Computer Vision

ECE/CSE 576 Corner Detection

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Review: What's an edge?

- Image is a function
- Edges are rapid changes in this function





Image derivatives

Recall: $f'(a) = \lim_{h \to 0} \frac{f(a+h) - f(a)}{h}.$ Want smoothing too! f(x)1/2× -101 * **Sobel Operator** 2 0 -2 f'(x)

Laplacian (2nd derivative)!

Crosses zero at extrema 1 0 **Recall:** $f''(x) = \lim_{h \to 0} \frac{f(x+h) - 2f(x) + f(x-h)}{h^2}$ Laplacian: $\Delta f = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2} \qquad f(x)$ f(x)f(x)Again, have to estimate f"(x): f'(x) f'(x) f''(x) f''(x) •••

Laplacians also sensitive to noise

- Again, use gaussian smoothing
- Can just use one kernel since convs commute
- Laplacian of Gaussian, LoG
- Can get good approx. with
 5x5 9x9 kernels



Difference of Gaussian (DoG)

- Gaussian is a low pass filter
- Strongly reduce components with frequency $f < \sigma$
- (g*I) low frequency components
- I (g*I) high frequency components
- g(σ1)*I g(σ2)*I
 - Components in between these frequencies
- $g(\sigma 1)^*I g(\sigma 2)^*I = [g(\sigma 1) g(\sigma 2)]^*I$



DoGs



Canny Edge Detection

- Your first image processing pipeline!
 - Old-school CV is all about pipelines

Algorithm:

- Smooth image (only want "real" edges, not noise)
- Calculate gradient direction and magnitude
- Non-maximum suppression perpendicular to edge
- Threshold into strong, weak, no edge
- Connect together components

Gradient magnitude and direction

- Sobel filter







Non-maximum suppression



Non-maximum suppression



Non-maximum suppression



Threshold edges

- Still some noise
- Only want strong edges
- 2 thresholds, 3 cases
 - R > T: strong edge
 - R < T but R > t: weak edge
 - R < t: no edge
- Why two thresholds?



http://bigwww.epfl.ch/demo/ip/demos/edgeDetector/

Connect 'em up!

- Strong edges are edges!
- Weak edges are edges iff they connect to strong
- Look in some neighborhood (usually 8 closest)



http://bigwww.epfl.ch/demo/ip/demos/edgeDetector/

Features!

- Highly descriptive local regions
- Ways to describe those regions
- Useful for:
 - Matching
 - Recognition
 - Detection











Keypoint descriptor





How to create a panorama

- Say we are stitching a panorama
- Want patches in image to match to other image
- Hopefully only match one spot





Q1: How close are two patches?

- Sum squared difference
- Images I, J
- $\Sigma_{x,y} (I(x,y) J(x,y))^2$

Q2: How can we find unique patches?

- Sky: bad
 - Very little variation
 - Could match any other sky



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- Edge: ok
 - Variation in one direction
 - Could match other patches along same edge



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- Sky: bad
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- Edge: ok
 - Variation in one direction
 - Could match other patches along same edge
- Corners: good!
 - Only one alignment matches



What are we going to do?

- We are going to build a panorama from two (or more) images.
- We need to learn about
 - Finding interest points
 - Describing small patches about such points
 - Finding matches between pairs of such points on two images, using the descriptors
 - Selecting the best set of matches and saving them
 - Constructing homographies (transformations) from one image to the other and picking the best one
 - Stitching the images together to make the panorama

Preview: Harris detector



Interest points extracted with Harris (~ 500 points)

How can we find corresponding points?



Not always easy



NASA Mars Rover images

Answer below (look for tiny colored squares...)



NASA Mars Rover images with SIFT feature matches Figure by Noah Snavely

Human eye movements



What catches your interest?

Yarbus eye tracking

Interest points

- Suppose you have to click on some point, go away and come back after I deform the image, and click on the same points again.
 - Which points would you choose?



Intuition



Corners

- We should easily recognize the point by looking through a small window
- Shifting a window in any direction should give a large change in intensity



"flat" region: no change in all directions

Source: A. Efros

"edge": no change along the edge direction "corner": significant change in all directions



Let's look at the gradient distributions







Principal Component Analysis

Principal component is the direction of highest variance.

Next, highest component is the direction with highest variance *orthogonal* to the previous components.

How to compute PCA components:

1. Subtract off the mean for each data point.

- 2.Compute the covariance matrix.
- 3.Compute eigenvectors and eigenvalues.

4. The components are the eigenvectors ranked by the eigenvalues.

$$Hx = \lambda x$$



Definition: A scalar λ is called an eigenvalue of the n×n matrix A if there is a nontrivial solution x of Ax= λ x. Such x is called an eigenvector corresponding to the eigenvalue λ .

Corners have ...



Both eigenvalues are large!

Second Moment Matrix or Harris Matrix

$$H = \begin{cases} | \Sigma_i W_i |_X |_X & \Sigma_i W_i |_X |_Y | \\ | \Sigma_i W_i |_X |_Y & \Sigma_i W_i |_Y |_Y \end{cases}$$

2 x 2 matrix of image derivatives smoothed by Gaussian weights.



• First compute I_x , I_y , and $I_x I_{x_j} I_y I_{y_j} I_x I_y$; then apply Gaussian to each.

From HW3: Structure matrix

- Weighted sum of gradient information
 - $| \Sigma_i w_i I_x(i) I_x(i) \Sigma_i w_i I_x(i) I_y(i) |$
 - $| \Sigma_i w_i I_x(i) I_y(i) \Sigma_i w_i I_y(i) I_y(i) |$

We'll tell you how to store this!

- Use Gaussian weighting
- Eigen vectors/values of this matrix summarize the distribution of the gradients nearby
- λ_1 and λ_2 are eigenvalues
 - λ_1 and λ_2 both small: no gradient
 - $\lambda_1 >> \lambda_2$: gradient in one direction
 - λ_1 and λ_2 similar: multiple gradient directions, corner

Estimating Response

$$H = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \quad \lambda_{\pm} = \frac{1}{2} \left((a+d) \pm \sqrt{4bc + (a-d)^2} \right)$$

- A few methods we use to estimate:
- Calculate these directly from the 2x2 matrix
 - det(S) = ad bc = $\lambda_1^* \lambda_2$
 - trace(S) = a + d = $\lambda_1 + \lambda_2$
- Estimate formula 1: R = det(S) α trace(S)² = $\lambda_1 \lambda_2 \alpha (\lambda_1 + \lambda_2)^2$
- Estimate formula 2: R = det(S) / trace(S) = $\lambda_1 \lambda_2 / (\lambda_1 + \lambda_2)$
- If these estimates are large, we call it a corner

Harris Corner Detector

- Calculate derivatives I_x and I_y
- Calculate 3 measures $I_x I_x$, $I_y I_y$, $I_x I_y$
- Calculate weighted sums
 - Want a weighted sum of nearby pixels, guess what this is?
 - Gaussian!
- Estimate response
- Non-max suppression!



Compute corner response R



Find points with large corner response: R > threshold



Take only the points of local maxima of R



Harris Detector: Results



Properties of the Harris corner detector



- Rotation invariant?
- Scale invariant?





All points will be classified as edges





- Can we do better than Harris?
- The Harris corner detector is not widely used except in class assignments.
- The SIFT detector/descriptor is the standard.
- Let's take a look.

Scale



What is the "best" scale?

Scale Invariance



How can we independently select interest points in each image, such that the detections are repeatable across different scales?

K. Grauman, B. Leibe

Differences between Inside and Outside



1. We can use a Laplacian function

Scale

But we use a Gaussian.

Why Gaussian?

It is invariant to scale change, i.e., $f * \mathcal{G}_{\sigma} * \mathcal{G}_{\sigma'} = f * \mathcal{G}_{\sigma''}$ and has several other nice properties. Lindeberg, 1994

In practice, the Laplacian is approximated using a Difference of Gaussian (DoG).



Difference-of-Gaussian (DoG)



G1 - G2 = DoG





K. Grauman, B. Leibe



DoG example

Take Gaussians at multiple spreads and uses DoGs.















Scale invariant interest points

Interest points are local maxima in both position and scale.



Scale (Lowe uses multiple scales)

In practice the image is downsampled for larger sigmas.



Lowe, 2004.

Lowe's Pyramid Scheme



Key point localization

s+2 difference images.top and bottom ignored.s planes searched.

- Scale
- Each point is compared to its 8 neighbors in the current image and 9 neighbors each in the scales above and below

Detect maxima and minima

of difference-of-Gaussian in

scale space

For each max or min found, output is the **location** and the **scale**.

Scale-space extrema detection: experimental results over 32 images that were synthetically transformed and noise added.



- Sampling in scale for efficiency
 - How many scales should be used per octave? S=?
 - More scales evaluated, more keypoints found
 - S < 3, stable keypoints increased too
 - S > 3, stable keypoints decreased
 - S = 3, maximum stable keypoints found

Results: Difference-of-Gaussian



K. Grauman, B. Leibe





How can we find correspondences?



Similarity transform

百列

Rotation invariance



- Rotate patch according to its dominant gradient orientation
- This puts the patches into a canonical orientation.

Orientation Normalization

- Compute orientation histogram
- Select dominant orientation
- Normalize: rotate to fixed orientation

[Lowe, SIFT, 1999]



What's next?

Once we have found the keypoints and a dominant orientation for each,

we need to describe the (rotated and scaled) neighborhood about each.



Important Point

- People just say "SIFT".
- But there are TWO parts to SIFT.
 - 1. an interest point detector
 - 2. a region descriptor
- They are independent. Many people use the region descriptor without looking for the points.