

# Topics in Probabilistic and Statistical Databases

## Lecture 10: Sampling and Review

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# References

- Towards Estimation Error Guarantees for Distinct Values, Charikar, Chaudhuri, Motwani, Narasayya, PODS 2000
- Sampling-Based Estimation of the Number of Distinct Values of an Attribute, Haas, Naughton, Seshadri, Stokes, VLDB 1995

# Distinct Values

- Problem definition:
- Data set with  $n$  tuples
- Column of interest has values  $\{1, \dots, D\}$
- Let  $n_i$  = number of times value  $i$  occurs
- $n = \sum_{i=1, D} n_i$
- Goal: estimate  $D$ , denote the estimate  $\check{D}$
- Error is  $\check{D}/D$ , or  $D/\check{D}$ , whichever is  $> 1$

# Negative Result

**Theorem** [Charikar'00] Consider any (possibly adaptive and randomized) estimator  $\check{D}$  for the number of distinct values  $D$  that examines at most  $r$  rows in a table with  $n$  rows. Then, for any  $\gamma > \exp(-r)$ , there exist a choice of the input data such that with probability at least  $\gamma$ :

$$\text{error}(\check{D}) \geq \sqrt{(n-r)/2r * \ln(1/\gamma)}$$

Proof in class

# Estimators

- Goodman's unbiased estimator
- Many specialized estimators from the statistics literature (won't discuss; see [Haas'95])
- GEE [Charikar'95]; will discuss because it matches the lower bound

# Notations

- Select random sample of size  $r$
- $d$ =number of distinct values in the sample
- $f_i$ =number of distinct values that occur exactly  $i$  times
- Thus:  $d = \sum_{i=1,r} f_i$        $r = \sum_{i=1,r} i * f_i$

# Goodman's Unbiased Estimator

Goodman proved in 1949 that:

- If  $r \geq \max(n_1, \dots, n_D)$  then there exists only one unbiased estimator:

$$\hat{D}_{\text{Good}} = d + \sum_{i=1}^n (-1)^{i+1} \frac{(N - r + i - 1)! (r - i)!}{(N - r - 1)! r!} f_i$$

- If  $r < \max(n_1, \dots, n_D)$  then there exists no unbiased estimator

Very unstable, with errors of 20,000%

# The GEE Estimator

**Definition** The GEE is:  $\check{D} = \sqrt{n/r} f_1 + \sum_{i=2,r} f_i$

**Theorem.** Expected ratio error is  $O(\sqrt{n/r})$



# Review of this Course

Three areas in Probabilistic and Statistical  
Databases

- Explicit probabilities
- Implicit probabilities
- Statistics

# Explicit Probabilistic Data

- “Classical” probabilistic databases
- Each tuple has a probability value
  - “maybe-tuple”
  - “x-tuple”
- Possible worlds semantics

# Explicit Probabilistic Data

- What are some key applications ?
- What is lineage and why is it important ?

# Explicit Probabilistic Data

- Rule of thumb 1:
  - ProbDB = IncompleteDB + Probabilities
- Rule of thumb 2:
  - ProbDB = Disjoint/IndependentDB + Joins
- Rule of thumb 3:
  - GM Factorization = DB-normalization + probabilities

# Explicit Probabilistic Data

Query Evaluation is #P hard in general:

- General methods: Monte Carlo, OBDDs, ...
- Safe queries and safe plans
- Top k query answering

# Explicit Probabilistic Data

- Major Open Research Problems  
[IN CLASS]

# Implicit Probabilistic Data

- All tuples have the same probability
- What are the major differences from explicit probabilistic data ?

# Implicit Probabilistic Data

- Dense random graphs
  - $\Pr(t) = 1/2$
- Fagin's 0/1 law for FO
  - For every sentence  $\varphi$ ,  $\lim \Pr(\varphi) = 0$  or  $=1$
- “Theory of almost certain sentences” = ?
- “**THE** random graph” = ?



# Implicit Probabilistic Data

- Material random graphs:
  - $\Pr(t) = \beta / n^{\text{arity}(R)}$
- Every conjunctive query has an explicit asymptotic formula:
  - $\Pr(q) = C(q) / n^{\text{exp}(q)} + O(n^{\text{exp}(q)+1})$

# Implicit Probabilistic Data

- General Random Graphs:  $G(n,p)$   
[WHAT IS THAT ?]
- Erdos and Renyi's theorem
- Random graphs  $G(n, \beta/n^\alpha)$ :
  - Threshold values for  $\alpha$  (no 0/1 laws):  
 $2, 1+1/2, 1+1/3, \dots, 1+1/k, \dots 1, [\text{rationals}], 0$
  - Everywhere else: 0/1 Law for FO

# Implicit Probabilistic Data

- The major applications today:
  - ?
  
- ... but great theory !

# Implicit Probabilistic Data

- Research topics: [IN CLASS]

# Data Statistics

- What is their main usage in database systems ?

# Data Statistics

- Histograms
  - Eqwidth, eqdepth, V-optimal
- Sampling
  - Sequential sampling techniques
  - Join synopses

# Data Statistics

- Limitations of how data statistics are used today: [IN CLASS]
- Major research topics in data statistics: [IN CLASS]

# Final Thoughts

- Computer Science in the past:
  - Driven by better algorithms
- Computer Science today:
  - Driven by massive amounts of data
  - Processed with approximate methods
  - Data itself is often imprecise
- Computer Science tomorrow:
  - Probabilistic databases ☺