

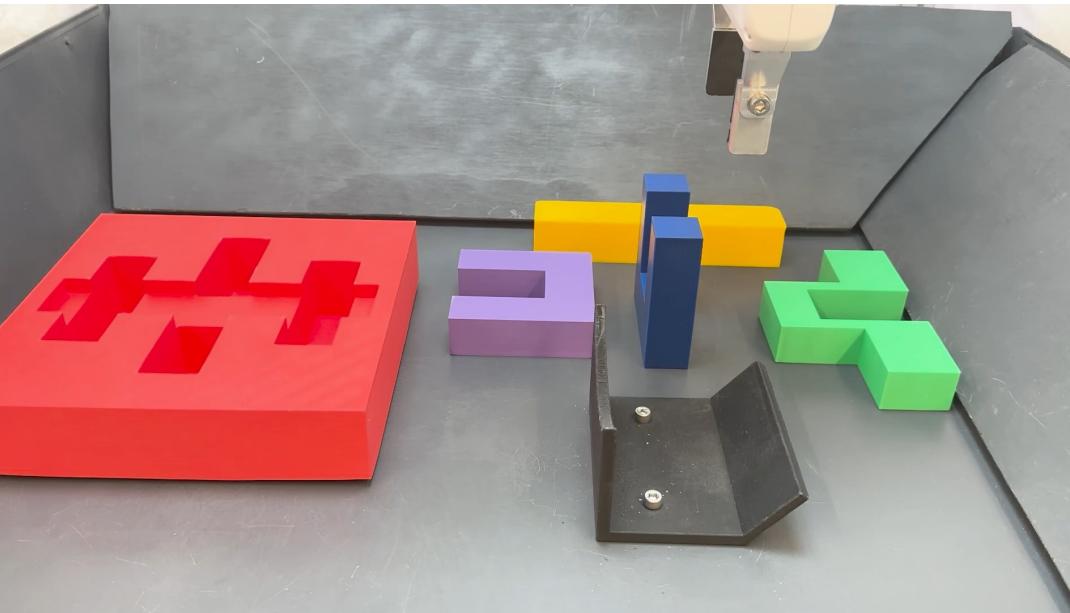
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Reinforcement Learning

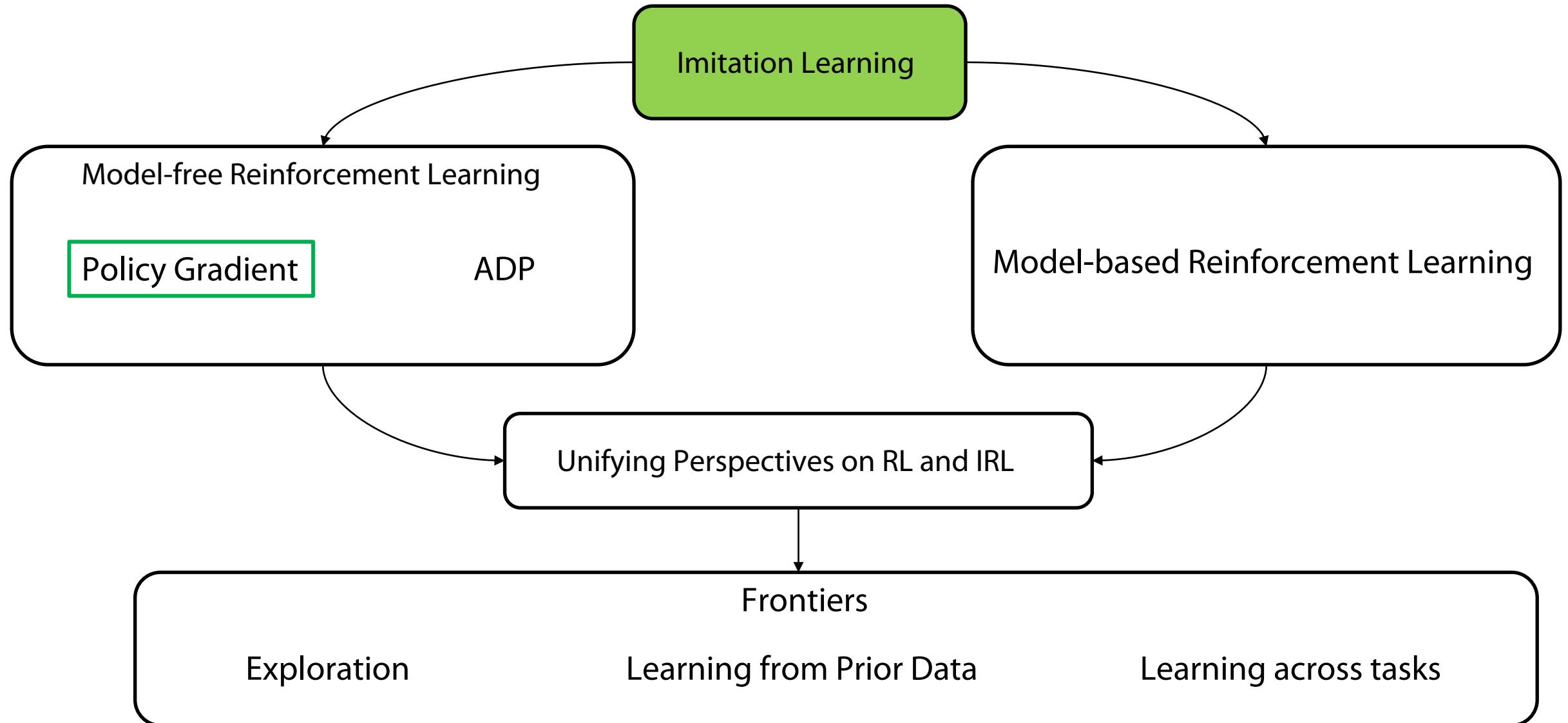
Autumn 2024

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Class Structure



Lecture outline

Recap: Policy Gradient and Variance Reduction



Natural Policy Gradients and Covariant Parameterization

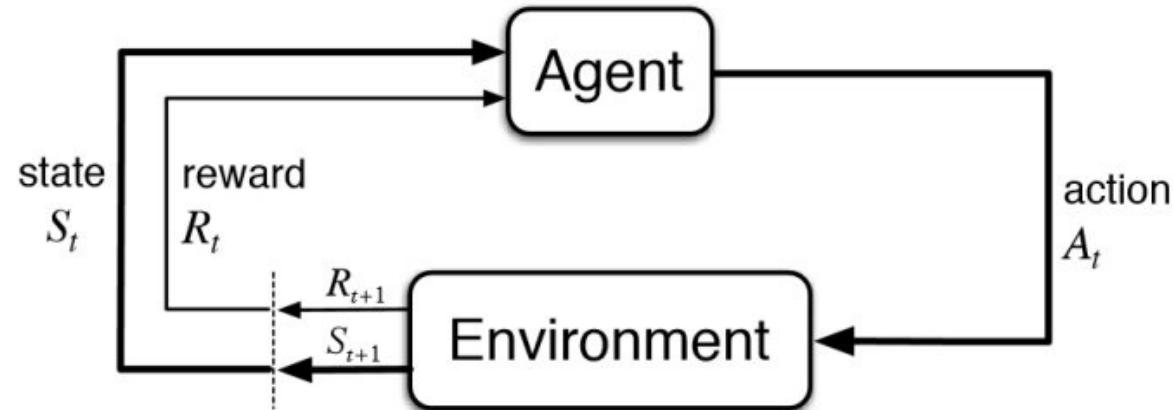


Trust Region Policy Optimization



Proximal Policy Optimization

Optimizing the RL Objective



$$\max_{\theta} \mathbb{E}_{\tau \sim \pi_{\theta}} \left[\sum_{t=0}^T r(s_t, a_t) \right]$$

Gradient Ascent

Dynamic Programming

Model-Based Optimization

Each method has it's own +/−

Taking the gradient of return

$$\nabla_{\theta} J(\theta) = \mathbb{E}_{\tau \sim p_{\theta}(\tau)} \left[\nabla_{\theta} \log p_{\theta}(\tau) \sum_{t=0}^T r(s_t, a_t) \right]$$

$$\nabla_{\theta} J(\theta) = \mathbb{E}_{\substack{s_0 \sim p(s_0) \\ s_{t+1} \sim p(s_{t+1}|s_t, a_t) \\ a_t \sim \pi(a_t|s_t)}} \left[\sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t|s_t) \sum_{t'=0}^T r(s_t, a_t) \right]$$

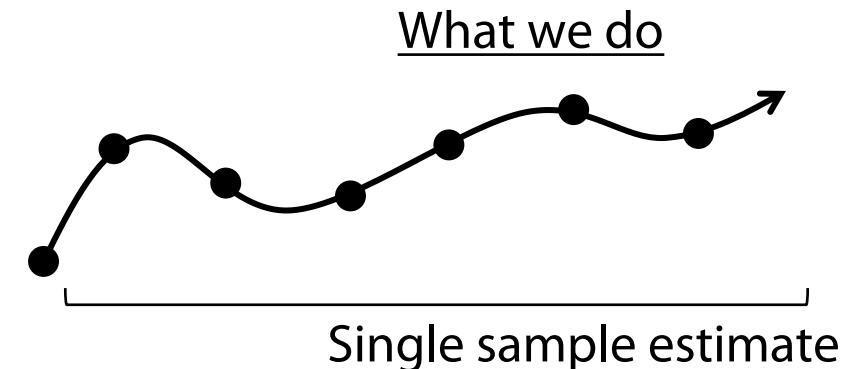
$$\approx \frac{1}{N} \sum_{i=0}^N \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \sum_{t'=0}^T r(s_{t'}^i, a_{t'}^i) \quad (\text{approximating using samples})$$

(Monte-Carlo approximation)

What makes policy gradient challenging?

Hard to tell what matters without many samples

$$\begin{aligned} \nabla_{\theta} J(\theta) &= \int p_{\theta}(\tau) \nabla_{\theta} \log p_{\theta}(\tau) d\tau \\ &\approx \frac{1}{N} \sum_{i=0}^N \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \sum_{t'=0}^T r(s_{t'}^i, a_{t'}^i) \end{aligned}$$



For every (s, a) pair, weight by only the sum of rewards in the current trajectory

Couples together all actions

Susceptible to scale variations

Susceptible to lucky samples

Makes policy gradient unstable, requires huge numbers of samples and huge batch size

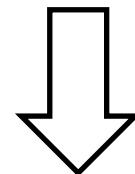
Variance Reduction with Causality

Idea: Trajectory returns depend on past and future, but we only care about the future, since actions cannot affect the past. Instead, consider "**return-to-go**"

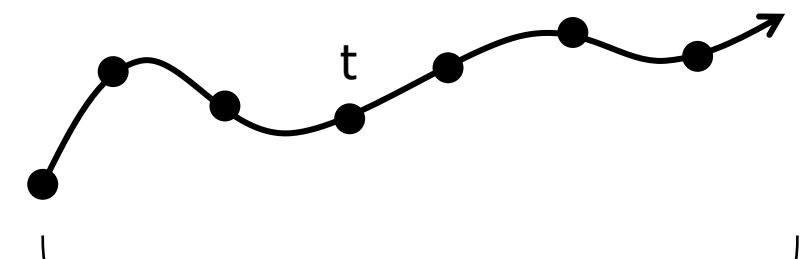
$$\approx \frac{1}{N} \sum_{i=0}^N \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \sum_{t'=0}^T r(s_{t'}^i, a_{t'}^i)$$

Includes $t' < t$

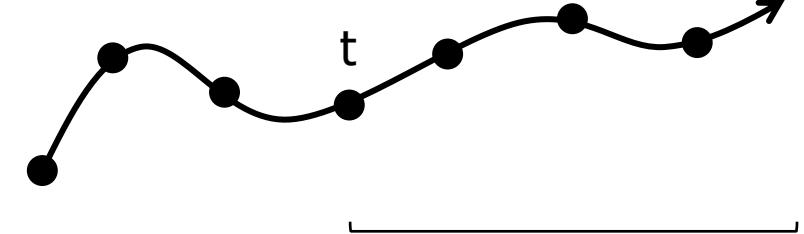
Ignore past terms



$$\frac{1}{N} \sum_{i=0}^N \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \sum_{t'=t}^T r(s_{t'}^i, a_{t'}^i)$$



Full trajectory return



Return to go

Variance Reduction with a Baseline

Idea: We can reduce variance by subtracting a current state dependent function from the policy gradient return

$$\frac{1}{N} \sum_{i=1}^N \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \left[\sum_{t'=t}^T r(s_{t'}^i, a_{t'}^i) - b(s_t) \right]$$

Baseline: Centers the returns, reduces variance

We proved this was unbiased!

Lecture outline

Recap: Policy Gradient and Variance Reduction



Natural Policy Gradients and Covariant Parameterization



Trust Region Policy Optimization



Proximal Policy Optimization

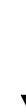
Take a deeper look at REINFORCE

$$\nabla_{\theta} J(\theta) = \int p_{\theta}(\tau) \nabla_{\theta} \log p_{\theta}(\tau) d\tau \approx \frac{1}{N} \sum_{i=0}^N \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \sum_{t'=0}^T r(s_{t'}^i, a_{t'}^i)$$

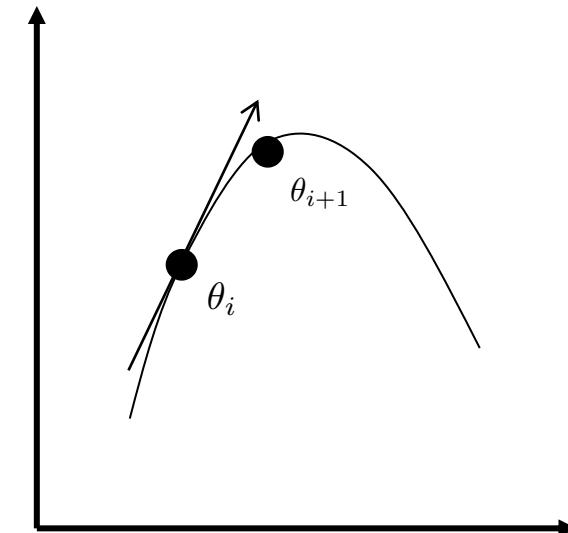
Gradient ascent is steepest ascent on linear approximation under the Euclidean metric!

$$\max \quad J(\theta_i) + \nabla_{\theta} J(\theta)|_{\theta=\theta_i} (\theta - \theta_i) \quad \text{Linear approximation}$$

$$(\theta - \theta_i)^T (\theta - \theta_i) \leq \epsilon \quad \text{Quadratic Constraint}$$

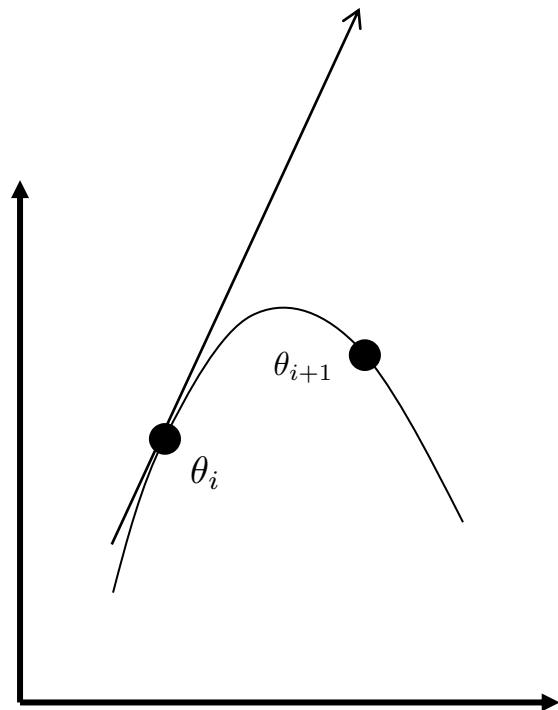


$$\theta = \theta_i + \alpha \nabla_{\theta} J(\theta)|_{\theta=\theta_i}$$



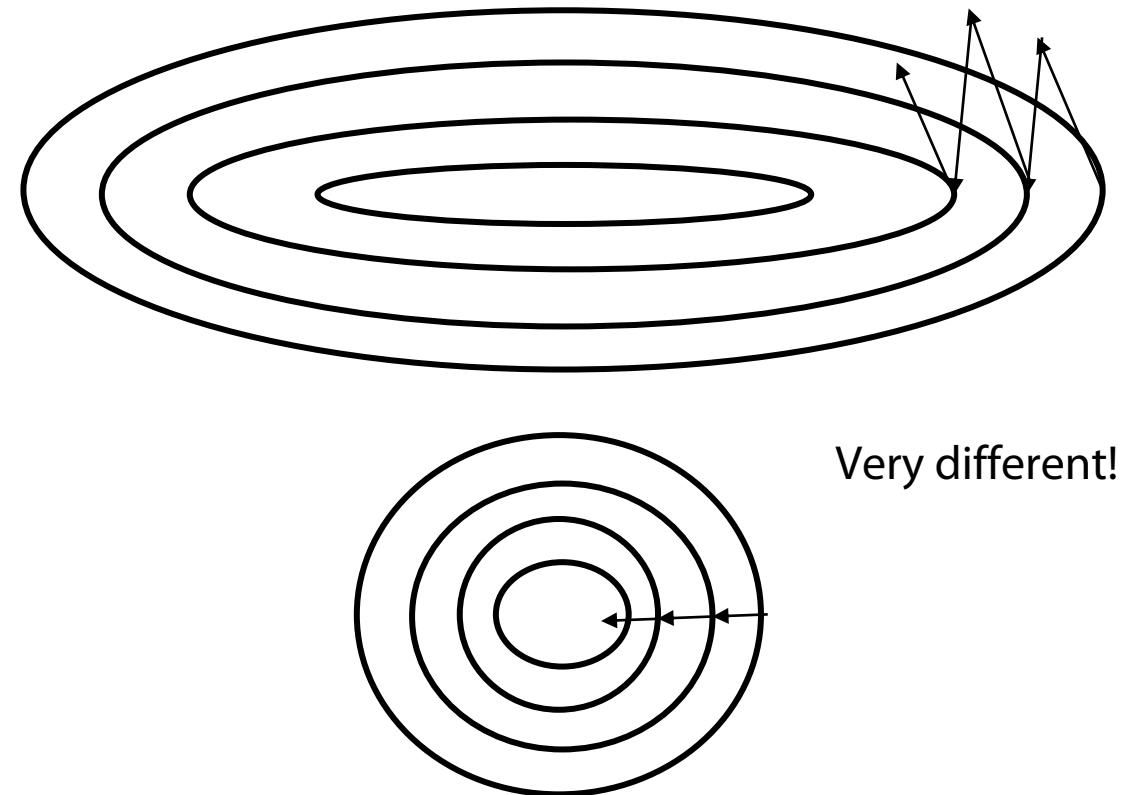
When might this fail?

Large step sizes may cause collapse



Must use very small step sizes, slow!

Sensitive to Policy Parameterization



Can struggle for a deep neural network!

Covariant Policy Gradient Updates

$$\begin{aligned} \max \quad & J(\theta_i) + \nabla_{\theta} J(\theta)|_{\theta=\theta_i} (\theta - \theta_i) \\ & (\theta - \theta_i)^T G(\theta - \theta_i) \leq \epsilon \end{aligned}$$

What should G be?

$$\begin{aligned} \max \quad & J(\theta_i) + \nabla_{\theta} J(\theta)|_{\theta=\theta_i} (\theta - \theta_i) \\ & D_{\text{KL}}(\pi_{\theta} || \pi_{\theta_i}) \leq \epsilon \end{aligned}$$

Let us use the constraint as
KL divergence on the policy
(2nd order Taylor expansion)

Measures functional distance, not parameter distance

Resulting “Natural” Policy Gradient

$$\max J(\theta_i) + \nabla_{\theta} J(\theta)|_{\theta=\theta_i} (\theta - \theta_i)$$

$$D_{\text{KL}}(\pi_{\theta} || \pi_{\theta_i}) \leq \epsilon$$

2nd order approximation of KL → Fisher Information Metric

$$F = \mathbb{E}_{\pi_{\theta}} [(\nabla_{\theta} \log \pi_{\theta})(\nabla_{\theta} \log \pi_{\theta})^T]$$

$$\max J(\theta_i) + \nabla_{\theta} J(\theta)|_{\theta=\theta_i} (\theta - \theta_i)$$

$$(\theta - \theta_i)^T F (\theta - \theta_i) \leq \epsilon$$

Resulting update

$$\theta_{i+1} = \theta_i + \alpha F^{-1} \nabla_{\theta} J(\theta)|_{\theta=\theta_i} \quad \text{Covariant to parameterization}$$

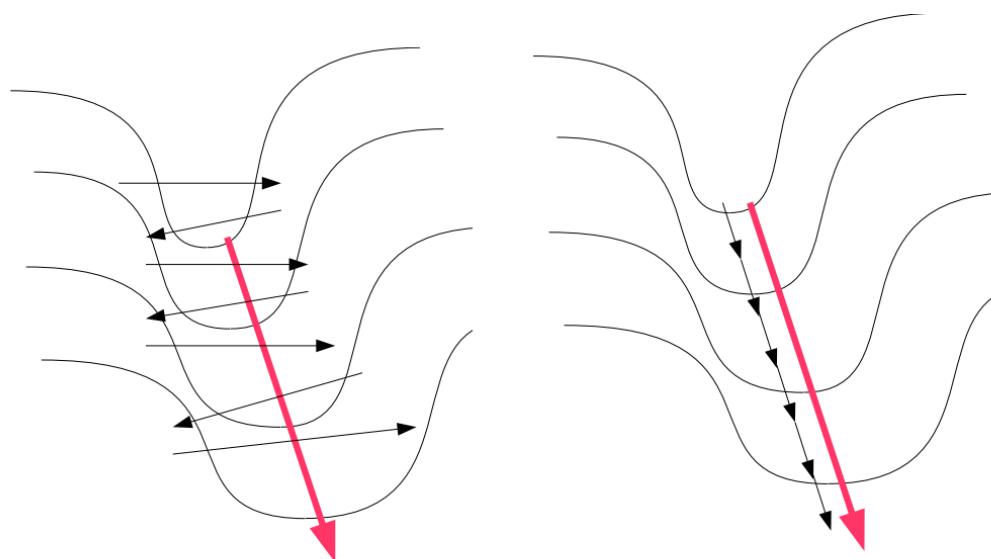
Fisher Information as a Gauss-Newton Approximation

Fisher Information is generalized Gauss Newton Approximation to the Hessian

$$E(\boldsymbol{\theta}) = \mathbb{E}_{(\mathbf{x},\mathbf{y})} [-\log p(\mathbf{y}|\mathbf{x}; \boldsymbol{\theta})]$$

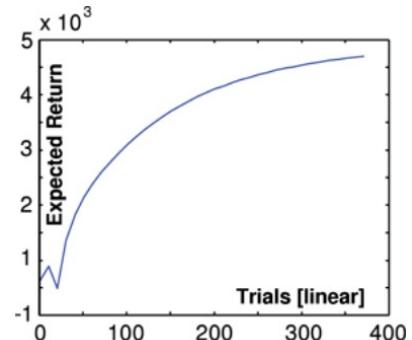
SGD

Natural Gradient

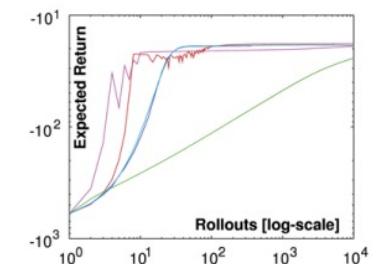
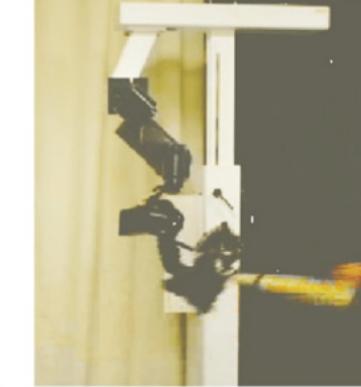
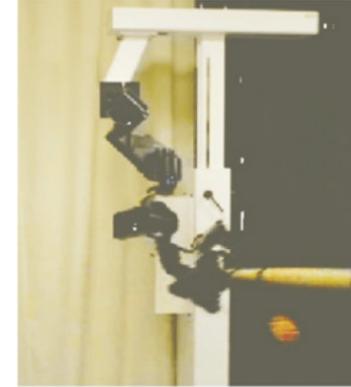


$$\begin{aligned}\mathbf{H}(E)(\boldsymbol{\theta}) &= \nabla^2 \mathbb{E}_{(\mathbf{x},\mathbf{y})} [-\log p(\mathbf{y}|\mathbf{x}; \boldsymbol{\theta})] \\ &= -\mathbb{E}_{(\mathbf{x},\mathbf{y})} [\nabla^2 \log p(\mathbf{y}|\mathbf{x}; \boldsymbol{\theta})] \\ &= -\mathbb{E}_{(\mathbf{x},\mathbf{y})} \left[-\frac{\nabla p(\mathbf{y}|\mathbf{x}; \boldsymbol{\theta}) \nabla p(\mathbf{y}|\mathbf{x}; \boldsymbol{\theta})^T}{p(\mathbf{y}|\mathbf{x}; \boldsymbol{\theta})^2} + \frac{\nabla^2 p(\mathbf{y}|\mathbf{x}; \boldsymbol{\theta})}{p(\mathbf{y}|\mathbf{x}; \boldsymbol{\theta})} \right] \\ &= \mathbf{F}_{\boldsymbol{\theta}} - \mathbb{E}_{(\mathbf{x},\mathbf{y})} \left[\frac{\nabla^2 p(\mathbf{y}|\mathbf{x}; \boldsymbol{\theta})}{p(\mathbf{y}|\mathbf{x}; \boldsymbol{\theta})} \right]\end{aligned}$$

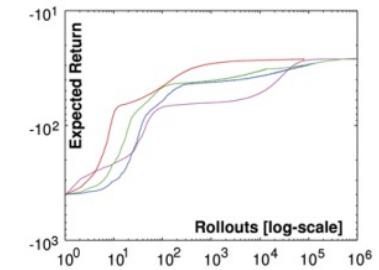
Natural Policy Gradient in Action



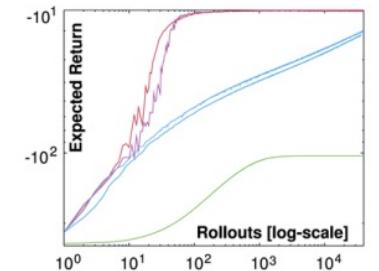
(a) Performance.



(b) Minimum motor command with motor primitives



(c) Passing through a point with splines



(d) Passing through a point with motor primitives

- Finite Difference Gradient
- Vanilla Policy Gradient with constant baseline
- Vanilla Policy Gradient with time-variant baseline
- Episodic Natural Actor-Critic with single offset basis functions
- Episodic Natural Actor-Critic with time-variant offset basis functions

Lecture outline

Recap: Policy Gradient and Variance Reduction



Natural Policy Gradients and Covariant Parameterization



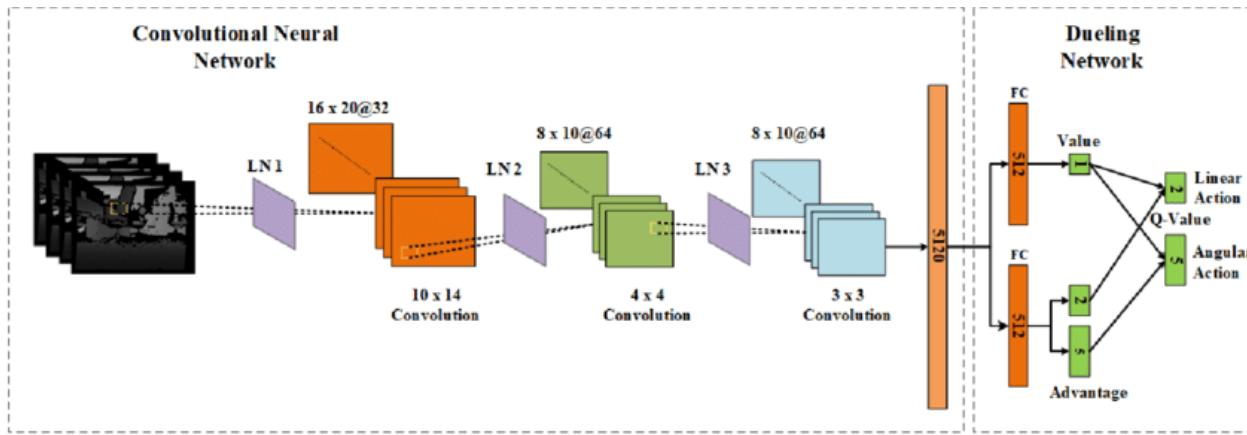
Trust Region Policy Optimization



Proximal Policy Optimization

Natural Policy Gradient - is it enough?

Huge matrix inversion

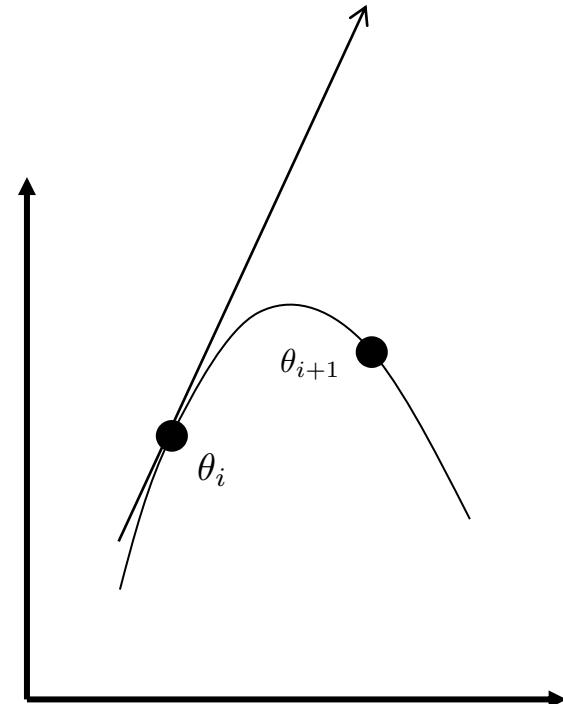


$$F \in \mathbb{R}^{d \times d}$$

For a standard convnet – d is in the millions

Hessian is way out of memory / hard to invert!

Step-size?



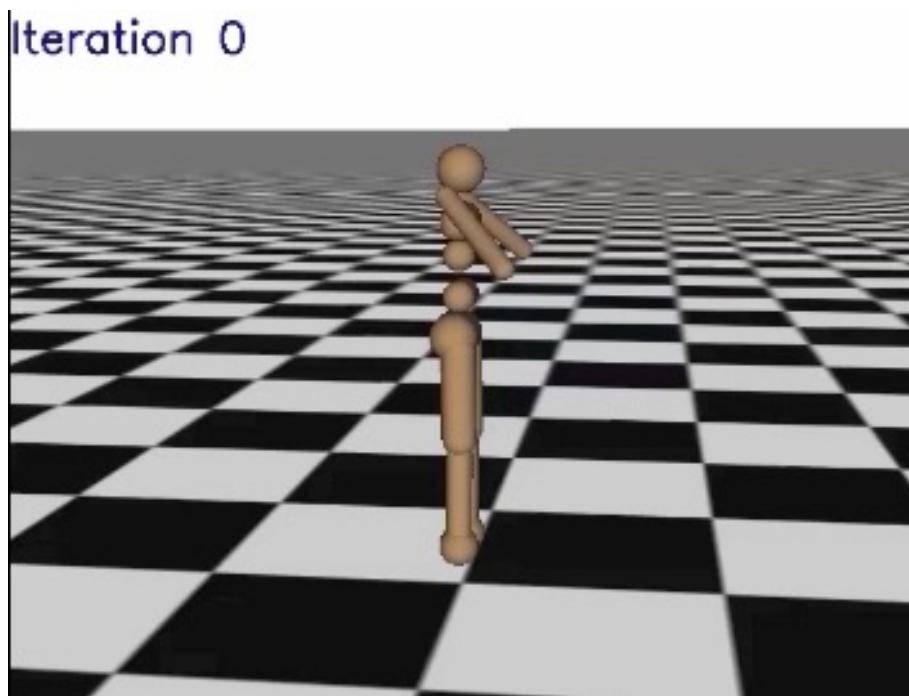
Can easily overstep and collapse performance

Also, only a single gradient step at a time before recollecting data!

Trust Region Policy Optimization

3 key ideas:

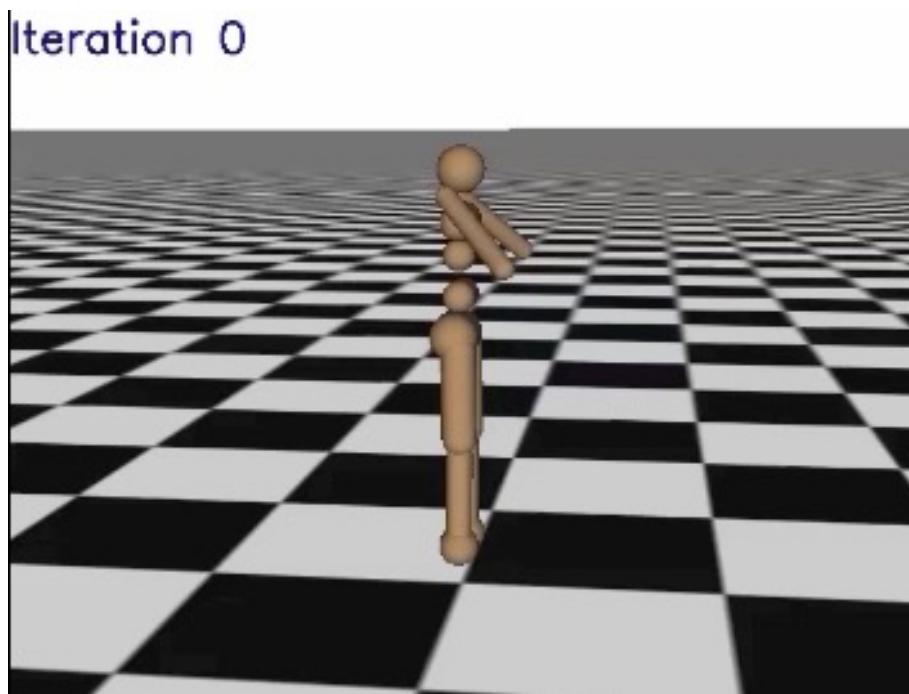
1. On-policy updates → importance sampled objective
2. Huge matrix inversion → conjugate gradient method
3. Step size may be too large → backtracking line search



Trust Region Policy Optimization

3 key ideas:

1. On-policy updates → importance sampled objective
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Off Policy Policy Gradient – Importance Sampling

Problem with original policy gradient objective – hard to evaluate without samples from θ

$$J(\theta) = \mathbb{E}_{\tau \sim p_\theta(\tau)} [R(\tau)] \quad \nabla_\theta J(\theta) = \mathbb{E}_{\tau \sim p_\theta(\tau)} [\nabla_\theta \log \pi_\theta(\tau) R(\tau)]$$



Can we be off-policy?

$$J(\theta) = \int p_\theta(\tau) R(\tau)$$

Can rederive policy gradient from this perspective

$$J(\theta) = \int \frac{q(\tau)}{p_\theta(\tau)} p_\theta(\tau) R(\tau)$$

Has numerical challenges

$$J(\theta) = \mathbb{E}_{\tau \sim q(\tau)} \left[\frac{p_\theta(\tau)}{q(\tau)} R(\tau) \right]$$

Deriving Policy Gradient from Importance Sampling

$$J(\theta) = \int p_\theta(\tau) R(\tau)$$

$$J(\theta) = \int \frac{q(\tau)}{q(\tau)} p_\theta(\tau) R(\tau)$$

$$J(\theta) = \mathbb{E}_{\tau \sim q(\tau)} \left[\frac{p_\theta(\tau)}{q(\tau)} R(\tau) \right]$$

$$\nabla_\theta J(\theta) = \mathbb{E}_{\tau \sim q(\tau)} \left[\frac{\nabla_\theta p_\theta(\tau)}{q(\tau)} R(\tau) \right]$$

Set $q(\tau) = p_{\theta_i}(\tau)$

$$\nabla_\theta J(\theta) = \mathbb{E}_{\tau \sim p_{\theta_i}(\tau)} \left[\frac{\nabla_\theta p_\theta(\tau)}{p_{\theta_i}(\tau)} R(\tau) \right]$$

$$\nabla_\theta J(\theta)|_{\theta=\theta_i} = \mathbb{E}_{\tau \sim p_{\theta_i}(\tau)} [\nabla_\theta \log p_\theta(\tau)|_{\theta=\theta_i} R(\tau)]$$

Same as PG in first order!

Expanding the Importance Sampling Objective

$$J(\theta) = \int p_\theta(\tau) R(\tau)$$

$$J(\theta) = \int \frac{q(\tau)}{q(\tau)} p_\theta(\tau) R(\tau)$$

$$J(\theta) = \mathbb{E}_{\tau \sim q(\tau)} \left[\frac{p_\theta(\tau)}{q(\tau)} R(\tau) \right]$$

$$J(\theta) = \mathbb{E}_{\tau \sim q(\tau)} \left[\left(\prod_{t=1}^T \frac{\pi_\theta(a_t | s_t)}{q(a_t | s_t)} \right) \left(R(\tau) \right) \right]$$

Numerically unstable, high variance!

Trust Region Policy Optimization – Importance Sampling without the Pain

Cannot evaluate without resampling

Original Objective

$$J(\theta) = \mathbb{E}_{\tau \sim p_\theta(\tau)} [R(\tau)]$$

$$J(\theta) = \mathbb{E}_{s \sim p_\theta(s), a \sim \pi_\theta(a|s)} [Q(s, a)]$$

Importance Sampling(ish)

$$J(\theta) = \mathbb{E}_{s \sim p_{\theta_i}(s), a \sim \pi_{\theta_i}(a|s)} \left[\frac{p_\theta(s)}{p_{\theta_i}(s)} \frac{\pi_\theta(a|s)}{\pi_{\theta_i}(a|s)} Q(s, a) \right]$$

(Surrogate Objective)

$$\approx \mathbb{E}_{s \sim p_{\theta_i}(s), a \sim \pi_{\theta_i}(a|s)} \left[\frac{\pi_\theta(a|s)}{\pi_{\theta_i}(a|s)} Q(s, a) \right]$$

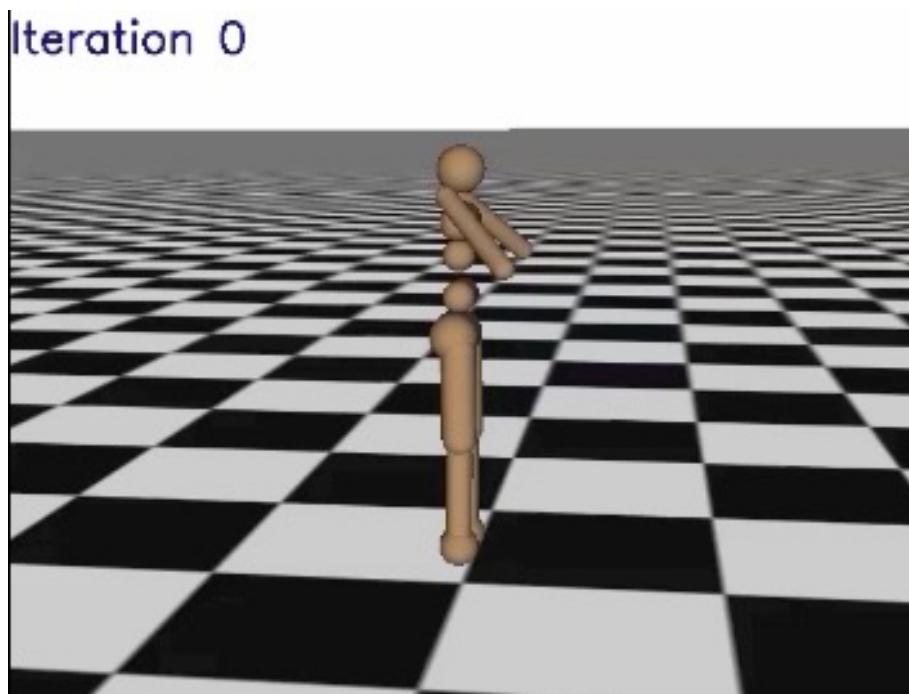
If policies are close, we can show that this is not so bad!

Often replaced by $A = Q - V$

Trust Region Policy Optimization

3 key ideas:

1. On-policy updates → importance sampled objective
2. Huge matrix inversion → conjugate gradient method
3. Step size may be too large → backtracking line search



Trust Region Policy Optimization – Conjugate Gradient

Challenging to compute F^{-1} and then get $F^{-1}g$



Convert into an iterative minimization problem!

Solution to

$$Fx = g$$

same as

Solution to

$$\min_x \frac{1}{2}x^T F x - x^T g + c$$

Trust Region Policy Optimization – Conjugate Gradient

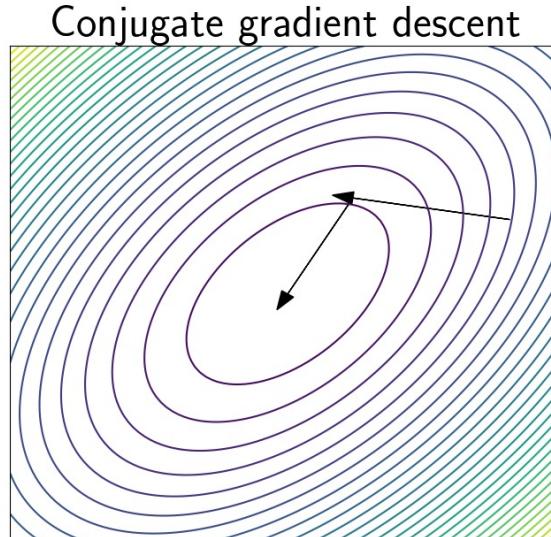
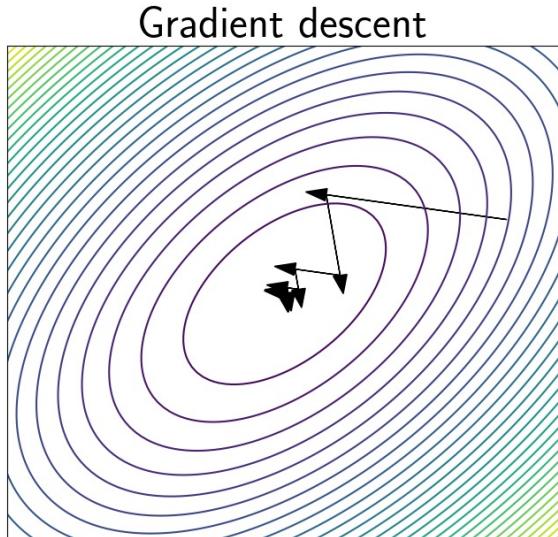
Challenging to compute F^{-1} and then get $F^{-1}g$



Convert into an iterative minimization problem!

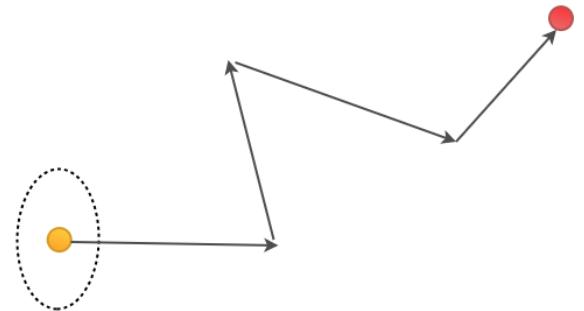


Solve with conjugate gradient



Do coordinate descent in geometry aligned orthogonal directions

Trust Region Policy Optimization – Conjugate Gradient



Gradient ascent

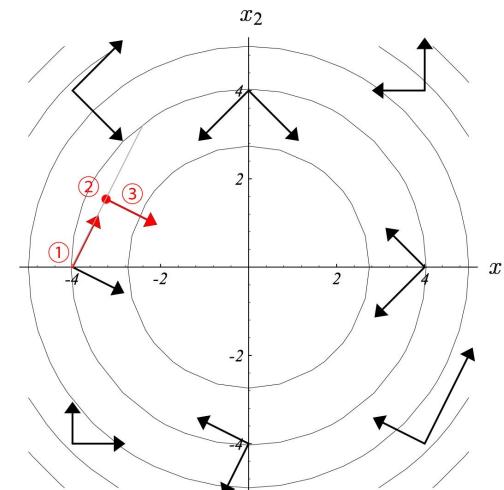
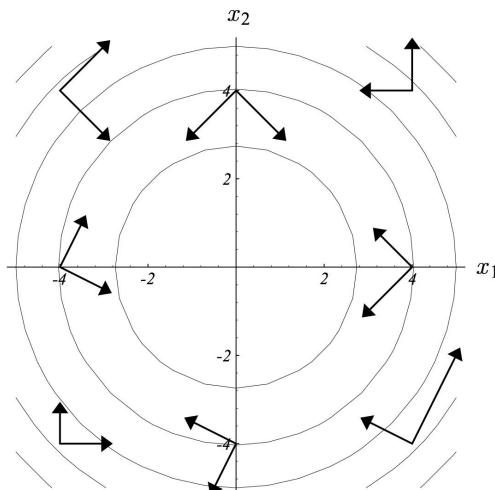


Conjugate gradient

$$\min_x \frac{1}{2} x^T F x - x^T g + c$$

Find search directions at every step that are F -orthogonal with previous directions

$$d_{(i)}^T F d_{(i)} = 0$$



Converges in approx N steps!

Only requires matrix-vector product

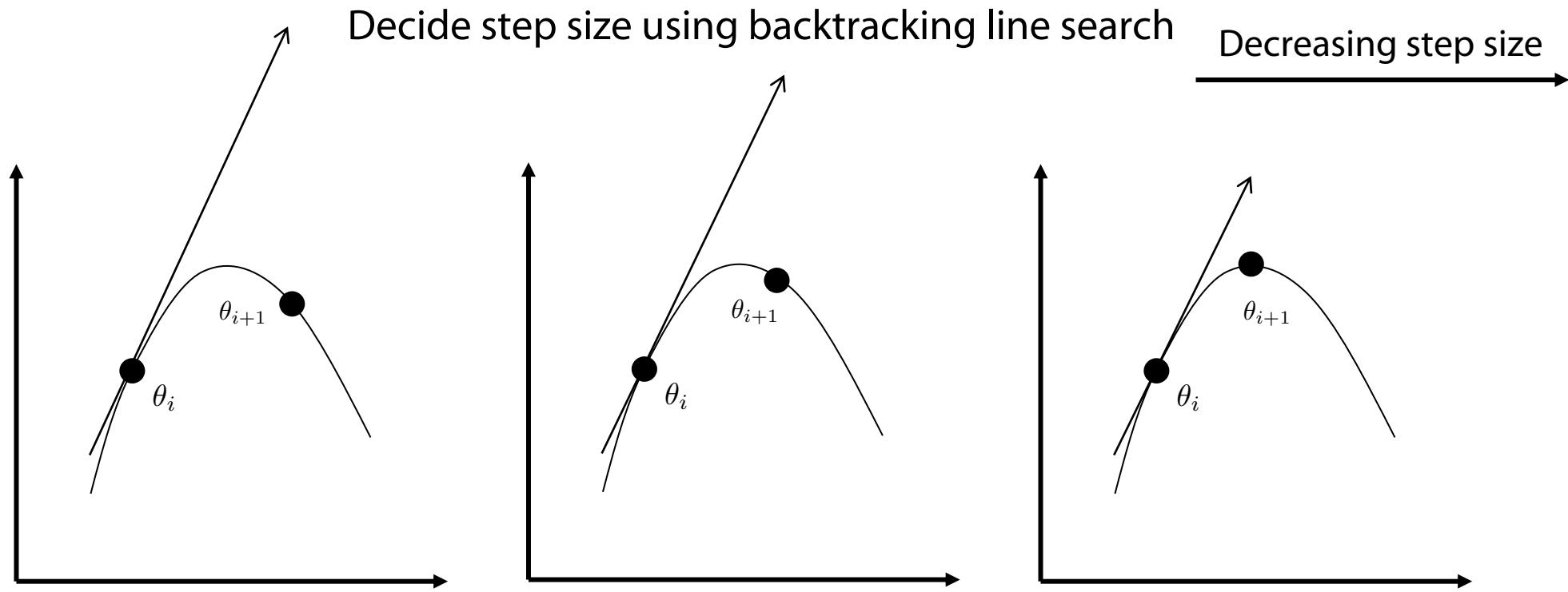
Trust Region Policy Optimization

3 key ideas:

1. On-policy updates → importance sampled objective
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Trust Region Policy Optimization – Backtracking line search



1. Choose parameter $\beta \in (0, 1)$, given search direction $s = F^{-1}g$
 2. Compute maximal step size such that constraint is satisfied - $\frac{1}{2}(ts)^T F(ts) = \epsilon \rightarrow t = \sqrt{\frac{2\epsilon}{s^T F s}}$
 3. While $J(\theta_i + ts) < J(\theta_i)$, set $t = \beta t$
- Backtracking

Trust Region Policy Optimization

3 key ideas:

1. On-policy updates → importance sampled objective
2. Huge matrix inversion → conjugate gradient method
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Algorithm 3 Trust Region Policy Optimization

Input: initial policy parameters θ_0

for $k = 0, 1, 2, \dots$ **do**

 Collect set of trajectories \mathcal{D}_k on policy $\pi_k = \pi(\theta_k)$

 Estimate advantages $\hat{A}_t^{\pi_k}$ using any advantage estimation algorithm

 Form sample estimates for

- policy gradient \hat{g}_k (using advantage estimates)
- and KL-divergence Hessian-vector product function $f(v) = \hat{H}_k v$

 Use CG with n_{cg} iterations to obtain $x_k \approx \hat{H}_k^{-1} \hat{g}_k$

 Estimate proposed step $\Delta_k \approx \sqrt{\frac{2\delta}{x_k^T \hat{H}_k x_k}} x_k$

 Perform backtracking line search with exponential decay to obtain final update

$$\theta_{k+1} = \theta_k + \alpha^j \Delta_k$$

end for

Can we say anything formal about updates?

$$\eta(\tilde{\pi}) \geq L_{\pi}(\tilde{\pi}) - CD_{\text{KL}}^{\max}(\pi, \tilde{\pi}),$$

$$\text{where } C = \frac{4\epsilon\gamma}{(1-\gamma)^2}.$$

Ensures that policies are non-decreasing in performance

Performance difference
lemma

$$\eta(\tilde{\pi}) = \eta(\pi) + \mathbb{E}_{\tau \sim \tilde{\pi}} \left[\sum_{t=0}^{\infty} \gamma^t A_{\pi}(s_t, a_t) \right]$$

Express advantage
in terms of TVD

Theorem 1. Let $\alpha = D_{\text{TV}}^{\max}(\pi_{\text{old}}, \pi_{\text{new}})$. Then the following bound holds:

$$\eta(\pi_{\text{new}}) \geq L_{\pi_{\text{old}}}(\pi_{\text{new}}) - \frac{4\epsilon\gamma}{(1-\gamma)^2} \alpha^2 \quad (8)$$

where $\epsilon = \max_{s,a} |A_{\pi}(s, a)|$

Key idea: by bounding how different the policies are, we can bound how different returns are

TRPO in action

Trust Region Policy Optimization

Why might TRPO not be enough?

Algorithm 3 Trust Region Policy Optimization

Input: initial policy parameters θ_0

for $k = 0, 1, 2, \dots$ **do**

 Collect set of trajectories \mathcal{D}_k on policy $\pi_k = \pi(\theta_k)$

 Estimate advantages $\hat{A}_t^{\pi_k}$ using any advantage estimation algorithm

 Form sample estimates for

- policy gradient \hat{g}_k (using advantage estimates)
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 Use CG with n_{cg} iterations to obtain $x_k \approx \hat{H}_k^{-1} \hat{g}_k$

 Estimate proposed step $\Delta_k \approx \sqrt{\frac{2\delta}{x_k^T \hat{H}_k x_k}} x_k$

 Perform backtracking line search with exponential decay to obtain final update

$$\theta_{k+1} = \theta_k + \alpha^j \Delta_k$$

end for

Advantage estimation is too high variance

Optimization expensive/unstable

Better Advantage Estimation - Generalized Advantage Estimation

Advantage estimator

$$A_N^\theta(s_1, a_1) = r_1 + \gamma r_2 + \cdots + \gamma^{N-1} r_N - V(s_1)$$

High variance!

N step advantage estimator

$$A_N^\theta(s_1, a_1) = r_1 + \gamma r_2 + \cdots + \gamma^{N-1} r_N - V(s_1)$$

N-1 step advantage estimator

$$A_{N-1}^\theta(s_1, a_1) = r_1 + \gamma r_2 + \cdots + \gamma^{N-2} V(s_{N-1}) - V(s_1)$$

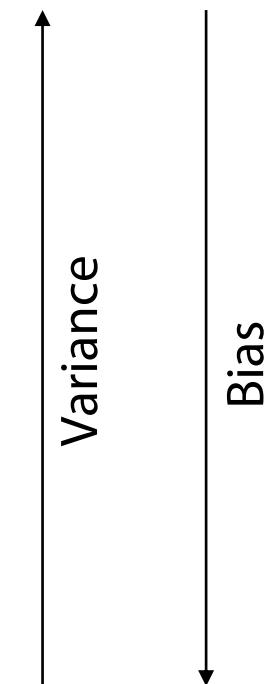
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2 step advantage estimator

$$A_2^\theta(s_1, a_1) = r_1 + \gamma r_2 + \cdots + \gamma^2 V(s_3) - V(s_1)$$

1 step advantage estimator

$$A_1^\theta(s_1, a_1) = r_1 + \gamma V(s_2) - V(s_1)$$



Generalized Advantage Estimation

Sum up all the estimators in a geometric sum

$$A_N^\theta(s_1, a_1) = r_1 + \gamma r_2 + \cdots + \gamma^{N-1} r_N - V(s_1)$$

$$A_{N-1}^\theta(s_1, a_1) = r_1 + \gamma r_2 + \cdots + \gamma^{N-2} V(s_{N-1}) - V(s_1)$$

$$A_2^\theta(s_1, a_1) = r_1 + \gamma r_2 + \cdots + \gamma^2 V(s_3) - V(s_1)$$

$$A_1^\theta(s_1, a_1) = r_1 + \gamma V(s_2) - V(s_1)$$

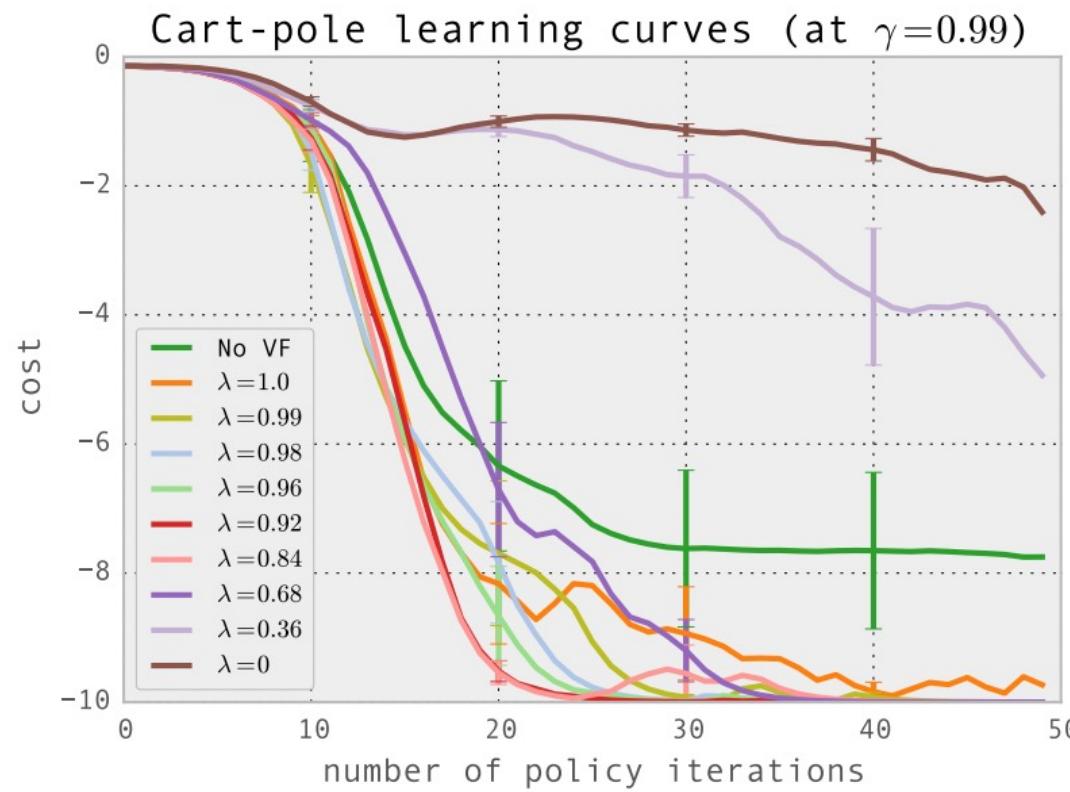
Geometric sum

$$A_\lambda^\theta(s_1, a_1) = \sum_{j=1}^N \lambda^j A_j^\theta(s, a)$$

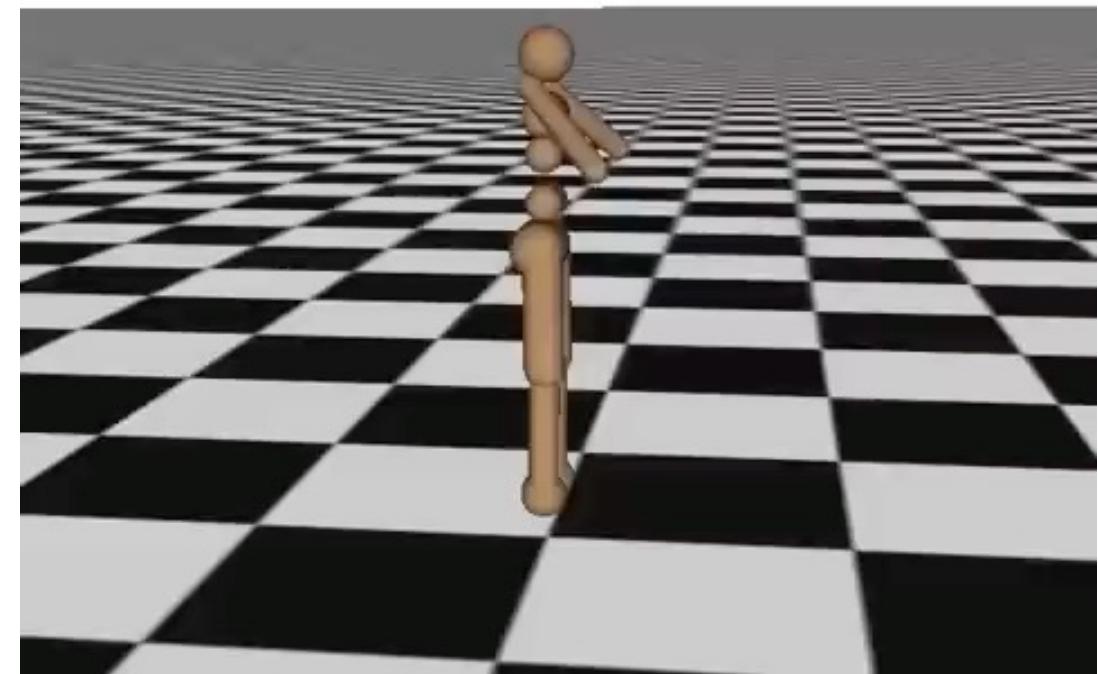
λ controls bias-variance tradeoff

Best of both worlds – very similar idea to eligibility traces

Generalized Advantage Estimation in Action



Iteration 0



Lecture outline

Recap: Policy Gradient and Variance Reduction



Natural Policy Gradients and Covariant Parameterization



Trust Region Policy Optimization



Proximal Policy Optimization

Avoiding Second Order Optimization

Algorithm 3 Trust Region Policy Optimization

Input: initial policy parameters θ_0

for $k = 0, 1, 2, \dots$ **do**

 Collect set of trajectories \mathcal{D}_k on policy $\pi_k = \pi(\theta_k)$

 Estimate advantages $\hat{A}_t^{\pi_k}$ using any advantage estimation algorithm

 Form sample estimates for

- policy gradient \hat{g}_k (using advantage estimates)
- and KL-divergence Hessian-vector product function $f(v) = \hat{H}_k v$

 Use CG with n_{cg} iterations to obtain $x_k \approx \hat{H}_k^{-1} \hat{g}_k$

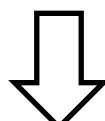
 Estimate proposed step $\Delta_k \approx \sqrt{\frac{2\delta}{x_k^T \hat{H}_k x_k}} x_k$

 Perform backtracking line search with exponential decay to obtain final update

$$\theta_{k+1} = \theta_k + \alpha^j \Delta_k$$

end for

Expensive second order optimization, can we avoid?



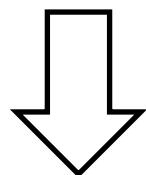
What if we just restricted how much the policy changes directly!

Proximal Policy Optimization Update

Trust Region Policy Optimization

$$\max J(\theta_i) + \nabla_{\theta} J(\theta)|_{\theta=\theta_i} (\theta - \theta_i)$$

$$D_{\text{KL}}(\pi_{\theta} || \pi_{\theta_i}) \leq \epsilon$$



Restrict the amount the policy moves

Proximal Policy Optimization

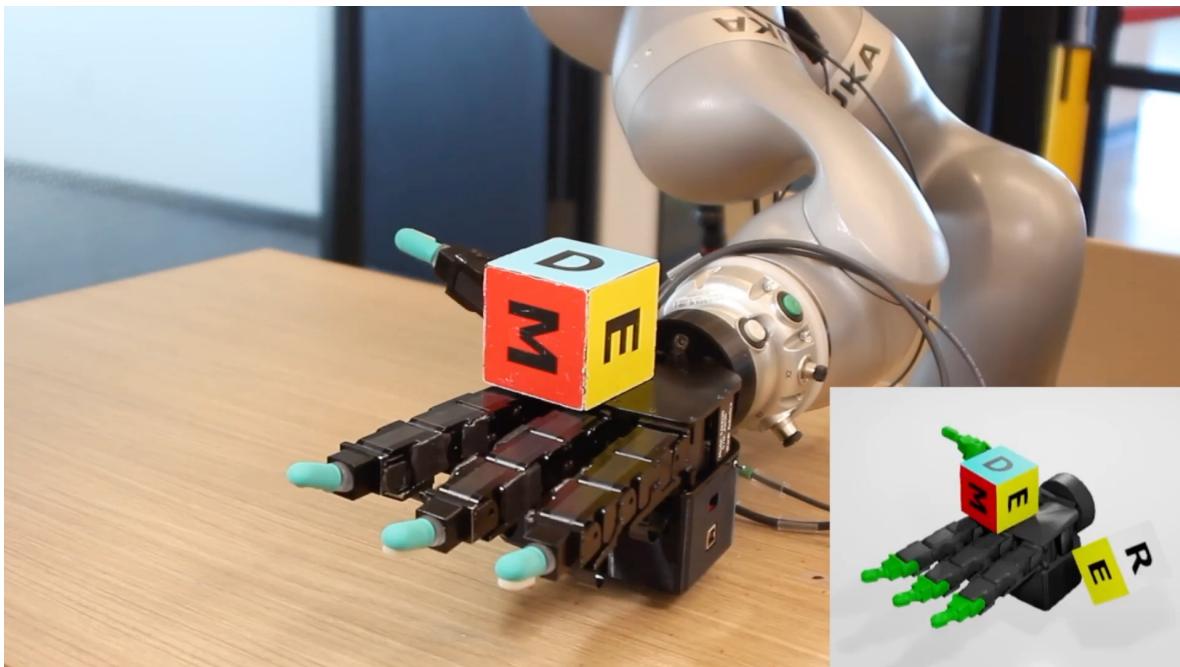
$$\mathcal{L}(s, a, \theta_i, \theta) = \min \left(\frac{\pi_{\theta}(a|s)}{\pi_{\theta_i}(a|s)} A(s, a), \text{clip} \left(\frac{\pi_{\theta}(a|s)}{\pi_{\theta_i}(a|s)}, 1 - \epsilon, 1 + \epsilon \right) A(s, a) \right)$$

Proximal Policy Optimization Algorithm

$$\mathcal{L}(s, a, \theta_i, \theta) = \min \left(\frac{\pi_\theta(a|s)}{\pi_{\theta_i}(a|s)} A(s, a), \text{clip} \left(\frac{\pi_\theta(a|s)}{\pi_{\theta_i}(a|s)}, 1 - \epsilon, 1 + \epsilon \right) A(s, a) \right)$$

- ✓ Multiple minibatch gradient steps
- ✓ No second order optimization
- ✓ Simple and stable, without huge updates

PPO in Action



PPO in Action



Scene 1: Attacking Mid

ACTIONS OBSERVATIONS

Action: Ability Nethertoxin

<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>

Target Necrophos

<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>									

Offset X

-400	-300	-200	-100	0	100	200	300	400
<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>				

Offset Y

-400	-300	-200	-100	0	100	200	300	400
<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>				

Action Delay

<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>



So should we just use PPO for everything?

IMPLEMENTATION MATTERS IN DEEP POLICY GRADIENTS: A CASE STUDY ON PPO AND TRPO

Logan Engstrom^{1*}, Andrew Ilyas^{1*}, Shibani Santurkar¹, Dimitris Tsipras¹,
Firdaus Janoos², Larry Rudolph^{1,2}, and Aleksander Mądry¹

Open question!

STEP	MUJoCo TASK		
	WALKER2D-V2	HOPPER-V2	HUMANOID-V2
PPO	3292 [3157, 3426]	2513 [2391, 2632]	806 [785, 827]
PPO-M	2735 [2602, 2866]	2142 [2008, 2279]	674 [656, 695]
TRPO	2791 [2709, 2873]	2043 [1948, 2136]	586 [576, 596]
TRPO+	3050 [2976, 3126]	2466 [2381, 2549]	1030 [979, 1083]
AAI	242	99	224
ACLI	557	421	444

Code optimizations may make a
bigger impact than algorithmic ones
→ needs more investigation!

Lecture outline

Recap: Policy Gradient and Variance Reduction



Natural Policy Gradients and Covariant Parameterization



Trust Region Policy Optimization

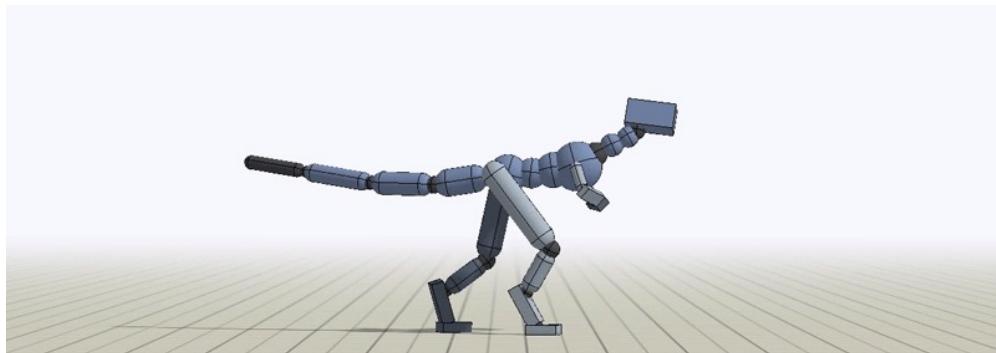
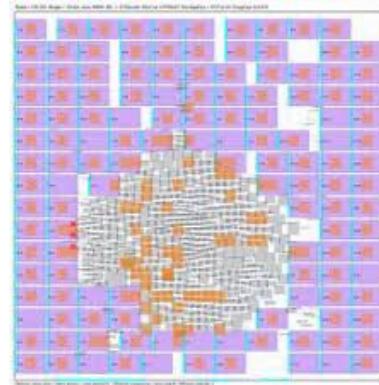


Proximal Policy Optimization

Pros/Cons of Policy Gradient Methods

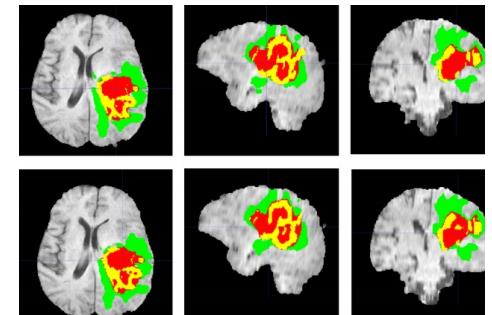
Pros

- Conceptually simple, easy to implement
- Stable, good asymptotic performance
- Compatible with deep models
- Require minimal modeling



Cons

- Sample inefficient
- Unable to reuse prior data effectively → on-policy
- Blackbox, can be hard to debug



Frontiers of Policy Gradient Research

Major open challenges in policy gradient research:

Convergence guarantees

Asynchronous/Parallel Methods

Better Variance Reduction

Learning from high-dimensional inputs

Bootstrapping from prior data

Multi-agent Policy Gradient

Frontiers of Policy Gradient Research

Convergence guarantees and empirical investigations

Globally Convergent in LQR/LQG Case

- Gradient descent case: For an appropriate (constant) setting of the stepsize η ,

$$\eta = \text{poly} \left(\frac{\mu \sigma_{\min}(Q)}{C(K_0)}, \frac{1}{\|A\|}, \frac{1}{\|B\|}, \frac{1}{\|R\|}, \sigma_{\min}(R) \right)$$

and for

$$N \geq \frac{\|\Sigma_{K^*}\|}{\mu} \log \frac{C(K_0) - C(K^*)}{\varepsilon} \\ \times \text{poly} \left(\frac{C(K_0)}{\mu \sigma_{\min}(Q)}, \|A\|, \|B\|, \|R\|, \frac{1}{\sigma_{\min}(R)} \right),$$

then, with high probability, gradient descent (Equation 8) enjoys the following performance bound:

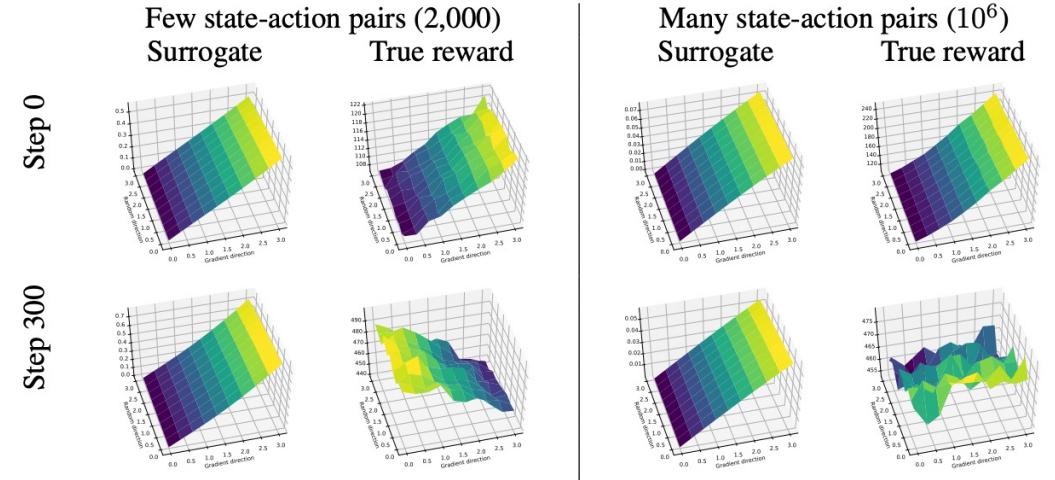
$$C(K_N) - C(K^*) \leq \varepsilon.$$

Global Convergence of Policy Gradient Methods for the Linear Quadratic Regulator, Fazel et al '19

Global Convergence of Policy Gradient Methods to (Almost) Locally Optimal Policies, Zhang et al, '19

Globally convergent policy search over dynamic filters for output estimation, Umenberger '21

Practical Algorithms Deviate from Theory



Is the Policy Gradient a Gradient?, Nota et al, '19

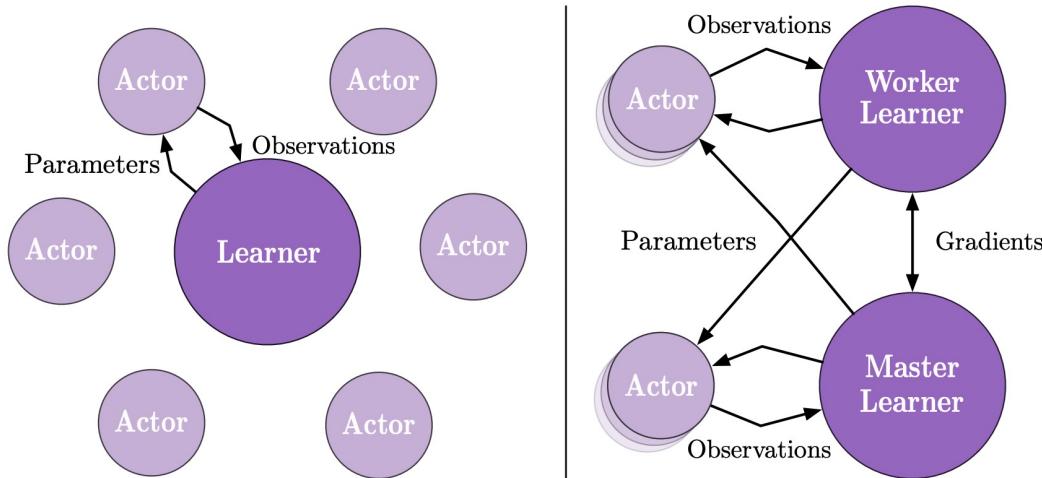
A Closer Look at Deep Policy Gradients, Illyas et al '19

An Empirical Analysis of Proximal Policy Optimization with Kronecker-factored Natural Gradients, Song et al '18

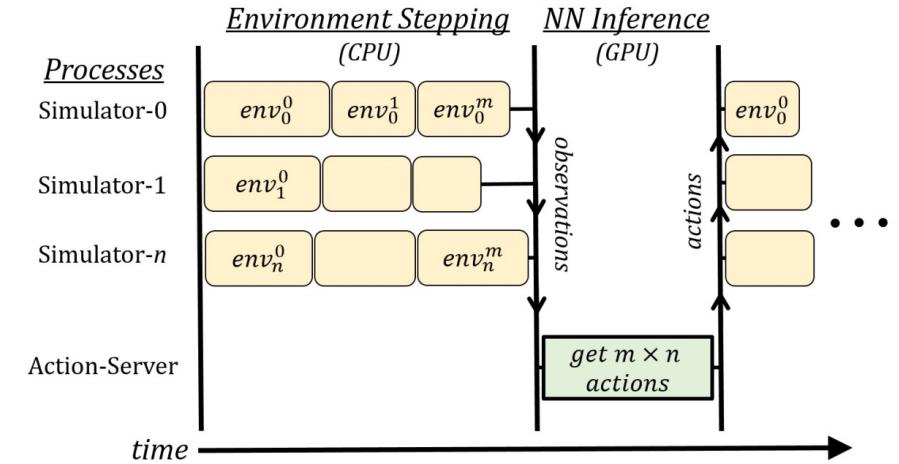
What Matters In On-Policy Reinforcement Learning? A Large-Scale Empirical Study, Andrychowicz et al '20

Frontiers of Policy Gradient Research

Asynchronous methods for large scale speedup



IMPALA: Scalable Distributed Deep-RL with Importance Weighted Actor-Learner Architectures, Espeholt '18



Accelerated Methods for Deep Reinforcement Learning, Stooke et al '19



Frontiers of Policy Gradient Research

Better Variance Reduction Methods

Action dependent baselines

$$\pi_\theta(a_t|s_t) = \prod_{i=1}^m \pi_\theta(a_t^i|s_t)$$

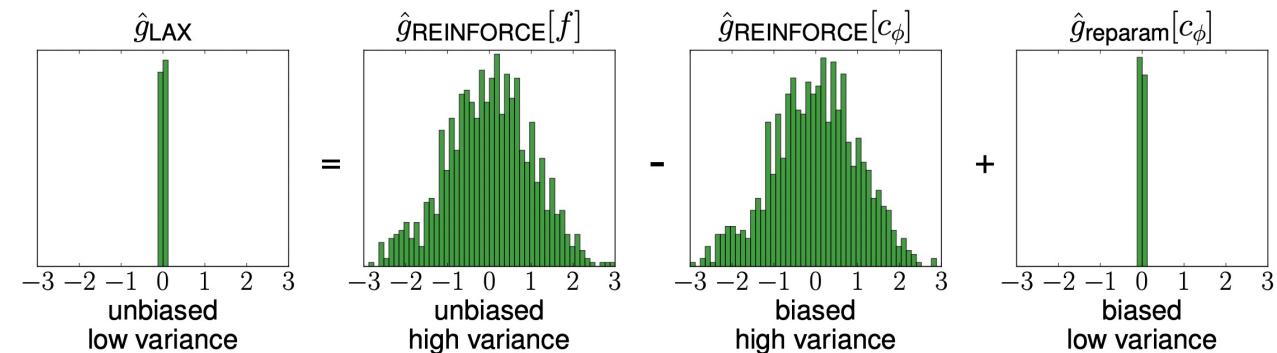
$$\nabla_\theta \eta(\pi_\theta) = \mathbb{E}_{\rho_\pi, \pi} \left[\sum_{i=1}^m \nabla_\theta \log \pi_\theta(a_t^i|s_t) \left(\hat{Q}(s_t, a_t) - b_i(s_t, a_t^{-i}) \right) \right]$$

For factorized spaces, baselines can depend on independent action factors

The Mirage of Action-Dependent Baselines in Reinforcement Learning, Tucker et al '18

Variance Reduction for Policy Gradient with Action-Dependent Factorized Baselines, Wu et al '18

Alternative Estimators



Q-Prop: Sample-Efficient Policy Gradient with An Off-Policy Critic, Gu et al '16

Backpropagation through the Void: Optimizing control variates for black-box gradient estimation, Grathwohl et al '17

Categorical Reparameterization with Gumbel-Softmax, Jang et al '16

Frontiers of Policy Gradient Research

Learning from High Dimensional Observations

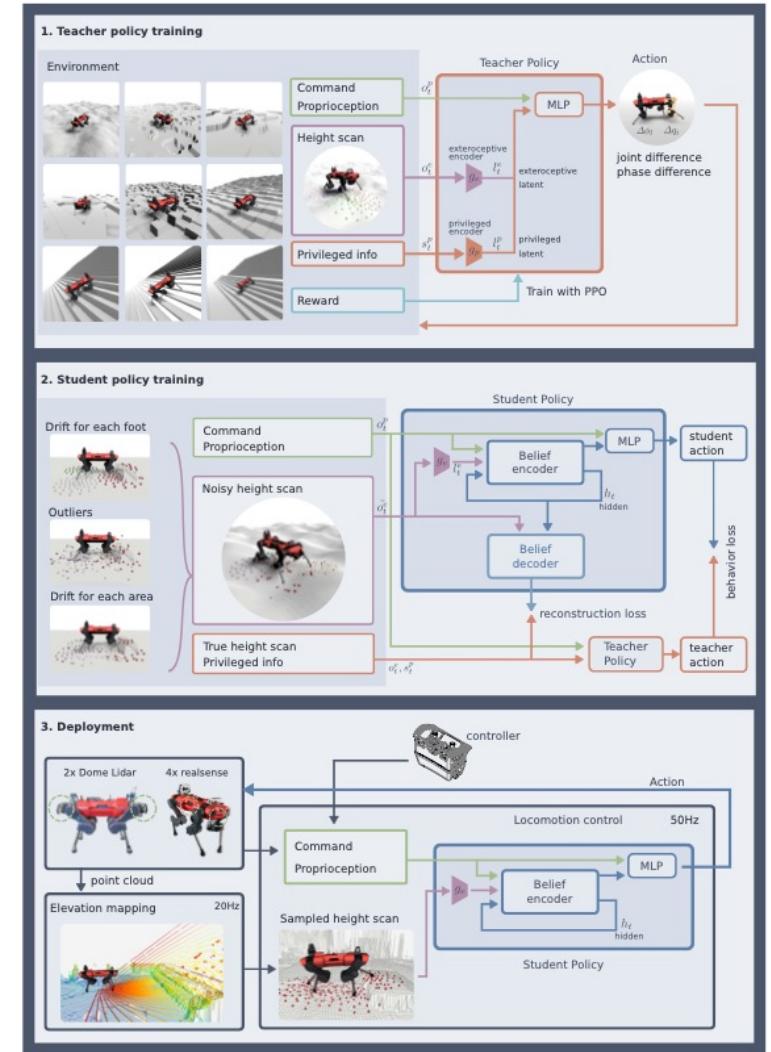
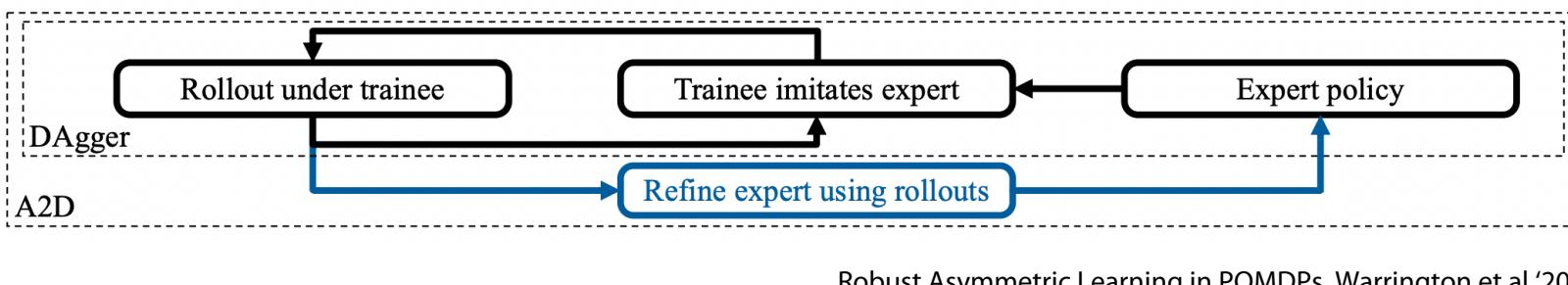


Learning Quadrupedal Locomotion over Challenging Terrain, Lee et al '20



A System for General In-Hand Reorientation, Chen et al '21

Challenging to provide guarantees in partially observed settings!



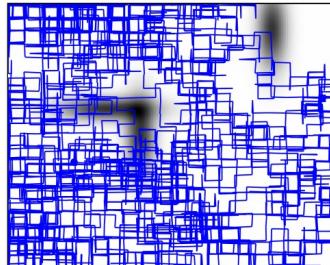
Frontiers of Policy Gradient Research

Bootstrapping from Prior/Off-Policy Data

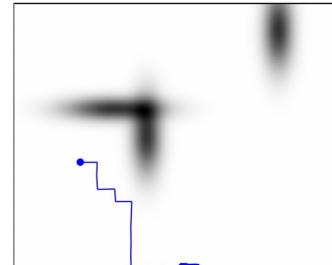
Off-policy policy gradient

$$\mathbb{E}_\beta \left[\frac{\pi_\theta(a|s)}{\beta(a|s)} Q^\pi(s, a) \nabla_\theta \ln \pi_\theta(a|s) \right]$$

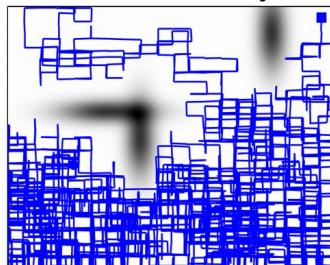
Behavior



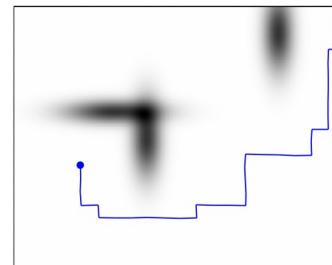
Greedy-GQ



Softmax-GQ

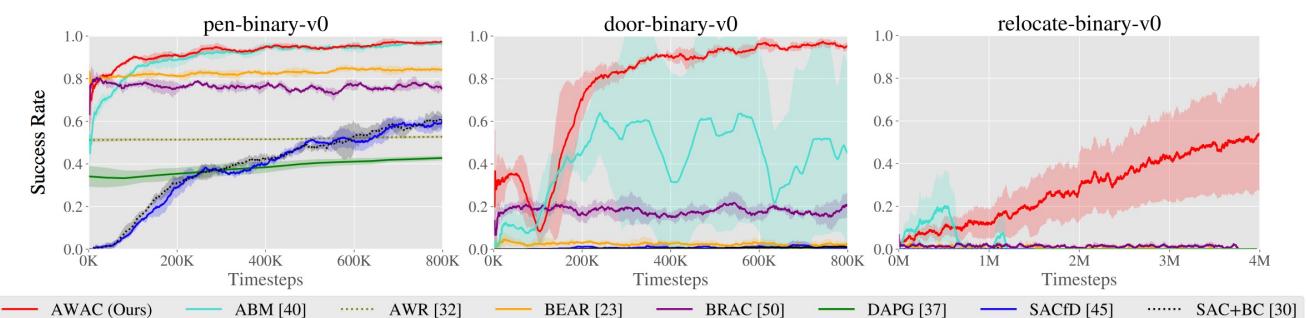


Off-PAC



Off-Policy Actor-Critic, Degris et al '13

Learning from Prior Data



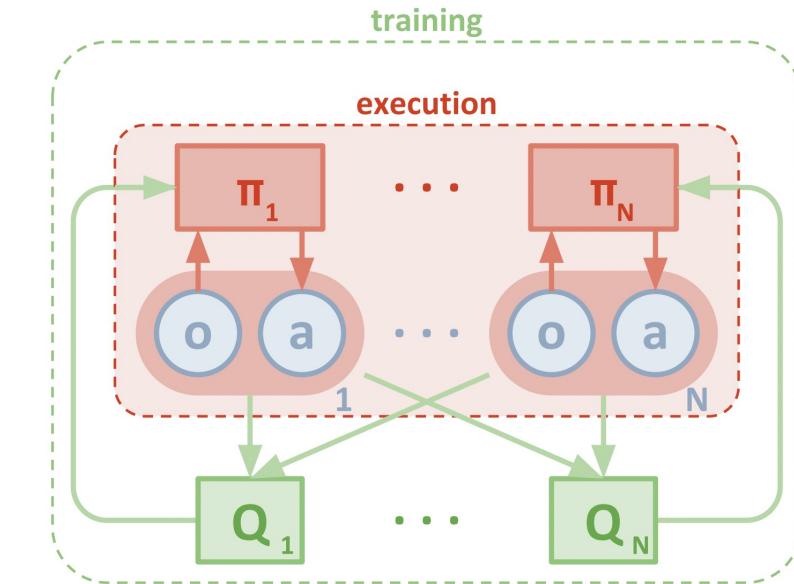
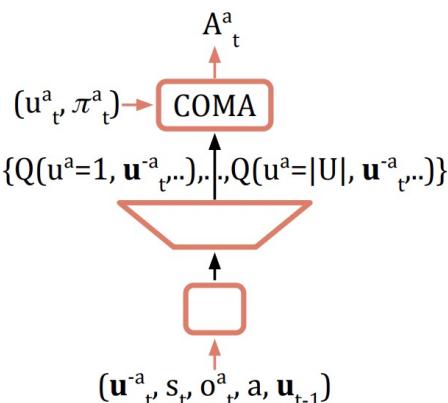
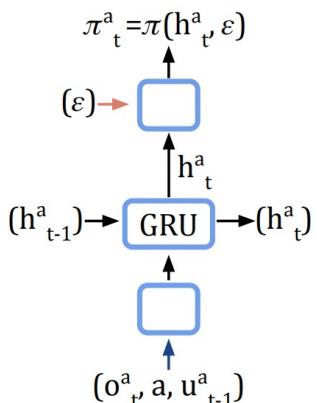
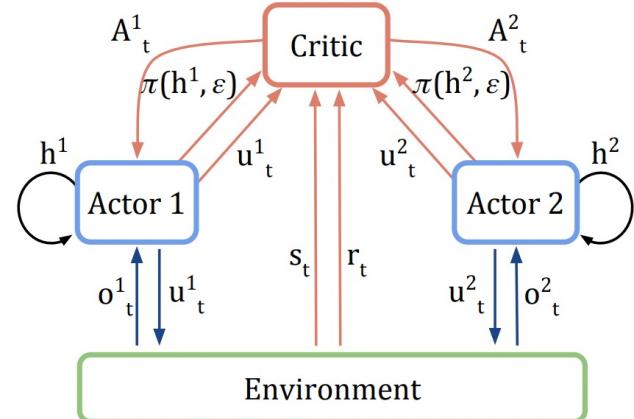
Advantage Weighted Actor Critic, Nair et al '20

DDPGfD, Vecerik '17

DAPG, Rajeswaran '17

Frontiers of Policy Gradient Research

Multi-agent policy gradient



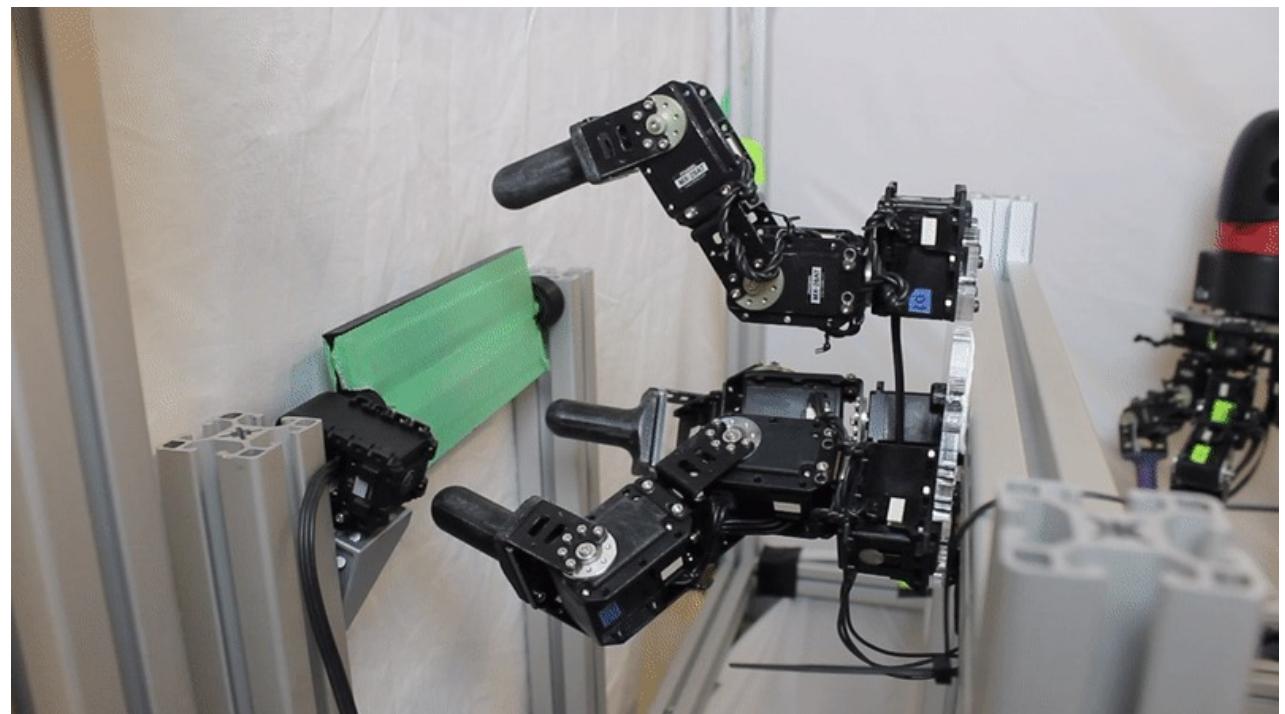
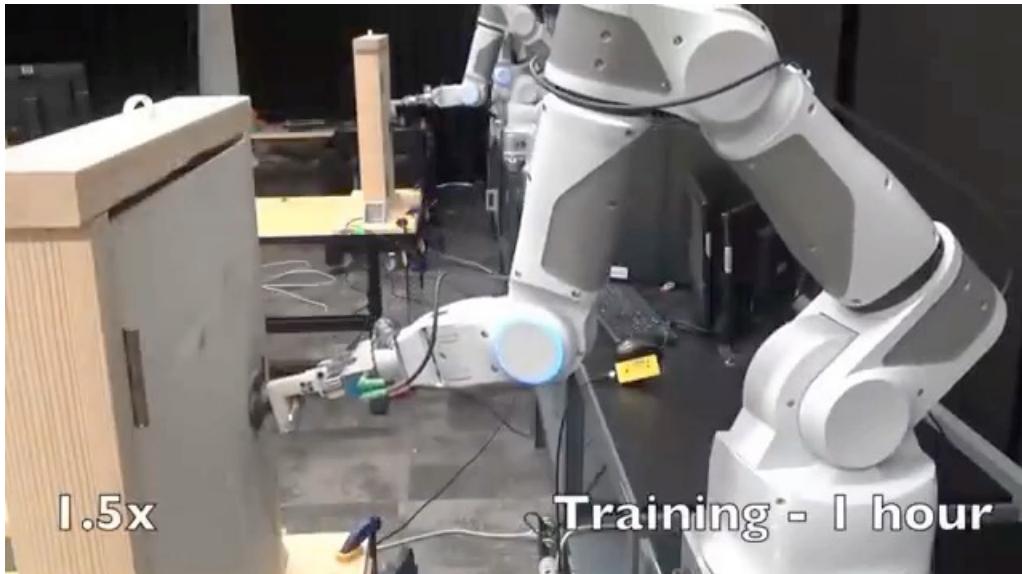
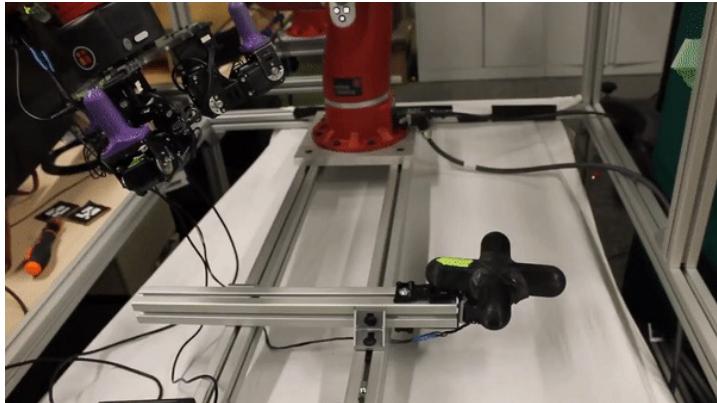
Counterfactual Multi-Agent Policy Gradients, Foerster et al '17

Multi-Agent Actor-Critic for Mixed Cooperative-Competitive Environments, Lowe et al '17

- Primary challenges:**
1. Non-stationarity
 2. Data-efficiency
 3. Communication

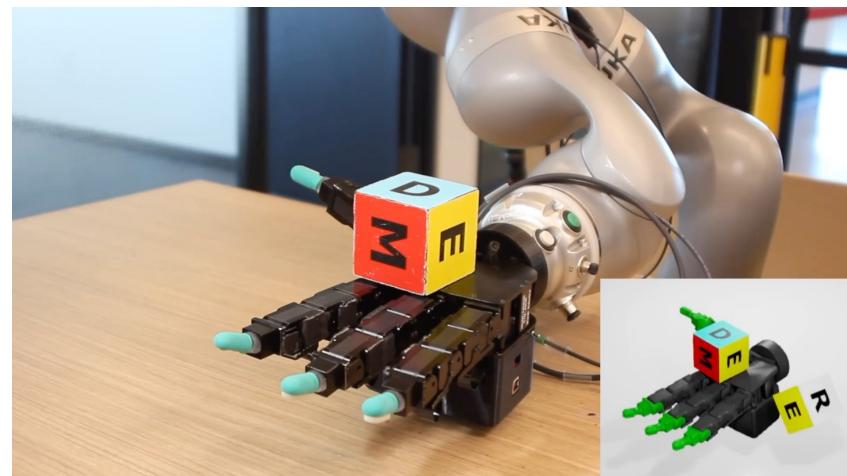
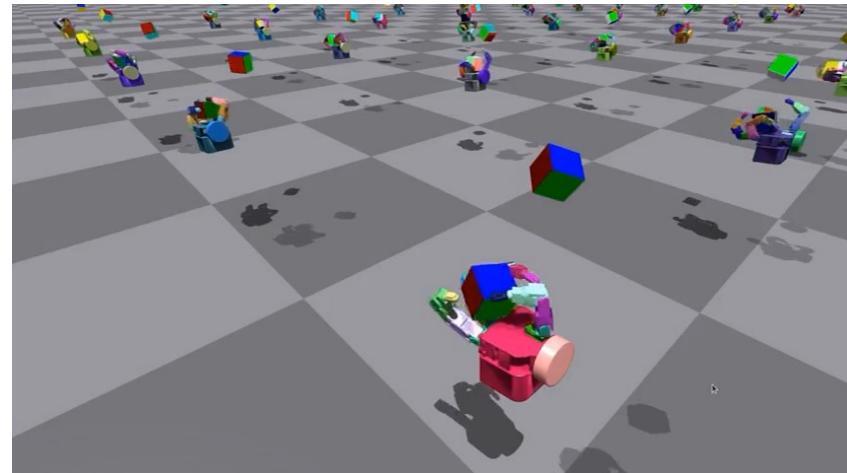
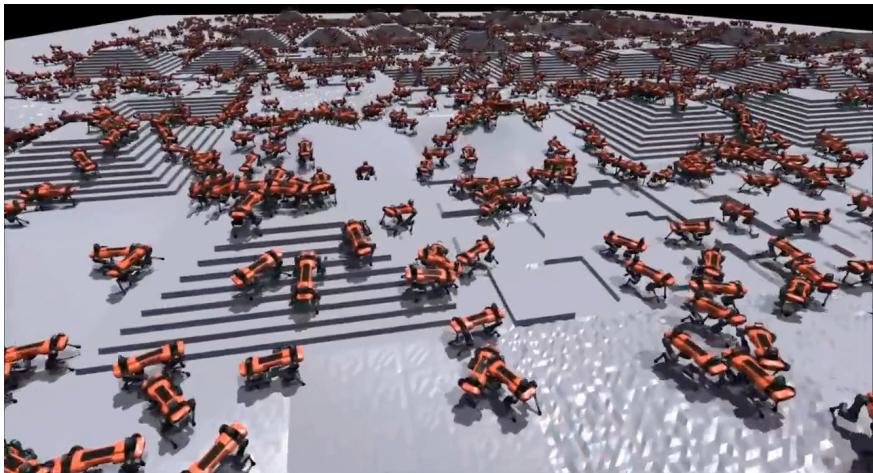
How is this useful for robotics?

Can be used to train robots in the real world but only in limited settings



How is this useful for robotics?

Largely useful for pretraining in simulation



More in the sim2real lecture!

Summary

- Policy gradient methods form an effective solution technique to the RL problem
- Techniques range from vanilla policy gradient to NPG to PPO, each with it's own pros and cons
- PG can be very adept at solving black-box optimization asymptotically, but can be very slow
- Several open frontiers still exist for research into PG methods
- Most promising use of PG methods in robotics is through simulation to reality transfer