
Final project ideas

Discussion by Steve Seitz and Rick Szeliski

...

Projective Geometry

Lecture slides by Steve Seitz (mostly)
Lecture presented by Rick Szeliski

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Projective geometry



[Ames Room](#)

Readings

- Mundy, J.L. and Zisserman, A., Geometric Invariance in Computer Vision, Appendix: Projective Geometry for Machine Vision, MIT Press, Cambridge, MA, 1992, (read 23.1 - 23.5, 23.10)
 - available online: <http://www.cs.cmu.edu/~ph/869/papers/zisser-mundy.pdf>

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Projective geometry—what's it good for?

Uses of projective geometry

- Drawing
- Measurements
- Mathematics for projection
- Undistorting images
- Focus of expansion
- Camera pose estimation, match move
- Object recognition

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Applications of projective geometry

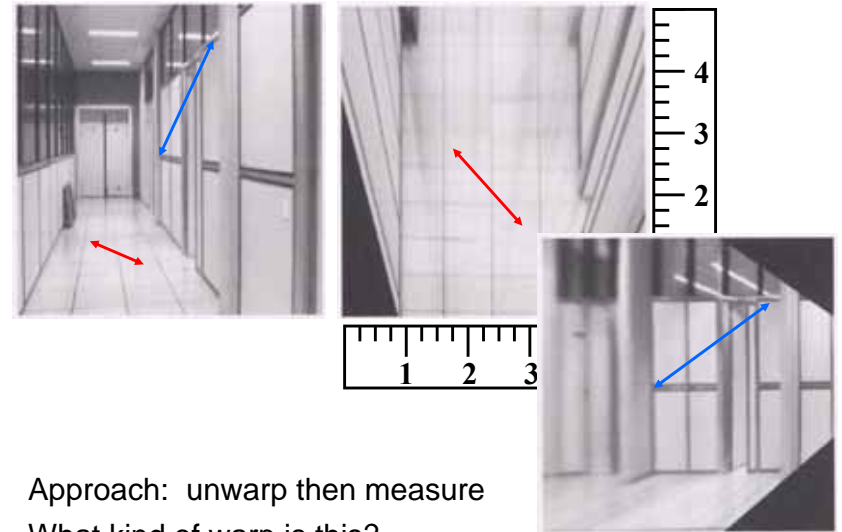


Vermeer's *Music Lesson*



Reconstructions by Criminisi et al.

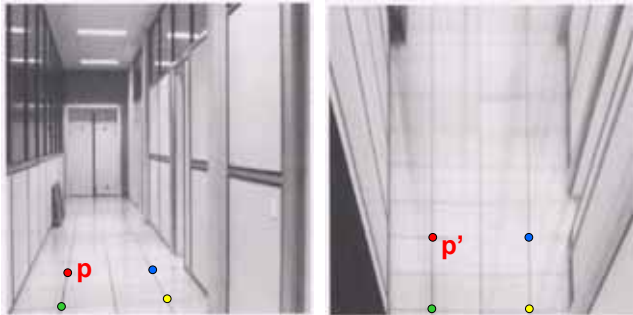
Measurements on planes



Approach: unwarpage then measure

What kind of warp is this?

Image rectification



To unwarpage (rectify) an image

- solve for homography \mathbf{H} given \mathbf{p} and \mathbf{p}'
- solve equations of the form: $w\mathbf{p}' = \mathbf{H}\mathbf{p}$
 - linear in unknowns: w and coefficients of \mathbf{H}
 - \mathbf{H} is defined up to an arbitrary scale factor
 - how many points are necessary to solve for \mathbf{H} ?

Solving for homographies

$$\begin{bmatrix} x'_i \\ y'_i \\ 1 \end{bmatrix} \cong \begin{bmatrix} h_{00} & h_{01} & h_{02} \\ h_{10} & h_{11} & h_{12} \\ h_{20} & h_{21} & h_{22} \end{bmatrix} \begin{bmatrix} x_i \\ y_i \\ 1 \end{bmatrix}$$

$$x'_i = \frac{h_{00}x_i + h_{01}y_i + h_{02}}{h_{20}x_i + h_{21}y_i + h_{22}}$$

$$y'_i = \frac{h_{10}x_i + h_{11}y_i + h_{12}}{h_{20}x_i + h_{21}y_i + h_{22}}$$

$$x'_i(h_{20}x_i + h_{21}y_i + h_{22}) = h_{00}x_i + h_{01}y_i + h_{02}$$

$$y'_i(h_{20}x_i + h_{21}y_i + h_{22}) = h_{10}x_i + h_{11}y_i + h_{12}$$

$$\begin{bmatrix} x_i & y_i & 1 & 0 & 0 & 0 & -x'_i x_i & -x'_i y_i & -x'_i \\ 0 & 0 & 0 & x_i & y_i & 1 & -y'_i x_i & -y'_i y_i & -y'_i \end{bmatrix} \begin{bmatrix} h_{00} \\ h_{01} \\ h_{02} \\ h_{10} \\ h_{11} \\ h_{12} \\ h_{20} \\ h_{21} \\ h_{22} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

Solving for homographies

$$\begin{bmatrix} x_1 & y_1 & 1 & 0 & 0 & 0 & -x'_1 x_1 & -x'_1 y_1 & -x'_1 \\ 0 & 0 & 0 & x_1 & y_1 & 1 & -y'_1 x_1 & -y'_1 y_1 & -y'_1 \\ & & & & & & \vdots & & \\ x_n & y_n & 1 & 0 & 0 & 0 & -x'_n x_n & -x'_n y_n & -x'_n \\ 0 & 0 & 0 & x_n & y_n & 1 & -y'_n x_n & -y'_n y_n & -y'_n \end{bmatrix} \begin{bmatrix} h_{00} \\ h_{01} \\ h_{02} \\ h_{10} \\ h_{11} \\ h_{12} \\ h_{20} \\ h_{21} \\ h_{22} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \end{bmatrix}$$

\mathbf{A} \mathbf{h} $\mathbf{0}$
 $2n \times 9$ 9 $2n$

Defines a least squares problem: minimize $\|\mathbf{A}\mathbf{h} - \mathbf{0}\|^2$

- Since \mathbf{h} is only defined up to scale, solve for unit vector $\hat{\mathbf{h}}$
- Solution: $\hat{\mathbf{h}}$ = eigenvector of $\mathbf{A}^T\mathbf{A}$ with smallest eigenvalue
- Works with 4 or more points

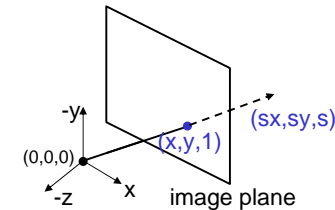
The projective plane

Why do we need homogeneous coordinates?

- represent points at infinity, homographies, perspective projection, multi-view relationships

What is the geometric intuition?

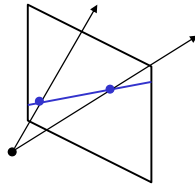
- a point in the image is a ray in projective space



- Each point (x,y) on the plane is represented by a ray (sx, sy, s)
 – all points on the ray are equivalent: $(x, y, 1) \equiv (sx, sy, s)$

Projective lines

What does a line in the image correspond to in projective space?



- A line is a *plane* of rays through origin
 – all rays (x,y,z) satisfying: $ax + by + cz = 0$

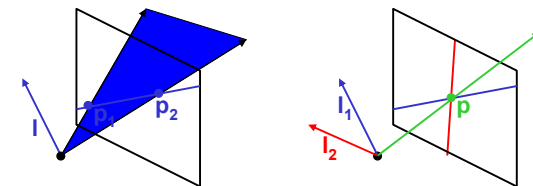
in vector notation: $0 = \begin{bmatrix} a & b & c \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}$

\mathbf{l} \mathbf{p}

- A line is also represented as a homogeneous 3-vector \mathbf{l}

Point and line duality

- A line \mathbf{l} is a homogeneous 3-vector
- It is \perp to every point (ray) \mathbf{p} on the line: $\mathbf{l} \cdot \mathbf{p} = 0$



What is the line \mathbf{l} spanned by rays \mathbf{p}_1 and \mathbf{p}_2 ?

- \mathbf{l} is \perp to \mathbf{p}_1 and $\mathbf{p}_2 \Rightarrow \mathbf{l} = \mathbf{p}_1 \times \mathbf{p}_2$
- \mathbf{l} is the plane normal

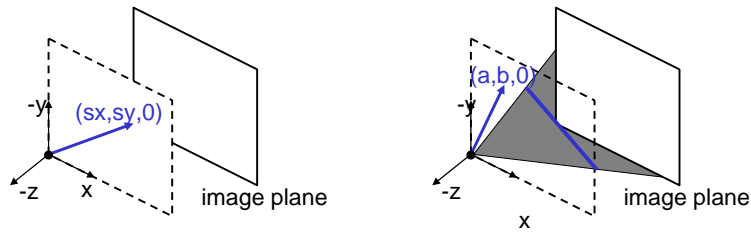
What is the intersection of two lines \mathbf{l}_1 and \mathbf{l}_2 ?

- \mathbf{p} is \perp to \mathbf{l}_1 and $\mathbf{l}_2 \Rightarrow \mathbf{p} = \mathbf{l}_1 \times \mathbf{l}_2$

Points and lines are *dual* in projective space

- given any formula, can switch the meanings of points and lines to get another formula

Ideal points and lines



Ideal point (“point at infinity”)

- $p \equiv (x, y, 0)$ – parallel to image plane
- It has infinite image coordinates

Ideal line

- $l \equiv (a, b, 0)$ – parallel to image plane
- Corresponds to a line in the image (finite coordinates)
 - goes through image origin (*principle point*)

Homographies of points and lines

Computed by 3x3 matrix multiplication

- To transform a point: $p' = Hp$
- To transform a line: $lp=0 \rightarrow l'p'=0$
 - $0 = lp = lH^{-1}Hp = lH^{-1}p' \Rightarrow l' = lH^{-1}$
 - lines are transformed by postmultiplication of H^{-1}

3D projective geometry

These concepts generalize naturally to 3D

- Homogeneous coordinates
 - Projective 3D points have four coords: $P = (X, Y, Z, W)$
- Duality
 - A plane N is also represented by a 4-vector
 - Points and planes are dual in 3D: $N P=0$
- Projective transformations
 - Represented by 4x4 matrices T : $P' = TP$, $N' = N T^{-1}$

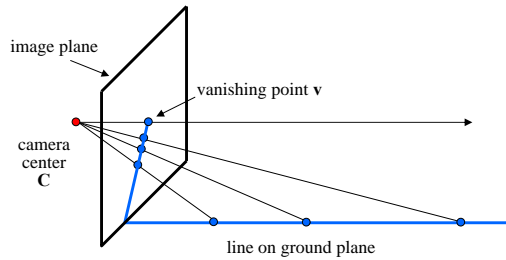
3D to 2D: “perspective” projection

Matrix Projection:
$$p = \begin{bmatrix} wx \\ wy \\ w \end{bmatrix} = \begin{bmatrix} * & * & * & * \\ * & * & * & * \\ * & * & * & * \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix} = \mathbf{P}P$$

What is *not* preserved under perspective projection?

What IS preserved?

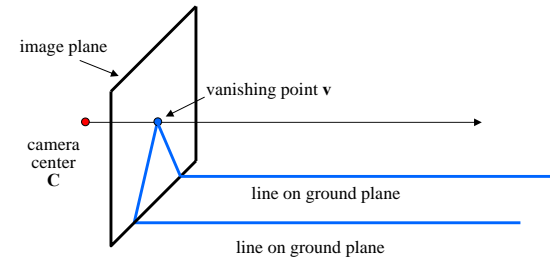
Vanishing points



Vanishing point

- projection of a point at infinity

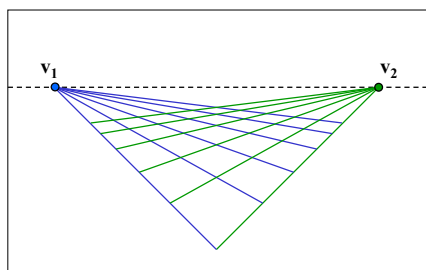
Vanishing points



Properties

- Any two parallel lines have the same vanishing point v
- The ray from C through v is parallel to the lines
- An image may have more than one vanishing point
 - in fact every pixel is a potential vanishing point

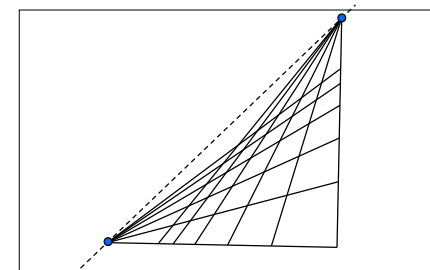
Vanishing lines



Multiple Vanishing Points

- Any set of parallel lines on the plane define a vanishing point
- The union of all of vanishing points from lines on the same plane is the *vanishing line*
 - For the ground plane, this is called the *horizon*

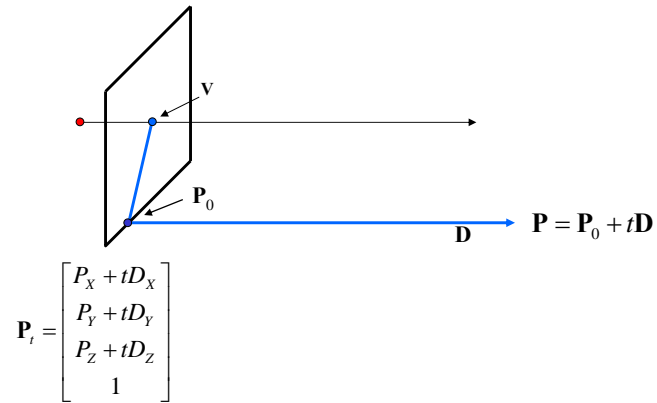
Vanishing lines



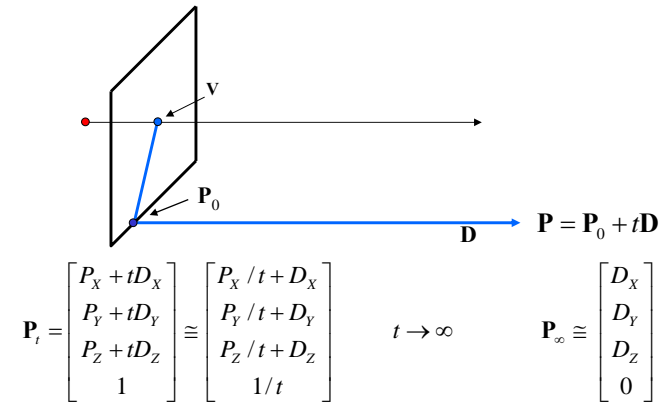
Multiple Vanishing Points

- Different planes define different vanishing lines

Computing vanishing points



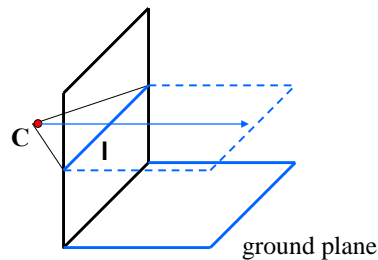
Computing vanishing points



Properties $\mathbf{v} = \mathbf{I}\mathbf{P}_\infty$

- \mathbf{P}_∞ is a point at *infinity*, \mathbf{v} is its projection
- They depend only on line *direction*
- Parallel lines $\mathbf{P}_0 + t\mathbf{D}$, $\mathbf{P}_1 + t\mathbf{D}$ intersect at \mathbf{P}_∞

Computing the horizon

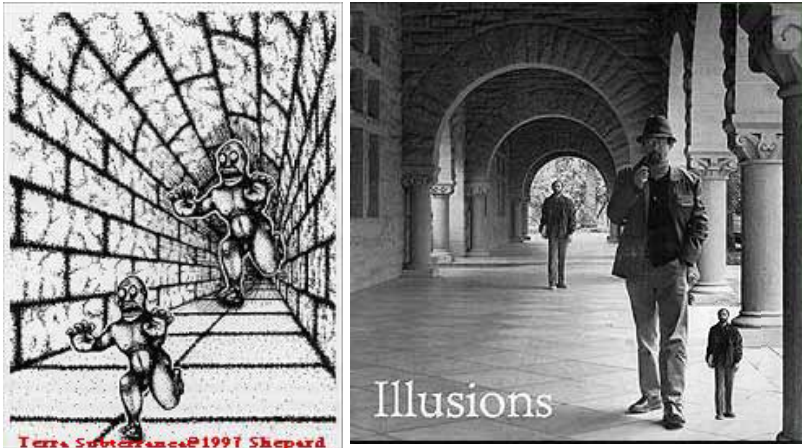


Properties

- \mathbf{I} is intersection of horizontal plane through \mathbf{C} with image plane
- Compute \mathbf{I} from two sets of parallel lines on ground plane
- All points at same height as \mathbf{C} project to \mathbf{I}
 - points higher than \mathbf{C} project above \mathbf{I}
- Provides way of comparing height of objects in the scene



Fun with vanishing points

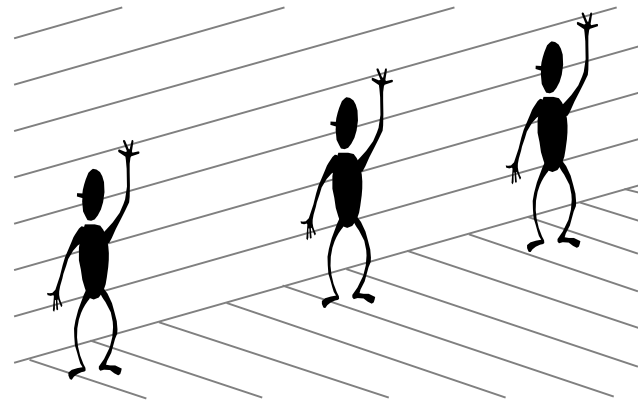


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Perspective cues

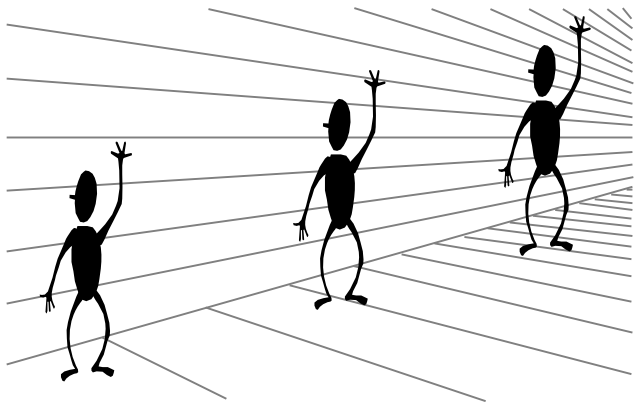


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Perspective cues

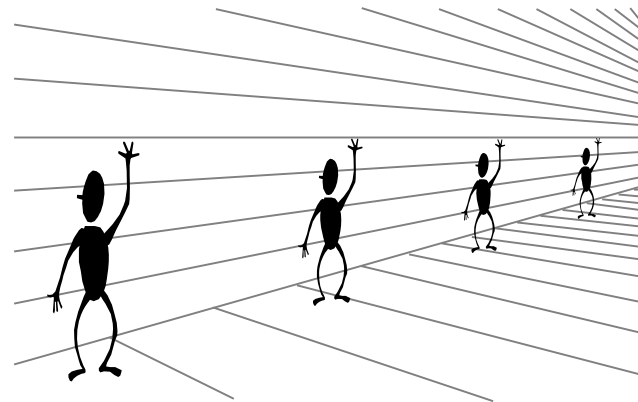


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Perspective cues

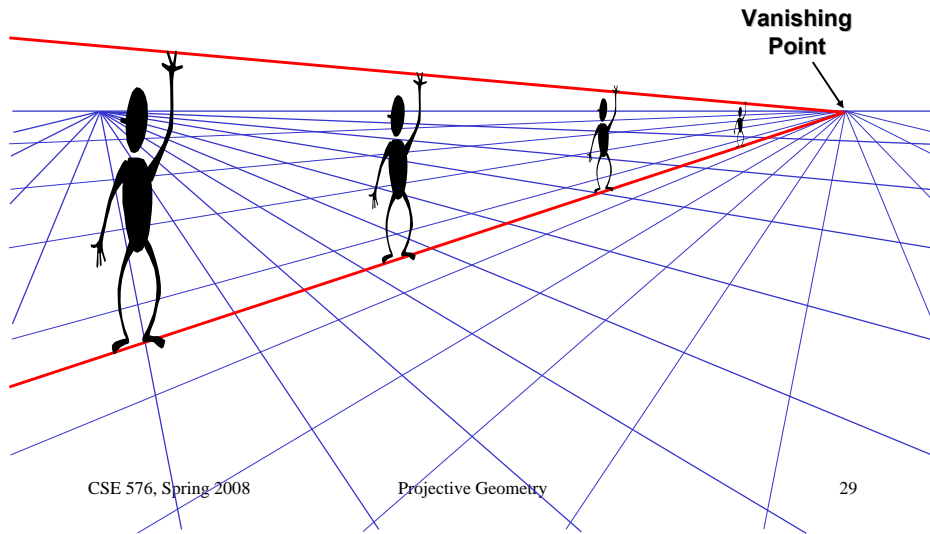


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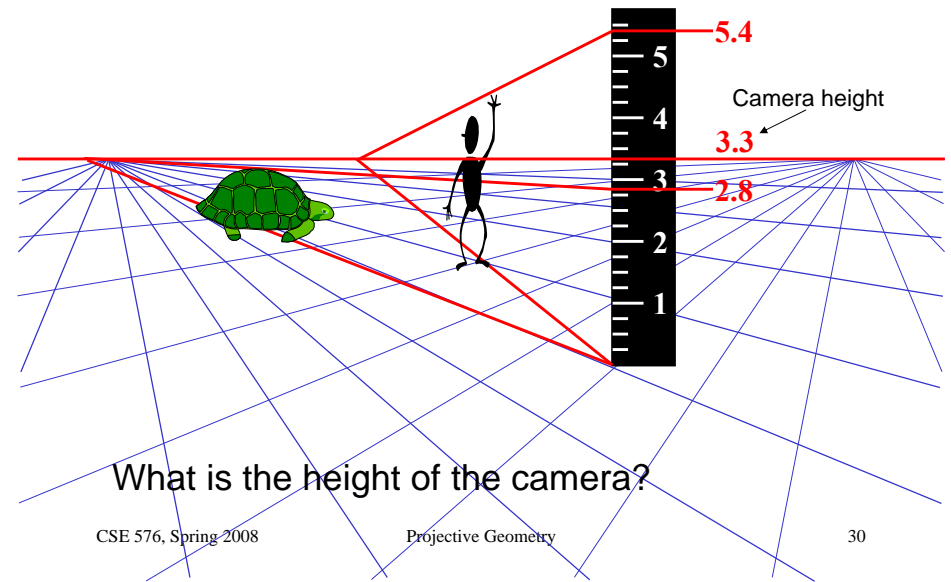
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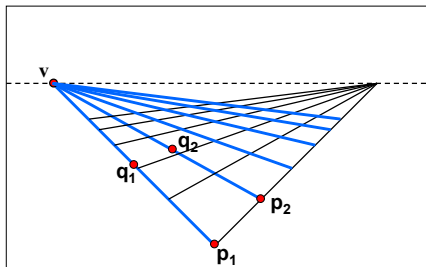
Comparing heights



Measuring height



Computing vanishing points (from lines)



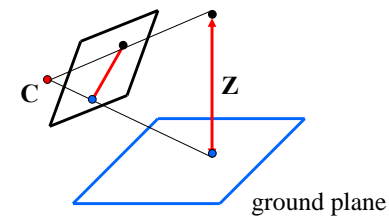
Intersect p_1q_1 with p_2q_2

$$v = (p_1 \times q_1) \times (p_2 \times q_2)$$

Least squares version

- Better to use more than two lines and compute the “closest” point of intersection
- See notes by [Bob Collins](http://www-2.cs.cmu.edu/~ph/869/www/notes/vanishing.txt) for one good way of doing this:
 - <http://www-2.cs.cmu.edu/~ph/869/www/notes/vanishing.txt>

Measuring height without a ruler



Compute Z from image measurements

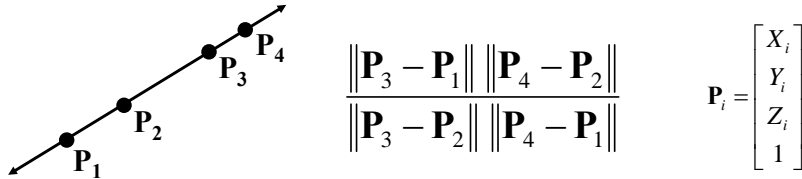
- Need more than vanishing points to do this

The cross ratio

A Projective Invariant

- Something that does not change under projective transformations (including perspective projection)

The cross-ratio of 4 collinear points

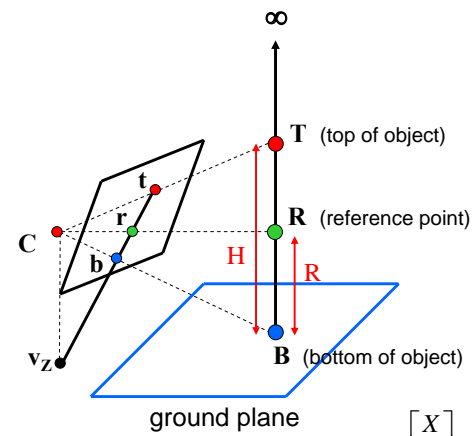


Can permute the point ordering $\frac{\|P_1 - P_3\| \|P_4 - P_2\|}{\|P_1 - P_2\| \|P_4 - P_3\|}$

- $4! = 24$ different orders (but only 6 distinct values)

This is the fundamental invariant of projective geometry

Measuring height



$$\frac{\|T - B\| \|\infty - R\|}{\|R - B\| \|\infty - T\|} = \frac{H}{R}$$

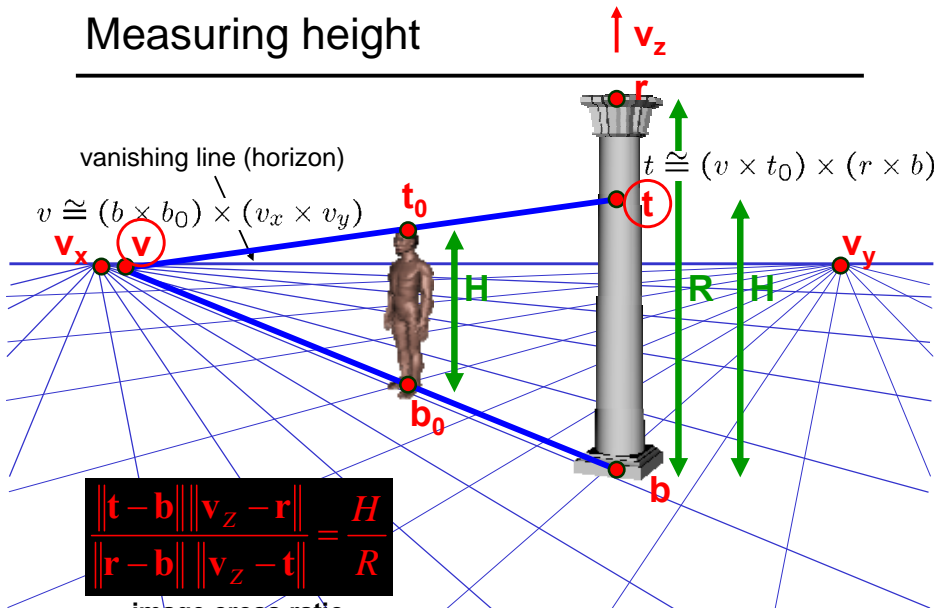
scene cross ratio

$$\frac{\|t - b\| \|v_z - r\|}{\|r - b\| \|v_z - t\|} = \frac{H}{R}$$

image cross ratio

scene points represented as $P = \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$ image points as $p = \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$

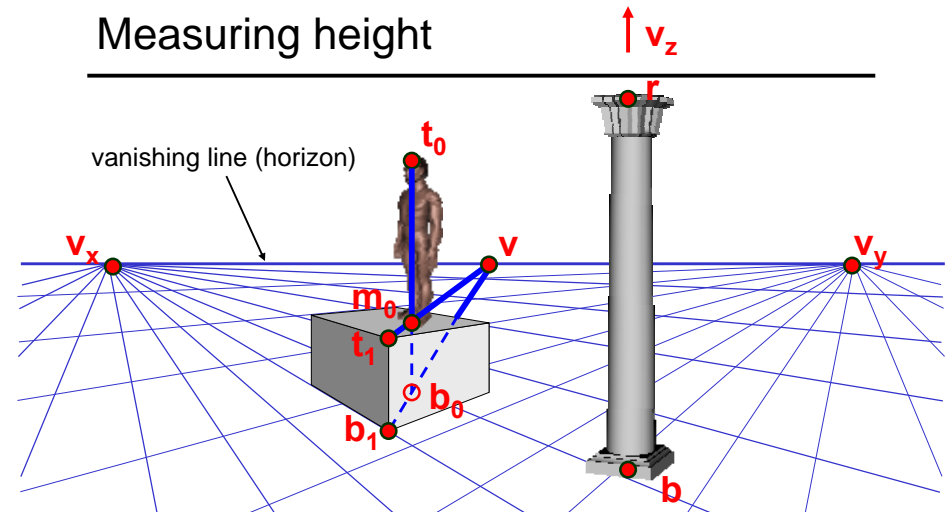
Measuring height



$$\frac{\|t - b\| \|v_z - r\|}{\|r - b\| \|v_z - t\|} = \frac{H}{R}$$

image cross ratio

Measuring height



What if the point on the ground plane b_0 is not known?

- Here the guy is standing on the box, height of box is known
- Use one side of the box to help find b_0 as shown above



Computing (X,Y,Z) coordinates

Camera calibration

Goal: estimate the camera parameters

- Version 1: solve for projection matrix

$$\mathbf{x} = \begin{bmatrix} wx \\ wy \\ w \end{bmatrix} = \begin{bmatrix} * & * & * & * \\ * & * & * & * \\ * & * & * & * \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix} = \mathbf{\Pi} \mathbf{x}$$

- Version 2: solve for camera parameters separately
 - intrinsics (focal length, principle point, pixel size)
 - extrinsics (rotation angles, translation)
 - radial distortion

Vanishing points and projection matrix

$$\mathbf{\Pi} = \begin{bmatrix} * & * & * & * \\ * & * & * & * \\ * & * & * & * \\ \pi_1 & \pi_2 & \pi_3 & \pi_4 \end{bmatrix} = [\pi_1 \quad \pi_2 \quad \pi_3 \quad \pi_4]$$

- $\pi_1 = \mathbf{\Pi} [1 \ 0 \ 0 \ 0]^T = \mathbf{v}_x$ (X vanishing point)
- similarly, $\pi_2 = \mathbf{v}_y$, $\pi_3 = \mathbf{v}_z$
- $\pi_4 = \mathbf{\Pi} [0 \ 0 \ 0 \ 1]^T =$ projection of world origin

$$\mathbf{\Pi} = [\mathbf{v}_x \quad \mathbf{v}_y \quad \mathbf{v}_z \quad \mathbf{o}]$$

Not So Fast! We only know \mathbf{v} 's and \mathbf{o} up to a scale factor

$$\mathbf{\Pi} = [a \mathbf{v}_x \quad b \mathbf{v}_y \quad c \mathbf{v}_z \quad d \mathbf{o}]$$

- Need a bit more work to get these scale factors...

Finding the scale factors...

Let's assume that the camera is reasonable

- Square pixels
- Image plane parallel to sensor plane
- Principal point in the center of the image

$$\mathbf{P} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1/f \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} r_{11} & r_{12} & r_{13} & 0 \\ r_{21} & r_{22} & r_{23} & 0 \\ r_{31} & r_{32} & r_{33} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & t_1 \\ 0 & 1 & 0 & t_2 \\ 0 & 0 & 1 & t_3 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} r_{11} & r_{12} & r_{13} & t'_1 \\ r_{21} & r_{22} & r_{23} & t'_2 \\ r_{31}/f & r_{32}/f & r_{33}/f & t'_3/f \end{bmatrix} \begin{bmatrix} t'_1 \\ t'_2 \\ t'_3 \end{bmatrix} = \begin{bmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{bmatrix} \begin{bmatrix} t_1 \\ t_2 \\ t_3 \end{bmatrix}$$

$$= \begin{bmatrix} a \mathbf{v}_X & b \mathbf{v}_Y & c \mathbf{v}_Z & d \mathbf{o} \end{bmatrix}$$

Solving for f

$$\begin{bmatrix} v_{x1} & v_{y1} & v_{z1} & o_1 \\ v_{x2} & v_{y2} & v_{z2} & o_2 \\ v_{x3} & v_{y3} & v_{z3} & o_3 \end{bmatrix} = \begin{bmatrix} r_{11}/a & r_{12}/b & r_{13}/c & t'_1/d \\ r_{21}/a & r_{22}/b & r_{23}/c & t'_2/d \\ r_{31}/af & r_{32}/bf & r_{33}/cf & t'_3/df \end{bmatrix}$$

$$\begin{bmatrix} v_X & v_Y & v_Z & o \end{bmatrix}$$

$$\begin{bmatrix} v_{x1} & v_{y1} & v_{z1} & o_1 \\ v_{x2} & v_{y2} & v_{z2} & o_2 \\ fv_{x3} & fv_{y3} & fv_{z3} & fo_3 \end{bmatrix} = \begin{bmatrix} r_{11}/a & r_{12}/b & r_{13}/c & t'_1/d \\ r_{21}/a & r_{22}/b & r_{23}/c & t'_2/d \\ r_{31}/a & r_{32}/b & r_{33}/c & t'_3/d \end{bmatrix}$$

Orthogonal vectors Orthogonal vectors

$$v_{x1}v_{y1} + v_{x2}v_{y2} + f^2v_{x3}v_{y3} = 0 \quad \rightarrow \quad f = \frac{\sqrt{v_{x1}v_{y1} + v_{x2}v_{y2}}}{-v_{x3}v_{y3}}$$

Solving for a, b, and c

$$\begin{bmatrix} v_{x1}/f \\ v_{x2}/f \\ v_{x3} \end{bmatrix} \begin{bmatrix} v_{y1}/f \\ v_{y2}/f \\ v_{y3} \end{bmatrix} \begin{bmatrix} v_{z1}/f \\ v_{z2}/f \\ v_{z3} \end{bmatrix} \begin{bmatrix} o_1/f \\ o_2/f \\ o_3 \end{bmatrix} = \begin{bmatrix} r_{11}/a \\ r_{21}/a \\ r_{31}/a \end{bmatrix} \begin{bmatrix} r_{12}/b \\ r_{22}/b \\ r_{32}/b \end{bmatrix} \begin{bmatrix} r_{13}/c \\ r_{23}/c \\ r_{33}/c \end{bmatrix} \begin{bmatrix} t'_1/d \\ t'_2/d \\ t'_3/d \end{bmatrix}$$

Norm = 1/a Norm = 1/a

Solve for a, b, c

- Divide the first two rows by f, now that it is known
- Now just find the norms of the first three columns
- Once we know a, b, and c, that also determines R

How about d?

- Need a reference point in the scene

Solving for d

$$\begin{bmatrix} wu \\ wv \\ w \end{bmatrix} = \begin{bmatrix} r_{11} & r_{12} & r_{13} & t'_1/d \\ r_{21} & r_{22} & r_{23} & t'_2/d \\ r_{31} & r_{32} & r_{33} & t'_3/d \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ H \\ 1 \end{bmatrix}$$

Suppose we have one reference height H

- E.g., we know that (0, 0, H) gets mapped to (u, v)

$$u = \frac{r_{13}H + t'_1/d}{r_{33}H + t'_3/d} \quad d = \frac{t'_1 - ut'_3}{ur_{33}H - r_{13}H}$$

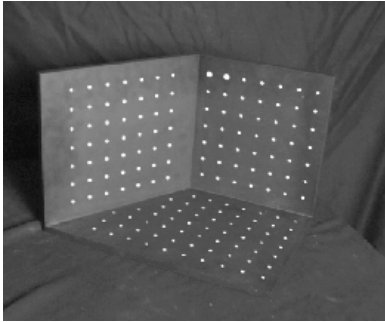
Finally, we can solve for t

$$\begin{bmatrix} t_1 \\ t_2 \\ t_3 \end{bmatrix} = \begin{bmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{bmatrix}^T \begin{bmatrix} t'_1 \\ t'_2 \\ t'_3 \end{bmatrix}$$

Calibration using a reference object

Place a known object in the scene

- identify correspondence between image and scene
- compute mapping from scene to image



Issues

- must know geometry very accurately
- must know 3D->2D correspondence

Chromaglyphs

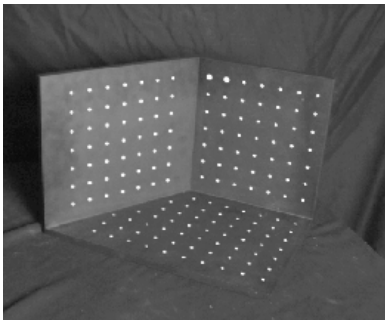


Courtesy of Bruce Culbertson, HP Labs
http://www.hpl.hp.com/personal/Bruce_Culbertson/ibr98/chromagl.html

Estimating the projection matrix

Place a known object in the scene

- identify correspondence between image and scene
- compute mapping from scene to image



$$\begin{bmatrix} u_i \\ v_i \\ 1 \end{bmatrix} \cong \begin{bmatrix} m_{00} & m_{01} & m_{02} & m_{03} \\ m_{10} & m_{11} & m_{12} & m_{13} \\ m_{20} & m_{21} & m_{22} & m_{23} \end{bmatrix} \begin{bmatrix} X_i \\ Y_i \\ Z_i \\ 1 \end{bmatrix}$$

Direct linear calibration

$$\begin{bmatrix} u_i \\ v_i \\ 1 \end{bmatrix} \cong \begin{bmatrix} m_{00} & m_{01} & m_{02} & m_{03} \\ m_{10} & m_{11} & m_{12} & m_{13} \\ m_{20} & m_{21} & m_{22} & m_{23} \end{bmatrix} \begin{bmatrix} X_i \\ Y_i \\ Z_i \\ 1 \end{bmatrix}$$

$$u_i = \frac{m_{00}X_i + m_{01}Y_i + m_{02}Z_i + m_{03}}{m_{20}X_i + m_{21}Y_i + m_{22}Z_i + m_{23}}$$

$$v_i = \frac{m_{10}X_i + m_{11}Y_i + m_{12}Z_i + m_{13}}{m_{20}X_i + m_{21}Y_i + m_{22}Z_i + m_{23}}$$

$$u_i(m_{20}X_i + m_{21}Y_i + m_{22}Z_i + m_{23}) = m_{00}X_i + m_{01}Y_i + m_{02}Z_i + m_{03}$$

$$v_i(m_{20}X_i + m_{21}Y_i + m_{22}Z_i + m_{23}) = m_{10}X_i + m_{11}Y_i + m_{12}Z_i + m_{13}$$

$$\begin{bmatrix} X_i & Y_i & Z_i & 1 & 0 & 0 & 0 & 0 & -u_i X_i & -u_i Y_i & -u_i Z_i & -u_i \\ 0 & 0 & 0 & 0 & X_i & Y_i & Z_i & 1 & -v_i X_i & -v_i Y_i & -v_i Z_i & -v_i \end{bmatrix} \begin{bmatrix} m_{00} \\ m_{01} \\ m_{02} \\ m_{03} \\ m_{10} \\ m_{11} \\ m_{12} \\ m_{13} \\ m_{20} \\ m_{21} \\ m_{22} \\ m_{23} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

Direct linear calibration

$$\begin{bmatrix} X_1 & Y_1 & Z_1 & 1 & 0 & 0 & 0 & 0 & -u_1 X_1 & -u_1 Y_1 & -u_1 Z_1 & -u_1 \\ 0 & 0 & 0 & 0 & X_1 & Y_1 & Z_1 & 1 & -v_1 X_1 & -v_1 Y_1 & -v_1 Z_1 & -v_1 \\ & & & & & & & & & & & \vdots \\ X_n & Y_n & Z_n & 1 & 0 & 0 & 0 & 0 & -u_n X_n & -u_n Y_n & -u_n Z_n & -u_n \\ 0 & 0 & 0 & 0 & X_n & Y_n & Z_n & 1 & -v_n X_n & -v_n Y_n & -v_n Z_n & -v_n \end{bmatrix} = \begin{bmatrix} m_{00} \\ m_{01} \\ m_{02} \\ m_{03} \\ m_{10} \\ m_{11} \\ m_{12} \\ m_{13} \\ m_{20} \\ m_{21} \\ m_{22} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \\ 0 \end{bmatrix}$$

Can solve for m_{ij} by linear least squares

- use eigenvector trick that we used for homographies

Direct linear calibration

Advantage:

- Very simple to formulate and solve

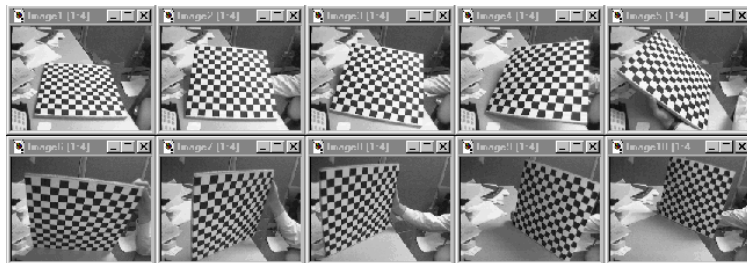
Disadvantages:

- Doesn't tell you the camera parameters
- Doesn't model radial distortion
- Hard to impose constraints (e.g., known focal length)
- Doesn't minimize the right error function

For these reasons, *nonlinear methods* are preferred

- Define error function E between projected 3D points and image positions
 - E is nonlinear function of intrinsics, extrinsics, radial distortion
- Minimize E using nonlinear optimization techniques
 - e.g., variants of Newton's method (e.g., Levenberg Marquart)

Alternative: multi-plane calibration



Images courtesy Jean-Yves Bouquet, Intel Corp.

Advantage

- Only requires a plane
- Don't have to know positions/orientations
- Good code available online!
 - Intel's OpenCV library: <http://www.intel.com/research/mrl/research/opencv/>
 - Matlab version by Jean-Yves Bouquet: http://www.vision.caltech.edu/bouquetj/calib_doc/index.html
 - Zhengyou Zhang's web site: <http://research.microsoft.com/~zhang/Calib/>

Some Related Techniques

Image-Based Modeling and Photo Editing

- Mok et al., SIGGRAPH 2001
- <http://graphics.csail.mit.edu/ibedit/>

Single View Modeling of Free-Form Scenes

- Zhang et al., CVPR 2001
- <http://grail.cs.washington.edu/projects/svm/>

Tour Into The Picture

- Anjyo et al., SIGGRAPH 1997
- http://koigakubo.hitachi.co.jp/little/DL_TipE.html