

Pattern Recognition

Pattern recognition is:

1. The name of the journal of the Pattern Recognition Society.
2. A research area in which patterns in data are found, recognized, discovered, ...whatever.
3. A catchall phrase that includes
 - classification
 - clustering
 - data mining
 -

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Two Schools of Thought

1. **Statistical Pattern Recognition**

The data is reduced to vectors of numbers and statistical techniques are used for the tasks to be performed.
2. **Structural Pattern Recognition**

The data is converted to a discrete structure (such as a grammar or a graph) and the techniques are related to computer science subjects (such as parsing and graph matching).

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In this course

1. How should objects to be classified be represented?
2. What algorithms can be used for recognition (or matching)?
3. How should learning (training) be done?

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Classification in Statistical PR

- A **class** is a set of objects having some important properties in common
- A **feature extractor** is a program that inputs the data (image) and extracts features that can be used in classification.
- A **classifier** is a program that inputs the feature vector and assigns it to one of a set of designated classes or to the "reject" class.

With what kinds of classes do you work?

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Feature Vector Representation

- ♦ $X=[x_1, x_2, \dots, x_n]$, each x_j a real number
- ♦ x_j may be an object measurement
- ♦ x_j may be count of object parts
- ♦ Example: object rep. [#holes, #strokes, moments, ...]

```
000000001000000000 000000001110000000
000000001000000000 000000100001000000
00000000101000000000 00000010000001100000
0000000010000100000000 00001100000000110000
0000001000001000000000 00001000000000000000
00000100000001000000 00001100000000010000
00001000000000000000 00001100000000010000
00011000000000000000 00001100000000010000
00010000000000010000 00001100000000010000
0001000000000001000 00001100000000010000
00110000000000000010 00110000000000010000
00100000000000000010 0010000000000000001000
00100000000000000010 0010000000000000001000
01100000000000000010 00011000000000010000
01000000000000000000 00001000000000110000
00000000000000000000 00000011111100000000
```

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Possible features for char rec.

(class)	character	area	height	width	#holes	number	number	(cx,cy)	best	least
'A'	medium	high	3/4	1	3	1/2,2/3	90	medium		
'B'	medium	high	3/4	2	1	1/3,1/2	90	large		
'g'	medium	high	2/3	2	0	1/2,1/2	90	medium		
'O'	medium	high	2/3	1	0	1/2,1/2	90	large		
'1'	low	high	1/4	0	1	1/2,1/2	90	low		
'W'	high	high	1	0	4	1/2,2/3	90	large		
'X'	high	high	3/4	0	2	1/2,1/2	?	large		
'*'	medium	low	1/2	0	0	1/2,1/2	?	large		
'-'	low	low	2/3	0	1	1/2,1/2	0	low		
'/'	low	high	2/3	0	1	1/2,1/2	60	low		

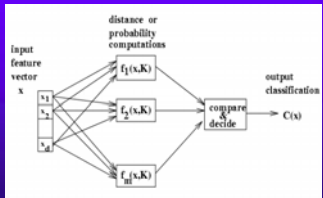
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Some Terminology

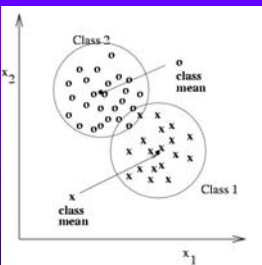
- ◆ **Classes:** set of m known categories of objects
 - (a) might have a known description for each
 - (b) might have a set of samples for each
- ◆ **Reject Class:**
 - a generic class for objects not in any of the designated known classes
- ◆ **Classifier:**
 - Assigns object to a class based on features

Discriminant functions

- ◆ Functions $f(x, K)$ perform some computation on feature vector x
- ◆ Knowledge K from training or programming is used
- ◆ Final stage determines class

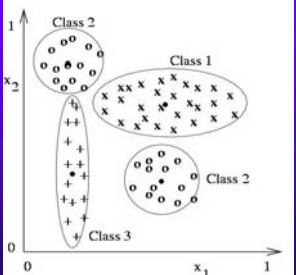


Classification using nearest class mean



- ◆ Compute the Euclidean distance between feature vector X and the mean of each class.
- ◆ Choose closest class, if close enough (reject otherwise)

Nearest mean might yield poor results with complex structure



- ◆ Class 2 has two modes; **where is its mean?**
- ◆ But if modes are detected, two subclass mean vectors can be used

Scaling coordinates by std dev

We can compute a modified distance from feature vector x to class mean vector x_c by scaling by the spread or *standard deviation* σ_i of class c along each dimension i .

scaled Euclidean distance from x to class mean x_c

$$\|x - x_c\| = \sqrt{\sum_{i=1,d} ((x[i] - x_c[i]) / \sigma_i)^2}$$

Nearest Neighbor Classification

- Keep all the training samples in some efficient look-up structure.
- Find the nearest neighbor of the feature vector to be classified and assign the class of the neighbor.
- Can be extended to K nearest neighbors.

Receiver Operating Curve ROC

- Plots correct detection rate versus false alarm rate
- Generally, false alarms go up with attempts to detect higher percentages of known objects

actual input object	decision	error type?
frack	frack	correct alarm (no error)
not a frack	frack	false alarm (error)
frack	not a frack	false dismissal (error)
not a frack	not a frack	correct dismissal (no error)

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A recent ROC from our work:

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Confusion matrix shows empirical performance

		class j output by the pattern recognition system											
		'0'	'1'	'2'	'3'	'4'	'5'	'6'	'7'	'8'	'9'	'R'	
true object class	'0'	97	0	0	0	0	0	1	0	0	1	1	
	'1'	0	98	0	0	1	0	0	1	0	0	0	
	'2'	0	0	96	1	0	1	0	1	0	0	1	
	'3'	0	0	2	95	0	1	0	0	1	0	1	
	'4'	0	0	0	0	98	0	0	0	0	0	2	
i	'5'	0	0	0	1	0	97	0	0	0	0	2	
	'6'	1	0	0	0	0	1	98	0	0	0	0	
	'7'	0	0	1	0	0	0	0	98	0	0	1	
	'8'	0	0	0	0	1	0	0	1	0	96	1	
	'9'	1	0	0	0	3	0	0	0	1	95	0	

Confusion may be unavoidable between some classes, for example, between 9's and 4's.

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Bayesian decision-making

- Classify into class w that is most likely based on observations X . The following distributions are needed.

- class conditional distribution: $p(x|\omega_i)$ for each class ω_i
- a priori probability: $P(\omega_i)$ for each class ω_i
- unconditional distribution: $p(x)$

- Then we have:

$$P(\omega_i|x) = \frac{p(x|\omega_i)P(\omega_i)}{p(x)} = \frac{p(x|\omega_i)P(\omega_i)}{\sum_{t=1, \dots, m} p(x|\omega_t)P(\omega_t)}$$

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Classifiers often used in CV

- Decision Tree Classifiers
- Artificial Neural Net Classifiers
- Bayesian Classifiers and Bayesian Networks (Graphical Models)
- Support Vector Machines

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Decision Trees

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Decision Tree Characteristics

1. Training
How do you construct one from training data?
Entropy-based Methods
2. Strengths
Easy to Understand
3. Weaknesses
Overtraining

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Entropy-Based Automatic Decision Tree Construction

Training Set S

$$x_1 = (f_{11}, f_{12}, \dots, f_{1m})$$

$$x_2 = (f_{21}, f_{22}, \dots, f_{2m})$$

$$\vdots$$

$$x_n = (f_{n1}, f_{n2}, \dots, f_{nm})$$

Node 1
What feature should be used?
What values?

Quinlan suggested **information gain** in his ID3 system and later the **gain ratio**, both based on **entropy**.

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Entropy

Given a set of training vectors S, if there are c classes,

$$\text{Entropy}(S) = \sum_{i=1}^c -p_i \log_2(p_i)$$

Where p_i is the proportion of category i examples in S.

If all examples belong to the same category, the entropy is 0 (no discrimination).

The greater the discrimination power, the larger the entropy will be.

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Information Gain

The **information gain** of an attribute A is the expected reduction in entropy caused by partitioning on this attribute.

$$\text{Gain}(S, A) = \text{Entropy}(S) - \sum_{v \in \text{Values}(A)} \frac{|S_v|}{|S|} \text{Entropy}(S_v)$$

where S_v is the subset of S for which attribute A has value v.

Choose the attribute A that gives the maximum information gain.

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Information Gain (cont)

Set S

Attribute A

v1 v2 vk

Set S' $S' = \{s \in S \mid \text{value}(A) = v_1\}$

repeat recursively

Information gain has the disadvantage that it prefers attributes with large number of values that split the data into small, pure subsets.

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Gain Ratio

Gain ratio is an alternative metric from Quinlan's 1986 paper and used in the popular C4.5 package (free!).

$$\text{GainRatio}(S, A) = \frac{\text{Gain}(S, A)}{\text{SplitInfo}(S, A)}$$

$$\text{SplitInfo}(S, A) = \sum_{i=1}^{m_i} \frac{|S_i|}{|S|} \log_2 \left(\frac{|S_i|}{|S|} \right)$$

where S_i is the subset of S in which attribute A has its ith value.

SplitInfo measures the amount of information provided by an attribute that is not specific to the category.

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Information Content

The information content $I(C:F)$ of the class variable C with possible values $\{c_1, c_2, \dots, c_n\}$ with respect to the feature variable F with possible values $\{f_1, f_2, \dots, f_m\}$ is defined by:

$$I(C:F) = \sum_{i=1}^m \sum_{j=1}^n P(C = c_i, F = f_j) \log_2 \frac{P(C = c_i, F = f_j)}{P(C = c_i)P(F = f_j)}$$

- $P(C = c_i)$ is the probability of class C having value c_i .
- $P(F = f_j)$ is the probability of feature F having value f_j .
- $P(C = c_i, F = f_j)$ is the joint probability of class $C = c_i$ and variable $F = f_j$.

These are estimated from frequencies in the training data.

Using Information Content

- Start with the root of the decision tree and the whole training set.
- Compute $I(C,F)$ for each feature F .
- Choose the feature F with highest information content for the root node.
- Create branches for each value f of F .
- On each branch, create a new node with reduced training set and repeat recursively.

Artificial Neural Nets

Artificial Neural Nets (ANNs) are networks of artificial neuron nodes, each of which computes a simple function.

An ANN has an input layer, an output layer, and "hidden" layers of nodes.

Inputs

Outputs

Node Functions

$$\text{output} = g(\sum a_j * w(j,i))$$

Function g is commonly a step function, sign function, or sigmoid function (see text).

Neural Net Learning

That's beyond the scope of this text; only simple feed-forward learning is covered.

The most common method is called **back propagation**.

We've been using a free package called NevProp.

What do you use?

Support Vector Machines (SVM)

Support vector machines are learning algorithms that try to find a hyperplane that separates the differently classified data the most. They are based on two key ideas:

- Maximum margin hyperplanes
- A kernel 'trick'.

Maximal Margin

Find the hyperplane with maximal margin for all the points. This originates an optimization problem which has a unique solution (convex problem).

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Non-separable data

What can be done if data cannot be separated with a hyperplane?

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The kernel trick

The SVM algorithm implicitly maps the original data to a feature space of possibly infinite dimension in which data (which is not separable in the original space) becomes separable in the feature space.

Original space R^k

0	0	1
0	1	0
0	0	0
1	1	0

Kernel trick

Feature space R^n

0	0	1	1
0	0	1	1
0	0	0	1
0	0	0	1

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Our Current Application

- Sal Ruiz is using support vector machines in his work on 3D object recognition.
- He is training classifiers on data representing deformations of a 3D model of a class of objects.
- The classifiers learn what kinds of surface patches are related to key parts of the model (ie. A snowman's face)

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Snowman with Patches

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We are also starting to use SVMs for Insect Recognition

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