CSE P 501 – Compilers

Value Numbering & Optimizations Hal Perkins Autumn 2019

Agenda

- Optimization (Review)
 - Goals
 - Scope: local, superlocal, regional, global (intraprocedural), interprocedural
- Control flow graphs (reminder)
- Value numbering
- Dominators
- Ref.: Cooper/Torczon ch. 8

Code Improvement (1)

- Pick a better algorithm(!)
- Use machine resources efficiently
 - Instructions, registers
 - More later...

Code Improvement (2)

- Local optimizations basic blocks
 - Algebraic simplifications
 - Constant folding
 - Common subexpression elimination (i.e., redundancy elimination)
 - Dead code elimination
 - Specialize computation based on context
 - etc., etc., ...

Code Improvement (3)

- Global optimizations
 - Code motion
 - Moving invariant computations out of loops
 - Strength reduction (replace multiplications by repeated additions, for example)
 - Global common subexpression elimination
 - Global register allocation
 - Many others...



- None of these improvements are truly "optimal"
 - Hard problems (in theory-of-computation sense)
 - Proofs of optimality assume artificial restrictions
- Best we can do is to improve things

- Most (much?) (some?) of the time

 Realistically: try to do better for common idioms both in the code and on the machine

Optimization Phase

- Goal
 - Discover, at compile time, information about the runtime behavior of the program, and use that information to improve the generated code

A First Running Example: Redundancy Elimination

- An expression x+y is *redundant* at a program point iff, along every path from the procedure's entry, it has been evaluated and its constituent subexpressions (x and y) have <u>not</u> been redefined
- If the compiler can prove the expression is redundant:
 - Can store the result of the earlier evaluation
 - Can replace the redundant computation with a reference to the earlier (stored) result

Common Pattern for Code Improvement

- Typical for most compiler optimizations
- First, discover opportunities through program analysis
- Then, modify the IR to take advantage of the opportunities
 - Historically, goal usually was to decrease execution time
 - Other possibilities: reduce space, power, ...

Issues (1)

- Safety transformation must not change program meaning
 - Must generate correct results
 - Can't generate spurious errors
 - Optimizations must be conservative
 - Large part of analysis goes towards proving safety
 - Can pay off to speculate (be optimistic) but then need to recover if reality is different

Issues (2)

- Profitibility
 - If a transformation is possible, is it profitable?
 - Example: loop unrolling
 - Can increase amount of work done on each iteration, i.e., reduce loop overhead
 - Can eliminate duplicate operations done on separate iterations

Issues (3)

- Downside risks
 - Even if a transformation is generally worthwhile, need to think about potential problems
 - Example:
 - Transformation might need more temporaries, putting additional pressure on registers
 - Increased code size could cause cache misses, or, in bad cases, increase page working set

Example: Value Numbering

- Technique for eliminating redundant expressions: assign an identifying number VN(n) to each expression
 - VN(x+y)=VN(j) if x+y and j have the same value
 - Use hashing over value numbers for effeciency
- Old idea (Balke 1968, Ershov 1954)
 - Invented for low-level, linear IRs
 - Equivalent methods exist for tree IRs, e.g., build a DAG

Uses of Value Numbers

- Improve the code
 - Replace redundant expressions
 - Simplify algebraic identities
 - Discover, fold, and propagate constant valued expressions

Local Value Numbering

- Algorithm
 - For each operation o = <op, o1,o2> in a basic block
 - 1. Get value numbers for operands from hash lookup
 - 2. Hash <op, VN(o1), VN(o2)> to get a value number for o (If op is commutative, sort VN(o1), VN(o2) first)
 - 3. If o already has a value number, replace o with a reference to the value
 - 4. If o1 and o2 are constant, evaluate o at compile time and replace with an immediate load
- If hashing behaves well, this runs in linear time

Example

Code Rewritten a = x + y b = x + y a = 17c = x + y

Bug in Simple Example

- If we use the original names, we get in trouble when a name is reused
- Solutions
 - Be clever about which copy of the value to use (e.g., use c=b in last statement)
 - Create an extra temporary
 - Rename around it (best!)

Renaming

- Idea: give each value a unique name a^j means ith definition of a with VN = j
- Somewhat complex notation, but meaning is reasonably clear
- This is the idea behind SSA (Static Single Assignment)
 - Popular modern IR exposes many opportunities for optimizations

Example Revisited

Code Rewritten a = x + y b = x + y a = 17c = x + y

Simple Extensions to Value Numbering

- Constant folding
 - Add a bit that records when a value is constant
 - Evaluate constant values at compile time
 - Replace op with load immediate
- Algebraic identities: x+0, x*1, x-x, ...
 - Many special cases
 - Switch on op to narrow down checks needed
 - Replace result with input VN

Larger Scopes

- This algorithm works on straight-line blocks of code (basic blocks)
 - Best possible results for single basic blocks
 - Loses all information when control flows to another block
- To go further we need to represent multiple blocks of code and the control flow between them

Control Flow Graph (CFG) reminder

- Nodes: basic blocks
 - Key property: all statements executed sequentially if any are
- Edges: include a directed edge from n1 to n2 if there is *any* possible way for control to transfer from block n1 to n2 during execution

Optimization Categories (1)

- Local methods
 - Usually confined to basic blocks
 - Simplest to analyze and understand
 - Most precise information

Optimization Categories (2)

- Superlocal methods
 - Operate over *Extended Basic Blocks* (EBBs)
 - An EBB is a set of blocks b₁, b₂, ..., b_n where b₁ has multiple predecessors and each of the remaining blocks b_i (2≤i≤n) have only b_{i-1} as its unique predecessor
 - The EBB is entered only at b₁, but may have multiple exits
 - A single block b_i can be the head of multiple EBBs (these EBBs form a tree rooted at b_i)
 - Use information discovered in earlier blocks to improve code in successors

Optimization Categories (3)

- Regional methods
 - Operate over scopes larger than an EBB but smaller than an entire procedure/ function/method
 - Typical example: loop body
 - Difference from superlocal methods is that there may be merge points in the graph (i.e., a block with two or more predecessors)
 - Facts true at merge point are facts known to be true on all possible paths to that point

Optimization Categories (4)

Global methods

- Operate over entire procedures
- Sometimes called *intraprocedural* methods
- Motivation is that local optimizations sometimes have bad consequences in larger context
- Procedure/method/function is a natural unit for analysis, separate compilation, etc.
- Almost always need global *data-flow* analysis information for these

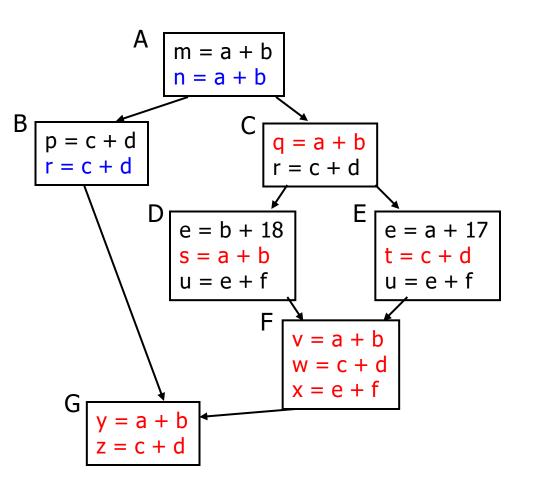
Optimization Categories (5)

• Whole-program methods

- Operate over more than one procedure
- Sometimes called *interprocedural* methods
- Challenges: name scoping and parameter binding issues at procedure boundaries
- Classic examples: inline method substitution, interprocedural constant propagation
- Common in aggressive JIT compilers and optimizing compilers for object-oriented languages

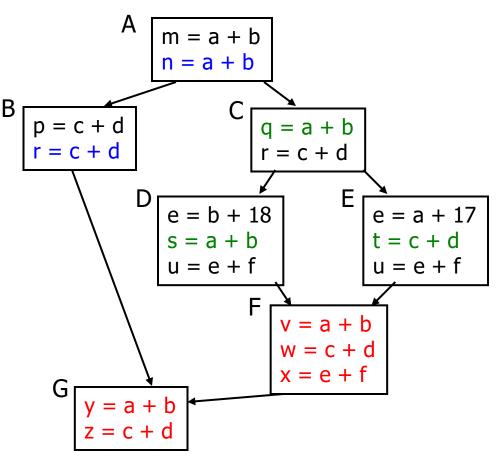
Value Numbering Revisited

- Local Value Numbering
 - 1 block at a time
 - Strong local results
 - No cross-block effects
- Missed opportunities



Superlocal Value Numbering

- Idea: apply local method to EBBs
 - {A,B}, {A,C,D}, {A,C,E}
- Final info from A is initial info for B, C; final info for D, E
- Gets reuse from ancestors
- Avoid reanalyzing A, C
- Doesn't help with F, G



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SSA Name Space (from before)

Code	Rewritten
$a_0^3 = x_0^1 + y_0^2$	$a_0^3 = x_0^1 + y_0^2$
$b_0^3 = x_0^1 + y_0^2$	$b_0^3 = a_0^3$
a ₁ ⁴ = 17	a ₁ ⁴ = 17
$c_0^3 = x_0^1 + y_0^2$	$c_0^3 = a_0^3$

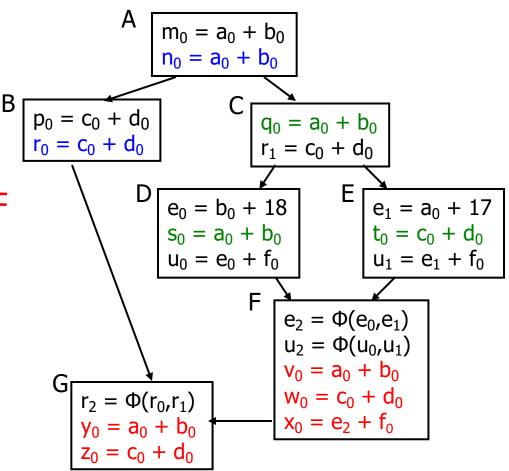
- Unique name for each definition
- Name ⇔ VN
- a_0^3 is available to assign to c_0^3

SSA Name Space

- Two Principles
 - Each name is defined by exactly one operation
 - Each operand refers to exactly one definition
- Need to deal with merge points
 - Add Φ functions at merge points to reconcile names
 - Use subscripts on variable names for uniqueness

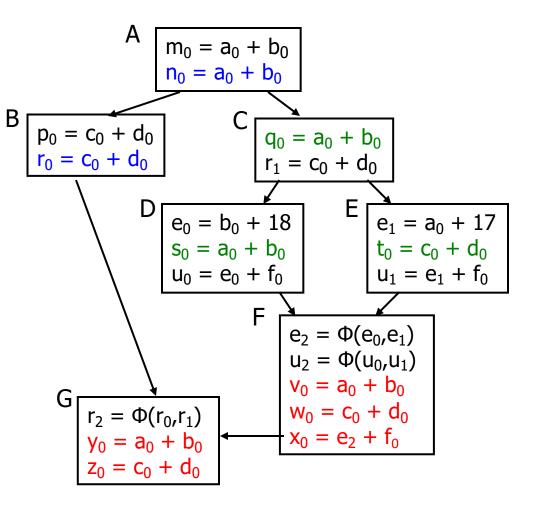
Superlocal Value Numbering with All Bells & Whistles

- Finds more redundancies
- Little extra cost
- Still does nothing for F and G



Larger Scopes

- Still have not helped F and G
- Problem: multiple predecessors
- Must decide what facts hold in F and in G
 - For G, combine B & F?
 - Merging states is expensive
 - Fall back on what we know



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Dominators

- Definition
 - x *dominates* y iff every path from the entry of the control-flow graph to y includes x
- By definition, x dominates x
- Associate a Dom set with each node
 - $\mid Dom(x) \mid \geq 1$
- Many uses in analysis and transformation
 - Finding loops, building SSA form, code motion

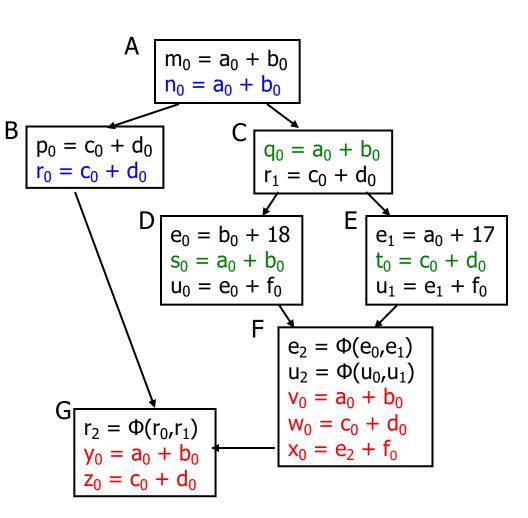
Immediate Dominators

- For any node x, there is a y in Dom(x) closest to x
- This is the *immediate dominator* of x

- Notation: IDom(x)

Dominator Sets

Block Dom IDom

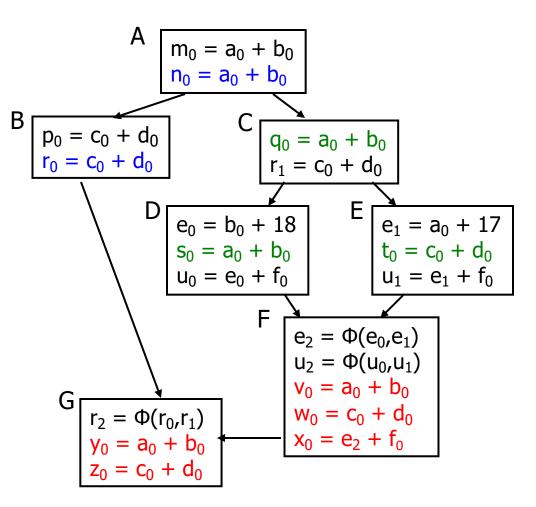


Note that the IDOM relation defines a tree!

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Dominator Value Numbering

- Still looking for a way to handle F and G
- Idea: Use info from IDom(x) to start analysis of x
 - Use C for F and A for G
- <u>D</u>ominator <u>VN</u>
 <u>T</u>echnique (DVNT)

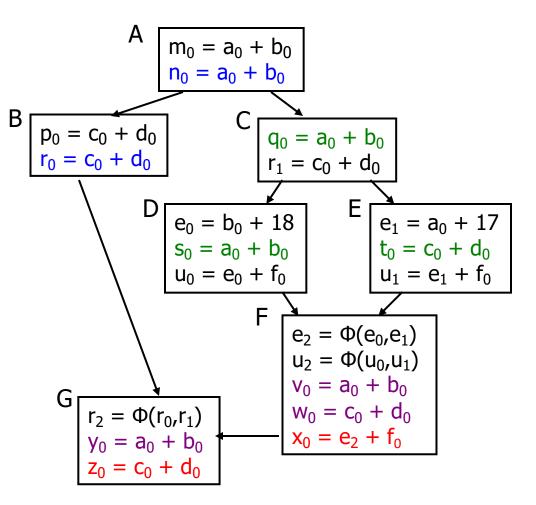


DVNT algorithm

- Use superlocal algorithm on extended basic blocks
 - Use scoped hash tables & SSA name space as before
- Start each node with table from its IDOM
- No values flow along back edges (i.e., loops)
- Constant folding, algebraic identities as before

Dominator Value Numbering

- Advantages
 - Finds more redundancy
 - Little extra cost
- Shortcomings
 - Misses some opportunities (common calculations in ancestors that are not IDOMs)
 - Doesn't handle loops or other back edges



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The Story So Far...

- Local algorithm
- Superlocal extension
 - Some local methods extend cleanly to superlocal scopes
- Dominator VN Technique (DVNT)
- All of these propagate along forward edges
- None are global

Coming Attractions

- Data-flow analysis
 - Provides global solution to redundant expression analysis
 - Catches some things missed by DVNT, but misses some others
 - Generalizes to many other analysis problems, both forward and backward
- Loops
- SSA for general transformations