# CSE P 501 – Compilers

SSA
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### Agenda

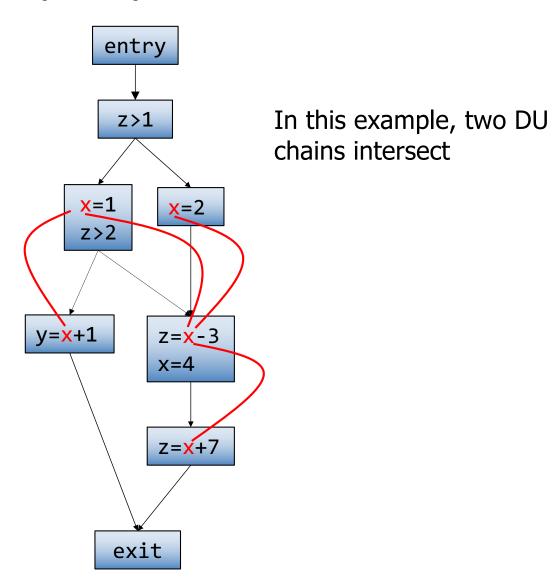
- Overview of SSA IR
  - Constructing SSA graphs
  - Sample of SSA-based optimizations
  - Converting back from SSA form

• Sources: Appel ch. 19, also an extended discussion in Cooper-Torczon sec. 9.3, Mike Ringenburg's CSE 401 slides (13wi)

### Def-Use (DU) Chains

- Common dataflow analysis problem: Find all sites where a variable is used, or find the definition sites of a variable used in an expression
- Traditional solution: def-use chains additional data structure on top of the dataflow graph
  - Link each statement defining a variable to all statements that use it
  - Link each use of a variable to its definition

# Def-Use (DU) Chains



### **DU-Chain Drawbacks**

- Expensive: if a typical variable has N uses and M definitions, the total cost per-variable is O(N \* M), i.e., O(n²)
  - Would be nice if cost were proportional to the size of the program
- Unrelated uses of the same variable are mixed together
  - Complicates analysis variable looks live across all uses even if unrelated

### SSA: Static Single Assignment

- IR where each variable has only one definition in the program text
  - This is a single *static* definition, but that definition can be in a loop, function, or other code that is executed dynamically many times
- Makes many analyses (and related optimizations) more efficient
- Separates values from memory storage locations
- Complementary to CFG/DFG better for some things, but cannot do everything

### SSA in Basic Blocks

Idea: for each original variable  $x_n$  create a new variable  $x_n$  at the  $n^{th}$  definition of the original x. Subsequent uses of x use  $x_n$  until the next definition point.

#### Original

$$- a := x + y$$

$$- b := a - 1$$

$$- a := y + b$$

$$- b := x * 4$$

$$- a := a + b$$

#### SSA

$$- a_1 := x + y$$

$$-b_1 := a_1 - 1$$

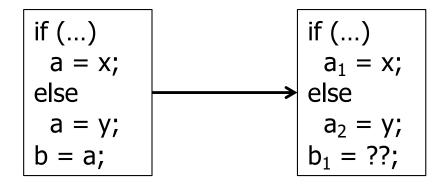
$$- a_2 := y + b_1$$

$$-b_2 := x * 4$$

$$- a_3 := a_2 + b_2$$

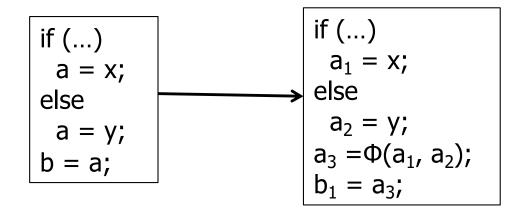
### Merge Points

The issue is how to handle merge points



### Merge Points

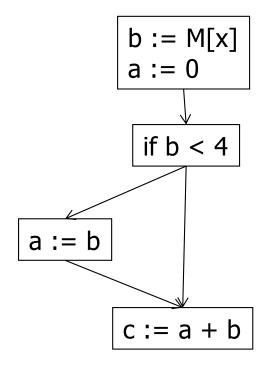
The issue is how to handle merge points



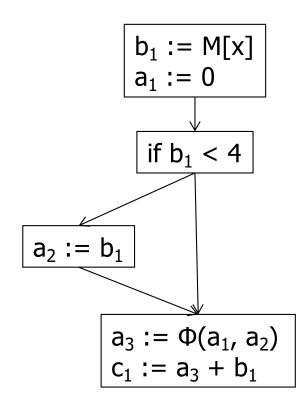
- Solution: introduce a Φ-function
  - $a_3 := \Phi(a_1, a_2)$
- Meaning:  $a_3$  is assigned either  $a_1$  or  $a_2$  depending on which control path is used to reach the  $\Phi$ -function

# **Another Example**

### Original



#### SSA

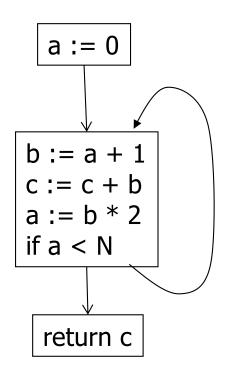


### How Does Φ "Know" What to Pick?

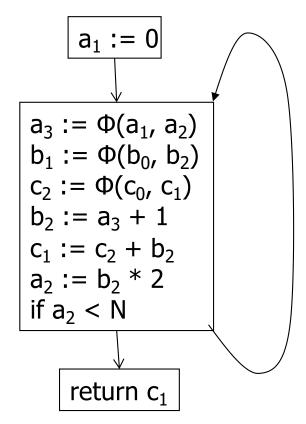
- It doesn't
- Φ-functions don't actually exist at runtime
  - When we're done using the SSA IR, we translate back out of SSA form, removing all Φ-functions
    - Basically by adding code to copy all SSA x<sub>i</sub> values to the single, non-SSA, actual x
  - For analysis, all we typically need to know is the connection of uses to definitions – no need to "execute" anything

### Example With a Loop

#### Original



#### SSA



#### Notes:

- •Loop back edges are also merge points, so require Φ-functions
- •a<sub>0</sub>, b<sub>0</sub>, c<sub>0</sub> are initial values of a, b, c on entry to initial block
- •b<sub>1</sub> is dead can delete later
- •c is live on entry either input parameter or uninitialized

# What does SSA "buy" us?

No need for DU or UD chains – implicit in SSA

Compact representation

• SSA is "recent" (i.e., 80s)

Prevalent in real compilers for { } languages

### **Converting To SSA Form**

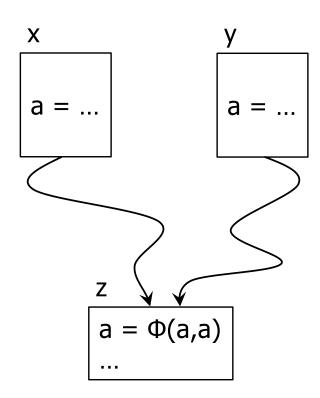
- Basic idea
  - First, add Φ-functions
  - Then, rename all definitions and uses of variables by adding subscripts

### Inserting **Φ-Functions**

- Could simply add Φ-functions for every variable at every join point(!)
- Called "maximal SSA"
- But
  - Wastes way too much space and time
  - Not needed in many cases

# Path-convergence criterion

- Insert a Φ-function for variable a at point z when:
  - There are blocks x and y,
     both containing definitions
     of a, and x ≠ y
  - There are nonempty pathsfrom x to z and from y to z
  - These paths have no common nodes other than z

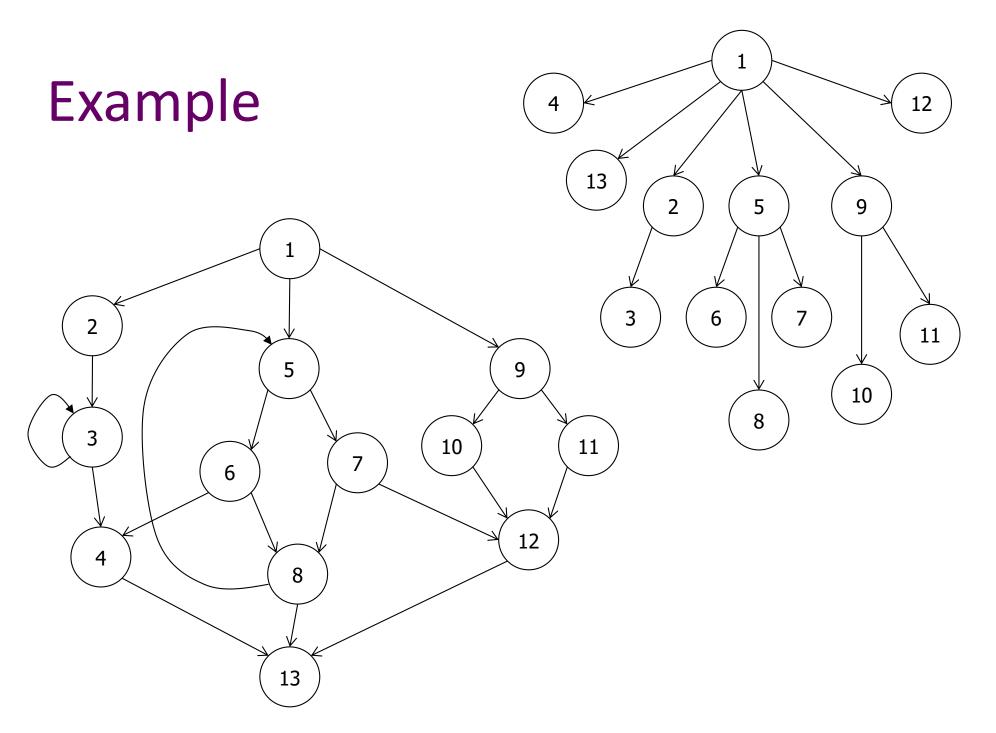


### **Details**

- The start node of the flow graph is considered to define every variable (even if "undefined")
- Each Φ-function itself defines a variable, which may create the need for a new Φfunction
  - So we need to keep adding Φ-functions until things converge
- How can we do this efficiently?
   Use a new concept: dominance frontiers

# Dominators (review)

- Definition: a block x dominates a block y iff every path from the entry of the control-flow graph to y includes x
- So, by definition, x dominates x
- We can associate a Dom(inator) set with each CFG node x – set of all blocks dominated by x
  - $| Dom(x) | \ge 1$
- Properties:
  - Transitive: if a dom b and b dom c, then a dom c
  - There are no cycles, thus can represent the dominator relationship as a tree
- WARNING: this is different from the DOM(x) relationship we used with loops – that was the set of all blocks that dominate x (sigh)



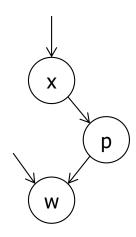
### **Dominators and SSA**

- One property of SSA is that definitions dominate uses; more specifically:
  - If  $x := \Phi(...,x_i,...)$  is in block B, then the definition of  $x_i$  dominates the i<sup>th</sup> predecessor of B
  - If x is used in a non-Φ statement in block B, then the definition of x dominates block B

### Dominance Frontier (1)

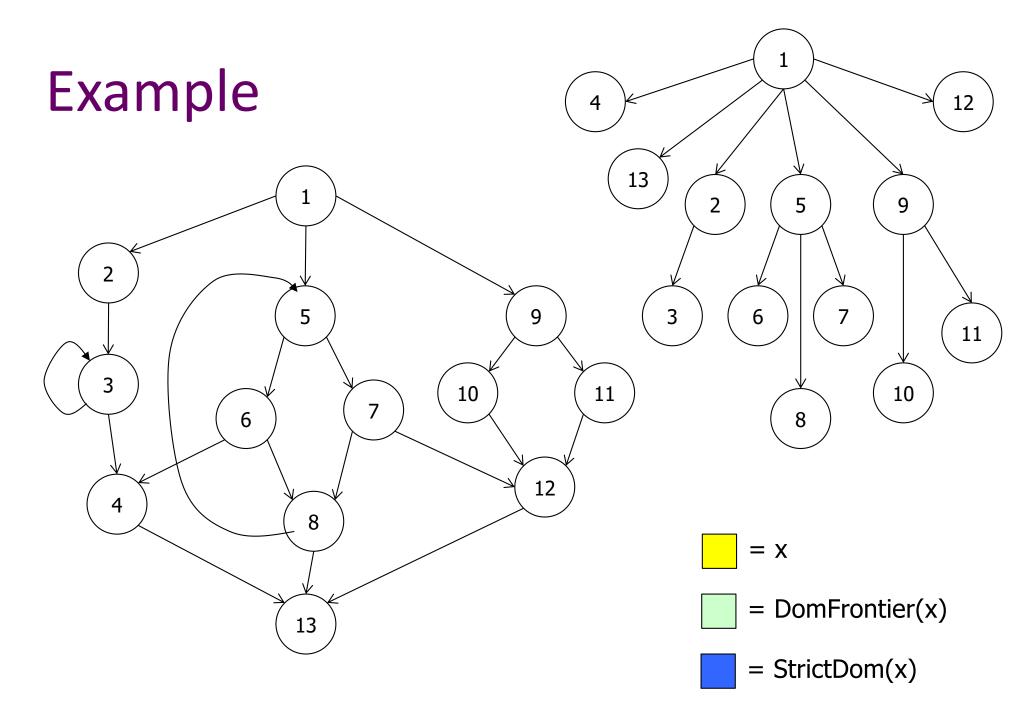
- To get a practical algorithm for placing Φfunctions, we need to avoid looking at all combinations of nodes leading from x to y
- Instead, use the dominator tree in the flow graph

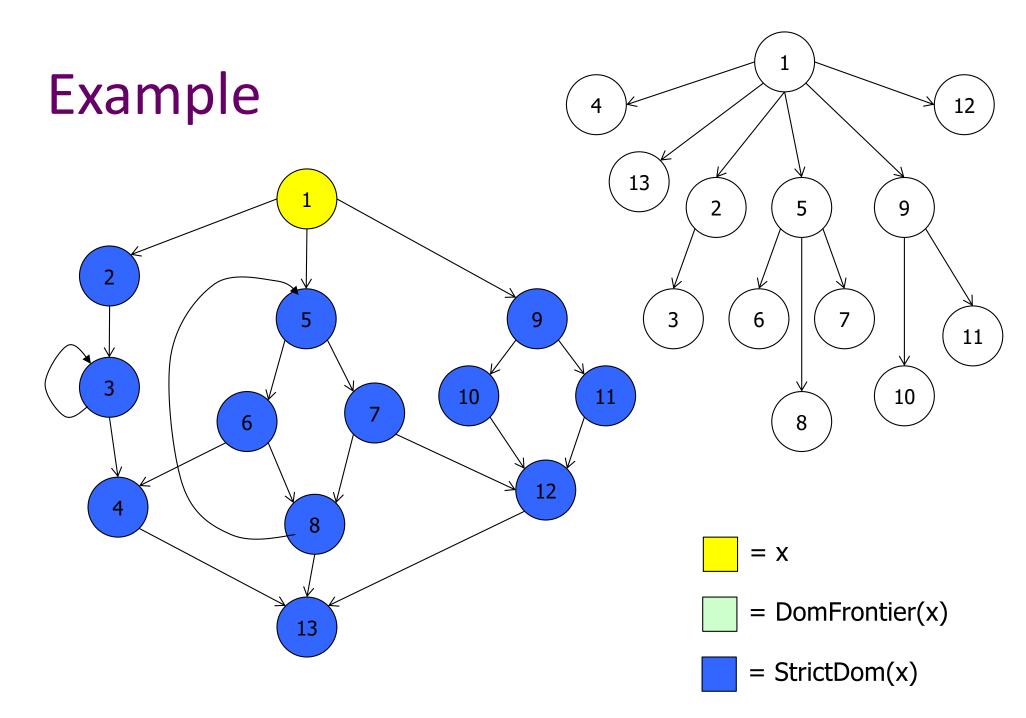
# Dominance Frontier (2)

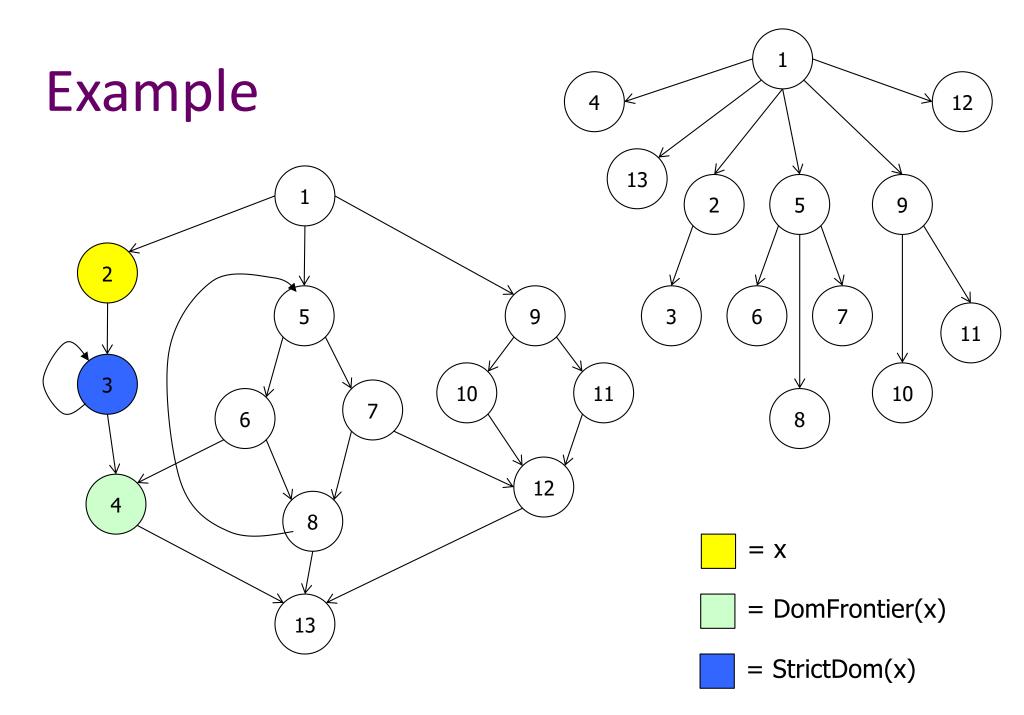


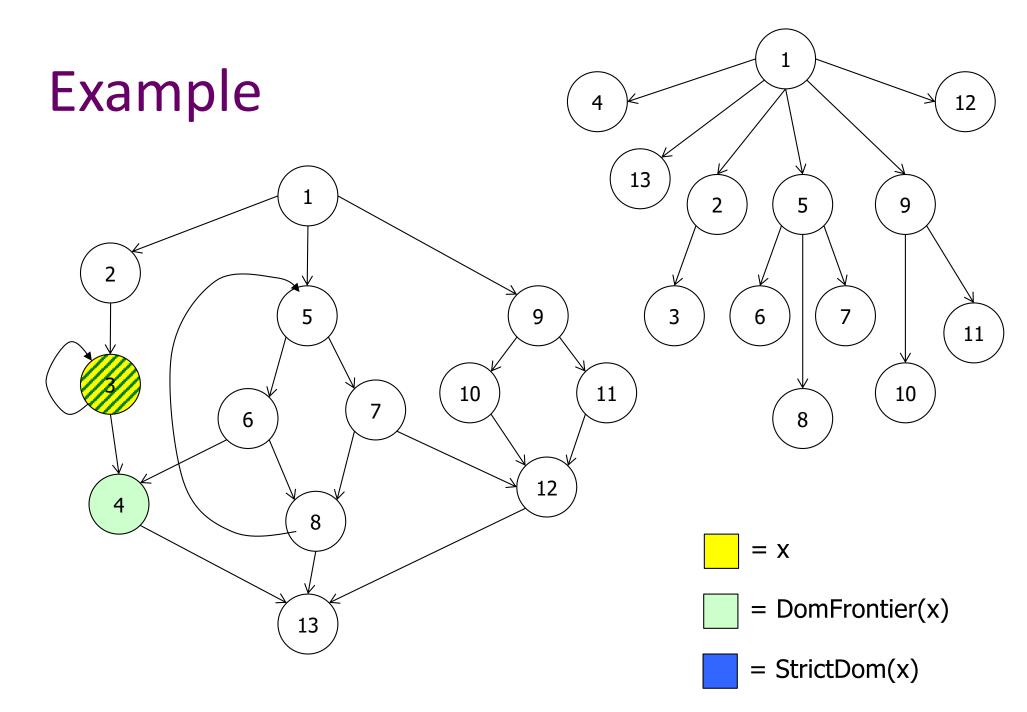
#### Definitions

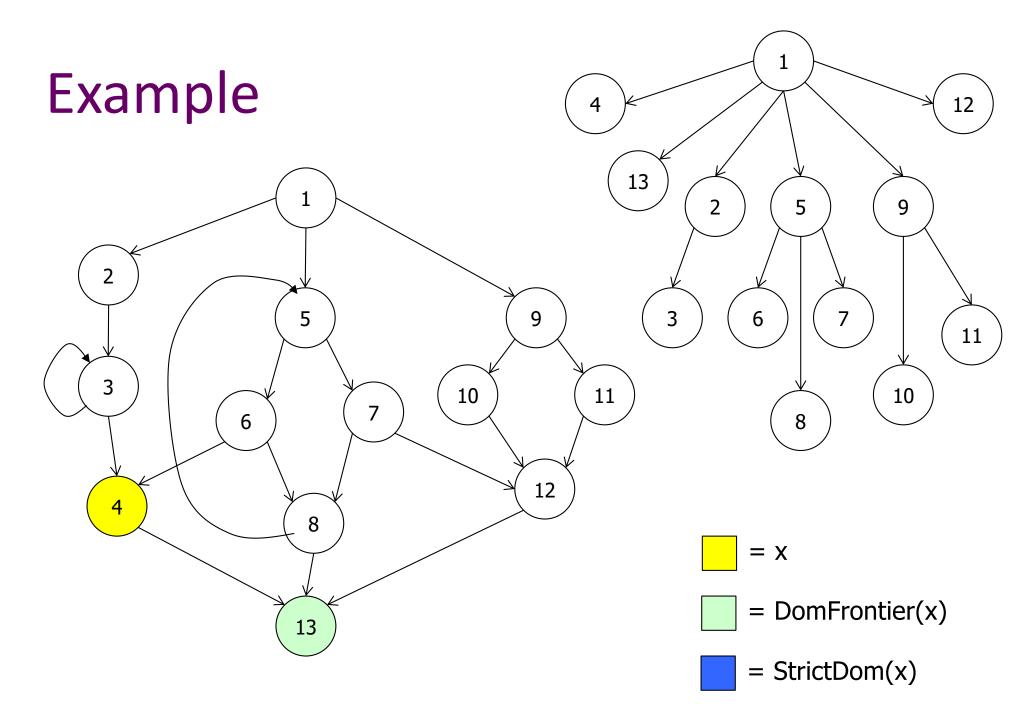
- x strictly dominates y if x dominates y and  $x \neq y$
- The dominance frontier of a node x is the set of all nodes w such that x dominates a predecessor of w, but x does not strictly dominate w
  - This means that x can be in *it's own* dominance frontier! That can happen if there is a back edge to x (i.e., x is the head of a loop)
- Essentially, the dominance frontier is the border between dominated and undominated nodes

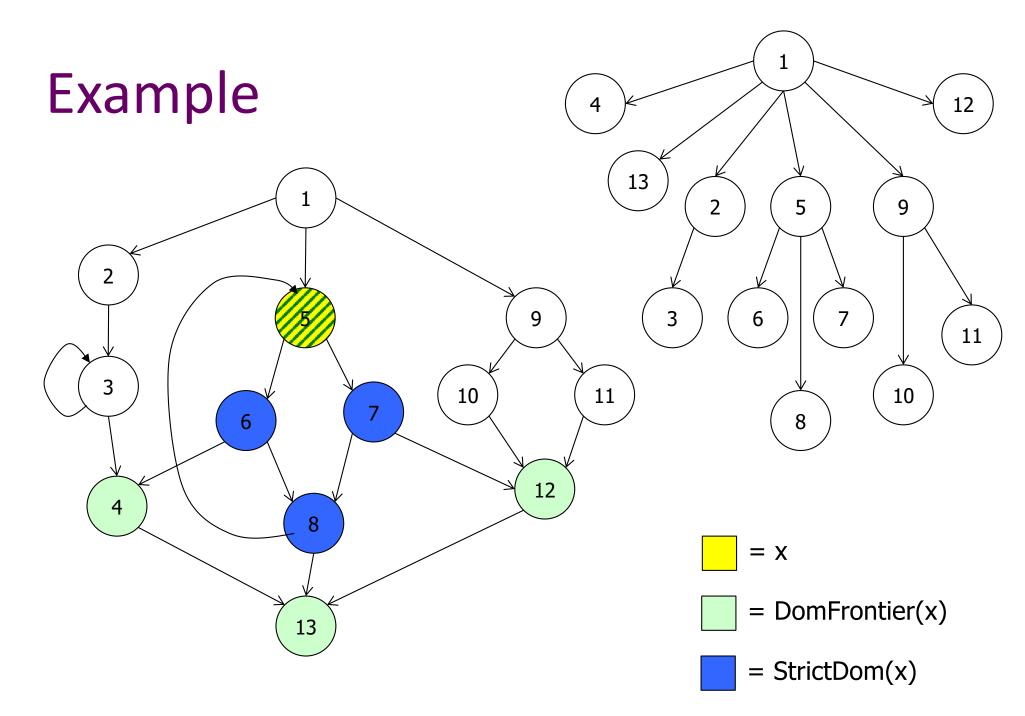


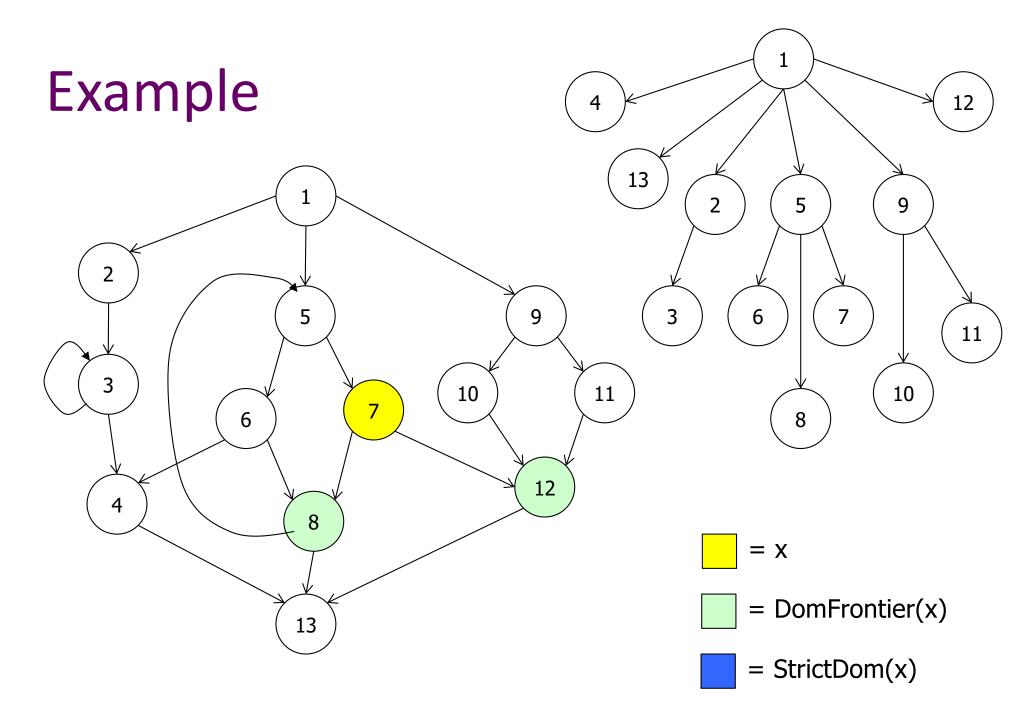


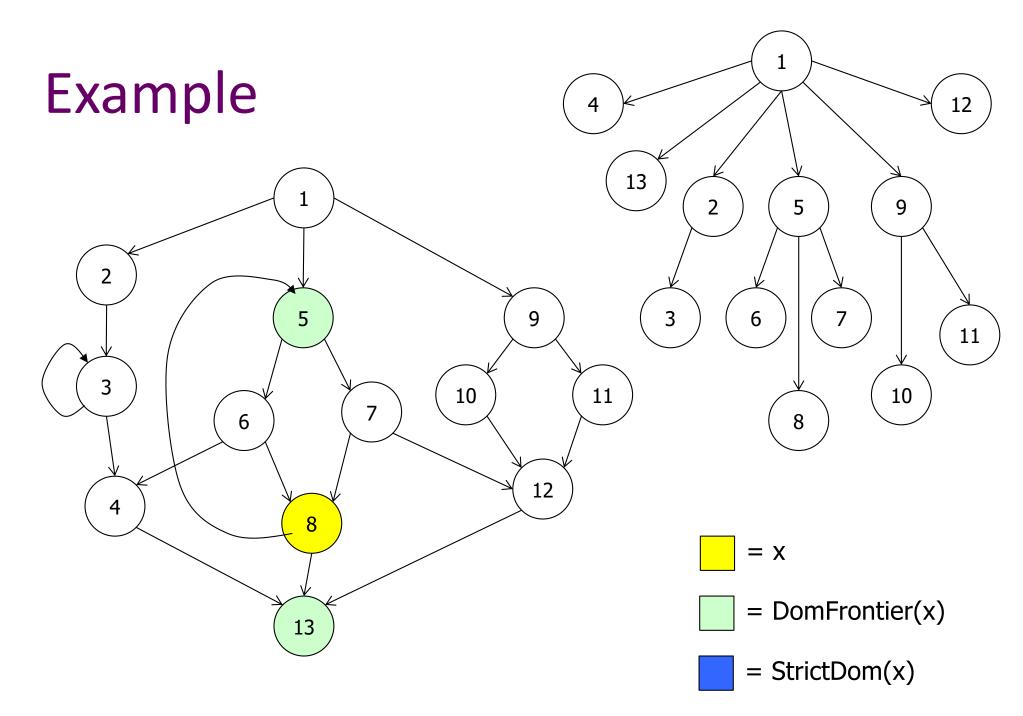


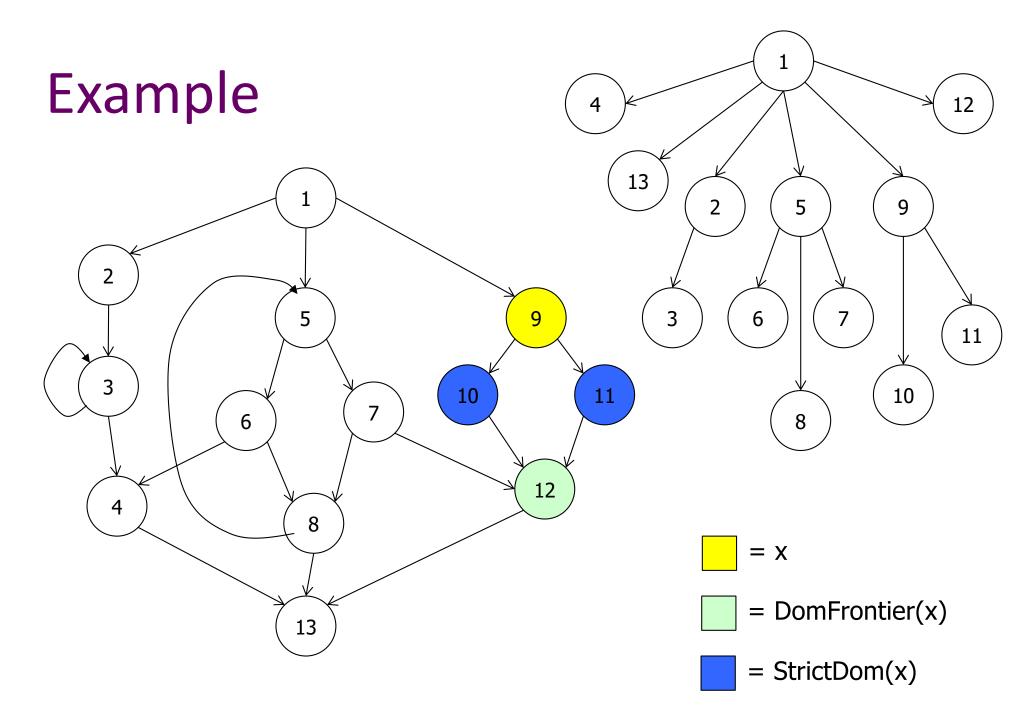


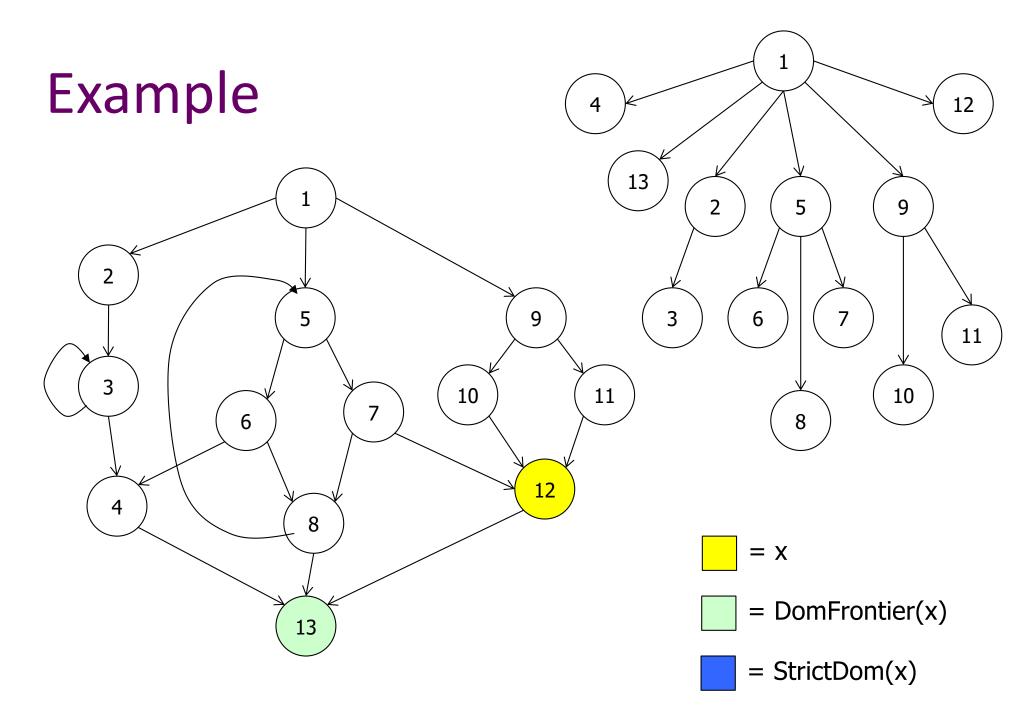


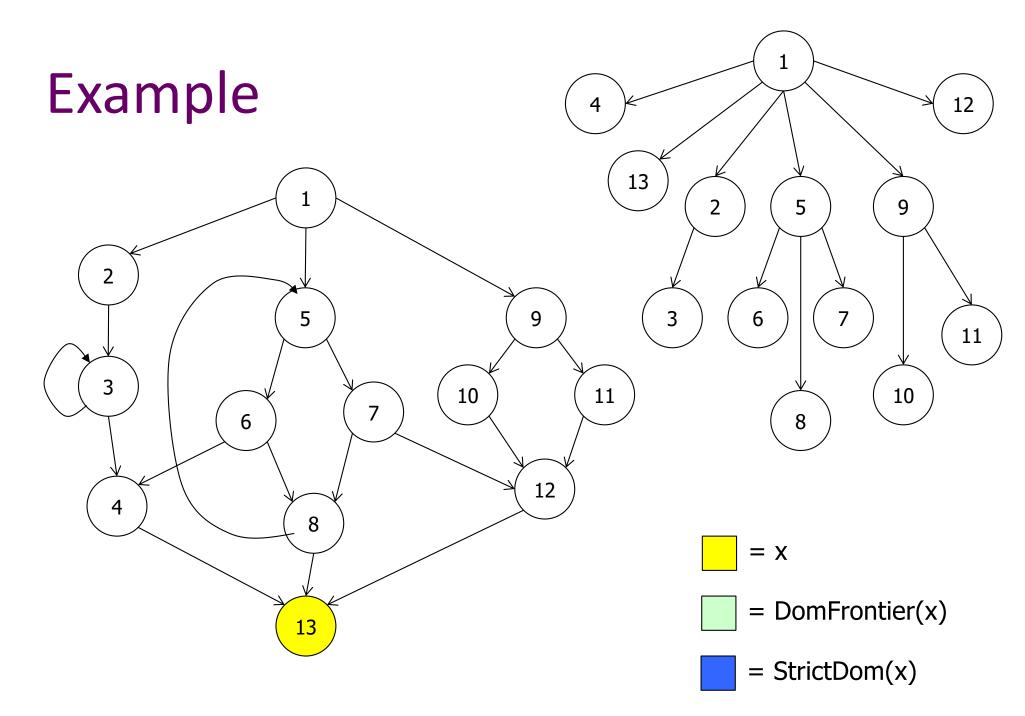




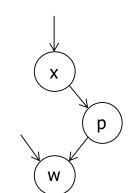








# Dominance Frontier Criterion for Placing Φ-Functions



- If a node x contains the definition of variable a, then every node in the dominance frontier of x needs a Φfunction for a
  - Idea: Everything dominated by x will see x's definition of a. The dominance frontier represents the first nodes we could have reached via an alternative path, which will have an alternate reaching definition of a (recall the convention that the entry node defines all variables with version  $0 a_0$ )
    - Why is this right for loops? Hint: strict dominance...
  - Since the Φ-function itself is a definition, this placement rule needs to be iterated until it reaches a fixed-point
- Theorem: this algorithm places exactly the same set of Ф-functions as the path criterion given previously

### Placing Φ-Functions: Details

- See the book for the full construction, but the basic steps are:
  - 1. Compute the dominance frontiers for each node in the flowgraph
  - Insert just enough Φ-functions to satisfy the criterion. Use a worklist algorithm to avoid reexamining nodes unnecessarily
  - 3. Walk the dominator tree and rename the different definitions of each variable a to be  $a_1$ ,  $a_2$ ,  $a_3$ , ...

### **Efficient Dominator Tree Computation**

- Goal: SSA makes optimizing compilers faster since we can find definitions/uses without expensive bit-vector algorithms
- So, need to be able to compute SSA form quickly
- Computation of SSA from dominator trees are efficient, but...

### Lengauer-Tarjan Algorithm

- Iterative set-based algorithm for finding dominator trees is slow in worst case
- Lengauer-Tarjan is near linear time
  - Uses depth-first spanning tree from start node of control flow graph
  - See books for details

### **SSA Optimizations**

- Why go to the trouble of translating to SSA?
- Because SSA makes many optimizations and analyses simpler and more efficient
  - We'll give a couple of examples
- But first, what do we know? (i.e., what information is kept in the SSA graph?)

### SSA Data Structures

#### For each ...

- Statement: links to: containing block, next and previous statements, variables defined, variables used
- Variable: link to its (single) definition and (possibly multiple) use sites
- Block: List of contained statements, ordered list of predecessor(s), successor(s) blocks

### Dead-Code Elimination

- A variable is live its list of uses is not empty(!)
  - That's it! Nothing further to compute
- Algorithm to delete dead code:
  - while there is some variable v with no uses if the statement that defines v has no other side effects, then delete it
  - Need to remove this statement from the list of uses for its operand variables – which may cause those variables to become dead

### Simple Constant Propagation

- If c is a constant in v := c, any use of v can be replaced by c
  - So update every use of v to use constant c
- If the  $c_i$ 's in  $v := \Phi(c_1, c_2, ..., c_n)$  are all the same constant c, we can replace this with v := c
- Incorporate copy propagation, constant folding, and others in the same worklist algorithm

### Simple Constant Propagation

```
W := list of all statements in SSA program
while W is not empty
  remove some statement S from W
  if S is v:=\Phi(c, c, ..., c), replace S with v:=c
  if S is v:=c
    delete S from the program
    for each statement T that uses v
      substitute c for v in T
      add T to W
```

### Converting Back from SSA

- Unfortunately, real machines do not include a Ф instruction
- So after analysis, optimization, and transformation, need to convert back to a "Φ-less" form for execution
  - (Also sometimes needed for different kinds of analysis or transformation. A production optimizer might convert the IR into and out of SSA form multiple times)

# Translating Φ-functions

- The meaning of  $x := \Phi(x_1, x_2, ..., x_n)$  is "set  $x := x_1$  if arriving on edge 1, set  $x := x_2$  if arriving on edge 2, etc."
- So, for each i, insert x := x<sub>i</sub> at the end of predecessor block i
- Rely on copy propagation and coalescing in register allocation to eliminate redundant copy instructions

### SSA Wrapup

- More details needed to fully and efficiently implement SSA, but these are the main ideas
  - See recent compiler books (but not the Dragon book!)
- Allows efficient implementation of many optimizations
- SSA is used in most modern optimizing compilers (Ilvm is based on it) and has been retrofitted into many older ones (gcc is a well-known example)
- Not a silver bullet some optimizations still need non-SSA forms, but very effective for many