

## Efficient Key Distribution for Secure Multicast

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## Multicast Security

- Multicast is broadcast to a group, not to everyone.
- Multicast group – group of members who have a right (have paid) to be in the group.
- Applications
  - Pay-per-view live broadcast
  - Video-on-demand for a fee
  - Software update group
  - Authorized for database access

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## Key Distribution Problem

- Group key to secure content
  - Change (**re-key**) on membership change
    - *ADD(u)* - u does not have access to data prior to operation, but does after operation
    - *DELETE(u)* - u does not have access to data after operation
  - Distribute group key to current members
    - Additional keys needed to secure group key

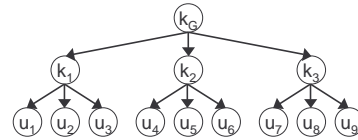
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## Logical Key Trees

(Wong *et al.*, 1998)  
(Wallner *et al.*, 1998)

- Shows keys held by each member
  - Nodes represent keys
  - Leaf nodes represent members
  - Members hold all keys on path to root

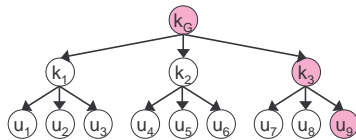


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## Encryption

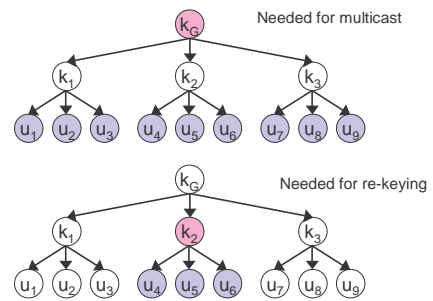
- Each member  $i$  has a private key  $u_i$  which is distributed using public key encryption.
- Each key  $k_g$  encrypts data multicast to the leaves of the tree rooted at  $g$ .
- Member  $i$  holds all the keys on its path to the root.



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## Group keys



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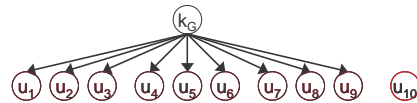
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## Re-keying Messages

- $E(k_a, k_g)$  is a message to the group rooted at  $g$  that is encrypted using  $k_g$  and contains a new key  $k_a$  for some ancestor  $a$  of  $g$ .
- Goal is to minimize the number of these re-keying messages.

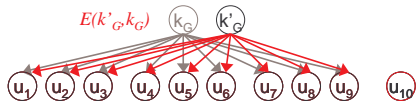
## Re-keying (ADD)

- 2 level tree
- $ADD(u)$  requires 2 messages per key
- Example:  $ADD(u_{10})$



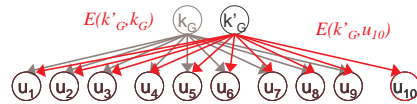
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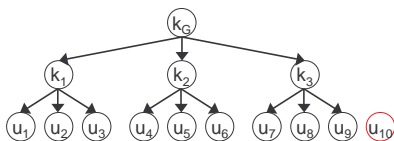
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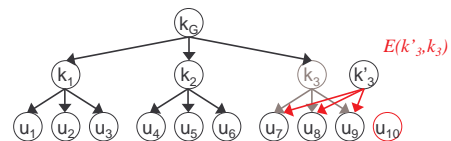
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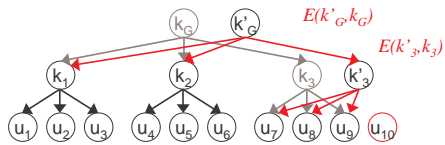
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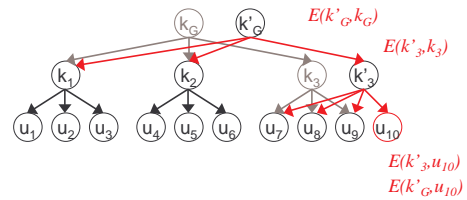


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### Re-keying (ADD)

- Example:  $ADD(u_{10})$

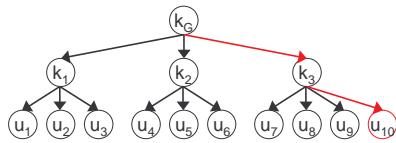


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### Re-keying (ADD)

- Define  $d_u$  to be the depth of  $u$ .
- $ADD(u)$  cost is  $2d_u$  messages

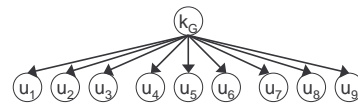


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### Re-keying (DELETE)

- $DELETE(u)$  requires a linear number of messages, each of the form  $E(k'_G, u_i)$

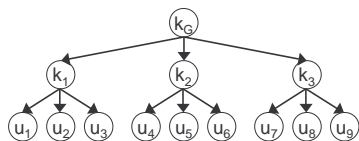


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### Re-keying (DELETE)

- Example:  $DELETE(u_9)$

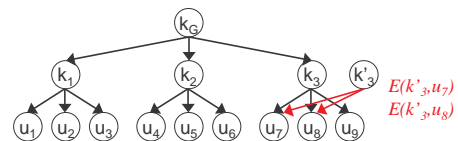


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### Re-keying (DELETE)

- Example:  $DELETE(u_9)$

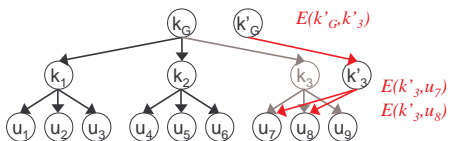


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## Re-keying (DELETE)

- Example:  $DELETE(u_9)$

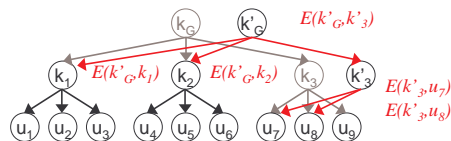


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## Re-keying (DELETE)

- Example:  $DELETE(u_9)$

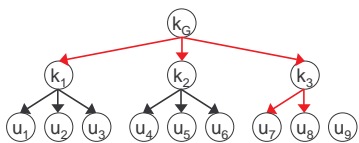


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## Re-keying (DELETE)

- Define **ancestor weight**  $w_u$  to be sum of degrees on path from  $u$  to root
- $DELETE(u)$  cost is  $w_u - 1$  messages



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## Asymmetry

- ADD and DELETE have different costs
  - ADD  $2d_u$
  - DELETE  $w_u - 1$
- ADD has more freedom than DELETE
  - ADD can go anywhere in the tree
  - DELETE is where it happens

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## Fundamental Problem

- What is the best key tree for a given mix of ADDs and DELETES?
- Our approach is to use balanced trees.
- Evaluation of the approach
  - Theoretical worst case analysis
  - Simulation studies

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## Previous Results

(Poovendran and Baras, 2001)  
(Snoeyink et al., 2001)

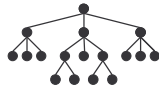
- Amortized worst-case cost lower bound is  $\Omega(\log n)$  per operation.
- Constructed static multiway trees that are optimal for ancestor weight.

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## Cost Components for On-line Algorithms

- **Tree structure cost** due to  $w_u$
- **Restructuring cost** to maintain structure



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## Algorithms

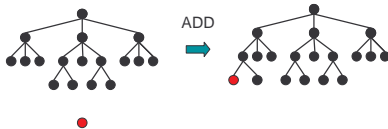
- K-ary trees
- B-trees
- 2-k trees (like AVL trees)
- Weight balanced trees

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## K-ary Trees (Wong *et al.*, 2000)

- **ADD(u)** - insert into the tree to keep  $w_u$  as small as possible.
- **DELETE(u)** - simple remove it at cost  $w_u$ 
  - If only one child, then collapse



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## B-Tree Algorithm

- All leaves have same depth
- All internal nodes (except the root) have degree in the interval  $[\lceil t/2 \rceil, t]$ , where  $t$  is the order of the B-tree.
- Use existing algorithms for maintaining B-Tree property
  - John Hopcroft, 2-3 trees, 1970
  - Bayer and McCreight, 1972.

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## Height-Balanced 2-k Algorithm

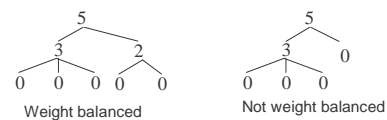
- All nodes are balanced
  - Height of children differ by at most 1
- All internal nodes have degree in the interval  $[2, k]$
- Extension of the AVL tree algorithm of Rodeh *et al.* (2001)

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## Weight-balanced Algorithm

- **Node weight** of  $u = \max w_i$  over all leaf nodes  $i$  in sub-tree rooted at  $u$
- Node  $u$  is **weight-balanced** if its children differ in node weight by at most 1



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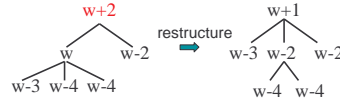
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## Weight-balanced Algorithm

- $DELETE(u)$  costs proportional to ancestor weight  $w_u$
- How about balancing by  $w_u$ ?
  - Can be done for 2-3 and 2-3-4 trees

## Weight-balanced Algorithm

- Defined restructuring rules to maintain balance
- Apply to key tree bottom up
- Example for 2-3 trees



## Worst-case Tree Structure Cost Analysis

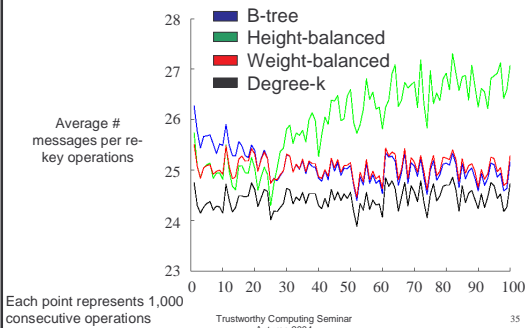
- Optimal worst-case bound is  $\lceil 3 \log_3 n \rceil$
- Derived worst-case bounds for our algorithms

Algorithm	$w_u$	Algorithm Bound
		Optimal Bound
Height-balanced 2-4	$4 \log_b n$ $\phi \approx 1.618$	$\approx 3.04$
B-tree of order 4	$4 \log_2 n$	$\approx 2.11$
Weight-balanced 2-3-4	$\log_b n$ $b \approx 1.325^*$	$\approx 1.30$

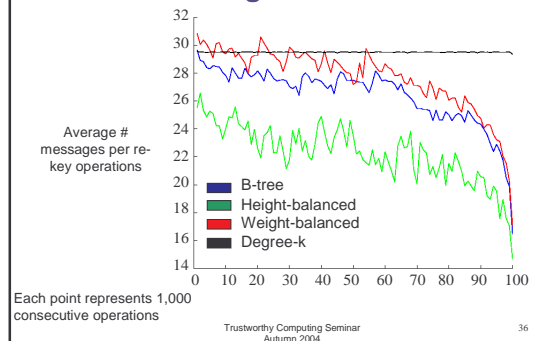
## Simulation Results

- Does good tree structure help performance?
  - We do not have a way to analyze restructuring cost
  - Trace data for multicast is problematic
- Simulation may yield insights

## Random Re-keying



## Pathological Deletions



### **Summary: Online Key Tree Algorithms**

- Algorithms to maintain balanced trees
- Identified 2 cost components
- Derived worst-case tree weight bounds
- Good performance, especially when tree becomes highly unbalanced

### **Future Potential**

- Crypto technology is probably adequate for deployment
- Future depends on popularity of multicast
- May be other distributed applications that need secure group management
  - Access control in databases
  - Access control in file systems