CSE P 501 – Compilers

Parsing & Context-Free Grammars Hal Perkins Autumn 2023

Administrivia (1)

- Written HW2 out now, due 11pm
 - Gradescope turnin will be added in a day or two
- HW1 solution available today during break
 - (If you haven't handed in hw1 yet, seal your copy in an opaque envelope & don't look until you've upload it)
- Exam reminder so we're sure it's on everyone's calendar: scheduled for 6:30-8:00 pm, Thursday, Nov. 30. We'll plan for 90 min., but if the exam misfires and is too long, let's keep the option to run late until maybe 8:20 or 8:30 to avoid time pressure.

Administrivia (2)

 Project partner signup: please find a partner and fill out the signup form by noon tomorrow if not done yet (one form per group please)

- Who's still looking for a partner? Mingle during break?

- First part of project scanner posted now, due a week from Thursday
 - Gitlab repos will be created sometime later tomorrow watch for gitlab email and ed posting when ready
 - Programming is fairly simple; this is the infrastructure shakedown cruise + read language/project info carefully
 - Short demo after break tonight

Agenda for Today

- Parsing overview
- Context free grammars
- Ambiguous grammars
- Reading: Cooper & Torczon 3.1-3.2
 - Dragon book is also particularly strong on grammars and languages

Syntactic Analysis / Parsing

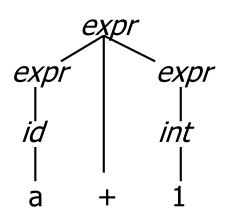
- Goal: Convert token stream to an abstract syntax tree
- Abstract syntax tree (AST):
 - Captures the structural features of the program
 - Primary data structure for next phases of compilation
- Plan
 - Study how context-free grammars specify syntax
 - Study algorithms for parsing and building ASTs

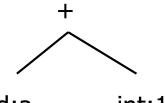
Concrete vs Abstract Syntax

- The full parse tree includes all of the derivation details. The Abstract Syntax Tree (AST) omits information that is necessary to parse the input, but not needed for later processing
- Example:

Concrete Syntax

Abstract Syntax





id:a int:1

Context-free Grammars

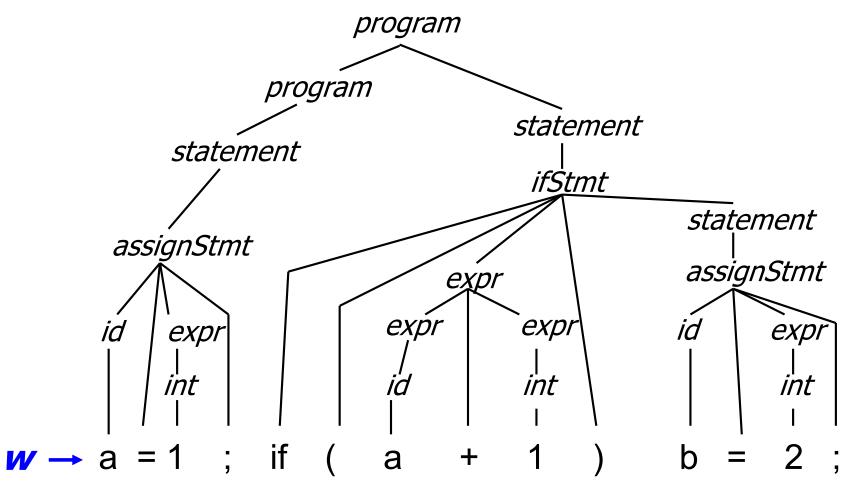
- The syntax of most programming languages can be specified by a context-free grammar (CGF)
- Compromise between
 - REs: can't nest or specify recursive structure
 - General grammars: too powerful, undecidable
- Context-free grammars are a sweet spot
 - Powerful enough to describe nesting, recursion
 - Easy to parse; restrictions on general CFGs improve speed
- Not perfect
 - Cannot capture semantics, like "must declare every variable" or "must be int" – requires later semantic pass
 - Can be ambiguous

Derivations and Parse Trees

- Derivation: a sequence of expansion steps, beginning with a start symbol and leading to a sequence of terminals
- Parsing: inverse of derivation
 - Given a sequence of terminals (aka tokens)
 recover (discover) the nonterminals and structure,
 i.e., the parse (concrete syntax) tree

Old Example

program ::= statement | program statement
 statement ::= assignStmt | ifStmt
 assignStmt ::= id = expr ;
 ifStmt ::= if (expr) statement
 expr ::= id | int | expr + expr
 id ::= a | b | c | i | j | k | n | x | y | z
 int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9



Parsing

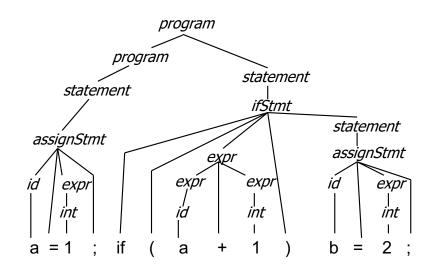
- Parsing: Given a grammar G and a sentence w in L(G), traverse the derivation (parse tree) for w in some standard order and do something useful at each node
 - The tree might not be produced explicitly, but the control flow of the parser will correspond to a traversal

"Standard Order"

- For practical reasons we want the parser to be deterministic (no backtracking), and we want to examine the source program from left to right.
 - (i.e., parse the program in linear time in the order it appears in the source file)

Common Orderings

- Top-down
 - Start with the root



- Traverse the parse tree depth-first, left-to-right (leftmost derivation)
- LL(k), recursive-descent
- Bottom-up
 - Start at leaves and build up to the root
 - Effectively a rightmost derivation in reverse(!)
 - LR(k) and subsets (LALR(k), SLR(k), etc.)

"Something Useful"

- At each point (node) in the traversal, perform some semantic action
 - Construct nodes of full parse tree (rare)
 - Construct abstract syntax tree (AST) (common)
 - Construct linear, lower-level representation (often produced in later phases of production compilers by traversing initial AST)
 - Generate target code on the fly (done in 1-pass compilers; not common in production compilers)
 - Can't generate great code in one pass, but useful if you need a quick 'n dirty working compiler

Context-Free Grammars

- Formally, a grammar G is a tuple <N,Σ,P,S> where
 - N is a finite set of non-terminal symbols
 - $-\Sigma$ is a finite set of *terminal* symbols (alphabet)
 - P is a finite set of productions
 - A subset of $N \times (N \cup \Sigma)^*$
 - S is the start symbol, a distinguished element of N
 - If not specified otherwise, this is usually assumed to be the non-terminal on the left of the first production

Standard Notations

- a, b, c elements of Σ
- w, x, y, z elements of Σ^*
- A, B, C elements of N
- X, Y, Z elements of $N \cup \Sigma$
- α, β, γ elements of (NUS)*
- $A \rightarrow \alpha \text{ or } A ::= \alpha \text{ if } <A, \alpha > \in P$

Derivation Relations (1)

- $\alpha \land \gamma \Rightarrow \alpha \beta \gamma$ iff $A ::= \beta$ in *P* - derives
- A =>* α if there is a chain of productions starting with A that generates α
 - transitive closure

Derivation Relations (2)

- w A $\gamma =>_{Im} w \beta \gamma$ iff A ::= β in P – derives leftmost
- $\alpha A w = \sum_{rm} \alpha \beta w$ iff $A ::= \beta in P$ - derives rightmost
- We will only be interested in leftmost and rightmost derivations – not random orderings

Languages

- For A in *N*, *L*(A) = { w | A =>* w }
- If S is the start symbol of grammar G, define
 L(G) = L(S)
 - Nonterminal on left of first rule is taken to be the start symbol if one is not specified explicitly

Reduced Grammars

• Grammar G is *reduced* iff for every production A ::= α in G there is a derivation

 $S =>* x A z => x \alpha z =>* xyz$

- i.e., no production is useless

- Convention: we will use only reduced grammars
 - There are algorithms for pruning useless productions from grammars – see a formal language or compiler book for details

Ambiguity

- Grammar G is *unambiguous* iff every w in L(G) has a unique leftmost (or rightmost) derivation
 - Fact: unique leftmost or unique rightmost implies the other
- A grammar without this property is *ambiguous*
 - But other grammars that generate the same language may be unambiguous – ambiguity is a property of grammars, not languages
- We need unambiguous grammars for parsing

Example: Ambiguous Grammar for Arithmetic Expressions

expr ::= expr + expr | expr - expr | expr * expr | expr / expr | int int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

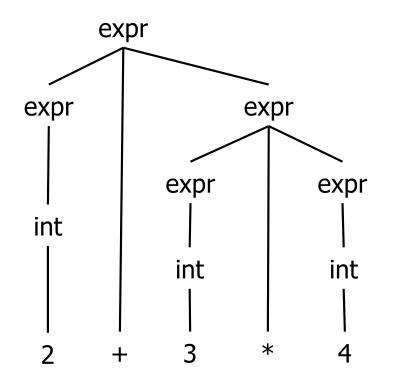
- Exercise: show that this is ambiguous
 - How? Show two different leftmost or rightmost derivations for the same string
 - Equivalently: show two different parse trees for the same string

expr ::= expr + expr | expr - expr | expr * expr | expr / expr | int int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

 Give a leftmost derivation of 2+3*4 and show the parse tree

expr ::= expr + expr | expr - expr | expr * expr | expr / expr | int int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

 Give a leftmost derivation of 2+3*4 and show the parse tree

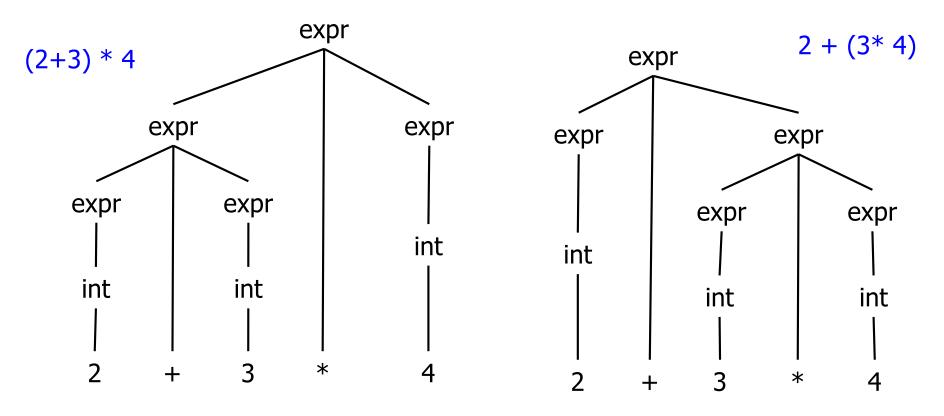


expr ::= expr + expr | expr - expr | expr * expr | expr / expr | int int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

 Give a different leftmost derivation of 2+3*4 and show the parse tree

expr ::= expr + expr | expr - expr | expr * expr | expr / expr | int int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

 Give a different leftmost derivation of 2+3*4 and show the parse tree



Another example

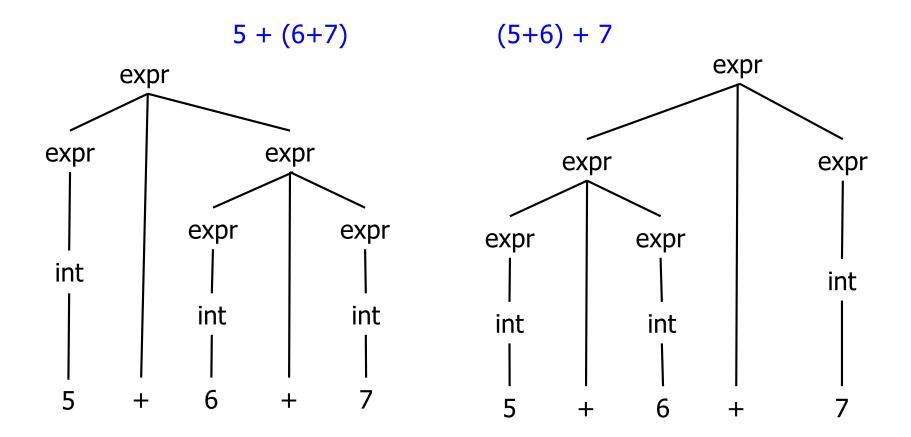
expr ::= expr + expr | expr - expr | expr * expr | expr / expr | int int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

• Give two different derivations of 5+6+7

Another example

expr ::= expr + expr | expr - expr | expr * expr | expr / expr | int int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

• Give two different derivations of 5+6+7



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What's going on here?

- The grammar has no notion of precedence or associatively
- Traditional solution
 - Create a non-terminal for each level of precedence
 - Isolate the corresponding part of the grammar
 - Force the parser to recognize higher precedence subexpressions first
 - Use left- or right-recursion for left- or right-associative operators

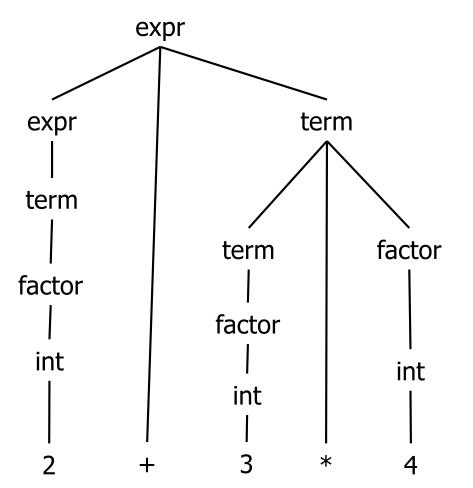
Classic Expression Grammar (first used in ALGOL 60)

expr ::= expr + term | expr - term | term term ::= term * factor | term / factor | factor factor ::= int | (expr) int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7

Check: Derive 2 + 3 * 4

expr ::= expr + term | expr - term | term term ::= term * factor | term / factor | factor factor ::= int | (expr) int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7

Check: Derive 2 + 3 * 4



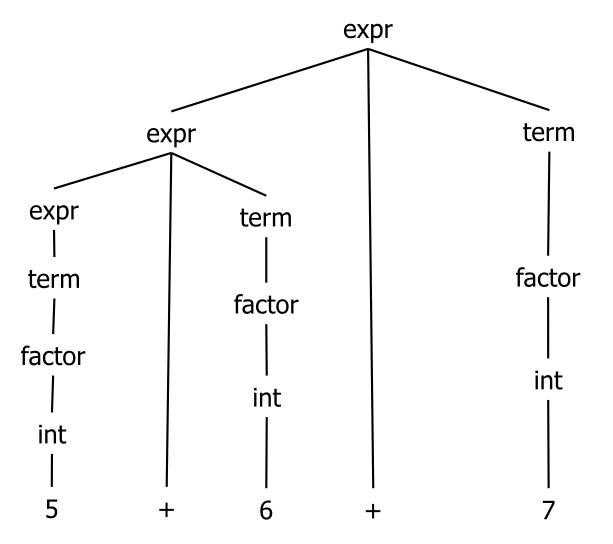
expr ::= expr + term | expr - term | term term ::= term * factor | term / factor | factor factor ::= int | (expr) int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7

> Separation of nonterminals enforces precedence

Check: Derive 5 + 6 + 7

expr ::= expr + term | expr - term | term
term ::= term * factor | term / factor | factor
factor ::= int | (expr)
int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7

Check: Derive 5 + 6 + 7



expr ::= expr + term | expr - term | term term ::= term * factor | term / factor | factor factor ::= int | (expr) int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7

> Note interaction between left- vs right-recursive rules and resulting associativity

Check: Derive 5 + (6 + 7)

expr ::= expr + term | expr - term | term term ::= term * factor | term / factor | factor factor ::= int | (expr) int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7

(left as an exercise ⁽ⁱ⁾)

Another Classic Example

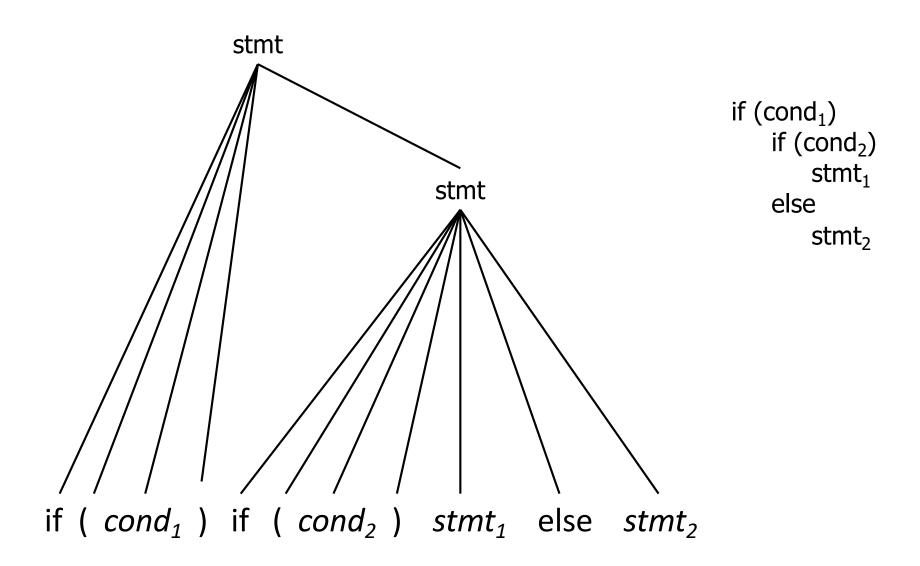
Grammar for conditional statements
 <prstate statements</p>
 <prstate statements</p>

 if (expr) state else state

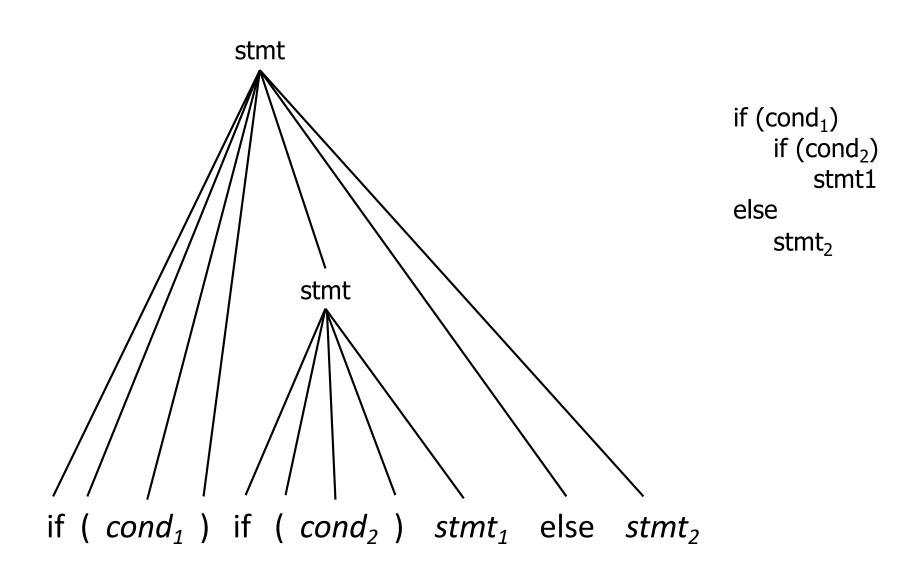
(This is the "dangling else" problem found in many, many grammars for languages, beginning with Algol 60)

- Exercise: show that this is ambiguous
 - How?

One Derivation



stmt ::= if (*cond*) *stmt* | if (*cond*) *stmt* else *stmt*



Solving "if" Ambiguity

- Fix the grammar to separate if statements with else clause and if statements with no else
 - Done in Java reference grammar
 - Adds lots of non-terminals
- or, Change the language
 - But it'd better be ok to with the language's community to do this
- or, Use some ad-hoc rule in the parser
 - "else matches closest unpaired if"

Resolving Ambiguity with Grammar (1)

```
Stmt ::= MatchedStmt | UnmatchedStmt
MatchedStmt ::= ... |
    if ( Expr ) MatchedStmt else MatchedStmt
UnmatchedStmt ::= ... |
    if ( Expr ) Stmt |
    if ( Expr ) MatchedStmt else UnmatchedStmt
```

- formal, no additional rules beyond syntax
- can be more obscure than original grammar

Check

Stmt ::= MatchedStmt | UnmatchedStmt
MatchedStmt ::= ... |
 if (Expr) MatchedStmt else MatchedStmt
UnmatchedStmt ::= if (Expr) Stmt |
 if (Expr) MatchedStmt else UnmatchedStmt

(exercise 🙂)

if (cond) if (cond) stmt else stmt

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Resolving Ambiguity with Grammar (2)

If you can (re-)design the language, just avoid the problem entirely

Stmt ::= ... | **if** Expr **then** Stmt **end** | **if** Expr **then** Stmt **else** Stmt **end**

- formal, clear, elegant
- allows sequence of Stmts in then and else branches, no { } needed
- extra end required for every if
 (But maybe this is a good idea anyway?)

Parser Tools and Operators

- Most parser tools can cope with ambiguous grammars
 - Makes life simpler if used with discipline
- Usually can specify precedence & associativity
 - Allows simpler, ambiguous grammar with fewer nonterminals as basis for parser – let the tool handle the details (but only when it makes sense)
 - (i.e., expr ::= expr+expr | expr*expr | ... with assoc. & precedence declarations can be the best solution)
- Take advantage of this to simplify the grammar when using parser-generator tools
 - We will do this in our compiler project

Parser Tools and Ambiguous Grammars

- Possible rules for resolving other problems:
 - Earlier productions in the grammar preferred to later ones (danger here if parser input changed)
 - Longest match used if there is a choice (good solution for dangling if and similar things)
- Parser tools normally allow for this
 - But be sure that what the tool does is really what you want
 - And that it's part of the permanent tool spec, so that v2 won't do something different (that you *don't* want!)

Coming Attractions

Next topic: LR parsing
 – Continue reading ch. 3