CSE P 501 – Compilers

LR Parsing
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Agenda

- LR Parsing
- Table-driven Parsers
- Parser States
- Shift-Reduce and Reduce-Reduce conflicts

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Bottom-Up Parsing



- Idea: Read the input left to right
- Whenever we've matched the right hand side of a production, reduce it to the appropriate non-terminal and add that non-terminal to the parse tree
- The upper edge of this partial parse tree is known as the frontier

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Example

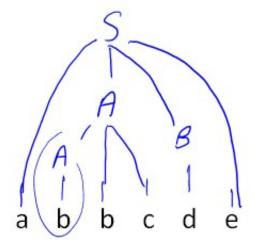
Grammar

S := aAB e

A ::= *A*bc | b

B := d

• Bottom-up Parse



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LR(1) Parsing

- We'll look at LR(1) parsers
 - Left to right scan, Rightmost derivation, 1 symbol lookahead
 - Almost all practical programming languages have a LR(1) grammar
 - LALR(1), SLR(1), etc. subsets of LR(1)
 - LALR(1) can parse most real languages, tables are more compact, and is used by YACC/Bison/CUP/etc.

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LR Parsing in Greek

- The bottom-up parser reconstructs a reverse rightmost derivation
- Given the rightmost derivation

```
S=>\beta_1=>\beta_2=>...=>\beta_{n-2}=>\beta_{n-1}=>\beta_n=w the parser will first discover \beta_{n-1}=>\beta_n , then \beta_{n-2}=>\beta_{n-1} , etc.
```

- Parsing terminates when
 - $-\beta_1$ reduced to S (start symbol, success), or
 - No match can be found (syntax error)

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How Do We Parse with This?



- Key: given what we've already seen and the next input symbol (the lookahead), decide what to do.
- Choices:
 - Perform a reduction
 - Look ahead further
- Can reduce $A => \beta$ if both of these hold:
 - $A=>\beta$ is a valid production, and
 - $A=>\beta$ is a step in *this* rightmost derivation
- This is known as a shift-reduce parser

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Sentential Forms

- If $S = >^* \alpha$, the string α is called a *sentential form* of the grammar
- In the derivation $S => \beta_1 => \beta_2 => \dots => \beta_{n-2} => \beta_{n-1} => \beta_n = w$ each of the β_i are sentential forms
- A sentential form in a rightmost derivation is called a right-sentential form (similarly for leftmost and leftsentential)

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Handles

- Informally, a production whose right hand side matches a substring of the tree frontier that is part of the rightmost derivation of the current input string (i.e., the "correct" production)
 - Even if A := β is a production, it is a handle only if β matches the frontier at a point where A := β was used in *this specific* derivation
 - β may appear in many other places in the frontier without designating a handle
- Bottom-up parsing is all about finding handles

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Handle Examples

- In the derivation $S \Rightarrow ABe \Rightarrow ABe$
 - abbcde is a right sentential form whose handle is
 A::=b at position 2
 - aAbcde is a right sentential form whose handle is
 A::=Abc at position 4
 - Note: some books take the left end of the match as the position

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Handles – The Dragon Book Defn.

• Formally, a *handle* of a right-sentential form γ is a production $A := \beta$ and a position in γ where β may be replaced by A to produce the previous right-sentential form in the rightmost derivation of γ

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Implementing Shift-Reduce Parsers

- Key Data structures
 - A stack holding the frontier of the tree
 - A string with the remaining input (tokens)
- We also need something to encode the rules that tell us what action to take next, given the state of the stack and the lookahead symbol
 - Typically a table that encodes a finite automata

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Shift-Reduce Parser Operations

- Reduce if the top of the stack is the right side of a handle A::=β, pop the right side β and push the left side A
- Shift push the next input symbol onto the stack
- Accept announce success
- Error syntax error discovered

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Shift-Reduce Example

S ::= aABe $A ::= Abc \mid b$

B := d

Stack	Input	Action
\$	abbcde\$	shift
\$a	66 cde \$	shift
tab	6cd-es	reduce
5aA	bode \$	shift shift
\$aAb	odes	
\$aAbc	74 /	1 -1 -1
80A	des	, veluce
ta Ad	e 8	shift
\$ a AB	*	reduce
\$ a ABe	\$	accept
\$ S		

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How Do We Automate This?

- Cannot use clairvoyance in a real parser (alas...)
- Defn. Viable prefix a prefix of a right-sentential form that can appear on the stack of the shift-reduce parser
 - Equivalent: a prefix of a right-sentential form that does not continue past the rightmost handle of that sentential form
 - In Greek: γ is a *viable prefix* of G if there is some derivation $S = \sum_{rm}^* \alpha A w = \sum_{rm}^* \alpha \beta w$ and γ is a prefix of $\alpha \beta$.
 - The occurrence of β in $\alpha\beta$ w is a *handle* of $\alpha\beta$ w

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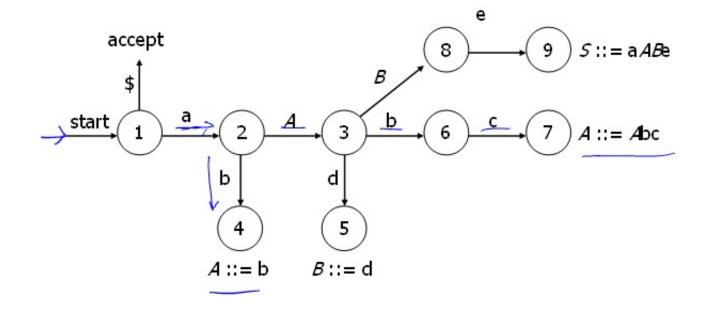
How Do We Automate This?

- Fact: the set of viable prefixes of a CFG is a regular language(!)
- Idea: Construct a DFA to recognize viable prefixes given the stack and remaining input
 - Perform reductions when we recognize them

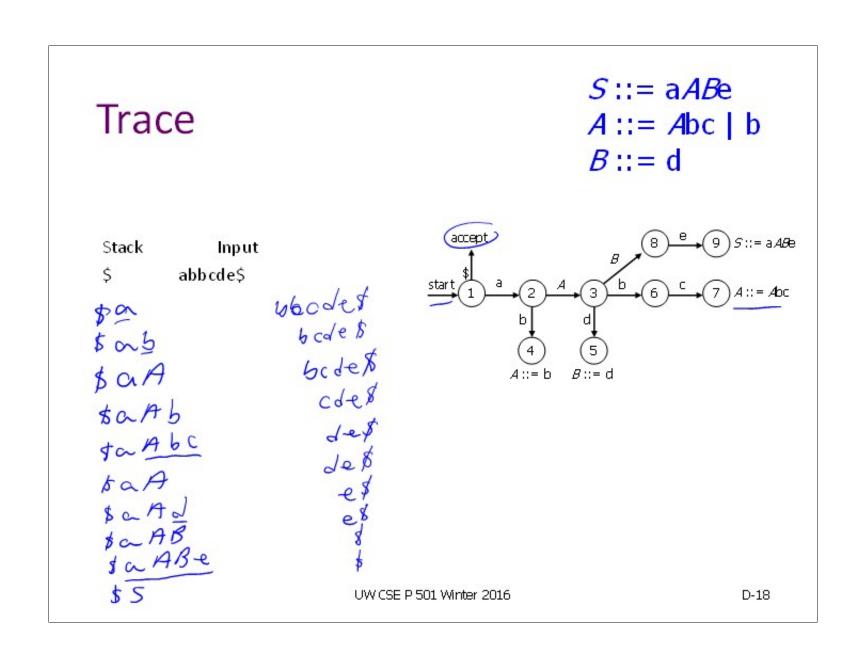
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DFA for prefixes of

```
S::= aABe
A::= Abc | b
B::= d
```



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Observations

- Way too much backtracking
 - We want the parser to run in time proportional to the length of the input
- Where the heck did this DFA come from anyway?
 - From the underlying grammar
 - Defer construction details for now

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Avoiding DFA Rescanning

- Observation: no need to restart DFA after a shift.
 Stay in the same state and process next token.
- Observation: after a reduction, the contents of the stack are the same as before except for the new nonterminal on top
 - Scanning the stack will take us through the same transitions as before until the last one
 - If we record state numbers on the stack, we can go directly to the appropriate state when we pop the right hand side of a production from the stack

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Stack

 Change the stack to contain pairs of states and symbols from the grammar

$$s_0 X_1 s_1 X_2 s_2 ... X_n s_n$$

- State s₀ represents the accept (start) state
 (Not always explicitly on stack depends on particular presentation)
- When we push a symbol on the stack, push the symbol plus the FA state
- When we reduce, popping the handle will reveal the state of the FA just prior to reading the handle
- Observation: in an actual parser, only the state numbers are needed since they
 implicitly contain the symbol information. But for explanations / examples it
 can help to show both.

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Encoding the DFA in a Table

- A shift-reduce parser's DFA can be encoded in two tables
 - One row for each state
 - action table encodes what to do given the current state and the next input symbol
 - goto table encodes the transitions to take after a reduction

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Actions (1)

- Given the current state and input symbol, the main possible actions are
 - si shift the input symbol and state i onto the stack (i.e., shift and move to state i)
 - rj reduce using grammar production j
 - The production number tells us how many <symbol, state> pairs to pop off the stack
 (= number of symbols on rhs of production)

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Actions (2)

- Other possible action table entries
 - accept
 - blank no transition syntax error
 - A LR parser will detect an error as soon as possible on a left-to-right scan
 - A real compiler needs to produce an error message, recover, and continue parsing when this happens

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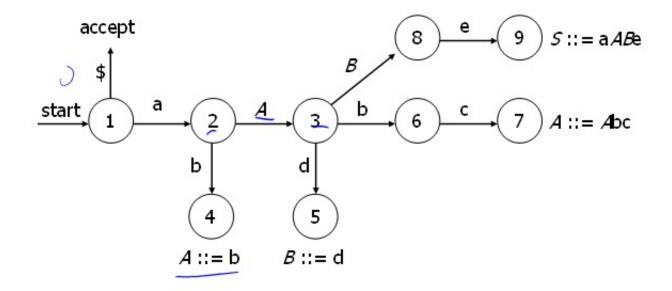
Goto

- When a reduction is performed using A ::= β, we pop |β| <symbol, state> pairs from the stack revealing a state uncovered_s on the top of the stack
- goto[uncovered_s, A] is the new state to push on the stack when reducing production A ::= β (after popping handle β and pushing A)

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Reminder: DFA for

S::= aABe A::= Abc | b B::= d



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LR Parse Table for

1. *S* ::= a*AB*e

2. A := Abc

3. A := b

4. B := d

	Ctato			aci	tion				goto	
	State	а	b	С	d	е	\$	Α	В	S
	0						acc			
	_1	s2								g0
	1 2 3	_	s4					g3		
	3		s6		s5				g8	
->	4	r3	r3	r3	r3	r3	r3			
	5	r4	r4	r4	r4	r4	r4			
	6			s7						
	7	r2	r2	r2	r2	r2	r2			
	8					s9				
	9	r1	r1	r1	r1	r1	r1			

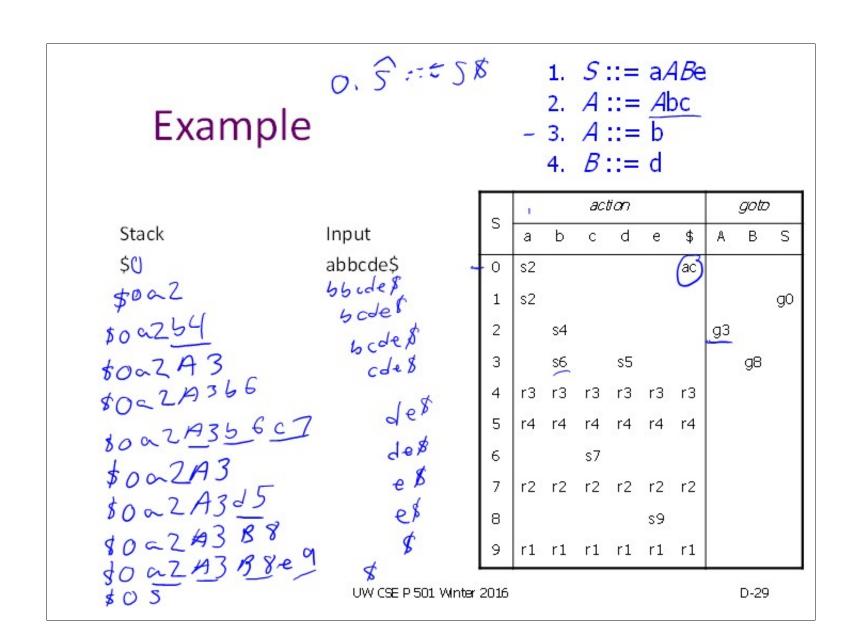
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LR Parsing Algorithm

```
tok = scanner.getToken();
while (true) {
    s = top of stack;
    if (action[s, tok] = si ) {
        push tok; push i (state);
        tok = scanner.getToken();
    } else if (action[s, tok] = rj ) {
        pop 2 * length of right side of production j (2*|β|);
        uncovered_s = top of stack;
        push left side A of production j;
        push state goto[uncovered_s, A];
    }
```

```
} else if (action[s, tok] = accept ) {
    return;
} else {
    // no entry in action table
    report syntax error;
    halt or attempt recovery;
}
```

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LR States

- Idea is that each state encodes
 - The set of all possible productions that we could be looking at, given the current state of the parse, and
 - Where we are in the right hand side of each of those productions

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Items

- An item is a production with a dot in the right hand side
- Example: Items for production A ::= X Y

$$A := XY$$

$$A := X \cdot Y$$

$$A := X Y$$
.

Idea: The dot represents a position in the production

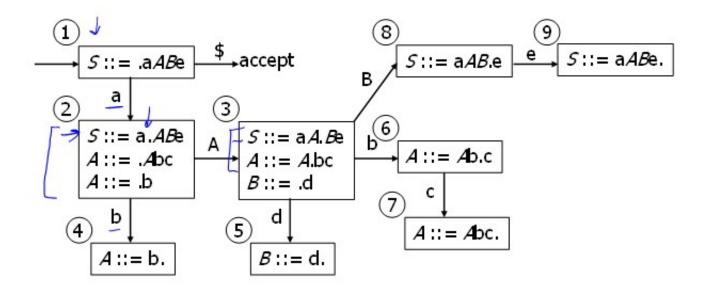
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DFA for

S ::= a*AB*e

 $A ::= Abc \mid b$

B := d



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Problems with Grammars

- Grammars can cause problems when constructing a LR parser
 - Shift-reduce conflicts
 - Reduce-reduce conflicts

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Shift-Reduce Conflicts

- Situation: both a shift and a reduce are possible at a given point in the parse (equivalently: in a particular state of the DFA)
- Classic example: if-else statement

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Parser States for

```
    S ::= ifthen S
    S ::= ifthen S else S
```

- State 3 has a shiftreduce conflict
 - Can shift past else into state 4 (s4)
 - Can reduce (r1)
 S ::= ifthen S

(Note: other *S* ::= . ifthen items not included in states 2-4 to save space)

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Solving Shift-Reduce Conflicts

- Fix the grammar
 - Done in Java reference grammar, others
- Use a parse tool with a "longest match" rule –
 i.e., if there is a conflict, choose to shift
 instead of reduce
 - Does exactly what we want for if-else case
 - Guideline: a few shift-reduce conflicts are fine, but be sure they do what you want (and that this behavior is guaranteed by the tool specification)

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Reduce-Reduce Conflicts

- Situation: two different reductions are possible in a given state
- · Contrived example

$$S ::= A$$

$$S ::= B$$

$$A := x$$

$$B ::= x$$

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Parser States for

2.
$$S := B$$

3.
$$A ::= x$$

4.
$$B := X$$

 State 2 has a reducereduce conflict (r3, r4)

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Handling Reduce-Reduce Conflicts

- These normally indicate a serious problem with the grammar.
- Fixes
 - Use a different kind of parser generator that takes lookahead information into account when constructing the states
 - · Most practical tools use this information
 - Fix the grammar

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Another Reduce-Reduce Conflict

Suppose the grammar tries to separate arithmetic and boolean expressions

```
expr ::= aexp | bexp

aexp ::= aexp * aident | aident

bexp ::= bexp && bident | bident

aident ::= id

bident ::= id
```

This will create a reduce-reduce conflict after recognizing id

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Covering Grammars

- A solution is to merge aident and bident into a single non-terminal like ident (or just use id in place of aident and bident everywhere they appear)
- This is a covering grammar
 - Will generate some programs (sentences) that are not generated by the original grammar
 - Use the type checker or other static semantic analysis to weed out illegal programs later

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Coming Attractions

- Constructing LR tables
 - We'll present a simple version (SLR(0)) in lecture, then talk about adding lookahead and then a little bit about how this relates to LALR(1) used in most parser generators
- LL parsers and recursive descent
- Continue reading ch. 3

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