Image Stitching

Computer Vision
CSE 576, Spring 2008
Richard Szeliski
Microsoft Research

Panoramic Image Mosaics



Full screen panoramas (cubic): http://www.panoramas.dk/ Mars: http://www.panoramas.dk/fullscreen3/f1.html 2003 New Years Eve: http://www.panoramas.dk/fullscreen3/f1.html

Richard Szeliski Image Stitching 2

Gigapixel panoramas & images

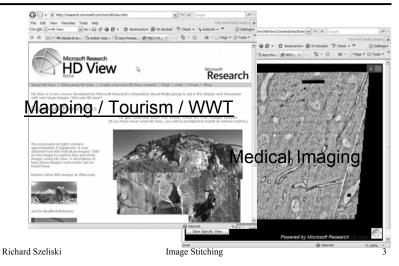
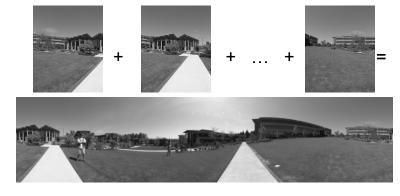


Image Mosaics



Goal: Stitch together several images into a seamless composite

Today's lecture

Image alignment and stitching

- · motion models
- · image warping
- point-based alignment
- complete mosaics (global alignment)
- · compositing and blending
- · ghost and parallax removal

Richard Szeliski

Image Stitching

5

Readings

- Szeliski, CVAA:
 - · Chapter 3.5: Image warping
 - Chapter 5.1: Feature-based alignment (in preparation)
 - · Chapter 8.1: Motion models
 - · Chapter 8.2: Global alignment
 - · Chapter 8.3: Compositing
- Recognizing Panoramas, Brown & Lowe, ICCV'2003
- Szeliski & Shum, SIGGRAPH'97

Richard Szeliski Image Stitching 6

Motion models

Motion models

What happens when we take two images with a camera and try to align them?

- translation?
- rotation?
- · scale?
- affine?



... see interactive demo (VideoMosaic)





Image Warping

Image Warping

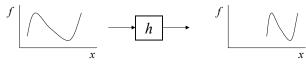
image filtering: change range of image

$$g(x) = h(f(x))$$

$$f = \int_{x}^{f} h \int_{x}^{f} f(x) dx$$

image warping: change domain of image

$$g(x) = f(h(x))$$



Richard Szeliski Image Stitching 10

Image Warping

image filtering: change range of image



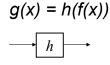




image warping: change domain of image g(x) = f(h(x))







11

Parametric (global) warping

Examples of parametric warps:





affine

Richard Szeliski



rotation



aspect



perspective



cylindrical

Richard Szeliski Image Stitching Image Stitching

2D coordinate transformations

x' = x + ttranslation: $\mathbf{x} = (x, y)$

rotation: x' = R x + t

x' = sRx + tsimilarity:

affine: x' = A x + t

perspective: $\underline{x}' \cong H \underline{x}$ $\underline{x} = (x, y, 1)$

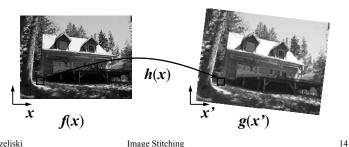
(<u>x</u> is a *homogeneous* coordinate)

These all form a nested *group* (closed w/ inv.)

Richard Szeliski 13 Image Stitching

Image Warping

Given a coordinate transform x' = h(x) and a source image f(x), how do we compute a transformed image g(x') = f(h(x))?

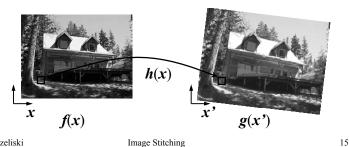


Richard Szeliski Image Stitching

Forward Warping

Send each pixel f(x) to its corresponding location x' = h(x) in g(x')

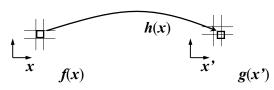
What if pixel lands "between" two pixels?



Forward Warping

Send each pixel f(x) to its corresponding location x' = h(x) in g(x')

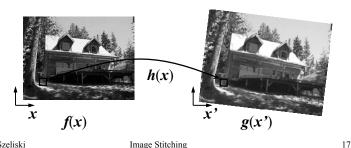
- What if pixel lands "between" two pixels?
- Answer: add "contribution" to several pixels, normalize later (splatting)



Inverse Warping

Get each pixel g(x') from its corresponding location x' = h(x) in f(x)

• What if pixel comes from "between" two pixels?

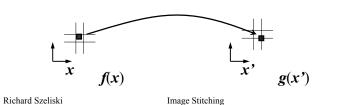


Richard Szeliski Image Stitching

Inverse Warping

Get each pixel g(x') from its corresponding location x' = h(x) in f(x)

- What if pixel comes from "between" two pixels?
- Answer: resample color value from interpolated (prefiltered) source image



Interpolation

Possible interpolation filters:

- · nearest neighbor
- bilinear
- bicubic (interpolating)
- sinc / FIR

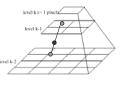
Needed to prevent "jaggies" and "texture crawl" (see demo)

Prefiltering

Essential for downsampling (decimation) to prevent aliasing

MIP-mapping [Williams'83]:

- 1. build pyramid (but what decimation filter?):
 - block averaging
 - Burt & Adelson (5-tap binomial)
 - 7-tap wavelet-based filter (better)
- 2. *trilinear* interpolation
 - bilinear within each 2 adjacent levels
 - linear blend between levels (determined by pixel size)



18

Image Stitching Richard Szeliski 19 Richard Szeliski Image Stitching 20

Prefiltering

Essential for downsampling (decimation) to prevent aliasing

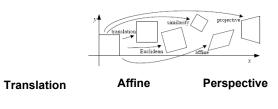
Other possibilities:

- · summed area tables
- elliptically weighted Gaussians (EWA) [Heckbert'86]

Richard Szeliski Image Stitching 21

Motion models (reprise)

Motion models





2 unknowns



6 unknowns



8 unknowns



3D rotation

3 unknowns

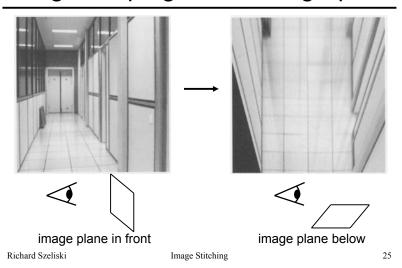
Plane perspective mosaics

- 8-parameter generalization of affine motion
 - works for pure rotation or planar surfaces
- · Limitations:
 - local minima
 - slow convergence
 - difficult to control interactively



Richard Szeliski Image Stitching 23 Richard Szeliski Image Stitching 24

Image warping with homographies



Rotational mosaics

- · Directly optimize rotation and focal length
- Advantages:
 - ability to build full-view panoramas
 - easier to control interactively
 - more stable and accurate estimates



Richard Szeliski Image Stitching

3D → 2D Perspective Projection

$$\begin{bmatrix} X_c \\ Y_c \\ Z_c \end{bmatrix} = \begin{bmatrix} \mathbf{R} \end{bmatrix}_{3\times3} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} + \mathbf{t} \qquad u$$

$$\begin{bmatrix} u \\ v \\ 1 \end{bmatrix} \sim \begin{bmatrix} U \\ V \\ W \end{bmatrix} = \begin{bmatrix} f & 0 & u_c \\ 0 & f & v_c \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X_c \\ Y_c \\ Z_c \end{bmatrix}$$

Rotational mosaic

Projection equations

1. Project from image to 3D ray

$$(x_0, y_0, z_0) = (u_0 - u_c, v_0 - v_c, f)$$

2. Rotate the ray by camera motion

$$(x_1,y_1,z_1) = \mathbf{R}_{0I}(x_0,y_0,z_0)$$

3. Project back into new (source) image

$$(u_1, v_1) = (fx_1/z_1 + u_c, fy_1/z_1 + v_c)$$

Richard Szeliski Image Stitching 27 Richard Szeliski Image Stitching 28

Image reprojection mosaic PP

The mosaic has a natural interpretation in 3D

- · The images are reprojected onto a common plane
- · The mosaic is formed on this plane

Richard Szeliski Image Stitching 29

Incremental rotation update

- 1. Small angle approximation $\Delta \mathbf{R} = \mathbf{I} + \sin\theta \left[\mathbf{n} \right]_{\times} + (1 \cos\theta) \left[\mathbf{n} \right]_{\times}^{2}$ $\stackrel{\approx}{\theta} \left[\mathbf{n} \right]_{\times} = \left[\boldsymbol{\omega} \right]_{\times}$ linear in $\boldsymbol{\omega}$
- 2. Update original R matrix $R \leftarrow R \Delta R$

Rotations and quaternions

How do we represent rotation matrices?

- 1. Axis / angle (n,θ) $R = I + \sin\theta [n]_x + (1-\cos\theta) [n]_x^2$ (Rodriguez Formula), with $[n]_x = \text{cross product matrix (see paper)}$
- 2. Unit quaternions [Shoemake SIGG'85] $q = (n \sin \theta/2, \cos \theta/2) = (w,s)$ quaternion multiplication (division is easy) $q_0 q_1 = (s_1 w_0 + s_0 w_1, s_0 s_1 w_0 \cdot w_1)$

Richard Szeliski Image Stitching 30

Perspective & rotational motion

Solve 8x8 or 3x3 system (see papers for details), and iterate (non-linear)

Patch-based approximation:

- 1. break up image into patches (say 16x16)
- 2. accumulate 2x2 linear system in each (local translational assumption)
- 3. compose larger system from smaller 2x2 results [Shum & Szeliski, ICCV'98]

Richard Szeliski Image Stitching 31 Richard Szeliski Image Stitching 32

Image Mosaics (Stitching)

[Szeliski & Shum, SIGGRAPH'97] [Szeliski, FnT CVCG, 2006]

Image Mosaics (stitching)

Blend together several overlapping images into one seamless *mosaic* (composite)

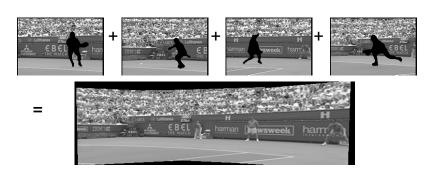




Richard Szeliski Image Stitching 34

Mosaics for Video Coding

Convert masked images into a background sprite for content-based coding



Establishing correspondences

- 1. Direct method:
 - Use generalization of affine motion model [Szeliski & Shum '97]
- 2. Feature-based method
 - Extract features, match, find consisten inliers [Lowe ICCV'99; Schmid ICCV'98, Brown&Lowe ICCV'2003]
 - Compute R from correspondences (absolute orientation)

Richard Szeliski Image Stitching 35 Richard Szeliski Image Stitching 36

Absolute orientation

[Arun *et al.*, PAMI 1987] [Horn *et al.*, JOSA A 1988] Procrustes Algorithm [Golub & VanLoan]

Given two sets of matching points, compute R

$$p_i$$
' = $R p_i$ 3D rays $A = \Sigma_i p_i p_i^T = \Sigma_i p_i p_i^T R^T = U S V^T = (U S U^T) R^T$ $V^T = U^T R^T$ $R = V U^T$

Richard Szeliski Image Stitching 37

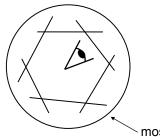
Stitching demo



Richard Szeliski Image Stitching 38

Panoramas

What if you want a 360° field of view?



mosaic Projection Cylinder

Cylindrical panoramas



Steps

- Reproject each image onto a cylinder
- Blend
- · Output the resulting mosaic

Richard Szeliski Image Stitching 39 Richard Szeliski Image Stitching 40

Cylindrical Panoramas

Map image to cylindrical or spherical coordinates

• need known focal length









Image 384x300

f = 180 (pixels)

f = 280

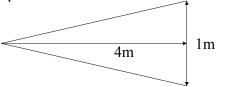
f = 380

41

Richard Szeliski Image Stitching

Determining the focal length

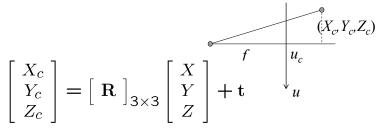
- 1. Initialize from homography *H* (see text or [SzSh'97])
- 2. Use camera's EXIF tags (approx.)
- 3. Use a tape measure



4. Ask your instructor

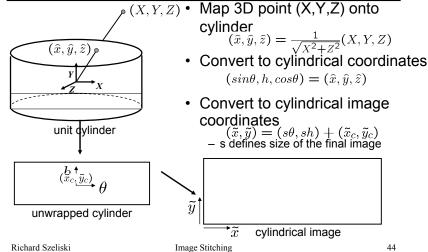
42 Richard Szeliski Image Stitching

3D → 2D Perspective Projection



$$\begin{bmatrix} u \\ v \\ 1 \end{bmatrix} \sim \begin{bmatrix} U \\ V \\ W \end{bmatrix} = \begin{bmatrix} f & 0 & u_c \\ 0 & f & v_c \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X_c \\ Y_c \\ Z_c \end{bmatrix}$$

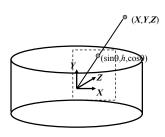
Cylindrical projection



Richard Szeliski Image Stitching 43 44

Cylindrical warping

Given focal length f and image center (x_c, y_c)



$$\theta = (x_{cyl} - x_c)/f$$

$$h = (y_{cyl} - y_c)/f$$

$$\hat{x} = \sin \theta$$

$$\hat{y} = h$$

$$\hat{z} = \cos \theta$$

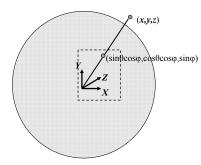
$$x = f\hat{x}/\hat{z} + x_c$$

 $y = f\hat{y}/\hat{z} + y_c$

Richard Szeliski Image Stitching 45

Spherical warping

Given focal length f and image center (x_c, y_c)



$$\theta = (x_{cyl} - x_c)/f$$

$$\varphi = (y_{cyl} - y_c)/f$$

$$\hat{x} = \sin \theta \cos \varphi$$

$$\hat{y} = \sin \varphi$$

$$\hat{z} = \cos \theta \cos \varphi$$

$$x = f\hat{x}/\hat{z} + x_c$$

$$y = f\hat{y}/\hat{z} + y_c$$

Richard Szeliski Image Stitching 46

3D rotation

Richard Szeliski

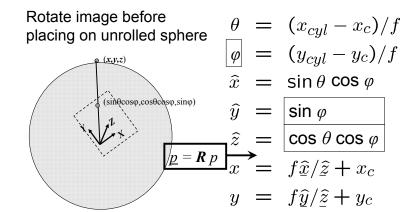
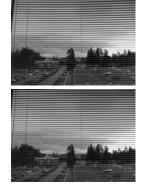


Image Stitching

47

Radial distortion

Correct for "bending" in wide field of view lenses



$$\hat{r}^2 = \hat{x}^2 + \hat{y}^2$$

$$\hat{x}' = \hat{x}/(1 + \kappa_1 \hat{r}^2 + \kappa_2 \hat{r}^4)$$

$$\hat{y}' = \hat{y}/(1 + \kappa_1 \hat{r}^2 + \kappa_2 \hat{r}^4)$$

$$x = f\hat{x}'/\hat{z} + x_c$$

$$y = f\hat{y}'/\hat{z} + y_c$$

Fisheye lens

Extreme "bending" in ultra-wide fields of view



$$\hat{r}^2 = \hat{x}^2 + \hat{y}^2$$

 $(\cos\theta\sin\phi,\sin\theta\sin\phi,\cos\phi) = s(x,y,z)$

uations become

$$x' = s\phi \cos \theta = s\frac{x}{r} \tan^{-1} \frac{r}{z},$$

$$y' = s\phi \sin \theta = s\frac{y}{r} \tan^{-1} \frac{r}{z},$$

Richard Szeliski

Image Stitching

Image Stitching

- 1. Align the images over each other
 - camera pan ↔ translation on cylinder
- 2. Blend the images together (demo)



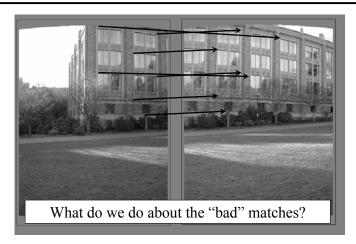
Richard Szeliski

50

Project 2 – image stitching

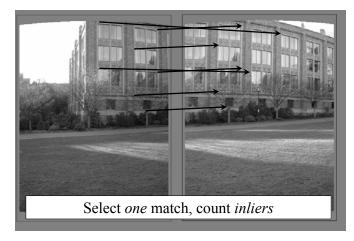
- 1. Take pictures on a tripod (or handheld)
- Warp images to spherical coordinates
- Extract features
- 4. Align neighboring pairs using RANSAC
- Write out list of neighboring translations
- Correct for drift
- 7. Read in warped images and blend them
- 8. Crop the result and import into a viewer

Matching features



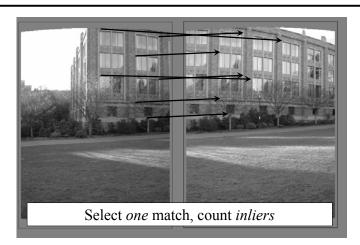
52 Richard Szeliski Image Stitching 51 Richard Szeliski Image Stitching

RAndom SAmple Consensus



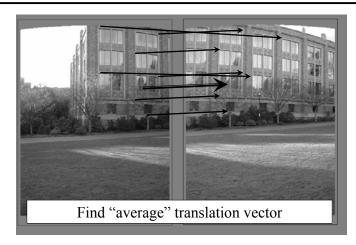
Richard Szeliski Image Stitching 53

RAndom SAmple Consensus

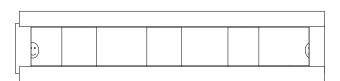


Richard Szeliski Image Stitching 54

Least squares fit



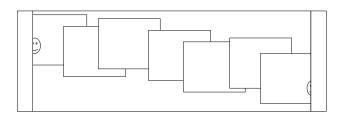
Assembling the panorama



Stitch pairs together, blend, then crop

Richard Szeliski Image Stitching 55 Richard Szeliski Image Stitching 56

Problem: Drift



Error accumulation

- small (vertical) errors accumulate over time
- apply correction so that sum = 0 (for 360° pan.)

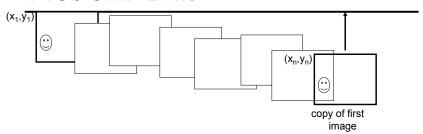
Richard Szeliski Image Stitching

57

Full-view (360° spherical) panoramas



Problem: Drift



Solution

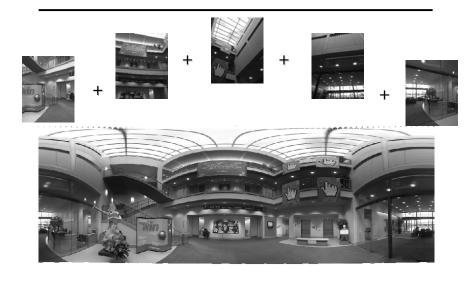
- · add another copy of first image at the end
- this gives a constraint: $y_n = y_1$
- there are a bunch of ways to solve this problem
 - add displacement of $(y_1 y_n)/(n-1)$ to each image after the first

58

Richard Szeliski compute a global warp Stiy hing y + ax

- run a big optimization problem, incorporating this

Full-view Panorama



Texture Mapped Model



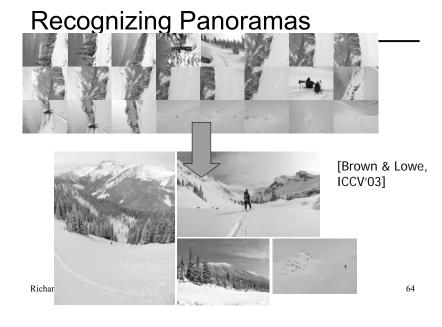
Global alignment

- Register all pairwise overlapping images
- Use a 3D rotation model (one R per image)
- Use direct alignment (patch centers) or feature based
- Infer overlaps based on previous matches (incremental)
- Optionally discover which images overlap other images using feature selection (RANSAC)

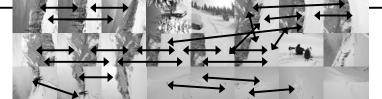
Richard Szeliski Image Stitching 62

Recognizing Panoramas

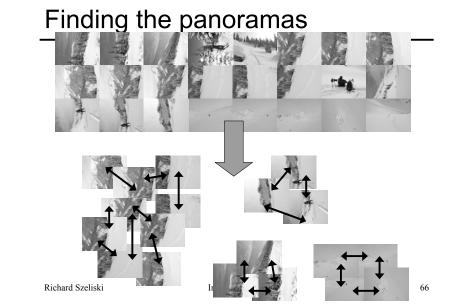
Matthew Brown & David Lowe ICCV'2003



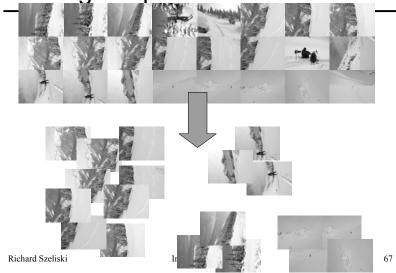
Finding the panoramas



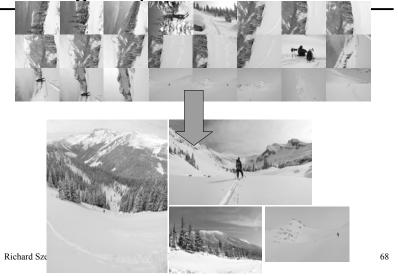
Richard Szeliski Image Stitching



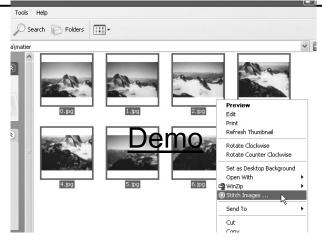
Finding the panoramas



Finding the panoramas



Fully automated 2D stitching

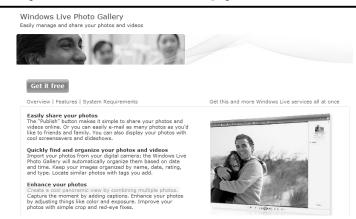


Richard Szeliski Image Stitching 69

Rec.pano.: system components

- 1. Feature detection and description
 - · more uniform point density
- 2. Fast matching (hash table)
- 3. RANSAC filtering of matches
- 4. Intensity-based verification
- 5. Incremental bundle adjustment
- [M. Brown, R. Szeliski, and S. Winder. Multi-image matching using multi-scale oriented patches, CVPR'2005]

Get you own free copy



http://get.live.com/photogallery/overview

Richard Szeliski Image Stitching 70

Multi-Scale Oriented Patches

Interest points

- · Multi-scale Harris corners
- · Orientation from blurred gradient
- · Geometrically invariant to similarity transforms

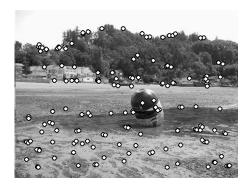
Descriptor vector

- Bias/gain normalized sampling of local patch (8x8)
- Photometrically invariant to affine changes in intensity

Richard Szeliski Image Stitching 71 Richard Szeliski Image Stitching 72

Feature irregularities

Distribute points evenly over the image



Richard Szeliski Image Stitching

Descriptor Vector

Orientation = blurred gradient Similarity Invariant Frame

• Scale-space position (x, y, s) + orientation (θ)

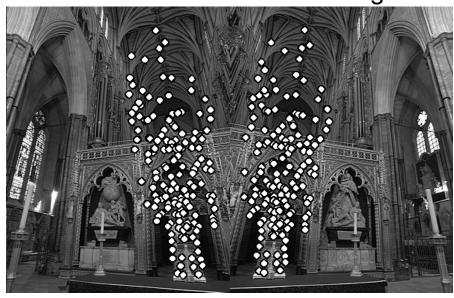


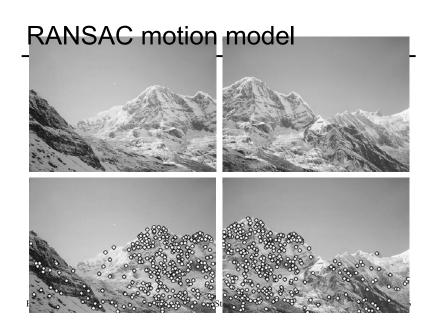
Richard Szeliski

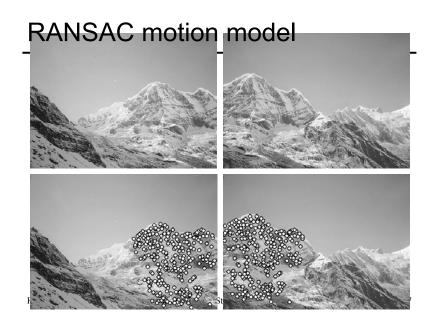
73

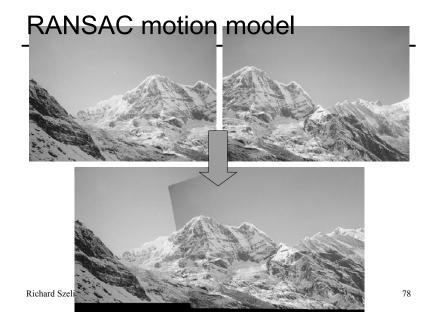
74

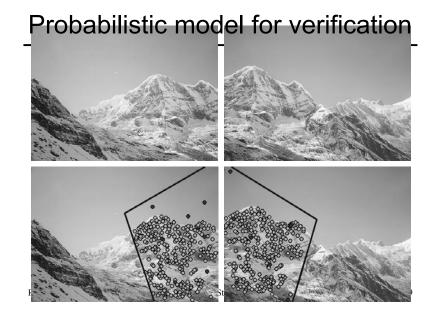
Probabilistic Feature Matching











How well does this work?

Test on 100s of examples...

How well does this work?

Test on 100s of examples...

...still too many failures (5-10%) for <u>consumer</u> application

Matching Mistakes: False Positive



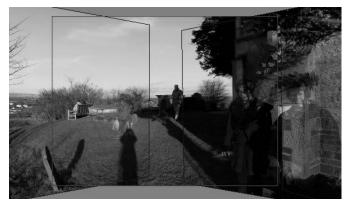
Matching Mistakes: False Positive



83

Matching Mistake: False Negative

Moving objects: large areas of disagreement



Matching Mistakes

Accidental alignment

repeated / similar regions

Failed alignments

- moving objects / parallax
- low overlap
- "feature-less" regions (more variety?)

No 100% reliable algorithm?



85

Richard Szeliski Image Stitching

How can we fix these?

Tune the feature detector

Tune the feature matcher (cost metric)

Tune the RANSAC stage (motion model)

Tune the verification stage

Use "higher-level" knowledge

- · e.g., typical camera motions
- → Sounds like a big "learning" problem
 - Need a large training/test data set (panoramas)

Richard Szeliski 86 Image Stitching

Image Blending

Image feathering

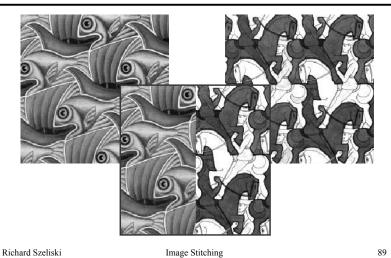
Weight each image proportional to its distance from the edge

(distance map [Danielsson, CVGIP 1980]

- 1. Generate weight map for each image
- 2. Sum up all of the weights and divide by sum: weights sum up to 1: $W_i' = W_i / (\sum_i W_i)$



Image Feathering



Feathering

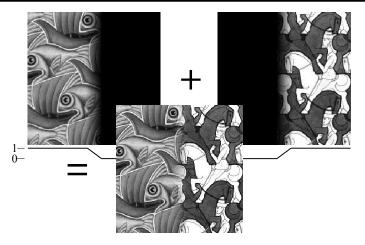
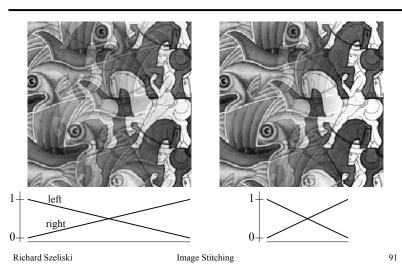
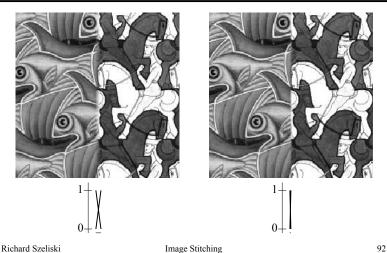


Image Stitching Richard Szeliski

Effect of window size



Effect of window size



Good window size



Image Stitching

 $0+\sum_{i=1}^{n+1}$

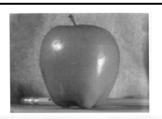
"Optimal" window: smooth but not ghosted

· Doesn't always work...

Richard Szeliski

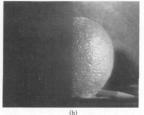
93

Pyramid Blending











Burt, P. J. and Adelson, E. H., <u>A multiresolution spline with applications to image</u> mosaics, ACM Transactions on Graphics, 42(4), October 1983, 217-236.

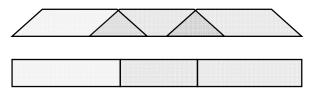
Laplacian level 2 Laplacian level 2 Laplacian level 0 Richard Szenski für pyramid Innagg sutding right pyramid blended pyramid

Laplacian image blend

- 1. Compute Laplacian pyramid
- 2. Compute Gaussian pyramid on *weight* image (can put this in A channel)
- 3. Blend Laplacians using Gaussian blurred weights
- 4. Reconstruct the final image
- Q: How do we compute the original weights?
- A: For horizontal panorama, use mid-lines
- Q: How about for a general "3D" panorama?

Weight selection (3D panorama)

Idea: use original feather weights to select strongest contributing image



Can be implemented using L- ∞ norm: (p = 10)

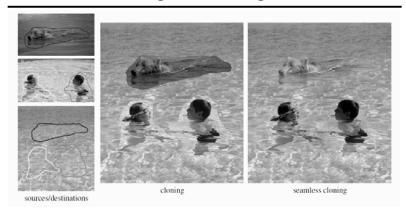
$$w_i' = [w_i^p / (\sum_i w_i^p)]^{1/p}$$

Richard Szeliski Image Stitching 9'

De-Ghosting



Poisson Image Editing



Blend the gradients of the two images, then integrate For more info: Perez et al, SIGGRAPH 2003

Richard Szeliski Image Stitching 98

Local alignment (deghosting)

Use local optic flow to compensate for small motions [Shum & Szeliski, ICCV'98]







Figure 3: Deghosting a mosaic with motion parallax: (a) with parallax; (b) after single deghosting step (patch size 32); (c) multiple steps (sizes 32, 16 and 8).

Local alignment (deghosting)

Use local optic flow to compensate for radial distortion [Shum & Szeliski, ICCV'98]





Figure 4: Deghosting a mosaic with optical distortion: (a) with distortion; (b) after multiple steps.

Richard Szeliski Image Stitching 101

Region-based de-ghosting

Select only one image in *regions-of-difference* using weighted vertex cover [Uyttendaele *et al.*, CVPR'01]





Figure 5 - (A) Ghosted mosaic. (B) Result of de-ghosting algorithm.

Richard Szeliski Image Stitching 102

Region-based de-ghosting

Select only one image in regions-of-difference using weighted vertex cover [Uyttendaele et al., CVPR'01]



Figure 6 - (A) Ghosted mosaic. (B) Result of de-ghosting algorithm.

Cutout-based de-ghosting

- •Select only one image per output pixel, using spatial continuity
- •Blend across seams using gradient continuity ("Poisson blending")





[Agarwala et al., SG'2004]

Richard Szeliski Image Stitching 103 Richard Szeliski Image Stitching 104

Cutout-based compositing

Photomontage [Agarwala et al., SG'2004]

 Interactively blend different images: group portraits



Figure 1 From a set of five source images (of which four are shown on the left), we quickly create a composite family portrait in which everyone is smiling and looking at the camera (right). We simply flip through the stack and coarsely draw strokes using the designated source image objective over the people we wish to add to the composite. The user-applied strokes and computed regions are color-coded by the borders of the source images on the left (middle).

Richard Szeliski Image Stitching 105

PhotoMontage

Technical details:

use Graph Cuts to optimize seam placement

Demo:

GroupShot application

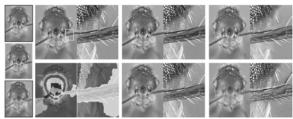


Richard Szeliski Image Stitching 106

Cutout-based compositing

Photomontage [Agarwala et al., SG'2004]

 Interactively blend different images: focus settings



Cutout-based compositing

Photomontage [Agarwala et al., SG'2004]

• Interactively blend *different* images: people's faces



hand-aligned, for example, to place all the noses in the same location. In the first two images in the second row, we replace the closed eyes of a potential with the open eyes of another. The user paints strokes with the designated source objective to openly desired features. Next, we create a factional person by combining these sources openly objective features. Next, we create a factional person by combining the control of the control

Richard Szeliski Image Stitching 107 Richard Szeliski Image Stitching 108

More stitching possibilities

- Video stitching
- · High dynamic range image stitching
 - see demo...
- Flash + Non-Flash
- · Video-based rendering

Next week's lecture: Computational Photography

Richard Szeliski 109 Image Stitching

Other types of mosaics



Can mosaic onto any surface if you know the geometry

- See NASA's Visible Earth project for some stunning earth mosaics
 - http://earthobservatory.nasa.gov/Newsroom/BlueMarble/

Richard Szeliski Image Stitching 110

Slit images

Richard Szeliski



y-t slices of the video volume are known as *slit images*

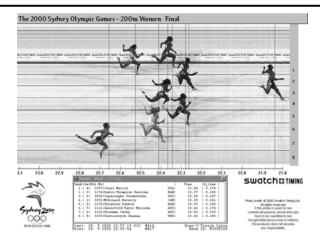
111

· take a single column of pixels from each input image Image Stitching

Slit images: cyclographs



Slit images: photofinish



Richard Szeliski Image Stitching 113

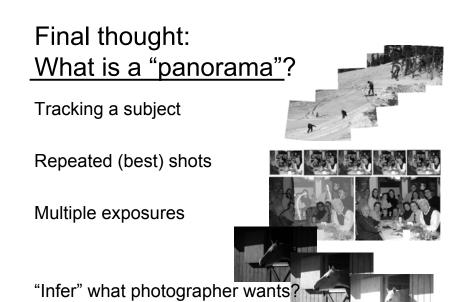


Image Stitching

Richard Szeliski