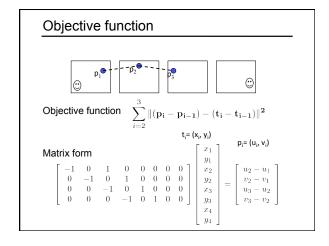
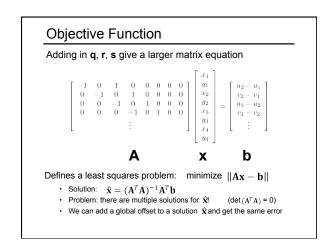
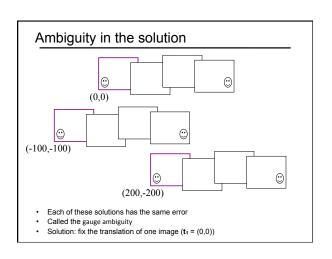


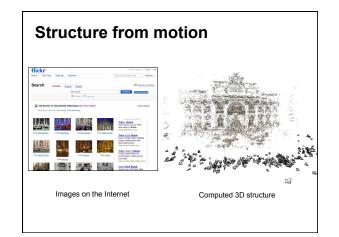
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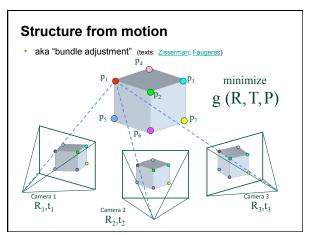
+ similar terms for q, r, s











# SfM objective function

Given point  $\boldsymbol{x}$  and rotation and translation  $\boldsymbol{R},\,\boldsymbol{t}$ 

$$\begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} = \mathbf{R}\mathbf{x} + \mathbf{t} \qquad u' = \frac{fx'}{z'} \\ v' = \frac{fy'}{z'} \qquad \begin{bmatrix} u' \\ v' \end{bmatrix} = \mathbf{P}(\mathbf{x}, \mathbf{R}, \mathbf{t})$$

Minimize sum of squared reprojection errors:

$$g(\mathbf{X}, \mathbf{R}, \mathbf{T}) = \sum_{i=1}^{m} \sum_{j=1}^{n} w_{ij} \cdot \left\| \underbrace{\mathbf{P}(\mathbf{x}_i, \mathbf{R}_j, \mathbf{t}_j)}_{\substack{\text{predicted} \\ \text{image location}}} - \underbrace{\begin{bmatrix} u_{i,j} \\ v_{i,j} \end{bmatrix} \end{bmatrix}^2}_{\substack{\text{observed} \\ \text{image location}}} \right\|_{\text{image location}}$$

### Solving structure from motion

## Minimizing g is difficult:

- g is non-linear due to rotations, perspective division
  lots of parameters: 3 for each 3D point, 6 for each camera
  difficult to initialize
- gauge ambiguity: error is invariant to a similarity transform (translation, rotation, uniform scale)

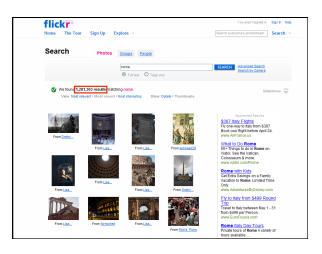
#### Many techniques use non-linear least-squares optimization (bundle adjustment)

- Levenberg-Marquardt is a popular algorithm
  http://en.wikipedia.org/wiki/Levenberg-Marquardt\_algorithm

#### Good code online

- Bundler: <a href="http://phototour.cs.washington.edu/bundler/">http://phototour.cs.washington.edu/bundler/</a>
  Multicore: <a href="http://grail.cs.washington.edu/projects/mcba/">http://grail.cs.washington.edu/projects/mcba/</a>



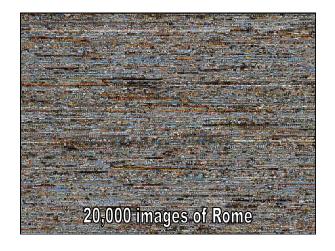








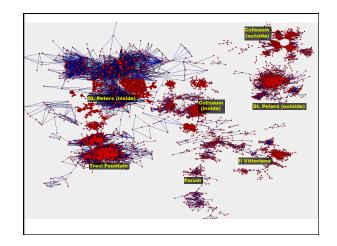


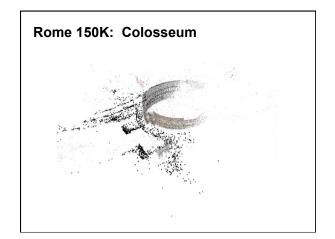


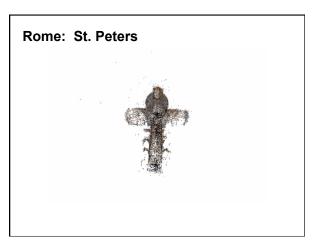


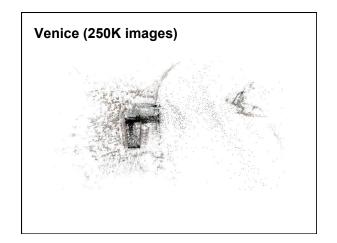
# **Reconstructing Rome**

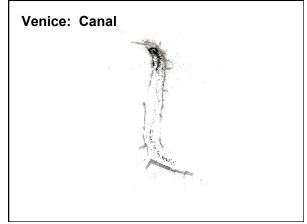
- •In a day...
- •From ~1M images
- •Using ~1000 cores
- •Sameer Agarwal, Noah Snavely, Rick Szeliski, Steve Seitz
- •http://grail.cs.washington.edu/rome

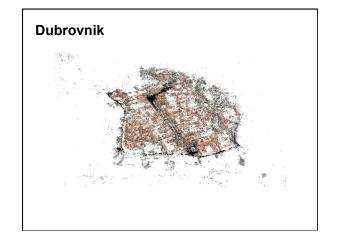












# More info

- Rome-in-a-day page
  - http://grail.cs.washington.edu/rome