

Name: \_\_\_\_\_

**CSE P505, Winter 2009, Final Examination**  
**19 March 2009**

Rules:

- The exam is closed-book, closed-note, except for one two-sided 8.5x11in piece of paper.
- **Please stop promptly at 8:20.**
- You can rip apart the pages.
- There are **100 points** total, distributed **unevenly** among **7** questions.
- The questions have multiple parts.

Advice:

- Read questions carefully. Understand a question before you start writing.
- Write down thoughts and intermediate steps so you can get partial credit.
- The questions are not necessarily in order of difficulty. **Skip around.** In particular, make sure you get to all the problems.
- If you have questions, ask.
- Relax. You are here to learn.

Name: \_\_\_\_\_

For your reference (page 1 of 2):

$$\begin{aligned}
 s & ::= \text{skip} \mid x := e \mid s ; s \mid \text{if } e \text{ s } s \mid \text{while } e \text{ s} \\
 e & ::= i \mid x \mid e + e \mid e * e \\
 (i & \in \{\dots, -2, -1, 0, 1, 2, \dots\}) \\
 (x & \in \{x_1, x_2, \dots, y_1, y_2, \dots, z_1, z_2, \dots, \dots\})
 \end{aligned}$$

$H ; e \Downarrow i$

$$\begin{array}{c}
 \text{CONST} \qquad \text{VAR} \qquad \text{ADD} \qquad \text{MULT} \\
 \frac{}{H ; c \Downarrow c} \quad \frac{}{H ; x \Downarrow H(x)} \quad \frac{H ; e_1 \Downarrow c_1 \quad H ; e_2 \Downarrow c_2}{H ; e_1 + e_2 \Downarrow c_1 + c_2} \quad \frac{H ; e_1 \Downarrow c_1 \quad H ; e_2 \Downarrow c_2}{H ; e_1 * e_2 \Downarrow c_1 * c_2}
 \end{array}$$

$H_1 ; s \Downarrow H_2$

$$\begin{array}{c}
 \text{SKIP} \qquad \text{ASSIGN} \qquad \text{SEQ} \\
 \frac{}{H ; \text{skip} \Downarrow H} \quad \frac{H ; e \Downarrow i}{H ; x := e \Downarrow H, x \mapsto i} \quad \frac{H_1 ; s_1 \Downarrow H_3 \quad H_3 ; s_2 \Downarrow H_2}{H_1 ; s_1 ; s_2 \Downarrow H_2} \\
 \text{IF1} \qquad \text{IF2} \qquad \text{WHILE} \\
 \frac{H_1 ; e \Downarrow i \quad i \neq 0 \quad H_1 ; s_1 \Downarrow H_2}{H_1 ; \text{if } e \text{ s } s_1 \text{ s } s_2 \Downarrow H_2} \quad \frac{H_1 ; e \Downarrow 0 \quad H_1 ; s_2 \Downarrow H_2}{H_1 ; \text{if } e \text{ s } s_1 \text{ s } s_2 \Downarrow H_2} \quad \frac{H_1 ; \text{if } e \text{ (s ; while } e \text{ s) skip} \Downarrow H_2}{H_1 ; \text{while } e \text{ s} \Downarrow H_2}
 \end{array}$$

$$\begin{aligned}
 e & ::= \lambda x. e \mid x \mid e e \mid c \mid (e, e) \mid e.1 \mid e.2 \mid \{l_1 = e_1, \dots, l_n = e_n\} \mid e.l_i \\
 & \quad \mid \text{letrec } f \text{ x. } e \mid \text{A}(e) \mid \text{B}(e) \mid (\text{match } e \text{ with } \text{A x. } e \mid \text{B x. } e) \\
 v & ::= \lambda x. e \mid \text{letrec } f \text{ x. } e \mid c \mid (v, v) \mid \{l_1 = v_1, \dots, l_n = v_n\} \mid \text{A}(v) \mid \text{B}(v) \\
 \tau & ::= \text{int} \mid \tau \rightarrow \tau \mid \tau * \tau \mid \{l_1 : \tau_1, \dots, l_n : \tau_n\} \mid \tau + \tau
 \end{aligned}$$

$e_1 \rightarrow e_2$

$$\begin{array}{c}
 \frac{}{(\lambda x. e) v \rightarrow e\{v/x\}} \quad \frac{e_1 \rightarrow e'_1}{e_1 e_2 \rightarrow e'_1 e_2} \quad \frac{e_2 \rightarrow e'_2}{v e_2 \rightarrow v e'_2} \quad \frac{e_1 \rightarrow e'_1}{(e_1, e_2) \rightarrow (e'_1, e_2)} \quad \frac{e_2 \rightarrow e'_2}{(v, e_2) \rightarrow (v, e'_2)} \\
 \frac{e \rightarrow e'}{e.1 \rightarrow e'.1} \quad \frac{e \rightarrow e'}{e.2 \rightarrow e'.2} \quad \frac{}{(v_1, v_2).1 \rightarrow v_1} \quad \frac{}{(v_1, v_2).2 \rightarrow v_2} \\
 \frac{}{(\text{letrec } f \text{ x. } e) v \rightarrow (e\{v/x\})\{\text{letrec } f \text{ x. } e/f\}} \quad \frac{}{\{l_1 = v_1, \dots, l_n = v_n\}.l_i \rightarrow v_i} \\
 \frac{e_i \rightarrow e'_i}{\{l_1 = v_1, \dots, l_{i-1} = v_{i-1}, l_i = e_i, \dots, l_n = e_n\} \rightarrow \{l_1 = v_1, \dots, l_{i-1} = v_{i-1}, l_i = e'_i, \dots, l_n = e_n\}} \\
 \frac{}{\text{match } \text{A}(v) \text{ with } \text{A x. } e_1 \mid \text{B y. } e_2 \rightarrow e_1\{v/x\}} \quad \frac{}{\text{match } \text{B}(v) \text{ with } \text{A x. } e_1 \mid \text{B y. } e_2 \rightarrow e_2\{v/y\}} \\
 \frac{e \rightarrow e'}{\text{A}(e) \rightarrow \text{A}(e')} \quad \frac{e \rightarrow e'}{\text{B}(e) \rightarrow \text{B}(e')} \quad \frac{e \rightarrow e'}{\text{match } e \text{ with } \text{A x. } e_1 \mid \text{B y. } e_2 \rightarrow \text{match } e' \text{ with } \text{A x. } e_1 \mid \text{B y. } e_2}
 \end{array}$$

$\boxed{\Gamma \vdash e : \tau}$

$$\begin{array}{c}
\frac{}{\Gamma \vdash c : \text{int}} \quad \frac{}{\Gamma \vdash x : \Gamma(x)} \quad \frac{\Gamma, x : \tau_1 \vdash e : \tau_2}{\Gamma \vdash \lambda x. e : \tau_1 \rightarrow \tau_2} \quad \frac{\Gamma \vdash e_1 : \tau_2 \rightarrow \tau_1 \quad \Gamma \vdash e_2 : \tau_2}{\Gamma \vdash e_1 e_2 : \tau_1} \\
\\
\frac{\Gamma \vdash e_1 : \tau_1 \quad \Gamma \vdash e_2 : \tau_2}{\Gamma \vdash (e_1, e_2) : \tau_1 * \tau_2} \quad \frac{\Gamma \vdash e : \tau_1 * \tau_2}{\Gamma \vdash e.1 : \tau_1} \quad \frac{\Gamma \vdash e : \tau_1 * \tau_2}{\Gamma \vdash e.2 : \tau_2} \quad \frac{\Gamma, f : \tau_1 \rightarrow \tau_2, x : \tau_1 \vdash e : \tau_2}{\Gamma \vdash \text{letrec } f x. e : \tau_1 \rightarrow \tau_2} \\
\\
\frac{\Gamma \vdash e_1 : \tau_1 \quad \dots \quad \Gamma \vdash e_n : \tau_n \quad \text{labels distinct}}{\Gamma \vdash \{l_1 = e_1, \dots, l_n = e_n\} : \{l_1 : \tau_1, \dots, l_n : \tau_n\}} \quad \frac{\Gamma \vdash e : \{l_1 : \tau_1, \dots, l_n : \tau_n\} \quad 1 \leq i \leq n}{\Gamma \vdash e.l_i : \tau_i} \\
\\
\frac{\Gamma \vdash e : \tau_1 + \tau_2 \quad \Gamma, x : \tau_1 \vdash e_1 : \tau \quad \Gamma, y : \tau_2 \vdash e_2 : \tau}{\Gamma \vdash \text{match } e \text{ with } \text{A}x. e_1 \mid \text{B}y. e_2 : \tau} \quad \frac{\Gamma \vdash e : \tau_1}{\Gamma \vdash \text{A}(e) : \tau_1 + \tau_2} \quad \frac{\Gamma \vdash e : \tau_2}{\Gamma \vdash \text{B}(e) : \tau_1 + \tau_2} \\
\\
\frac{\Gamma \vdash e : \tau \quad \tau \leq \tau'}{\Gamma \vdash e : \tau'}
\end{array}$$

$\boxed{\tau_1 \leq \tau_2}$

$$\begin{array}{c}
\frac{}{\{l_1 : \tau_1, \dots, l_n : \tau_n, l : \tau\} \leq \{l_1 : \tau_1, \dots, l_n : \tau_n\}} \\
\\
\frac{}{\{l_1 : \tau_1, \dots, l_{i-1} : \tau_{i-1}, l_i : \tau_i, \dots, l_n : \tau_n\} \leq \{l_1 : \tau_1, \dots, l_i : \tau_i, l_{i-1} : \tau_{i-1}, \dots, l_n : \tau_n\}} \\
\\
\frac{\tau_i \leq \tau'_i}{\{l_1 : \tau_1, \dots, l_i : \tau_i, \dots, l_n : \tau_n\} \leq \{l_1 : \tau_1, \dots, l_i : \tau'_i, \dots, l_n : \tau_n\}} \\
\\
\frac{\tau_3 \leq \tau_1 \quad \tau_2 \leq \tau_4}{\tau_1 \rightarrow \tau_2 \leq \tau_3 \rightarrow \tau_4} \quad \frac{}{\tau \leq \tau} \quad \frac{\tau_1 \leq \tau_2 \quad \tau_2 \leq \tau_3}{\tau_1 \leq \tau_3}
\end{array}$$

Module Thread:

```

type t
val create : ('a -> 'b) -> 'a -> t
val join : t -> unit

```

Module Mutex:

```

type t
val create : unit -> t
val lock : t -> unit
val unlock : t -> unit

```

Module Event:

```

type 'a channel
type 'a event
val new_channel : unit -> 'a channel
val send : 'a channel -> 'a -> unit event
val receive : 'a channel -> 'a event
val choose : 'a event list -> 'a event
val wrap : 'a event -> ('a -> 'b) -> 'b event
val sync : 'a event -> 'a

```

Name: \_\_\_\_\_

1. (Caml Programming and Type Inference) (17 points)

(a) Write a function `wgo_help1` such that this function:

```
let wgo1 max lst = wgo_help1 0 max lst
```

behaves as follows: If `lst` is a list of integers `[i1;i2;...;in]`, then `wgo1` returns the sum of a prefix of the list `i1 ... ij` such that:

- The sum is less than `max`.
- Either the sum of the next-larger prefix `i1 ... ij i` is not less than `max` or there is no next-larger prefix (i.e., the entire list has a sum less than `max`).

Do not define any other helper functions. Note `wgo` stands for, “without going over.”

(b) What is the type of `wgo_help1`?

(c) Write a function `wgo_help2` such that this function:

```
let wgo2 max lst = wgo_help2 (fun x -> x < max) (fun x y -> x+y) 0 lst
```

has the same observable behavior as `wgo1`. Do not define any other functions. `wgo_help2` should not contain an explicit addition.

(d) What is the type of `wgo_help2`?

(e) Rewrite `wgo1` and `wgo2` to be shorter.

Name: \_\_\_\_\_

2. (IMP and translation) (15 points)

Here is our Caml abstract syntax for IMP with one new kind of statement described below:

```
type exp = Int of int | Var of string | Plus of exp * exp | Times of exp * exp
type stmt = Skip | Assign of string * exp | Seq of stmt * stmt
           | If of exp * stmt * stmt | While of exp * stmt
           | CompareAndSwap of string * exp * exp
```

Recall that in the semantics the expression in an if-statement or while-statement is true if it is not zero.

In this problem, we consider a new kind of statement in IMP. The semantics of `CompareAndSwap(s, e1, e2)` is as follows:

- If evaluating `e1` under the current heap produces the same value that variable `s` holds under the current heap, then update the heap so `s` holds the value that `e2` evaluates to under the current heap.
- Otherwise make no change to the heap.

In Caml, write a *translation* from IMP-including-compare-and-swap statements to IMP-not-including-compare-and-swap statements. In other words, write a function `translate` of type `stmt -> stmt` such that (1) the result contains no compare-and-swap statements and (2) the result is equivalent to the argument.

Note: Some of you might recognize compare-and-swap as related to concurrency, but this problem has nothing to do with concurrency.

Name: \_\_\_\_\_

3. (Formal operational semantics) (18 points)

In this problem we define a small language that manipulates a stack of strings. You are given the syntax and the informal semantics.

The language syntax is a command list. A program state contains a command list and a stack of strings (the stack “grows to the right”):

$$\begin{array}{lll} \text{string } str & ::= & (\text{any string}) \\ \text{command } c & ::= & \text{push } str \mid \text{pop} \mid \text{dup} \mid \text{swap} \\ \text{command-list } lst & ::= & [] \mid c::lst \\ \text{stack } stk & ::= & \cdot \mid stk, str \end{array}$$

Informally, the commands behave as follows:

- **push**  $str$  makes a bigger stack with  $str$  on top.
- **pop** makes a smaller stack by removing the top element.
- **dup** (short for duplicate) makes a bigger stack by placing a copy of the top stack-element on top.
- **swap** swaps the order of the top two elements on the stack.

A command list executes the commands in order.

- (a) Give large-step inference rules for the judgment  $stk_1; lst \Downarrow stk_2$ , meaning, “running  $lst$  starting from  $stk_1$  produces  $stk_2$ .” One rule is given to you as an example. You need to write down 4 other rules.

$$\frac{stk_1, str; lst \Downarrow stk_2}{stk_1; (\text{push } str)::lst \Downarrow stk_2}$$

- (b) The semantics can *get stuck*, i.e., there exists stacks  $stk_1$  and command-lists  $lst$  such that we cannot derive  $stk_1; lst \Downarrow stk_2$  for any  $stk_2$ . In English, describe why there may be not be a derivation.
- (c) Give a complete derivation that concludes  $\cdot; (\text{push “pl”})::\text{dup}::\text{swap}::[] \Downarrow \cdot, \text{“pl”}, \text{“pl”}$

Name: \_\_\_\_\_

*This page is intentionally blank since you might (or might not) want more room to answer problem 3.*

Name: \_\_\_\_\_

4. (Formal typing rules) (15 points)

- (a) Recall this typing rule, one of the three rules we added for sums:

$$\frac{\Gamma \vdash e : \tau_1}{\Gamma \vdash A(e) : \tau_1 + \tau_2}$$

Explain this rule in English. In particular, what expressions can this typing rule be used for and what types can it give to such expressions?

- (b) Recall this typing rule for functions:

$$\frac{\Gamma, x : \tau_1 \vdash e : \tau_2}{\Gamma \vdash \lambda x. e : \tau_1 \rightarrow \tau_2}$$

Explain this rule in English. In particular, what expressions can this typing rule be used for and what types can it give to such expressions?

- (c) Suppose we changed the typing rule for functions to the following:

$$\frac{\Gamma, x : \tau_2 \vdash e : \tau_2}{\Gamma \vdash \lambda x. e : \tau_2 \rightarrow \tau_2}$$

Explain why this change would not violate type safety. Explain why it is a bad idea anyway.



Name: \_\_\_\_\_

5. (Soundness/Completeness) (10 points)

Suppose you design a new type system for Java to prevent null-pointer dereferences. However, due to poor design, your type system has the strange property that there are exactly 47 programs that your type system accepts; it rejects all others.

**Explain your answers *briefly*.**

- (a) Is it possible that your type system is sound with respect to null-pointer dereferences?
- (b) Is it possible that your type system is complete with respect to null-pointer dereferences?
- (c) Is it definitely the case given just the information above that your type system is sound with respect to null-pointer dereferences?
- (d) Is it definitely the case given just the information above that your type system is complete with respect to null-pointer dereferences?

Name: \_\_\_\_\_

6. (Concurrent ML) (13 points)

In this problem you will use Concurrent ML to write a “server version” of `wgo` from problem 1. You will implement this interface:

```
type wgo_adder
val new_wgo_adder : int -> wgo_adder
val add : wgo_adder -> int -> int
```

The argument to `new_wgo_adder` is the new adder’s “max.” Initially an adder has “not reached its max.” While an adder has “not reached its max” each call to `add` returns the sum of all integers ever passed to `add` with this particular adder. However, if the argument to `add` plus the sum of all previous integers exceeds “max” then the “max is reached” and `add` should return the sum of all *previous* calls. After the “max is reached” all future calls to `add` with this adder return this same sum no matter what.

You must use Concurrent ML to support multiple threads calling `add`; do not use other synchronization mechanisms such as locks.

Hints: You do not need `choose` and `wrap`. The code you wrote in problem 1 is *not* particularly helpful.

Name: \_\_\_\_\_

7. (OOP overloading and casting) (12 points)

Consider a typical class-based OOP language like we did in class. Suppose somewhere in a program that type-checks we have `e.m(D)(new C())` where `C` is a subclass/subtype of `D`. Notice the argument in the method call is an explicit upcast. Consider modifying the program by removing this explicit upcast, i.e., replacing the call with `e.m(new C())`.

**Explain your answers *briefly*.**

- (a) If every class in the program has at most one method named `m`, can this change cause the program not to type-check?
- (b) If every class in the program has at most one method named `m`, can this change cause the program to produce a different result?
- (c) If classes can have multiple methods named `m` and method calls are resolved with static overloading, can this change cause the program to produce a different result?
- (d) If classes can have multiple methods named `m` and method calls are resolved with multimethods, can this change cause the program to produce a different result?