# Connectivity-based Parcellation of 

 Human Inferior Parietal Lobule using Diffusion MRI and Probabilistic Tractography
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## Outine

- Background
- Diffusion MRI
- Human inferior parietal lobule
- Materials \& Methods
- Data Collection
- Connectivity Map Preparation via preprocessing
- Unsupervised Classification Approaches (Spectral clustering)
- Results
- Pseudo truth from Jülich Atlas
- K means, Mixture Gaussian, and Spectral Clustering
- Correspondence accuracy metric for parcellation evaluation


## BACKGROUND

## Diffusion in White Matter



Diffusion 'Ellipse'
Water Motion

## Inferior Parietal Lobule

- Brain region with marked functional heterogeneity involved in visuospatial attention, memory, and mathematical cognition
- Availability of ECoG electrodes to verify and make testable predications in our study
- Consisted of seven cytoarchitectonic regions (PGp, PGa, PF, PFcm, PFm, PFt, Pfop)


## Prior Knowledge of IPL Connectivity

Connectivity patern of five IPL areas


Significant results of the comparisor, of seed-target vs. "free" tracing for five IPL areas cist layed on a schematic drawing of a hemisphero. Colored dots mark connections of the respectively crior-c eded IPL areas. Only target areas with atleast one significant connection with an IPL area are displayed.

Rostral IPL areas: targets in the prefrontal, motor, somatosensory, and anterior superior parietal cortex

Caudal IPL areas: targets in the posterior superior parietal and temporal areas

## MATERIALS \& METHODS

## Data

- One subject
- Diffusion weighted data ( $128 \times 128 \times 70$ )
- B value - 1000
- Acquired in 63 gradient directions
- T1 coronal data ( $256 \times 256 \times 208$ )
- Manually extracted brain data
- T1 MNI 152 1mm standard data
(182x218x182)
- Juelich atlas


## Tools for Brain Analysis

- FreeSurfer: automated tools for reconstruction of the brain's cortical surface from structural MRI data, and overlay of functional MRI data onto the reconstructed surface.
- FSL: a comprehensive library of analysis tools for FMRI, MRI and DTI brain imaging data.
FSL runs on Apples, Linux, and Windows. Most of the tools can be run both from the command line and as GUIs.
- SPM: a statistical package for processing brain data including fMRI, SPECT, PET, EEG, MEG.


## Juelich Atlas

Juelich histological (cyto- and myelo-architectonic) atlas
A probabilistic atlas created by averaging multi-subject post-mortem cyto- and myelo-architectonic segmentations. The atlas contains 52 grey matter structures and 10 white matter structures. This is an update to the data used in Eickhoff's Anatomy Toolbox v1.5.

The atlas is based on the miscroscopic and quantitative histological examination of ten human post-mortem brains. The histological volumes of these brains were 3D reconstructed and spatially normalized into the space of the MNI single subject template to create a probabilistic map of each area. For the FSL version of this atlas, these probabilistic maps were then linearly transformed into MNI152 space.

## Flowchart



## Estimation of Distribution of Diffusion using FSL BEDPOSTX

- Bayesian Estimation of Diffusion Parameters Obtained using Sampling Techniques (BEDPOSTX) to build up distribution of diffusion parameters at each voxel
- Partial model allowing for fiber direction mixed with an isotropic ally diffusion model
- A parameterized model of the transfer function between a distribution of fiber orientations in a voxel and the measured diffusion weighted signal
- Use of Markov Chain Monte Carlo (MCMC) sampling to estimate the posterior distribution on parameters of interest


## WGMI Partition using Freesurfer

- White gray matter interface (WGMI) Partition
- Gray matter does not have enough connectivity information for parcellation
- Atlas based cortical registration (a2009 atlas)
- Seed regions: inferior parietal lobule (IPC) including angus and super marginal
- Target regions: all cortical regions except IPC


## Connectivity Matrix Calculation using Probabilistic Tractography (FSL PROBTRACKX)

- Each value in the connectivity matrix indicates the probability that the seed particle can reach the target region through probabilistic tractography

ID \# of target regions

connectivity probability =
(number of particles that reached the target region) / (total number of particles issued from the seed voxel)

Connectivity matrix

## Juelich Atlas for Verification



Post-process group averaged probability map

## Labeling Approaches

- K-Means Clustering
- Mixture of Gaussians (EM Clustering)
- Spectral Clustering (Graph - cut)


## Spectral Clustering

- Spectral Clustering
- Build the similarity graph through pair-voxel correlation of connectivity similarity and spatial affinity
- Solve the normalized graph-cut problem through Eigen decomposition of similarity matrix



## Normalized cut of the Similarity Graph

- Normalized cut

$$
\operatorname{Ncut}(\mathrm{A}, \mathrm{~B})=\begin{array}{rr|}
\hline \operatorname{cut}(\mathrm{A}, \mathrm{~B}) & \operatorname{cut}(\mathrm{A}, \mathrm{~B}) \\
------------------ \\
\operatorname{asso}(\mathrm{A}, \mathrm{~V}) & \operatorname{asso}(\mathrm{B}, \mathrm{~V}) \\
\hline
\end{array}
$$

- Example


## A



## RESULTS

## Data Summary

- Left Hemisphere IPL Parcellation (LH-IPL)
- 667 voxels selected as seed for probabilistic tractography
- 148 targets are selected for probabilistic tractography, 3 targets are discarded due to lack of enough connectivity
- Right hemisphere IPL Parcellation (RH-IPL)
-617 voxels selected as seed for probabilistic tractography
- 148 targets are selected for probabilistic tractography, 2 targets are discarded due to lack of enough connectivity


## Lh-IPL: 3D Sagittal View



Kmeans ( $\mathrm{N}=5$ )


Spectral clustering ( $\mathrm{N}=5$ )

## Lh-IPL - 2D Views (Kmeans, N=5)



Grey clusters are the atlas, while the colored ones are clustered by kmeans

## Lh-IPL - 2D Views (EM, N=5)



Grey clusters are the atlas, while the colored ones are clustered by EM

## Lh-IPL - 2D Views (SC, N=5)



Grey clusters are the atlas, while the colored ones are clustered by Spectral Clustering

## Normalized Connectivity Matrix

3211-lh-ipc-Connectivity matrix before spectral clustering


Before spectral clustering

3211-lh-ipc-Connectivity matrix after spectral clustering


After spectral clustering

## Connectivity Similarity Matrix of Spectral Clustering



Before spectral clustering


After spectral clustering

## Affinity Matrix of Spectral Clustering



Before spectral clustering


After spectral clustering

## Interpretation of the Clusters (LH-IPL)

|  | PGp | PGa | PFm | PF | PFt | PFop | PFcm | Total | Top 3 connected targets |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cluster\#1 | $\begin{aligned} & 88 \\ & \text { (96.7\%) } \end{aligned}$ | 2 | 0 | 1 | 0 | 0 | 0 | 91 | wm_lh_S_temporal_sup wm_lh_S_oc_sup_and_transversal wm_lh_S_intrapariet_and_P_trans |
| Cluster \#2 | 0 | 0 | 4 | $\begin{aligned} & 69 \\ & (53.1 \%) \end{aligned}$ | 26 | 29 | 0 | 135 | wm_lh_S_postcentral wm_lh_G_and_S_subcentral wm_Ih_G_front_inf-Opercular |
| Cluster \#3 | $\begin{aligned} & 48 \\ & (40.1 \%) \end{aligned}$ | 25 | 31 | 14 | 0 | 0 | 0 | 119 | wm_Ih_S_intrapariet_and_P_trans wm_Ih_S_interm_prim-Jensen wm_lh_G_parietal_sup |
| Cluster \#4 | 0 | 0 | 0 | 33 | 0 | $\begin{aligned} & 66 \\ & (46.5 \%) \end{aligned}$ | 43 | 163 | wm_Ih_Lat_Fis-post wm_lh_G_and_S_subcentral wm_lh_S_circular_insula_sup |
| Cluster \#5 | 4 | 34 | 53 | $\begin{aligned} & 67 \\ & (42.1 \%) \end{aligned}$ | 0 | 0 | 1 | 159 | wm_lh_S_interm_prim-Jensen wm_lh_S_temporal_sup wm_Ih_G_temporal_middle |

# Additional Study 

Bilge Soran<br>Quals Project<br>November 2011

## Outline of Work

- Tried several variants of normalized graph cuts
- Used both connectivity and spatial distance information
- Tried several different connectivity similarity functions
- Tried several different spatial distance functions
- Developed a spatial affinity function
- Tried out a feature selection approach
- Developed a new metric for evaluation


## Similarity matrix computation

- Build a normalized connectivity matrix using probabilistic tractography. The values are normalized by dividing by the largest value of the matrix.
- Build a symmetric spatial distance matrix


## Connectivity Similarity Function

$$
W_{c o n n}^{i, j}=\exp \left(-\alpha * f_{c o n n}\left(p_{i}, p_{j}\right) / \sigma_{c o n n}^{2}\right)
$$

(whereo is a weighting factor and set to 2.)

Distance Functions:

- Euclidean
- Standardized Euclidean
- Mahalanobis
- City Block
- Minkowski
- Cheybchev
- Jaccard
- Cosine
- Correlation
- Hamming


## Spatial Affinity Functions

$$
\begin{gathered}
W_{s p a t i a l}^{i, j}=\exp \left(-(1-\alpha) * \operatorname{dist}(i, j) / \sigma_{\text {spatial }}^{2}\right) \\
W_{\text {spatial }}^{i, j}=2 *(1-\alpha) *(\operatorname{dist}(i, j)<\operatorname{median}(\operatorname{dist}))
\end{gathered}
$$

(whereo is a weighting factor and set to 0.5.)

$$
\begin{gathered}
\operatorname{dist}(i, j)=\max \left(\left|i_{x}-j_{x}\right|,\left|i_{y}-j_{y}\right|,\left|i_{z}-j_{z}\right|\right) \\
\operatorname{dist}(i, j)=\sqrt{\left(i_{x}-j_{x}\right)^{2}+\left(i_{y}-j_{y}\right)^{2}+\left(i_{z}-j_{z}\right)^{2}} \\
\operatorname{dist}(i, j)=\operatorname{dist}(i, j)=\left(i_{x}-j_{x}\right)+\left(i_{y}-j_{y}\right)+\left(i_{z}-j_{z}\right)
\end{gathered}
$$

## Similarity matrix computation

- Compute the composite similarity matrix with one of the equations below:

$$
\begin{aligned}
& W_{\text {similarity }}^{i, j}=W_{c o n n}^{i, j} * W_{\text {spatial }}^{i, j} \\
& W_{\text {similarity }}^{i, j}=W_{\text {conn }}^{i, j}+W_{\text {spatial }}^{i, j}
\end{aligned}
$$

## Graph-Cuts Variants

1. Standard Normalized Graph Cuts
2. Normalized Graph Cuts with Feature Selection
3. Normalized Graph Cuts with K-means

## Similarity matrix computation



## Feature Selection by Target Elimination

- Not all voxels have connections to all target regions.
- The variance of a target region is computed by using the connectivity values in its column of the connectivity matrix with the standard formula:

$$
\frac{1}{n} \sum_{i=1}^{n}\left(x_{i}-\mu\right)^{2}
$$

- After computing the variance for each target region, a threshold is applied to select targets with high variances since they are expected to carry discriminative information.


## Evaluation

- An example table used in evaluation:

|  | Atlas Cluster 1 | Atlas Cluster 2 | Atlas Cluster 3 \| | Alas Cluster 4 | Atlas Cluster 5 | Alas Cluster 6 | Atlas Cluster 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NCut Cluster 1 | 0 | 0 | 0 | 91 | 15 | 3 | 0 |
| NCut Cluster 2 | 0 | 0 | 0 | 24 | 0 | 79 | 8 |
| NCut Cluster 3 | 0 | 53 | 67 | 9 | 0 | 0 | 0 |
| NCut Cluster 4 | 6 | 78 | 14 | 4 | 0 | 0 | 2 |
| NCut Cluster 5 | 91 | 31 | 0 | 0 | 0 | 0 | 0 |

## Evaluation Metric

$$
\begin{gathered}
A=\left(\sum_{i} \max \left(\text { row }_{i}\right)\right) /\left(\sum_{i j} \text { cell }_{i j}\right) \\
B=\left(\sum_{j} \max \left(\text { column }_{i}\right)\right) /\left(\sum_{i j} \operatorname{cell}_{i j}\right) \\
I f(A-B)<0.2 \quad R=(A+B) / 2
\end{gathered}
$$

Else the resulting parcellation is wrong.

## RESULTS

## Parcellation of Subject 3211:

## Connectivity Matrix Before Parcellation

3211-1h pc -Connectivity matrix before spectral clustering


## Parcellation of Subject 3211:

## Connectivity Matrix After Parcellation



## Parcellation of Subject 3211: Connectivity Variances Before Parcellation

Variance of cluster raudata

$\begin{array}{lllllllllllll}5 & 10 & 15 & 20 & 25 & 30 & 354045 & 50 & 55 & 60 & 65707580859095100105110115120125130135140145 \\ \text { Target regions }\end{array}$

## Parcellation of Subject 3211: Variance of Each Cluster After Parcellation







## Parcellation of Subject 3211:

## Performances of Different Clustering Methods



## Parcellation of Subject 3211:

## Performances of Different Clustering Methods



Atlas


Mean-Shift


EM


Sparse K-means


K-means


Normalized Graph Cuts

## Work in Progress

## Parcellation of 19 Subjects:

Based on the selected parameters from the parcellation of Subject 3211

|  | LEFT HEMISPHERE |
| :---: | :---: |
|  | Normalized Cuts with Target Elimination |
|  | Alpha $=0.5$ |
|  | Similarity Matrix construction = SUM |
|  | Distance Function = Jaccard |
| SUBJECT | BEST RESULT |
| 3211 | 0.650273 |
| 3402 | 0.603636 |
| 3407 | 0.520629 |
| 3414 | 0.697107 |
| 3422 | 0.607826 |
| 3424 | 0.621622 |
| 3425 | 0.537037 |
| 3484 | 0.635490 |
| 3485 | 0.638649 |
| 3486 | 0.607445 |
| 3487 | 0.604724 |
| 3488 | 0.686678 |
| 3492 | 0.615960 |
| 3496 | 0.621302 |
| 3497 | 0.567294 |
| 3498 | 0.588542 |
| 3503 | 0.648148 |
| 3504 | 0.685022 |
| 3505 | 0.644431 |

## Parcellation of 19 Subjects:

Based on the selected parameters from the parcellation of Subject 3211

|  | RIGHT HEMISPHERE |
| :---: | :---: |
|  | Normalized Cuts with Target Elimination |
|  | Alpha $=0.5$ |
|  | Similarity Matrix construction = SUM |
|  | Distance Function =" Jaccard" |
| SUBJECT | BEST RESULT |
| 3211 | 0.619906 |
| 3402 | 0.671701 |
| 3407 | 0.597689 |
| 3414 | 0.620827 |
| 3422 | 0.638840 |
| 3424 | 0.564067 |
| 3425 | 0.673877 |
| 3484 | 0.575038 |
| 3485 | 0.566434 |
| 3486 | 0.551825 |
| 3487 | 0.633803 |
| 3488 | 0.561350 |
| 3492 | 0.671875 |
| 3496 | 0.669528 |
| 3497 | 0.608730 |
| 3498 | 0.660506 |
| 3503 | 0.575816 |
| 3504 | 0.645977 |
| 3505 | 0.617366 |

# Parcellation of 19 Subjects: Best Parameters (Left Hemisphere) 

| Method | \# of <br> Cluster | $\alpha$ | Distance <br> Function | Spatial <br> Coherence | Similarity <br> Matrix |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Normalized Graph Cuts | 5 | 0.9 | Hamming | Threshold | Multiply |
| Normalized Graph Cuts <br> with target elimination | 5 | 0.8 | City block | Weight | Sum |

## Parcellation of 19 Subjects:

## Parcellation Evaluation based on the

 training parameters (Left Hemisphere)| Subject | Normalized Graph Cuts | Normalized Graph Cuts <br> With Target Elimination |
| :--- | :--- | :--- |
| 3211 | 0.589481 | 0.661202 |
| 3402 | 0.660000 | 0.629091 |
| 3407 | 0.586444 | 0.605108 |
| 3414 | 0.706148 | 0.696203 |
| 3422 | 0.660870 | 0.726087 |
| 3424 | 0.689189 | 0.664619 |
| 3425 | 0.659612 | 0.567019 |
| 3484 | 0.597028 | 0.648601 |
| 3485 | 0.638649 | 0.630747 |
| 3486 | 0.586294 | 0.621827 |
| 3487 | 0.568504 | 0.609449 |
| 3488 | 0.696546 | 0.696546 |
| 3492 | 0.608479 | 0.569825 |
| 3496 | 0.640039 | 0.666667 |
| 3497 | 0.594067 | 0.569465 |
| 3498 | 0.618750 | 0.632292 |
| 3503 | 0.652778 | 0.577160 |
| 3504 | 0.615639 | 0.621145 |
| 3505 | 0.643819 | 0.605263 |
| AVERAGE | 0.632228 | 0.631490 |

## Parcellation with Target Elimination Results:

 Subjects 3414, 3422, 3488 (Left Hemisphere)

Atlas in 3422's FA space



3414


## Parcellation of 19 Subjects: Best Parameters (Right Hemisphere)

| Method | \# of <br> Cluster | $\alpha$ | Distance <br> Function | Spatial <br> Coherence | Similarity <br> Matrix |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Normalized Graph Cuts | 5 | 0.6 | Jaccard | Weight | Sum |
| Normalized Graph Cuts <br> with target elimination | 5 | 0.6 | Jaccard | Weight | Sum |
| N |  |  |  |  |  |

## Parcellation of 19 Subjects:

## Parcellation Evaluation based on the

 training parameters (Right Hemisphere)| Subject | Normalized Graph Cuts | Normalized Graph Cuts <br> With Target Elimination |
| :--- | :--- | :--- |
| 3211 | 0.625392 | 0.626959 |
| 3402 | 0.753577 | 0.751987 |
| 3407 | 0.718487 | 0.710084 |
| 3414 | 0.569952 | 0.570747 |
| 3422 | 0.652021 | 0.655536 |
| 3424 | 0.637883 | 0.646240 |
| 3425 | 0.640599 | 0.640599 |
| 3484 | 0.593415 | 0.601072 |
| 3485 | 0.627622 | 0.628497 |
| 3486 | 0.683212 | 0.682482 |
| 3487 | 0.590669 | 0.590669 |
| 3488 | 0.611452 | 0.615542 |
| 3492 | 0.747917 | 0.746875 |
| 3496 | 0.657725 | 0.653433 |
| 3497 | 0.666667 | 0.666667 |
| 3498 | 0.657588 | 0.701362 |
| 3503 | 0.600768 | 0.599808 |
| 3504 | 0.611494 | 0.611494 |
| 3505 | 0.670802 | 0.669847 |
| AVERAGE | 0.648276 | 0.651047 |

## Parcellation with Target Elimination Results:

 Subjects 3402, 3407, 3492 (Right Hemisphere)

Atlas in 3402's FA space



3407


3492

## Comparison of Normalized Graph Cuts

- Standard NGC with feature selection produced best results in most of the tests.
- Standard NGC without feature selection produced results very close to those with feature selection.
- NGC with k-means produced incorrect parcellations according to the metric.


## Conclusion

- Different clustering methods were applied to an anatomical connectivity map, which is obtained by DTI-based tractography of the IPL of a living subject to parcellate it into component regions with different connectivity patterns.
- Among the different methods investigated, normalized graph cuts showed the best performance.


## Conclusion

- The main difficulty of the evaluation was having no ground truth data by which to measure the quality of our parcellation.
- How many different regions exist in the IPL of a human being is still an unknown. Therefore in this work, different numbers of clusters were tried and the evaluation metric was designed to measure the quality of the overlap with different numbers of clusters.

