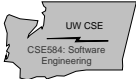


**CSE584: Software Engineering**  
Lecture 8 (May 27, 1997)

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**Lecture 8, Outline** [approximate minutes]

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- ◆ Approaches for quality assurance [15]
- ◆ Proofs of correctness [30]
- ◆ Reviews, inspections, etc. [30]
- ◆ Break [10]
- ◆ Statistically-based approaches [45]
- ◆ Wrap-up [10]
  
- ◆ Next week
  - PSP, CMM, ISO 9000
  - Testing
  - What's hot in software engineering research




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**Approaches to quality assurance**

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- ◆ Testing
- ◆ Proofs of correctness
- ◆ Process improvement
  - CMM, ISO 9000, reviews, inspections, ...
- ◆ Statistical measures
  - Reliability, Cleanroom, etc.
- ◆ Software safety (fault tree analysis, etc.)
- ◆ Others?




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**Proofs of program correctness**

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- ◆ Given a precise specification and an implementation, show that the implementation satisfies the specification
  - Distinct from proving properties about specifications
- ◆ Caveats
  - Not generally practical
  - Can provide some useful insights for programming




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**Pre- and post-conditions**

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- ◆ Pre-condition
  - Predicate describing state before a program executes
- ◆ Post-condition
  - Predicate describing state after a program executes




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**Hoare triples**

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- ◆  $\{P\} S \{Q\}$ 
  - A predicate that is true if and only if
    - » when pre-condition  $P$  is true
    - » and then  $S$  is executed
    - » then post-condition  $Q$  will be true
- ◆ Strong correctness requires  $S$  to terminate for  $\{P\} S \{Q\}$  to be true
- ◆ Weak correctness does not



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### Example


- ◆  $\{ x = X \wedge y = Y \}$   
 $t := x; x := y; y := t$   
 $\{ x = Y \wedge y = X \}$
- ◆ Compute intermediate assertions
  - $\{ x = X \wedge y = Y \}$
  - $t := x;$
  - $\{ x = X \wedge y = Y \wedge t = X \}$
  - $x := y;$
  - $\{ x = Y \wedge y = Y \wedge t = X \}$
  - $y := t;$
  - $\{ x = Y \wedge y = X \wedge t = X \}$
- ◆  $\{ x = Y \wedge y = X \wedge t = X \} \Rightarrow \{ x = Y \wedge y = X \}$



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### Semantics of statements


- ◆ In the example, I appealed to your intuition about what  $:=$  does
- ◆ But a more precise definition is needed
- ◆ This is often done using weakest preconditions (wp's) [Dijkstra]
  - $wp(S,Q)$  is the weakest condition that must be true beforehand so that  $S$  terminates in a state such that  $Q$  is true
- ◆ When  $S$  is a language construct, wp defines its semantics



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### Assignment wp


- ◆  $wp(x := E, Q(x)) = Q(E)$ 
  - For a condition  $Q(X)$  to be true after execution of  $x := E$ , the condition  $Q(E)$  must hold beforehand
- ◆  $wp(j := j+1, j \leq 1) = (j \leq 0)$
- ◆ What about side effects?



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### Hoare triples and wp's


- ◆ A nice relationship holds between Hoare triples and wp's
- ◆ To prove  $\{P\}S\{Q\}$ 
  - First compute  $wp(S,Q)$
  - And then prove  $P \Rightarrow wp(S,Q)$
- ◆ In essence, this computes backwards from the desired post-condition, through each statement, to the original pre-condition



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### Sequencing wp


- ◆  $wp((S1;S2), Q) = wp(S1, wp(S2, Q))$
- ◆  $wp(j := j+2; k := k-2, j+k=1) =$   
 $wp(j := j+2, wp(k := k-2, j+k=1)) =$   
 $wp(j := j+2, j+k-2=1) =$   
 $(j+2+k-2=1) =$   
 $j+k=1$



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### Example

- ◆  $wp(t := x; x := y; y := t, x=X \wedge y=Y)$
- ◆  $wp(t := x; x := y, wp(y := t, x=X \wedge y=Y))$
- ◆  $wp(t := x; x := y, x=X \wedge t=Y)$
- ◆  $wp(t := x, wp(x := y, x=X \wedge t=Y))$
- ◆  $wp(t := x, y=X \wedge t=Y)$
- ◆  $y=X \wedge x=Y$



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## Conditional wp's

- ◆  $wp(\text{if } C \text{ then } S1 \text{ else } S2, Q)$ 
  - Have to cover both parts of the conditional
- ◆  $(C \Rightarrow wp(S1, Q)) \wedge (\neg C \Rightarrow wp(S2, Q))$



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13

## Example

- ◆  $\{x \neq 0\}$   
 $\text{if } x < 0 \text{ then } x := -x \text{ else } x := x-1$   
 $\{x \geq 0\}$



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14

## Loops

- ◆ Weakest pre-conditions on loops are problematic since they need not terminate
- ◆ So instead we approximate the wp of a loop with a loop invariant
- ◆ A loop invariant differs from a weakest pre-condition
  - Does not imply termination
  - May be stronger than is strictly necessary



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15

## Loop invariants

- ◆ What role must the loop invariant  $I$  of  $\text{while } B \text{ do } S$  play to ensure post-condition  $Q$  holds afterwards?
- ◆ We need
  - $\{B \wedge I\} S \{I\}$
  - $\sim B \wedge I \Rightarrow Q$
- ◆ That is, the loop maintains the invariant and on termination, the post-condition holds



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16

## Example

- ◆  $\{T\}$   
 $j := 1; s := b[0];$   
 $\text{while } j < 11 \text{ do}$   
 $\quad j := j+1; s := b[j]$   
 $\text{od}$   
 $\{s = \sum_{k=0..10} b[k]\}$
- ◆ What's an appropriate loop invariant?



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17

## Termination

- ◆ Loop invariants don't address termination
- ◆ If termination is material, a separate proof is used
- ◆ These proofs generally use well-founded sets
  - Essentially, one finds a value that is monotonically increasing (decreasing) towards a fixed bound
  - In the last example,  $j$  monotonically approaches 11




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18

### Miscellaneous

- ◆ Recursion
- ◆ Side effects
- ◆ Procedures and functions
  - Parameter passing mechanisms
- ◆ Abstract data types




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### Correctness of ADTs [Hoare]

- ◆ Need to define pre- and post-conditions on both the abstract state and also the concrete state
- ◆ Relate these through a (many to one) representation function [Liskov & Gutttag]


The diagram illustrates a many-to-one mapping between abstract and concrete states. The abstract state is represented by a jagged-edged box containing the value  $[1,2]$ . The concrete state is represented by a similar jagged-edged box containing the value  $[2,1]$ . A vertical arrow labeled  $[r]$  points from the abstract state to the concrete state, representing the representation function. A horizontal arrow labeled  $[1,2]$  points from the concrete state back to the abstract state, representing the inverse mapping.



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### Reviews, etc.


- ◆ Reviews, walkthroughs, and inspections are all in a family of activities where an artifact (specification, code, etc.) is studied by a peer group to improve the artifact's quality
- ◆ There is a large and increasing literature that demonstrates the effectiveness (although not always the cost-effectiveness) of these approaches



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### Reviews, etc.


- ◆ N-heads are better than one
- ◆ Intended to
  - identify defects
  - identify needed improvements
  - encourage uniformity and conformance to standards
  - enforce subjective rules



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### Purposes


- ◆ Increase quality through peer review
- ◆ Provide management visibility
- ◆ Encourage preparation
- ◆ Explicit non-purpose
  - Assessment of individual abilities for promotion, pay increases, ranking, etc.
  - Management usually not permitted at reviews



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### Walkthrough

- ◆ A formal activity
- ◆ A programmer (designer) presents a program (design)
- ◆ Values of sample data are traced
- ◆ Peers evaluate technical aspects of the design



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## Inspections [Sommerville]

- ◆ Formal approach to code review
- ◆ Intended explicitly for defect *detection* (not correction)
- ◆ Defects include logical errors, anomalies in the code (such as uninitialized variables), non-compliance with standards, etc.



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25

## Inspection requirements

- ◆ A precise specification must be available
- ◆ Peers must be knowledgeable about organizational standards
- ◆ Code should be syntactically correct and basic tests passed
- ◆ Error checklist must be provided



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26

## Inspection process

- ◆ Plan
- ◆ Overview
- ◆ Individual preparation
  - Code, documentation distributed in advance
- ◆ Meeting
- ◆ Rework
- ◆ Follow-up



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27

## Inspection teams

- ◆ Four or more members
- ◆ Author of code
- ◆ Reader of code (reads to team)
- ◆ Inspector of code
- ◆ Moderator chairs meeting, takes notes, etc.



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28

## Inspection checklists

- ◆ Checklist of common errors drives inspection
- ◆ Checklist dependent on programming language
  - Weaker type systems usually imply longer checklists
- ◆ Examples
  - Initialization, loop termination, array bounds, ...



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29

## Inspection rate

- ◆ 500 statements/hour during overview
- ◆ 125 statements/hour during individual prep
- ◆ 90-125 statements/hour during review
- ◆ Inspecting 500 statements can take 40 person-hours
  - For 1MLOC, this would be about 40 person-years of effort



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30

## Issues in inspections

- ◆ Can groupware technology significantly improve inspections?
- ◆ Can you have inspections without meetings?
  - Since meetings are expensive to hold and schedule
  - Since the preparation may catch more defects than the meetings
- ◆ See Adam Porter's talk on Thursday



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31

## Statistical approaches

- ◆ There are a number of approaches to quality assurance that are (in varying senses) based on statistics
  - Software reliability
  - N-version programming
  - Cleanroom



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32

## Software reliability [RST]

- ◆ The probability that software will provide failure-free operation in a fixed environment for a fixed interval of time
  - A system might have reliability 0.96 when used for a one week period by an expert user
- ◆ Mean-time-to-failure is the average interval of time between failures
- ◆ One common use of software reliability models is to decide when it's OK to ship a product



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33

## Operational profiles

- ◆ An accurate operational profile is needed
  - Frequency of application of specific operations for the program being studied
- ◆ An operational profile is the probability density function (over the entire input space) that best represents how the inputs would be selected during the life-time of the software



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34

## Understood domains

- ◆ In industries such as telecommunications, operational profiles can be fairly easily gathered
- ◆ The phone company has records of virtually every call made in the last 20 years
  - Phones are used in pretty consistent ways



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## Less understood domains

- ◆ But for shrink-wrapped software products, operational profiles are harder to divine
- ◆ How will different users using different products with different features behave?
  - CPA's vs. college students using a spreadsheet?
- ◆ Will usage change over time?
  - More or less than the phone system?



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36

## Cost

- ◆ To assess reliabilities past the 3rd or 4th decimal place can require an enormous amount of testing
- ◆ Should all failures be considered equally bad?
  - Showstoppers vs. “wrong color”
- ◆ Oracles of “correctness” aren’t always easy
- ◆ Monitoring phone switches is relatively easy; monitoring shrinkwrap isn’t



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37

## Applying reliability models

- ◆ There is extensive real use of models in this style
- ◆ There is also a lot of theoretical work that is never validated
  - Variants on models never compared to reality
- ◆ There are courses, books, etc. about how to apply reliability modeling in practice



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38

## N-version programming

- ◆ The idea of N-version (multi-version) programming comes from a common hardware reliability approach--replication
- ◆ The basic notion is simple
  - Have N independent teams write N versions of a program
  - Run them all simultaneously and have them vote at specified points



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39

## Objective

- ◆ Since the programs are built independently, the objective is to improve the quality by a multiplicative factor
  - A bug only hurts if it also appears in another  $(N/2)+1$  versions
- ◆ This idea indeed works pretty well in hardware
- ◆ The cost issue in software is different, though
  - Not a matter of producing multiple chips, but of producing multiple implementations



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40

## Assumption

- ◆ But there is an underlying assumption at work
  - The implementations will fail independently
    - » Like the chips in hardware that fail based on physical structures
  - Otherwise, a multiplicative factor will not be gained
- ◆ Do independently built implementations of the same specification fail independently?



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41

## Probably not

- ◆ Knight and Leveson did some experiments that showed that this assumption is probably false
  - In particular, they showed that similar errors often arise in independently implemented versions of the same specifications
- ◆ An additive benefit may arise from N-version programming, but not a multiplicative one



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42

## Why?

- ◆ Errors are often in the specification
- ◆ Errors are often made at boundary conditions
- ◆ The complexity of a program is often in a small piece or two, which each group has trouble with
- ◆ The background and training of people in an organization are often similar



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43

## And now...

- ◆ N-version advocates are still out there in an aggressive way
  - I believe some organizations still require contracted software to be built this way
- ◆ There are some experiments showing independence
- ◆ There are attempts to introduce variety explicitly
  - Different specs, different languages, etc.
- ◆ I'm still completely opposed to this approach based on the Knight/Leveson experiments



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44

## Cleanroom [Harlan Mills]

- ◆ Cleanroom combines managerial and technical activities into a process intended to lead to very high quality software
  - Combines formal methods with statistical testing for reliability with incremental development
  - Does *not* allow unit execution or testing
- ◆ Effectiveness is a controversial issue



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45

## Basics: five points

- ◆ Formal specification
  - “Required system behavior and architecture”
  - Black box stimulus-response specification
- ◆ Incremental development
  - Partitioned into “user-function increments” that “accumulate into the final product”
- ◆ Structured programming
  - Limited use of control and data abstraction constructs; stepwise refinement of specification



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46

## Basics: five points (con't)

- ◆ Static verification
  - Components statically verified using mathematic correctness arguments
  - Individual components *neither* executed *nor* tested
    - » No white box testing, no black box testing, no coverage analysis
- ◆ Statistical testing
  - Each increment is tested statistically based on operational profile



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47

## Three teams

- ◆ Specification team
- ◆ Development team
  - Codes
  - Statically verifies using inspections
- ◆ Certification team
  - Develops and applies statistical tests
  - Reliability models used to decide when to ship



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48



## Claims

- ◆ Very aggressive positive claims
  - About 20-30 systems (all under 500KLOC)
- ◆ 100KLOC systems with (well) under 10 errors in the field in the first year or two
- ◆ Finds 1-4 errors/KLOC during statistical testing
- ◆ Some projects claim 70% improvement in development productivity



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49

## Counterclaims [Beizer]

- ◆ Several (related) questions raised
  - Are comparisons to other methods fair?
  - Why eliminate unit testing?
  - Why trust software reliability modeling so much?
    - » Especially hard to get good operational models
- ◆ Claim is that unless Cleanroom embraces modern testing approaches, it will fail to be used broadly



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50