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Abstract:

Two Bayesian models for text classification from the information science field were extended and applied to student produced essays. Both models were calibrated using 462 essays with two score points. The calibrated systems were applied to 80 new, pre-scored essays with 40 essays in each score group. Manipulated variables included the two models; the use of words, phrases and arguments; two approaches to trimming; stemming; and the use of stopwords. While the text classification literature suggests the need to calibrate on thousands of cases per score group, accuracy of over 80% was achieved with the sparse dataset used in this study.



Automated Essay Scoring Using Bayes' Theorem

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> It is not surprising that extended response items, typically short essays, are now an integral part of most large scale assessments. Extended response items provide an opportunity for students to demonstrate a wide range of skills and knowledge including higher-order thinking skills such as synthesis and analysis. Yet assessing students' writing is one of the most expensive and time consuming activities for assessment programs. Prompts need to be designed, rubrics created, multiple raters need to be trained and then the extended responses need to be scored, typically by multiple raters. With different people evaluating different essays, interrater reliability becomes an additional concern in the assessment process. Even with rigorous training, differences in the background training and experience of the raters can lead to subtle but important differences in grading (Blok & de Glopper, 1992).

> Computers and artificial intelligence have been proposed as tools to facilitate the evaluation of student essays. In theory, computer scoring can be faster, reduce costs, increase accuracy, and eliminate concerns about rater consistency and fatigue. Further, the computer can quickly rescore materials should the scoring rubric be redefined. Using different methods, Page (1966, 1994), Landauer, Holtz, and Laham (1998), and Burstein (1999) report very high correlations between human judgment and computer generated scores. Page uses a regression model with surface features of the text (document length, word length, and punctuation) as the independent variables and the essay score as the dependent variable. The approach by Landauer et al. (1998) is a factor-analytic model of word cooccurrences which emphasizes essay content. Burstein (1999) uses an eclectic model with different content features.

> This paper presents an approach to essay scoring that builds on the text classification literature in the information science field and incorporates Bayesian Networks.¹ In recent years, Bayesian Networks have become widely accepted and increasingly used in the statistics, medical, and business communities. The most visible Bayesian Networks are undoubtedly the ones embedded in Microsoft products, including the Answer Wizard of Office 95, the Office Assistant (the bouncy paperclip guy) of Office 97, and over 30 Technical Support Troubleshooters. Other prominent applications include risk assessment, medical diagnosis, data mining, and interactive troubleshooting. In education, Bayesian techniques have been applied to adaptive testing and intelligent learning systems (Welch and Frick, 1993) and are described in Rudner (2002).

Related Literature

Computer Grading Using Bayesian Networks

Several studies have reported favorably on computer grading of essays. The current systems have returned grades that correlated significantly and meaning-fully with human raters. A review of the research on Landauer's approach, Latent Semantic Analysis(LSA), found that its scores typically correlate as well with human raters as the raters do with each other, occasionally correlating less well, but occasionally correlating better (Chung & O'Neil, 1997). Research on Page's approach, Project Essay Grade (PEG), consistently reports superior correlations between PEG and human graders relative to correlations between human graders (e.g., Page, Poggio, & Keith, 1997). E-rater was deemed so impressive it is now operational and is used in scoring the General Management Aptitude Test (GMAT).²

Our approach to computer grading of essays can be viewed as an extension of Bayesian computer adaptive testing which has been described by Welch and Frick (1993), and Madigan, Hunt, Levidow, and Donnell (1995). With Bayesian CAT, the goal is to determine the most likely classification for the examinee, typically master/non-master based on optimally selected items. With Bayesian essay scoring, we extend the desired classification to a three- or four-point categorical or nominal scale (e.g., *extensive, essential, partial, unsatisfactory*) and use a large set of *items*. The *items* in our Bayesian essay scoring approach are a broad set of essay features including content features (specific words, phrases), and other essay characteristics such as the order certain concepts are presented and the occurrence of specific noun-verb pairs.

To explain Bayesian essay scoring, we will provide a simple example where the goal is to classify an examinee's response as being either complete, partially complete, or incomplete. As givens, we will have a collection of essay features for which we have determined the following three probabilities: 1) Probability that the feature is included in the essay given that the examinee has provided an appropriate response, 2) probability that the feature is included in the essay given that the examinee has provided a partially-appropriate response, and 3) probability that the feature is included in the essay given that the examinee has provided an inappropriate response. We will denote these as $P_i(u_i=1|A)$, $P_i(u_i=1|R)$, and $P_i(u_i=1|I)$, respectively; the subscript *i* denotes that we have different probabilities for each feature *i*, $u_i=1$ denotes that the essay included feature *i*, and *A*, *R*, and *I* denote the essay score as *Appropriate, Partial*, and *Inappropriate*, respectively. Here, these conditional probabilities will be determined from a large collection of essays scored by expert-trained human raters.

Automated Essay Scoring Using Bayes' Theorem

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Appropriate $P_i(u_i=1 A)$	Partial $P_i(u_i=1 R)$	Inappropriate $P_i(u_i=1 I)$			
.7	.6	.1			

As an example, consider an essay feature with the following conditional probabilities:

The goal is to classify the examinee essay as most likely being Appropriate, Partial, or Inappropriate based on essay features. Lacking any other information about the examinee's ability, we will assume equal prior probabilities (i.e., P(A)=.33, P(R)=.33 and P(I)=.33). After examining each feature, we will update P(A), P(R), and P(I) based on whether the feature was included in the student's essay. The updated values for P(A), P(R), and P(I) are referred to as the posterior probabilities. The process for computing these updated probabilities is referred to as Bayesian updating, belief updating (probabilities being a statement of belief), or evaluating the Bayesian network. The algorithm for updating comes directly from Bayes Theorem: P(A|B) * P(B) = P(B|A) * P(A).

Let us suppose our examinee essay contains the sample feature. By Bayes Theorem, the new probability that the essay is Appropriate is $P(A|u_i=1) = P(u_i=1|A) * P(A) / P(u_i=1)$

We know that the examinee responded correctly, so $P(u_i=1)=1.00$ and $P(A|u_i=1) = .7 * .33 = .233$. Similarly, $P(R|u_i=1) = P(u_i=1|R) * P(R) = .6 * .33 = .200$, and $P(I|u_i=1) = P(u_i=1|I) * P(I) = .1 * .33 = .033$. We can then divide by the sum of these joint probabilities to obtain posterior probabilities (i.e., P'(A) = .233 / (.233+.200+.033) = .500, P'(R) = .200 / (.233+.200+.033) = .429, and P'(I) = .033 / (.233+.200+.033) = .071).

At this point, it appears unlikely that the essay is Inappropriate. We next use these posterior probabilities as the new prior probabilities, examine the next feature and again update our estimates for P(A), P(R), and P(I) by computing new posterior probabilities. Under one model, we iterate the process until all calibrated features are examined. In practice, one would expect lower prior probabilities for each feature and the software would examine the presence of a large number of features.

In theory, this approach to computer grading can incorporate the best features of PEG, LSA, and e-rater plus it has several crucial advantages of its own. It can be employed on short essays, is simple to implement, can be applied to a wide range of content areas, can be used to yield diagnostic results, can be adapted to yield classifications on multiple skills, and is easy to explain to non-statisticians.

Models of Test Classification

Two Bayesian models are commonly used in the text classification literature (McCallum & Nigam, 1998). With the multivariate Bernoulli model, each essay is viewed as a special case of all the calibrated features. As in the example illustrated above, the presence or non-presence of all calibrated features is examined. A typical Bayesian Network application, this approach has been used in text classification by Lewis (1992), Kalt and Croft (1996) and others.

Under the multivariate Bernoulli model, the probability essay d_i should receive score classification c_j is

$$P(d_i \mid c_j) = \prod_{t=1}^{V} \left[B_{it} P(w_t \mid c_j) + (1 - B_{it})(1 - P(w_t \mid c_j)) \right]$$

where *V* is the number of features in the vocabulary, $B_{ii} \in (0,1)$ indicates whether feature *t* appears in essay *i* and $P(w_i|c_j)$ indicates the probability that feature w_i appears in a document whose score is c_j . For the multivariate Bernoulli model, $P(w_i|c_j)$ is the probability of feature w_i appearing at least once in an essay whose score is c_j . It is calculated from the training sample as

$$P(w_{t} \mid c_{j}) = \frac{1 + \sum_{i=1}^{D_{j}} B_{it}}{J + D_{j}}$$

where D_j is the number of essays in the training group scored c_j , and J is the number of score groups. The 1 in the numerator and J in the denominator are Laplacian values to adjust for the fact that this is a sample probability and to prevent $P(w_i|c_j)$ from equaling zero or unity. A zero value for $P(w_i|c_j)$ would dominate Equation 1 and render the rest of the features useless.

To score the trial essays, the probabilities that essay d_i should receive score classification c_j given by Equation 1 is multiplied by the prior probabilities and then normalized to yield the posterior probabilities. The score with the highest posterior probability is then assigned to the essay.

With the multinomial model, each essay is viewed as a sample of all the calibrated terms. The probability of each score for a given essay is computed as the product of the probabilities of the features contained in the essay.

(1)

(2)

(3)

(4)

$$P(d_i | c_j) = \prod_{t=1}^{V} \frac{P(w_t | c_j)^{N_{it}}}{N_{it}!}$$

where N_{it} is the number of times feature w_t appears in essay *i*. For the multinomial model, $P(w_t|c_j)$ is the probability of feature w_t being used in an essay whose score is c_i . It is calculated from the training sample as:

$$P(w_t | c_j) = \frac{1 + \sum_{i=1}^{D_j} N_{it}}{V + \sum_{i=1}^{D_i} N_{it}}$$

where *D*. is the total number of documents.

Often used in speech recognition where it is called a "unigram language model," this approach has been used in text classification by Mitchell (1997), McCallum, Rosenfeld, and Mitchell (1998), and others.

The key difference in the models is the computation of $P(w_i|c_j)$. The Bernoulli checks for the presence or absence of the feature in each essay. The multinomial accounts for multiple uses of the feature within an essay. After calibration, when scoring new essays, the multinomial model is computationally much quicker as only the features in a given essay need to be examined. For the multivariate Bernoulli model, all the features in the vocabulary need to be examined. McCallum and Nigam (1998) suggests that with a large vocabulary the multinomial model is more accurate than the Bernoulli model for many classification tasks. That finding, however, may not hold for essays which are typically graded based on the presence or absence of key concepts.

Stemming

Stemming refers to the process of removing suffixes to obtain word roots or stems. For example, *educ* is the common stem for *educate, education, educates, educating, educational,* and *educated.* Because terms with a common stem will often have similar meanings, one might expect a stemmed vocabulary to out perform an unstemmed vocabulary, especially when the number of terms and calibration documents is relatively small. This study incorporated Porter's (1980) widely used stemming algorithm.³

Stopwords

There are large numbers of common articles, pronouns, adjectives, adverbs, and prepositions, such as *the, are, in, and,* and *of,* in the English language. Search engines typically do not index these stopwords as they result in the retrieval of extraneous records. Some text classification studies have reported improved accuracy with trimmed stopwords (Mitchell, 1997).

Feature Selection

Vocabulary size can be manipulated to potentially improve classification accuracy. One approach is to select the items with the highest potential information gain (Cover & Thomas, 1991). The commonly used measure of information from information theory is entropy (Cover & Thomas, 1991; Shannon, 1948). Entropy is defined as:

$$H(S) = \sum_{j=1}^{J} - p_j \log_2 p_j$$

where p_i is the probability of belonging to class *j*.

Entropy can be viewed as a measure of the uniformness of a distribution and has a maximum value when $p_j = 1/J$ for all j. The goal is to have a peaked distribution of p_j . The potential information gain then is the reduction in entropy (i.e.,

where $H(S_0)$ is the initial entropy based on the prior probabilities and $H(S_i)$ is the expected entropy after scoring feature *t*.)

A second approach is to select features with more stable estimates of $P(w_i|c_j)$. Since many features will only appear in one or two essays, this can be accomplished by trimming features based on prevalence as measured by the number of occurrences per 1000 essays.

Research Design

Two Bayesian models for essay scoring were examined, a multivariate Bernoulli model and a multinomial model, using words, two-word phrases, and arguments as the calibrated features. Arguments are defined here as the occurrences of one term before another. For example, a good essay on ecology might use the term poison or toxin before using the word fish. We let the computer identify all such word pairs with one constraint. To eliminate large numbers of word pairs that were likely to be poorly calibrated and non-informative and to improve calibration time, each word within an argument had to occur in at least 2% of the calibrated essays.

(5)

This preliminary investigation analyzed responses to a biology item piloted for the upcoming Maryland High School Assessment (HSA). The typical response was about 75 words. Essays were professionally scored by two raters using a carefully constructed rubric. Rater agreement was 70% and we only examined essays for which the raters agreed. The initial sample had only 542 useable essays across four score levels—a value vastly smaller than the size suggested by the literature. Because the cell sizes of the top and bottom groups were extremely small, the lower two and top two categories were collapsed to two score groups. Forty essays from the lower group and 40 from the top group were randomly selected to be used as the trial sample. The remaining 385 essays from the lower group and 77 essays from the top group were then used as the training or calibration sample. With the cells combined, the equivalent IRT parameters are a=.77, b=.89. If we integrate the probability of a correct response and the Gaussian distribution over theta and use b=.89 as a cut score, then we would expect 76 percent of the essays to receive the correct score.

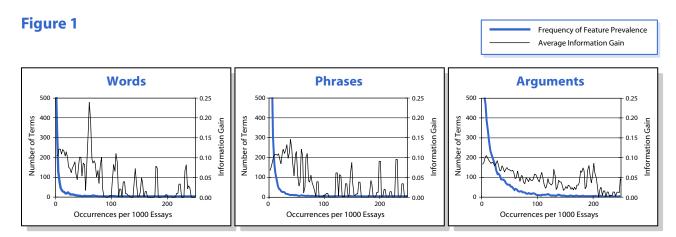
Using this one essay item and a small sample size, we compared the two models; evaluated accuracy for words, phrases and arguments; and examined unstemmed vocabularies, stemmed vocabularies, and vocabularies without stopwords.

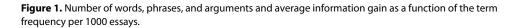
The text classification literature typically calibrates based on thousands of training passages for each category. Recognizing that this literature suggests that our calibration sample is extremely small, we tried two approaches toward feature selection. First we selected features (words, phrases, and arguments) based on the number of times the token appeared per 1000 essays. The higher the frequency the more stable the estimates of $P(w_l|c_j)$, the probability of the token given the essay score. The second approach was to select features based on information gain. The higher the information gain, the better the token is able to discriminate between scores.

Results

The analysis of the 462 calibration essays produced 1,208 unique words and 8,326 unique phrases. In order to reduce the number of infrequent arguments, we identified 15,640 unique arguments that incorporated words that occurred at least 20 times per thousand essays. The vast majority of these words, phrases, and arguments occur infrequently and the associated probabilities of their occurring with specific score categories are not well estimated. There are also terms that are so common, they contribute little to the classification prediction.

Figure 1 shows the relation between feature prevalence as measured by occurrences per 1000 essays, ability to contribute to the prediction as measured by average information gain (thin lines), and the frequency of feature prevalence for words, phrases and arguments (heavy lines). For example, from the middle graph, there are approximately 400 phrases that occur 10 times per 1000 (i.e., in about 1% of the essays). Their average information gain is about .1. The figure shows 1) that the number of terms at each prevalence level drops dramatically as prevalence increases and 2) information gain also decreases as prevalence increases and typically peaks somewhere along the continuum.





Using two approaches to feature selection, we next present and discuss graphs showing the accuracy of a)Bernoulli versus multinomial model using unstemmed word frequencies; b) words, phrases, and arguments using the Bernoulli model with unstemmed features; and c) stemmed, unstemmed, and trimmed stopwords using arguments and the Bernoulli model. The appendix shows the underlying resultant data for all trials.

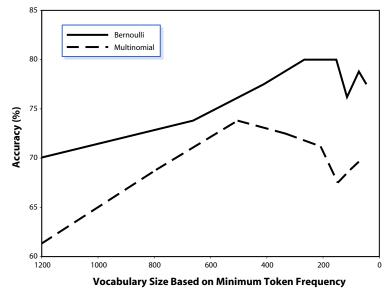
Feature Selection Based on Prevalence

First we selected features based on prevalence. The more selective we were, the better the estimates of $P(w_i|c_j)$. However, as we trimmed features, we would expect to be trimming out features that do an excellent job of predicting group membership.

As we trim unstable estimates on unstemmed words, the multivariate Bernoulli model consistently outperforms the multinomial model as shown in Figure 2. The accuracy of both models tends to increase as words are selected based on prevalence. The multivariate Bernoulli model reaches a maximum accuracy of 80% at a vocabulary size of 200 words. The multinomial model reaches a maximum of 74% accuracy at a vocabulary size of 500 words. Both models show that accuracy improves as we gradually trim out unstable estimates to some degree and it falls again.

Figure 2

Words Unstemmed



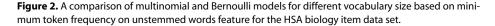


Figure 3 compares the accuracy of predicting group membership based on words, phrases, and arguments using the multivariate Bernoulli model with unstemmed feature as we trim based on minimum word frequency. As more unstable estimates are trimmed out, arguments perform better between minimum word frequency of 10 and 125 times per thousand and maintain about 80% accuracy. Phrases are a more accurate predictor than words or arguments when minimum word frequency is less than .01 (10 times per one thousand) and reach a maximum of 81% accuracy at the minimum word frequency of .01 which is equivalent to a vocabulary size of 2000.

Figure 3

Bernoulli Unstemmed (Minimum Token Frequency)

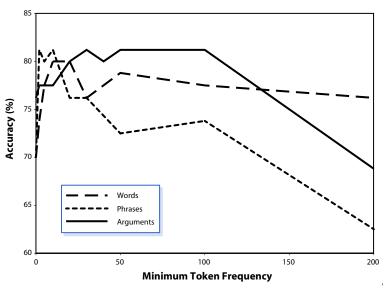


Figure 3. A comparison of Bernoulli unstemmed on words, phrases, and arguments for different minimum token frequency.

In the text classification literature, stemming and the elimination of stopwords often improves classification accuracy. Figure 4 shows results of stemming and eliminating stopwords for multivariate Bernoulli arguments using minimum word frequency. Unstemmed words have better accuracy than no stopwords and much better accuracy than stemmed words. Unstemmed words reach a maximum of 81% accuracy at a vocabulary size between 1000 and 100. There is a sharp drop in accuracy when the vocabulary size is trimmed to less than 100 arguments.

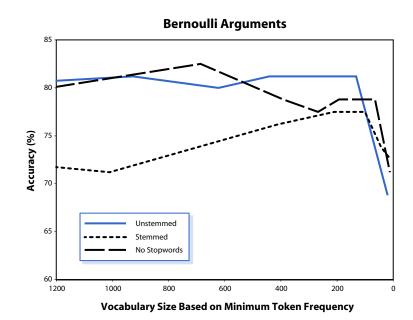
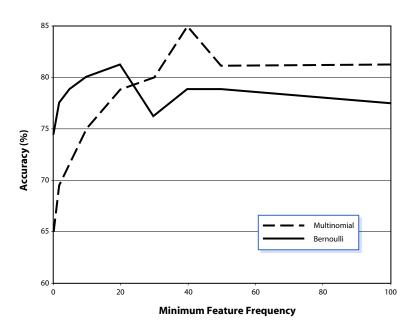


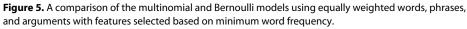
Figure 4. A comparison of Bernoulli arguments on unstemmed, stemmed, and no stopwords features for different vocabulary size based on minimum token frequency.

Figure 4

In Figure 5, we compared the accuracy of the two models using the product of equally weighted classification probabilities based on words, phrases, and arguments as a function of feature selection based on prevalence. With slight trimming, both models yield relatively high accuracy. The Bernoulli model initially out-performs the multinomial model and the curves cross at about 25 occurrences per 1000 essays.







Feature Selection Based on Information Gain

We next selected features based on information gain. The more selective we were, the better the features were in terms of predicting group membership. However, as we trimmed features, we would expect to be selecting terms with the less accurate estimates of $P(w_i|c_j)$.

In comparing the multivariate Bernoulli to the multinomial model for unstemmed words (Figure 6), the multivariate Bernoulli model has higher accuracy than the multinomial model when vocabulary size is greater than 500 words (corresponding to an information gain of .05). However, multinomial model works better in performance when trimming out words that contain less information and when smaller vocabulary size is used. The multinomial model reaches a maximum of 80% accuracy at 400 words, where the multivariate Bernoulli model performs more evenly across vocabulary size at about 70% accuracy.

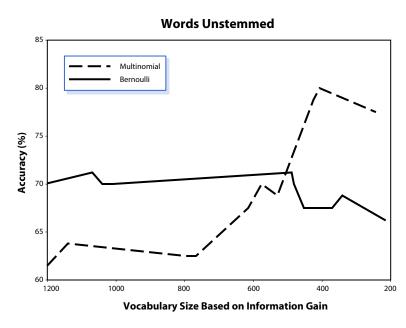
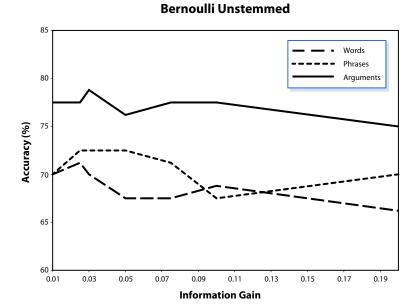


Figure 6. A comparison of multinomial and Bernoulli models on words unstemmed feature for different vocabulary size based on information gain.

Figure 7 compares the accuracy of predicting group membership based on words, phrases and arguments using the multivariate Bernoulli model with unstemmed feature as we trim based on information gain. Arguments consistently perform better than phrases or words across information gain or vocabulary size and reach a maximum of 79% accuracy. Phrases performance is typically better than words. As information gain reaches the level of .13, phrases perform better than words but still somewhat behind arguments performance.



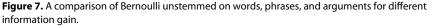


Figure 6

Figure 7



Figure 8

Looking at trimming stopwords and stemming for the multivariate Bernoulli arguments using information gain in Figure 8, unstemmed words' performance is better than that of stemmed words or no stopwords for most levels of information gain. Unstemmed words have a maximum of 79% accuracy at 9000 words and the accuracy drops a little as vocabulary size decreases. No pattern can be drawn among stemmed words and no stopwords. They perform interchangeably better than each other until the level of information gain is reached to approximately .10.

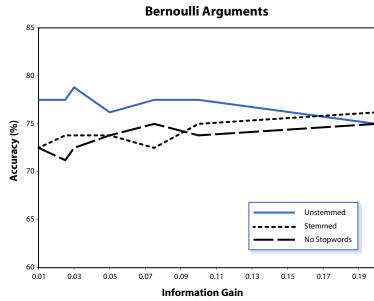


Figure 8. A comparison of unstemmed, stemmed, and no stopwords for different information gain using Bernoulli arguments.

Discussion

We presented a Bayesian approach to essay scoring based on the well developed text classification literature. Our preliminary evaluation of the approach based on one item, a sparse dataset and only two classifications is quite promising. With the right mix of feature selection, we were able to achieve 80% accuracy.

For this item, the Bernoulli model tended to out-perform the multinomial model, arguments tended to out perform words and phrases, and unstemmed features tended to out perform stemming and the elimination of stopwords. Slight trimming based on feature prevalence tended to improve accuracy.

Our results are consistent with the findings of McCallum and Nigam (1998) who found that, with vocabulary sizes less than 1000, classification based on words using the Bernoulli model was more accurate than classification based on the multinomial model, although the differences in our case were much larger. Also consistent with McCallum and Nigam, we found peak accuracies of around 80%.

We are encouraged by our observation that scoring based on arguments tends to outperform scoring based on key words or key phrases. In our study, arguments were identified by the computer using brute force. We defined an argument as an ordered word pair of every word with a prevalence greater than 20 occurrences per 1000 essays that preceded another word with that prevalence. The computer found all such pairs. In our next study, we intend to have humans trim this dataset to only include arguments that make sense.

We do not claim that this system replicates the process used by human beings. Rather we view this as an alternate approach to scoring, one that can be accomplished by a computer, that seeks to replicate the scores obtained by humans.

We emphasize that this is a preliminary investigation. We would like to see studies examining accuracy using multiple score categories, different essays, larger calibration samples, and different typical response lengths.

Appendix—Data summary

Words Unstemmed (No Stopwords)			Words Stemmed				d					
Bern N accu	N	Multi- nomial accuracy	N	Bernoulli accuracy	N	Multi- nomial accuracy	N	Bernoulli accuracy	N	Multi- nomial accuracy	N	Info Gain
066 72	1066	65.0	1066	76.2	710	58.8	710	70.0	1208	61.2	1208	0
938 72	938	63.8	701	73.8`	624	57.5	490	71.2	1069	63.8	1140	0.0025
932 72	932	67.5	678	75.0	615	57.5	475	70.0	1040	62.5	797	0.005
908 72	908	67.5	662	76.2	597	58.8	463	70.0	1010	62.5	767	0.01
422 73	422	70.0	515	73.8	281	61.2	366	71.2	489	67.5	615	0.025
416 73	416	68.8	507	78.8	276	61.2	345	70.0	482	70.0	576	0.03
393 70	393	73.8	471	71.2	256	66.2	320	67.5	453	68.8	530	0.05
334 68	334	78.8	380	70.0	215	70.0	268	67.5	371	78.8	425	0.075
313 68	313	76.2	314	72.5	202	73.8	251	68.8	341	80.0	407	0.1
202 66	202	75.0	237	78.8	125	67.5	157	66.2	215	77.5	243	0.2
Phrases Unstemmed (No Stopwords)				Phrases Stemmed				Phrases Stemmed				
Bern N accu	N	Multi- nomial accuracy	N	Bernoulli accuracy	N	Multi- nomial accuracy	N	Bernoulli accuracy	N	Multi- nomial accuracy	N	Info Gain
551 76	3551	55.0	3551	78.8	4240	62.5	4240	70.0	8326	57.5	8326	0
516 76	3516	55.0	3492	78.8	4182	62.5	4131	70.0	8219	57.5	8109	0.0025
515 76	3515	55.0	3481	78.8	4173	61.2	4119	70.0	7650	57.5	8092	0.005
295 75	1295	55.0	3473	80.0	1657	63.8	1862	70.0	7637	60.0	3644	0.01
278 75	1278	60.0	1460	78.8	1623	62.5	1833	72.5	3102	58.8	3580	0.025
265 76	1265	58.8	1452	80.0	1601	62.5	1828	72.5	3094	58.8	3570	0.03
156 72	1156	61.2	1274	80.0	1430	66.2	1578	72.5	2722	57.5	3079	0.05
136 73	1136	60.0	1060	80.0	1393	63.8	1292	71.2	2667	60.0	2487	0.075
108 73	1108	63.8	1051	80.0	1358	67.5	1267	67.5	2567	62.5	2433	0.1
929 68	929	63.8	930	80.0	1100	73.8	1082	70.0	2066	68.8	2024	0.2
Arguments Unstemmed (No Stopwords)				Arguments Stemmed				ned				
Bern	N	Multi- nomial	N	Bernoulli	Ν	Multi- nomial	N	Bernoulli	N	Multi- nomial	N	Info
	N	accuracy	N	accuracy	N	accuracy	N	accuracy	N	accuracy	N	Gain
	7329	68.8	7329	71.2	4507	63.8	4507	77.5	15640	62.0	15640	0
	6624	68.8	5498	71.2	4105	63.8	4072	77.5	14881	62.0	14126	0.0025
	6592	70.0	6405	71.2	4046	63.8	3953	72.2	10966	62.0	13538	0.005
-	4902	67.5	6236	72.5	3028	67.5	3830	77.5	10723	62.0	13915	0.01
	4579	70.0	4652	73.8	2846	66.2	2322	77.5	9362	63.8	9759	0.025
	4419	71.2	3718	73.8	2806	67.5	2310	78.8	9255	63.8	9656	0.03
	3414	73.8	3466	73.8	2143	67.5	2193	76.2	8931	63.8	7125	0.05
565 73	2565	68.8	2511	75.0	1589	68.8	1439	77.5	5203	68.8	4950	0.1
	2735 2565	70.0 68.8	3254 2511	72.5 75.0	1725 1589	70.0	1955 1439	77.5 77.5	5521 5203	65.0 68.8	6652 4950	0.075

475

71.2

1131

76.2

75.0

1611

75.0

825

Table 1Comparison of Multinomial and Bernoulli Models for Different Vocabulary
Size Based on Minimum Information Gain—HSA Biology Item

0.2

71.2

3072

75.0

1589

Comparison of Multinomial and Bernoulli Models for Different Vocabulary Table 2 Size Based on Minimum Token Frequency(MTF)—HSA Biology Item

	Words Stemmed					Words Stemmed				Words Unstemmed (No Stopwords)			
MTF	N	Multi- nomial accuracy	N	Bernoulli accuracy	N	Multi- nomial accuracy	N	Bernoulli accuracy	N	Multi- nomial accuracy	N	Bernoulli accuracy	
0	1208	61.2	1208	70.0	710	58.8	710	76.2	1066	65.0	1066	72.5	
2	794	68.8	662	73.8	469	62.5	381	71.2	669	76.2	540	76.2	
5	504	73.8	411	77.5	294	68.8	220	67.5	404	73.8	319	76.2	
10	334	72.5	267	80.0	193	65.0	143	68.8	253	75.0	190	75.0	
20	209	71.2	153	80.0	118	67.5	83	71.2	143	73.8	102	81.2	
30	148	67.5	115	76.2	78	70.0	60	76.2	96	71.2	71	76.2	
50	104	68.8	73	78.8	52	73.8	39	77.5	63	72.5	47	73.8	
100	59	70.0	46	77.5	32	71.2	23	77.5	36	73.8	29	73.8	
200	34	71.2	21	76.2									
	Phrases Stemmed			Phrases Stemmed				Phrases Unstemmed (No Stopwords)					
MTF	N	Multi- nomial accuracy	N	Bernoulli accuracy	N	Multi- nomial accuracy	N	Bernoulli accuracy	N	Multi- nomial accuracy	N	Bernoulli accuracy	
0	8326	57.5	8326	70.0	4240	62.5	4240	78.8	3551	55.0	3551	76.2	
2	2276	62.5	2219	81.2	1123	72.5	1103	77.5	784	67.5	765	81.2	
5	887	75.0	856	80.0	444	77.5	434	76.2	288	78.8	279	72.5	
10	361	73.8	344	81.2	218	75.0	214	77.5	108	71.2	105	68.8	
20	155	78.8	147	76.2	109	80.0	102	78.8	46	70.0	44	71.2	
30	99	72.5	85	76.2	69	75.0	67	76.2	28	68.8	24	71.2	
50	51	73.8	43	72.5	41	72.5	34	71.2	16	68.8	14	76.2	
100	26	70.0	21	73.8	15	73.8	13	75.0	8	76.2	8	78.8	
200	8	65.0	5	62.5	5	77.5	3	53.8	3	62.5	3	60.0	
	Arguments Stemmed			Arguments Stemmed				Arguments Unstemmed (No Stopwords)					
MTF	N	Multi- nomial accuracy	N	Bernoulli accuracy	N	Multi- nomial accuracy	N	Bernoulli accuracy	N	Multi- nomial accuracy	N	Bernoulli accuracy	
0	15640	65.8	15640	76.2	4507	66.2	4507	72.5	7329	68.8	7329	73.8	
2	11880	67.1	11880	77.5	3186	67.5	3186	73.8	3352	68.8	3352	73.8	
5	7593	67.1	7593	77.5	1934	70.0	1934	73.8	3352	68.8	3352	73.8	
10	4042	75.0	4041	77.5	1010	70.0	1010	71.2	1761	73.8	1761	77.5	
20	1641	77.5	1641	80.0	411	77.5	411	76.2	686	81.2	686	82.5	
30	928	78.8	927	81.2	210	75.0	210	77.5	392	78.8	392	78.8	
50	441	80.0	441	81.2	101	77.5	101	77.5	193	77.5	193	78.8	
100	132	82.5	132	81.2	43	73.8	43	73.8	65	80.0	65	78.8	
200	20	67.5	20	68.8	8	72.5	8	72.5	12	71.2	12	71.2	

	Words*Phrases*Arguments									
	Unster	nmed	Sten	nmed		Unstemmed (No Stopwords)				
MTF	Multi- nomial accuracy	Bernoulli accuracy	Multi- nomial accuracy	Bernoulli accuracy	Multi- nomial accuracy	Bernoulli accuracy				
0	64.6	73.8	68.8	72.5	71.2	75.0				
2	69.6	77.5	68.8	70.0	73.8	76.2				
5	72.2	78.8	75.0	71.2	72.5	75.0				
10	75.0	80.0	72.5	70.0	77.5	76.2				
20	78.8	81.2	78.8	71.2	82.5	78.8				
30	80.0	76.2	80.0	75.0	80.0	76.2				
40	85.0	78.8	80.0	78.8	80.0	77.5				
50	81.2	78.8	77.5	77.5	77.5	75.0				
100	81.2	77.5	78.8	77.5	77.5	73.8				

Notes

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- 1 See McCallum and Nigam, 1998, for a highly relevant paper on Bayesian Networks.
- 2 Good discussions of computerized essay scoring can be found in Whittington and Hunt (1999) and Wrench (1993).
- 3 An interactive, on-line, java-script stemmer using Porter's algorithm can be found at http://www.ils.unc.edu/keyes/java/porter/.

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