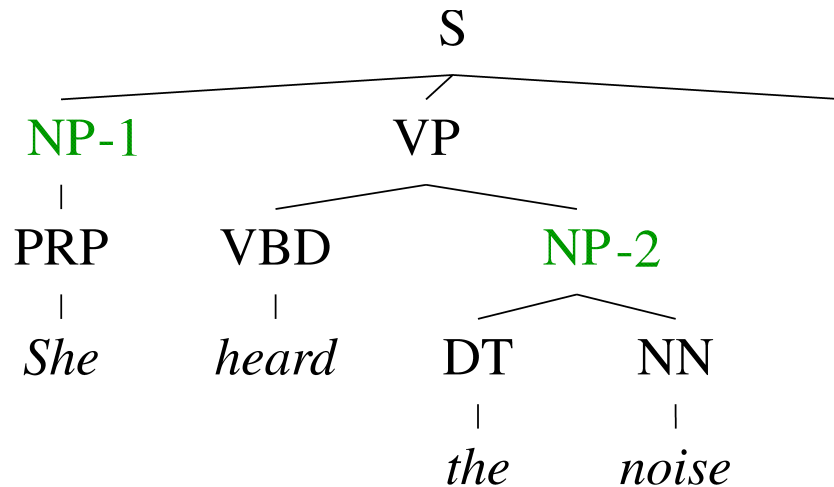
- The Collins parser prunes with per-cell beams [Collins 99]
  - Essentially, run the  $O(n^5)$  CKY
  - If we keep  $K$  hypotheses at each span, then we do at most  $O(nK^2)$  work per span (why?)
  - Keeps things more or less cubic
- Also: certain spans are forbidden entirely on the basis of punctuation (crucial for speed)



Model	F1
Naïve Treebank Grammar	72.6
Klein & Manning '03	86.3
Collins 99	88.6

# The Game of Designing a Grammar

---



- Annotation refines base treebank symbols to improve statistical fit of the grammar
- Parent annotation [Johnson '98]
- Head lexicalization [Collins '99, Charniak '00]
- Automatic Grammar Refinement?



# Manual Annotation

- Manually split categories

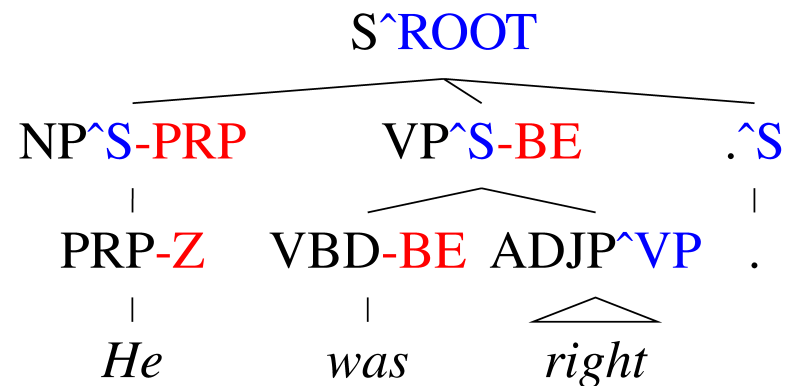
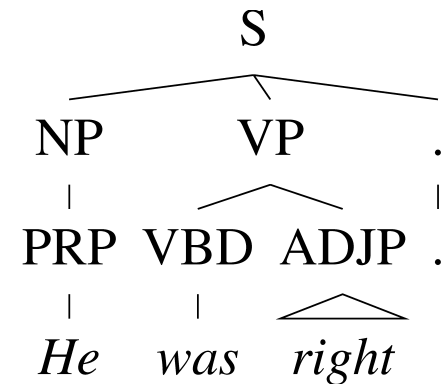
- NP: subject vs object
- DT: determiners vs demonstratives
- IN: sentential vs prepositional

- Advantages:

- Fairly compact grammar
- Linguistic motivations

- Disadvantages:

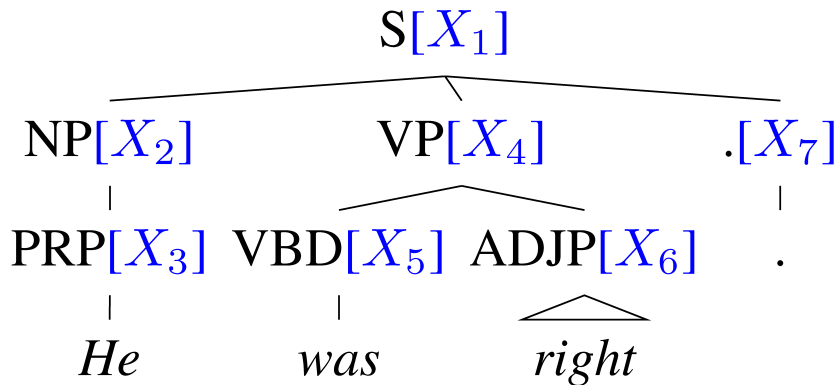
- Performance leveled out
- Manually annotated



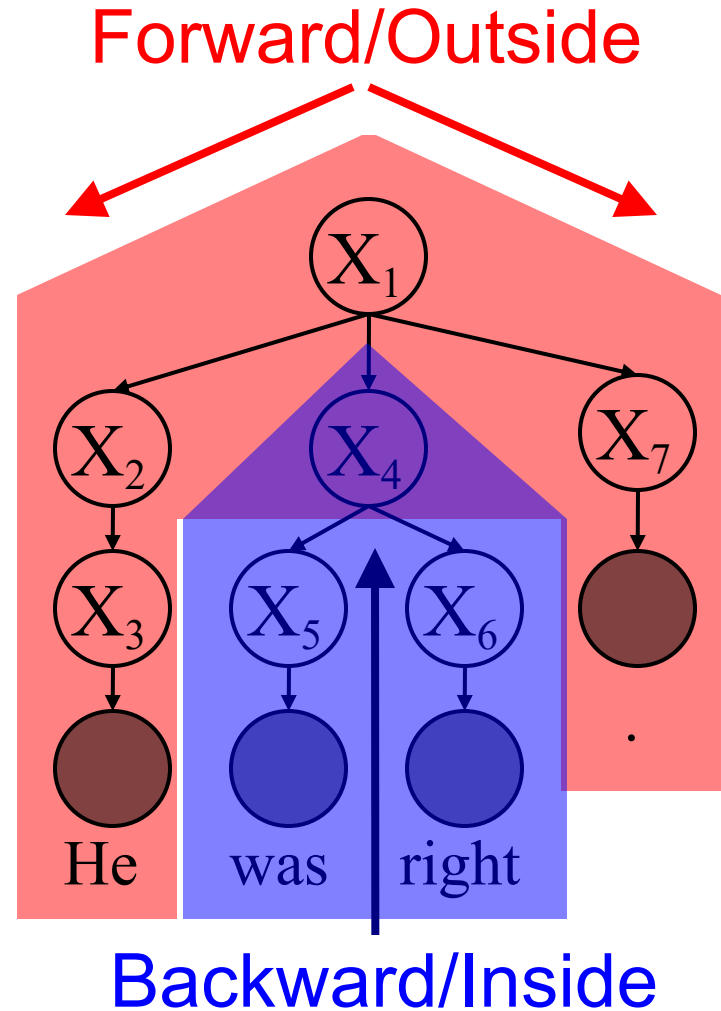
# Learning Latent Annotations

## Latent Annotations:

- Brackets are known
- Base categories are known
- Hidden variables for subcategories



Can learn with EM: like Forward-Backward for HMMs.

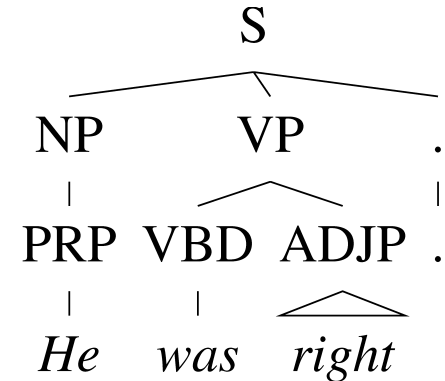


# Automatic Annotation Induction

- Advantages:

- Automatically learned:

- Label all nodes with latent variables.  
Same number  $k$  of subcategories  
for all categories.

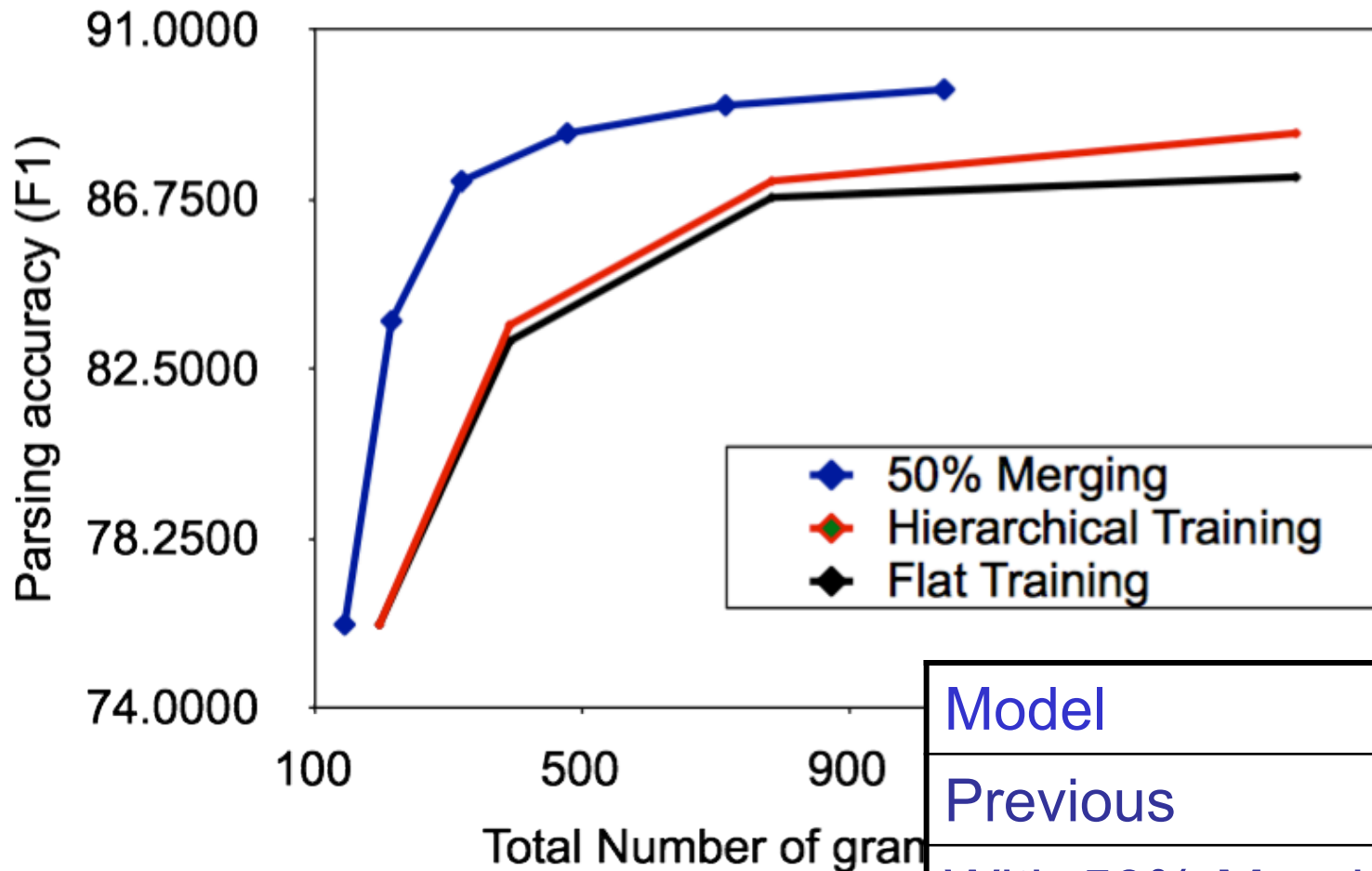


- Disadvantages:

- Grammar gets too large
  - Most categories are oversplit while others are undersplit.

Model	F1
Klein & Manning '03	86.3
Matsuzaki et al. '05	86.7

# Adaptive Splitting Results



Model	F1
Previous	88.4
With 50% Merging	89.5

# Final Results

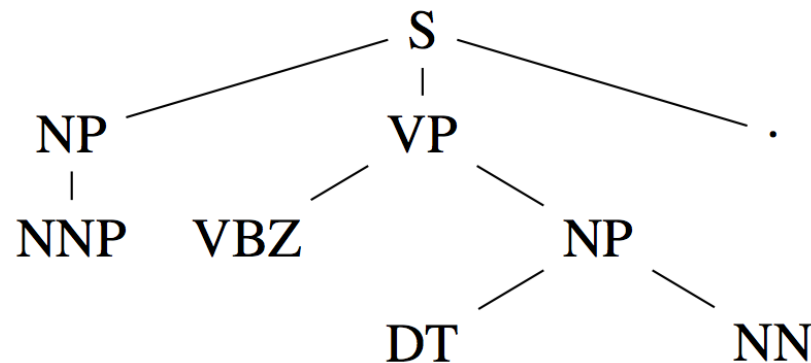
---

Parser	F1 $\leq 40$ words	F1 all words
Klein & Manning '03	86.3	85.7
Matsuzaki et al. '05	86.7	86.1
Collins '99	88.6	88.2
Charniak & Johnson '05	90.1	89.6
Petrov et. al. 06	90.2	89.7

# “Grammar as Foreign Language” (deep learning)

Vinyals et al., 2015

John has a dog →



John has a dog →

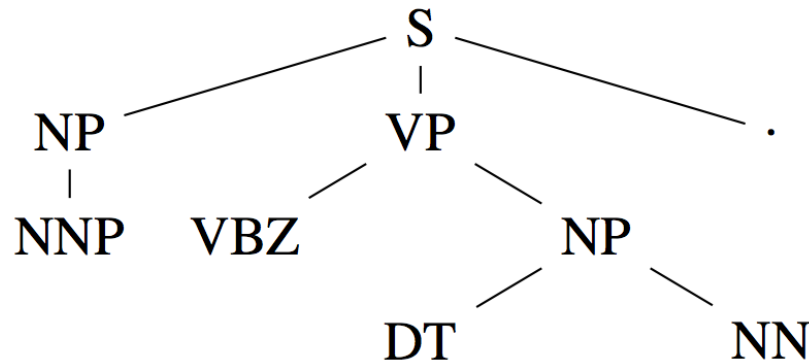
$(S (NP NNP)_{NP} (VP VBZ (NP DT NN)_{NP})_{VP} .)_{S}$

- Linearize a tree into a sequence
- Then parsing problem becomes similar to machine translation
  - Input: sequence
  - Output: sequence (of different length)
- Encoder-decoder LSTMs (Long short-term memory networks)

# “Grammar as Foreign Language” (deep learning)

Vinyals et al., 2015

John has a dog →



John has a dog →

$(S (NP NNP)_{NP} (VP VBZ (NP DT NN)_{NP})_{VP} .)_{S}$

- Penn treebank (~40K sentences) is too small to train LSTMs
- Create a larger training set with 11M sentences automatically parsed by two state-of-the-art parsers (and keep only those sentences for which two parsers agreed)

# “Grammar as Foreign Language” (deep learning)

Vinyals et al., 2015

Parser	Training Set	WSJ 22	WSJ 23
baseline LSTM+D	WSJ only	< 70	< 70
LSTM+A+D	WSJ only	88.7	88.3
LSTM+A+D ensemble	WSJ only	90.7	90.5
baseline LSTM	BerkeleyParser corpus	91.0	90.5
LSTM+A	high-confidence corpus	93.3	92.5
LSTM+A ensemble	high-confidence corpus	<b>93.5</b>	<b>92.8</b>
Petrov et al. (2006) [12]	WSJ only	91.1	90.4
Zhu et al. (2013) [13]	WSJ only	N/A	90.4
Petrov et al. (2010) ensemble [14]	WSJ only	92.5	91.8
Zhu et al. (2013) [13]	semi-supervised	N/A	91.3
Huang & Harper (2009) [15]	semi-supervised	N/A	91.3
McClosky et al. (2006) [16]	semi-supervised	92.4	92.1
Huang & Harper (2010) ensemble [17]	semi-supervised	92.8	92.4