Announcements

- · Today: evals
- · Monday: project presentations (8 min talks)

Photometric Stereo



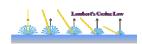
Merle Norman Cosmetics, Los Angele

Readings

 R. Woodham, Photometric Method for Determining Surface Orientation from Multiple Images. Optical Engineering 19(1)139-144 (1980). (PDF)

Diffuse reflection





$$R_e = k_d \mathbf{N} \cdot \mathbf{L} R_i$$

image intensity of P \longrightarrow $I=k_d {f N}\cdot {f L}$

Simplifying assumptions

- I = R_e : camera response function f is the identity function:
 - can always achieve this in practice by solving for f and applying f⁻¹ to each pixel in the image
- R_i = 1: light source intensity is 1
 - can achieve this by dividing each pixel in the image by R_i

Shape from shading



Suppose
$$k_d = 1$$

$$I = k_d \mathbf{N} \cdot \mathbf{L}$$

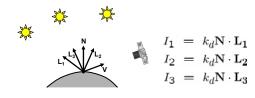
$$= \mathbf{N} \cdot \mathbf{L}$$

$$= \cos \theta_i$$

You can directly measure angle between normal and light source

- · Not quite enough information to compute surface shape
- · But can be if you add some additional info, for example
 - assume a few of the normals are known (e.g., along silhouette)
 - constraints on neighboring normals—"integrability"
 - smoothness
- · Hard to get it to work well in practice
 - plus, how many real objects have constant albedo?

Photometric stereo



Can write this as a matrix equation:

$$\begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = k_d \begin{bmatrix} \mathbf{L_1}^T \\ \mathbf{L_2}^T \\ \mathbf{L_3}^T \end{bmatrix} \mathbf{N}$$

Solving the equations

$$\begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = \begin{bmatrix} \mathbf{L}_1^T \\ \mathbf{L}_2^T \\ \mathbf{L}_3^T \end{bmatrix} k_d \mathbf{N}$$

$$\mathbf{I}_{3\times 1} \quad \mathbf{L}_{3\times 3} \quad \mathbf{G}$$

$$\mathbf{G} = \mathbf{L}^{-1} \mathbf{I}$$

$$k_d = \|\mathbf{G}\|$$

$$\mathbf{N} = \frac{1}{k_d} \mathbf{G}$$

More than three lights

Get better results by using more lights

$$\left[\begin{array}{c}I_1\\\vdots\\I_n\end{array}\right]=\left[\begin{array}{c}\mathbf{L_1}\\\vdots\\\mathbf{L_n}\end{array}\right]k_d\mathbf{N}$$

Least squares solution:

$$I = LG$$

$$L^{T}I = L^{T}LG$$

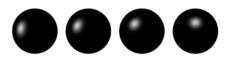
$$G = (L^{T}L)^{-1}(L^{T}I)$$

Solve for N, k_d as before

What's the size of LTL?

Computing light source directions

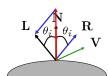
Trick: place a chrome sphere in the scene



· the location of the highlight tells you where the light source is

Recall the rule for specular reflection

For a perfect mirror, light is reflected about N



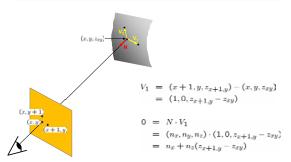
$$R_e = \begin{cases} R_i & \text{if } \mathbf{V} = \mathbf{R} \\ 0 & \text{otherwis} \end{cases}$$

We see a highlight when V = R

· then L is given as follows:

$$L = 2(N \cdot R)N - R$$

Depth from normals



Get a similar equation for V2

- Each normal gives us two linear constraints on z
- compute z values by solving a matrix equation (project 3)

Project 3







Limitations

Big problems

- · doesn't work for shiny things, semi-translucent things
- · shadows, inter-reflections

Smaller problems

- · camera and lights have to be distant
- · calibration requirements
 - measure light source directions, intensities
 - camera response function

Newer work addresses some of these issues

Some pointers for further reading:

- Zickler, Belhumeur, and Kriegman, "Helmholtz Stereopsis: Exploiting Reciprocity for Surface Reconstruction." IJCV, Vol. 49 No. 2/3, pp 215-227.
- Hertzmann & Seitz, "Example-Based Photometric Stereo: Shape Reconstruction with General, Varying BRDFs." IEEE Trans. PAMI 2005