Software Model Checking Improving Security of a Billion Computers

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Microsoft Research

# Acknowledgments

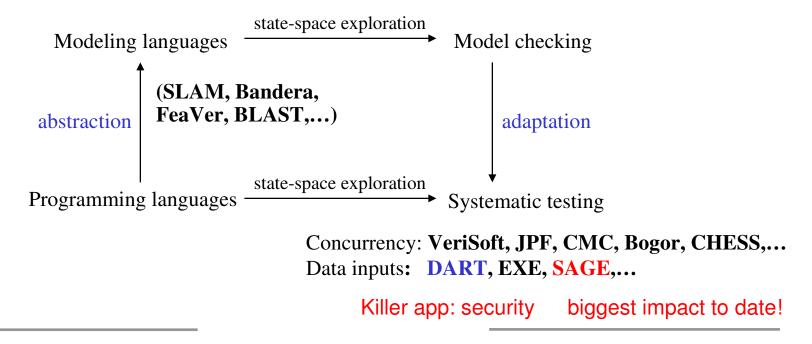
- Joint work with Michael Levin (CSE) and others:
  - Chris Marsh, Lei Fang, Stuart de Jong (CSE)
  - interns Dennis Jeffries (06), David Molnar (07),
     Adam Kiezun (07), Bassem Elkarablieh (08), ...
- Thanks to the entire SAGE team and users !
  - MSR: Ella Bounimova,...
  - Z3: Nikolaj Bjorner, Leonardo de Moura,...
  - WEX (Windows): Nick Bartmon, Eric Douglas,...
  - Office: Tom Gallagher, Octavian Timofte,...
  - SAGE users all across Microsoft!

# References

- see <u>http://research.microsoft.com/users/pg</u>
  - DART: Directed Automated Random Testing, with N. Klarlund and K. Sen, PLDI'2005
  - Compositional Dynamic Test Generation, POPL'2007
  - Automated Whitebox Fuzz Testing, with M. Levin and D. Molnar, NDSS'2008
  - Demand-Driven Compositional Symbolic Execution, with S. Anand and N. Tillmann, TACAS'2008
  - Grammar-Based Whitebox Fuzzing, with A. Kiezun and M. Levin, PLDI'2008
  - Active Property Checking, with M. Levin and D. Molnar, EMSOFT'2008
  - Precise Pointer Reasoning for Dynamic Test Generation, with B. Elkarablieh and M. Levin, ISSTA'2009

# A Brief History of Software Model Checking

- How to apply model checking to analyze software?
  - "Real" programming languages (e.g., C, C++, Java),
  - "Real" size (e.g., 100,000's lines of code).
- Two main approaches to software model checking:



# Security is Critical (to Microsoft)

- Software security bugs can be very expensive:
  - Cost of each Microsoft Security Bulletin: \$Millions
  - Cost due to worms (Slammer, CodeRed, Blaster, etc.): \$Billions
- Most security exploits are initiated via files or packets
  - Ex: Internet Explorer parses dozens of file formats
- Security testing: "hunting for million-dollar bugs"
  - Write A/V (always exploitable), Read A/V (sometimes exploitable), NULL-pointer dereference, division-by-zero (harder to exploit but still DOS attacks), etc.

# Hunting for Security Bugs

- Main techniques used by "black hats":
  - Code inspection (of binaries) and
  - Blackbox fuzz testing
- Blackbox fuzz testing:
  - A form of blackbox random testing [Miller+90]
  - Randomly fuzz (=modify) a well-formed input
  - Grammar-based fuzzing: rules that encode "well-formed"ness + heuristics about how to fuzz (e.g., using probabilistic weights)
- Heavily used in security testing
  - Ex: July 2006 "Month of Browser Bugs"
  - Simple yet effective: many bugs found this way...
  - At Microsoft, fuzzing is mandated by the SDL

#### I am from Belgium too!





INUVEINDER LUUZ

# Blackbox Fuzzing

- Examples: Peach, Protos, Spike, Autodafe, etc.
- Why so many blackbox fuzzers?
  - Because anyone can write (a simple) one in a week-end!
  - Conceptually simple, yet effective...
- Sophistication is in the "add-on"
  - Test harnesses (e.g., for packet fuzzing)
  - Grammars (for specific input formats)
- Note: usually, no principled "spec-based" test generation
  - No attempt to cover each state/rule in the grammar
  - When probabilities, no global optimization (simply random walks)

# Introducing Whitebox Fuzzing

- Idea: mix fuzz testing with dynamic test generation
  - Symbolic execution
  - Collect constraints on inputs
  - Negate those, solve with constraint solver, generate new inputs
  - do "systematic dynamic test generation" (=DART)
- Whitebox Fuzzing = "DART meets Fuzz"

Two Parts:

- 1. Foundation: DART (Directed Automated Random Testing)
- 2. Key extensions ("Whitebox Fuzzing"), implemented in SAGE

## Automatic Code-Driven Test Generation

Problem:

Given a sequential program with a set of input parameters, generate a set of inputs that maximizes code coverage

= "automate test generation using program analysis"

This is not "model-based testing" (= generate tests from an FSM spec)

# How? (1) Static Test Generation

- Static analysis to partition the program's input space [King76,...]
- Ineffective whenever symbolic reasoning is not possible
  - which is frequent in practice... (pointer manipulations, complex arithmetic, calls to complex OS or library functions, etc.)

```
Example:
```

```
int obscure(int x, int y) {
    if (x==hash(y)) error();
    return 0;
}
```

```
Can't statically generate
values for x and y
that satisfy "x==hash(y)" !
```

# How? (2) Dynamic Test Generation

- Run the program (starting with some random inputs), gather constraints on inputs at conditional statements, use a constraint solver to generate new test inputs
- Repeat until a specific program statement is reached [Korel90,...]
- Or repeat to try to cover ALL feasible program paths:
   DART = Directed Automated Random Testing
  - = systematic dynamic test generation [PLDI'05,...]
    - detect crashes, assertion violations, use runtime checkers (Purify,...)

#### DART = Directed Automated Random Testing

```
Example:

int obscure(int x, int y)

if (x==hash(y)) error();

return 0;

}

Run 1:- start with (random) x=33, y=42

- execute concretely and symbolically:

if (33 != 567) | if (x != hash(y))

constraint too complex

simplify it: x != 567

- solve: x==567 solution: x=567

- new test input: x=567, y=42

Run 2: the other branch is executed

All program paths are now covered !
```

- Observations:
  - Dynamic test generation extends static test generation with additional runtime information: it is more powerful
  - The number of program paths can be infinite: may not terminate!
  - Still, DART works well for small programs (1,000s LOC)
  - Significantly improves code coverage vs. random testing

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# DART Implementations

- Defined by symbolic execution, constraint generation and solving
  - Languages: C, Java, ×86, .NET,...
  - Theories: linear arith., bit-vectors, arrays, uninterpreted functions,...
  - Solvers: lp\_solve, CVCLite, STP, Disolver, Z3,...
- Examples of tools/systems implementing DART:
  - EXE/EGT (Stanford): independent ['05-'06] closely related work
  - CUTE = same as first DART implementation done at Bell Labs
  - SAGE (CSE/MSR) for x86 binaries and merges it with "fuzz" testing for finding security bugs (more later)
  - PEX (MSR) for .NET binaries in conjunction with "parameterized-unit tests" for unit testing of .NET programs
  - YOGI (MSR) for checking the feasibility of program paths generated statically using a SLAM-like tool
  - Vigilante (MSR) for generating worm filters
  - BitScope (CMU/Berkeley) for malware analysis
  - CatchConv (Berkeley) focus on integer overflows
  - Splat (UCLA) focus on fast detection of buffer overflows
  - Apollo (MIT) for testing web applications

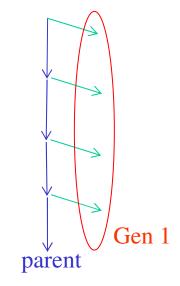
...and more!

# DART Summary

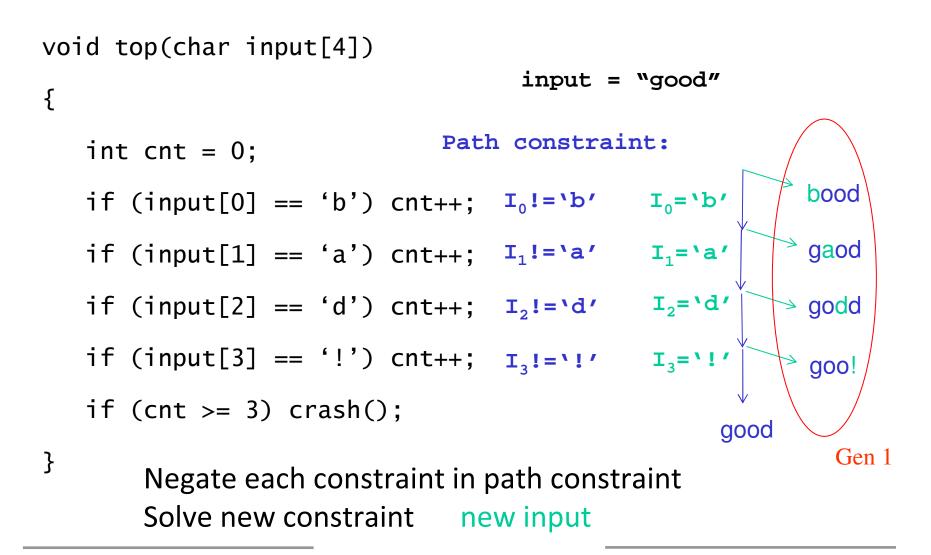
- DART attempts to exercise all paths (like model checking)
  - Covering a single specific assertion (verification): hard problem (often intractable)
  - Maximize path coverage while checking thousands of assertions all over: easier problem (optimization, best-effort, tractable)
  - Better coverage than pure random testing (with directed search)
- DART can work around limitations of symbolic execution
  - Symbolic execution is an adjunct to concrete execution
  - Concrete values are used to simplify unmanageable symbolic expressions
  - Randomization helps where automated reasoning is difficult
- Comparison with static analysis:
  - No false alarms (more precise) but may not terminate (less coverage)
  - "Dualizes" static analysis: static may vs. DART must
    - Whenever symbolic exec is too hard, under-approx with concrete values
    - If symbolic execution is perfect, no approx needed: both coincide!

# Whitebox Fuzzing [NDSS'08]

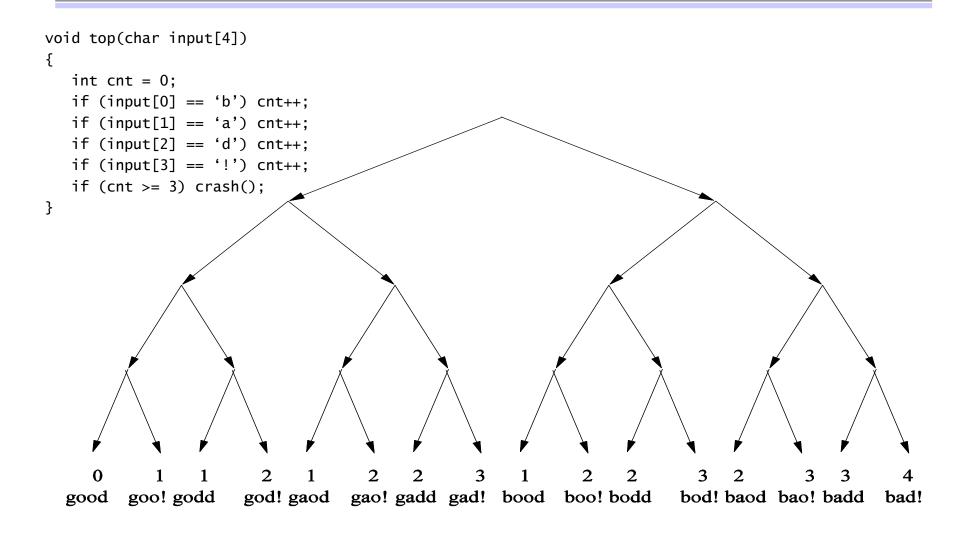
- Whitebox Fuzzing = "DART meets Fuzz"
- Apply DART to large applications (not unit)
- Start with a well-formed input (not random)
- Combine with a generational search (not DFS)
  - Negate 1-by-1 each constraint in a path constraint
  - Generate many children for each parent run
  - Challenge all the layers of the application sooner
  - Leverage expensive symbolic execution
- Search spaces are huge, the search is partial...
   yet effective at finding bugs !



# Example



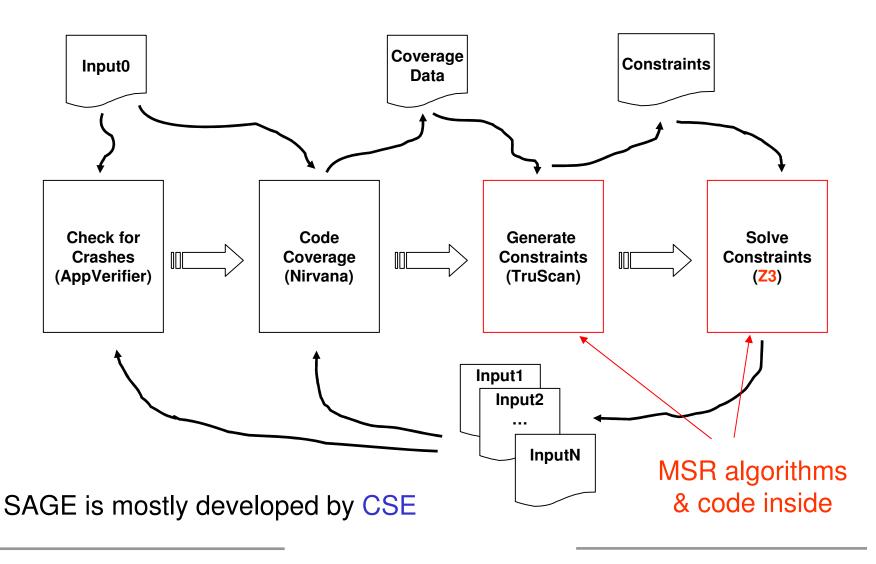
#### The Search Space



#### SAGE (Scalable Automated Guided Execution)

- Generational search introduced in SAGE
- Performs symbolic execution of x86 execution traces
  - Builds on Nirvana, iDNA and TruScan for x86 analysis
  - Don't care about language or build process
  - Easy to test new applications, no interference possible
- Can analyse any file-reading Windows applications
- Several optimizations to handle huge execution traces
  - Constraint caching and common subexpression elimination
  - Unrelated constraint optimization
  - Constraint subsumption for constraints from input-bound loops
  - "Flip-count" limit (to prevent endless loop expansions)

## SAGE Architecture



### Some Experiments

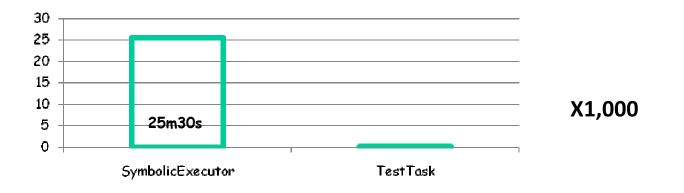
Most much (100x) bigger than ever tried before!

Seven applications - 10 hours search each

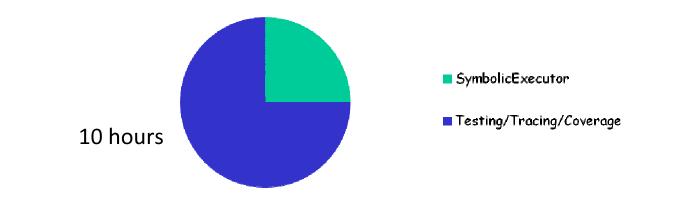
| App Tested                | #Tests | Mean Depth | Mean #Instr. | Mean Input<br>Size |  |
|---------------------------|--------|------------|--------------|--------------------|--|
| ANI                       | 11468  | 178        | 2,066,087    | 5,400              |  |
| Media1                    | 6890   | 73         | 3,409,376    | 65,536             |  |
| Media2                    | 1045   | 1100       | 271,432,489  | 27,335             |  |
| Media3                    | 2266   | 608        | 54,644,652   | 30,833             |  |
| Media4                    | 909    | 883        | 133,685,240  | 22,209             |  |
| Compressed<br>File Format | 1527   | 65         | 480,435      | 634                |  |
| OfficeApp                 | 3008   | 6502       | 923,731,248  | 45,064             |  |

#### Generational Search Leverages Symbolic Execution

Each symbolic execution is expensive



• Yet, symbolic execution does not dominate search time



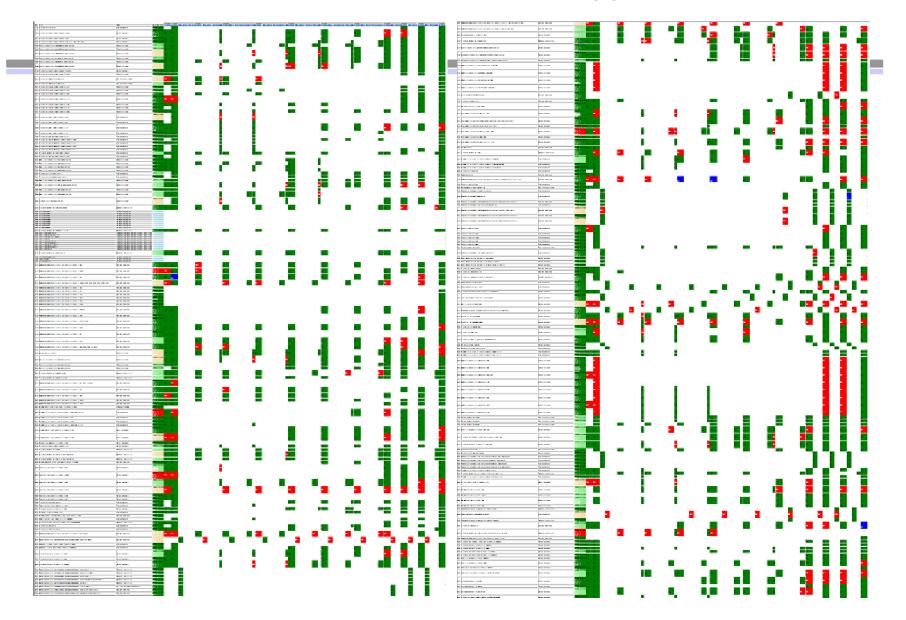
# SAGE Results

#### Since April'07 1<sup>st</sup> release: many new security bugs found (missed by blackbox fuzzers, static analysis)

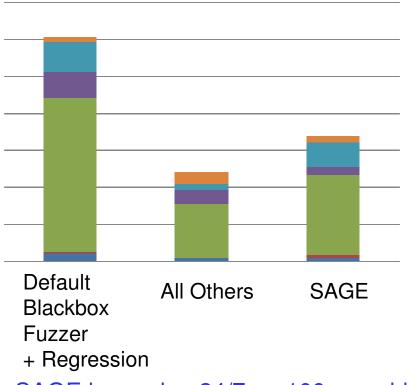
- Apps: image processors, media players, file decoders,...
- Bugs: Write A/Vs, Read A/Vs, Crashes,...
- Many triaged as "security critical, severity 1, priority 1" (would trigger Microsoft security bulletin if known outside MS)
- Example: WEX Security team for Win7
  - Dedicated fuzzing lab with 100s machines
  - 100s apps (deployed on 1billion+ computers)
  - ~1/3 of all fuzzing bugs found by SAGE !
- SAGE = gold medal at Fuzzing Olympics organized by SWI at BlueHat'08 (Oct'08)
- Credit due to entire SAGE team + users !



#### WEX Fuzz Dashboard Snippet



# WEX Fuzzing Lab Bug Yield for Win7



How fuzzing bugs found (2006-2009) :

SAGE is running 24/7 on 100s machines: "the largest usage ever of any SMT solver" N. Bjorner + L. de Moura (MSR, Z3 authors)

- 100s of apps, total number of fuzzing bugs is confidential
- But SAGE didn't exist in 2006
- Since 2007 (SAGE 1<sup>st</sup> release), ~1/3 bugs found by SAGE
- But SAGE currently deployed on only ~2/3 of those apps
- Normalizing the data by 2/3, SAGE found ~1/2 bugs
- SAGE is more CPU expensive, so it is run last in the lab, so all SAGE bugs were missed by everything else!

- Starting with 100 zero bytes ...
- SAGE generates a crashing test for Medial parser:

0000000h: 00000020h: ; 00 00 00 00 ; 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00000040h: ; 00 00 00 00 ; 0000060h: 00 00 00 00 ;

Generation 0 – seed file

- Starting with 100 zero bytes ...
- SAGE generates a crashing test for Medial parser:

00000000h: 52 49 46 46 00 00 00 00 00 00 00 00 00 00 00 00 ; RIFF.. 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; 00000010h: 00 00 00 00 ; 0000020h: 00 00 00 00 00 00 00 00 00 00 00 00 . . . . . . . . . . . . 00 00 00 00 ; 00000040h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; 00 00 00 00 ; 0000060h: 00 00 00 00

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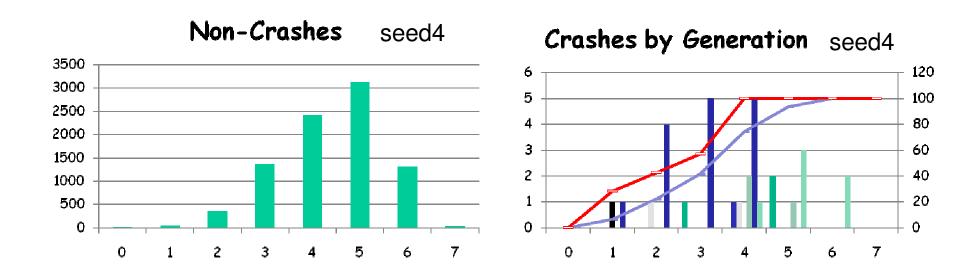
Generation 10 – crash bucket 1212954973!

Found after only 3 generations starting from seed3 file on next slide

## Different Seed Files, Different Crashes

| Bucket     | seed1   | seed2     | seed3     | seed4                   | seed5           | 100<br>zero<br>bytes |
|------------|---------|-----------|-----------|-------------------------|-----------------|----------------------|
| 1867196225 | X       | x         | X         | ×                       | X               |                      |
| 2031962117 | ×       | ×         | X         | ×                       | X               |                      |
| 612334691  |         | ×         | X         |                         |                 |                      |
| 1061959981 |         |           | X         | ×                       |                 |                      |
| 1212954973 |         |           | X         |                         |                 | ×                    |
| 1011628381 |         |           | X         | ×                       |                 | ×                    |
| 842674295  |         |           |           | ×                       |                 |                      |
| 1246509355 |         |           | ×         | ×                       |                 | ×                    |
| 1527393075 |         |           |           |                         | X               |                      |
| 1277839407 |         |           |           |                         | X               |                      |
| 1951025690 |         |           | X         | For the first time, we  | e tace bug tria | age issue            |
| Media1:    | 60 mach | ine-hours | , 44598 t | total tests, 357 crashe | es, 12 unique b | ouckets              |
| JW Seminar |         |           |           | Page 36                 |                 | November             |

# Most Bugs Found are "Shallow"



# SAGE Summary

- SAGE is so effective at finding bugs that, for the first time, we face "bug triage" issues with dynamic test generation
- What makes it so effective?
  - Works on large applications (not unit test)
  - Can detect bugs due to problems across components
  - Fully automated (focus on file fuzzing)
  - Easy to deploy (x86 analysis any language or build process !)
  - Now, used daily in various groups inside Microsoft

## More On the Research Behind SAGE

- Challenges:
  - How to recover from imprecision in symbolic execution? PLDI'05
  - How to scale symbolic exec. to billions of instructions? NDSS'08
  - How to check efficiently many properties together? EMSOFT'08
  - How to leverage gram. specs for complex input formats? PLDI'08
  - How to deal with path explosion in large prgms? POPL'07, TACAS'08
  - How to reason precisely about pointers? ISSTA'09
  - + research on constraint solvers (Z3, disolver,...)

# Extension: Active Property Checking

- Traditional property checkers are "passive"
  - Purify, Valgrind, AppVerifier, TruScan, etc.
  - Check only the current concrete execution
  - Can check many properties at once
- Combine with symbolic execution "active"
  - Reason about all inputs on same path
  - Apply heavier constraint solving/proving
  - "Actively" look for input violating property
- Ex: array ref a[i] where i depends on input, a is of size c
  - Try to force buffer over/underflow: add "(i < 0) OR (i >= c)" to the path constraint; if SAT, next test should hit a bug!
- Challenge: inject/manage all such constraints efficiently...

# Ext.: Compositionality = Key to Scalability

- Problem: executing all feasible paths does not scale !
- Idea: compositional dynamic test generation
  - use summaries of individual functions (arbitrary program blocks) like in interprocedural static analysis
  - If f calls g, test g separately, summarize the results, and use g's summary when testing f
  - A summary  $\varphi(g)$  is a disjunction of path constraints expressed in terms of input preconditions and output postconditions:

 $\varphi(g) = \lor \varphi(w)$  with  $\varphi(w) = pre(w) \land post(w)$ expressed in terms of g's inputs and outputs

- g's outputs are treated as symbolic inputs to a calling function f
- Can provide same path coverage exponentially faster !

## Some Other Related Work in MSR

- Pex: automatic test generation to the desktop
  - Unit testing, OO languages, .NET managed code, VS integration
  - contracts, rich interfaces, mock-object creation, program repair
- Yogi: combine testing with static analysis
  - Testing is precise but incomplete
  - Static analysis is complete but imprecise
  - SMASH: new compositional may-must algorithm (alternation) [POPL'2010]

Experiments with 69 Win7 device drivers, 85 properties:

 Better constraint solvers (ex: Z3), extend to concurrency (ex: CHESS), Etc. (active area of research)

50

• +

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mpositional-May-DASH

mpositional-Must-DASH

combine

15

### Conclusion: Blackbox vs. Whitebox Fuzzing

- Different cost/precision tradeoffs
  - Blackbox is lightweight, easy and fast, but poor coverage
  - Whitebox is smarter, but complex and slower
  - Note: other recent "semi-whitebox" approaches
    - Less smart (no symbolic exec, constr. solving) but more lightweight: Flayer (taint-flow, may generate false alarms), Bunny-the-fuzzer (taint-flow, source-based, fuzz heuristics from input usage), etc.
- Which is more effective at finding bugs? It depends...
  - Many apps are so buggy, any form of fuzzing find bugs in those !
  - Once low-hanging bugs are gone, fuzzing must become smarter: use whitebox and/or user-provided guidance (grammars, etc.)
- Bottom-line: in practice, use both! (We do at Microsoft)

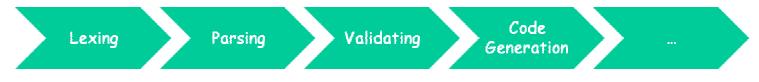
# Future Work (The Big Picture)

- During the last decade, code inspection for standard programming errors has largely been automated with static code analysis
- Next: automate testing (as much as possible)
  - Thanks to advances in program analysis, efficient constraint solvers and powerful computers
- Whitebox testing: automatic code-based test generation
  - Like static analysis: automatic, scalable, checks many properties
  - Today, we can exhaustively test small applications, or partially test large applications
  - Biggest impact so far: whitebox fuzzing for (Windows) security testing
    - Improved security for a billion computers worldwide!
  - Next: towards exhaustive testing of large applications (verification)
  - How far can we go?

# Back-up Slides

# Ext.: Grammar-Based Whitebox Fuzzing

- Input precondition specified as a context-free grammar
- Avoids path explosion in lexer and parser



 Faster, better and deeper coverage for applications with structured inputs (XML, etc.)

| generation strategy<br>(each ran 2 hours) | #inputs | total<br>coverage | coverage in<br>code gen |
|---|---------|-------------------|-------------------------|
| blackbox fuzzing                          | 8658    | 14%               | 51%                     |
| whitebox fuzzing                          | 6883    | 15%               | 54%                     |
| grammar-based blackbox fuzzing            | 7837    | 12%               | 61%                     |
| grammar-based whitebox fuzzing            | 2378    | 20%               | 82%                     |