

Announcements

- Project 1 artifact winners
 - not enough votes—please vote today!

Recognition



The "Margaret Thatcher Illusion", by Peter Thompson

Readings

- C. Bishop, "Neural Networks for Pattern Recognition", Oxford University Press, 1998, Chapter 1.
- Forsyth and Ponce, 22.3 (eigenfaces)

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Recognition problems

What is it?

- Object detection

Who is it?

- Recognizing identity

What are they doing?

- Activities

All of these are **classification** problems

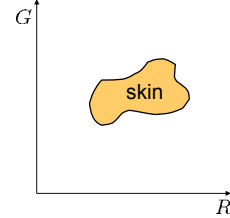
- Choose one class from a list of possible candidates

Face detection



How to tell if a face is present?

One simple method: skin detection



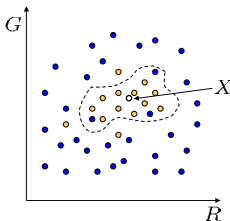
Skin pixels have a distinctive range of colors

- Corresponds to region(s) in RGB color space
 - for visualization, only R and G components are shown above

Skin classifier

- A pixel $X = (R, G, B)$ is skin if it is in the skin region
- But how to find this region?

Skin detection



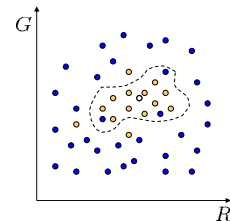
Learn the skin region from examples

- Manually label pixels in one or more "training images" as skin or not skin
- Plot the training data in RGB space
 - skin pixels shown in orange, non-skin pixels shown in blue
 - some skin pixels may be outside the region, non-skin pixels inside. Why?

Skin classifier

- Given $X = (R, G, B)$: how to determine if it is skin or not?

Skin classification techniques



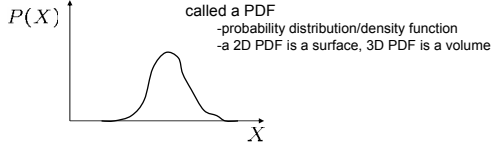
Skin classifier

- Given $X = (R, G, B)$: how to determine if it is skin or not?
- Nearest neighbor
 - find labeled pixel closest to X
 - choose the label for that pixel
- Data modeling
 - fit a model (curve, surface, or volume) to each class
- Probabilistic data modeling
 - fit a probability model to each class

Probability

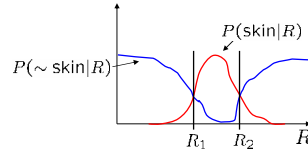
Basic probability

- X is a random variable
- P(X) is the probability that X achieves a certain value



- $0 \leq P(X) \leq 1$
- $\int_{-\infty}^{\infty} P(X)dX = 1$ or $\sum P(X) = 1$
 continuous X discrete X
- Conditional probability: $P(X | Y)$
 - probability of X given that we already know Y

Probabilistic skin classification



Now we can model uncertainty

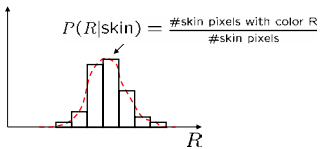
- Each pixel has a probability of being skin or not skin
 - $P(\sim \text{skin}|R) = 1 - P(\text{skin}|R)$

Skin classifier

- Given $X = (R,G,B)$: how to determine if it is skin or not?
- Choose interpretation of highest probability
 - set X to be a skin pixel if and only if $R_1 < X \leq R_2$

Where do we get $P(\text{skin}|R)$ and $P(\sim \text{skin}|R)$?

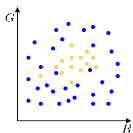
Learning conditional PDF's



We can calculate $P(R | \text{skin})$ from a set of training images

- It is simply a histogram over the pixels in the training images
 - each bin R_i contains the proportion of skin pixels with color R_i

This doesn't work as well in higher-dimensional spaces. Why not?

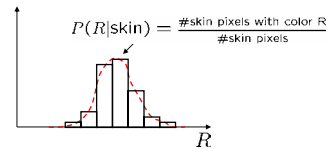


Approach: fit parametric PDF functions

- common choice is rotated Gaussian
 - center $c = \bar{X}$
 - covariance $\sum_X (X - \bar{X})(X - \bar{X})^T$

» orientation, size defined by eigenvecs, eigenvals

Learning conditional PDF's



We can calculate $P(R | \text{skin})$ from a set of training images

- It is simply a histogram over the pixels in the training images
 - each bin R_i contains the proportion of skin pixels with color R_i

But this isn't quite what we want

- Why not? How to determine if a pixel is skin?
- We want $P(\text{skin} | R)$ not $P(R | \text{skin})$
- How can we get it?

Bayes rule

$$P(X|Y) = \frac{P(Y|X)P(X)}{P(Y)}$$

In terms of our problem:

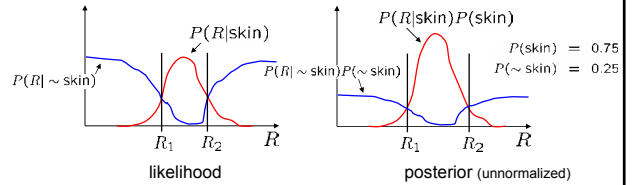
$$P(\text{skin}|R) = \frac{P(R|\text{skin}) P(\text{skin})}{P(R)}$$

$P(R) = P(R|\text{skin})P(\text{skin}) + P(R|\sim\text{skin})P(\sim\text{skin})$

The prior: $P(\text{skin})$

- Could use domain knowledge
 - $P(\text{skin})$ may be larger if we know the image contains a person
 - for a portrait, $P(\text{skin})$ may be higher for pixels in the center
- Could learn the prior from the training set. How?
 - $P(\text{skin})$ may be proportion of skin pixels in training set

Bayesian estimation



Bayesian estimation

= minimize probability of misclassification

- Goal is to choose the label (skin or ~skin) that maximizes the posterior
 - this is called **Maximum A Posteriori (MAP) estimation**
- Suppose the prior is uniform: $P(\text{skin}) = P(\sim\text{skin}) = 0.5$
 - in this case $P(\text{skin}|R) = cP(R|\text{skin})$, $P(\sim\text{skin}|R) = cP(R|\sim\text{skin})$
 - maximizing the posterior is equivalent to maximizing the likelihood
 - » $P(\text{skin}|R) > P(\sim\text{skin}|R)$ if and only if $P(R|\text{skin}) > P(R|\sim\text{skin})$
 - this is called **Maximum Likelihood (ML) estimation**

Skin detection results

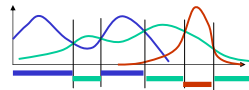


Figure 25.3. The figure shows a variety of images together with the output of the skin detector of Jones and Rehg applied to the image. Pixels marked black are skin pixels, and white are background. Notice that this process is relatively effective, and could certainly be used to focus attention on, say, faces and hands. Figure from "Statistical color models with application to skin detection," M.J. Jones and J. Rehg, Proc. Computer Vision and Pattern Recognition, 1999 © 1999, IEEE

General classification

This same procedure applies in more general circumstances

- More than two classes
- More than one dimension



Example: face detection

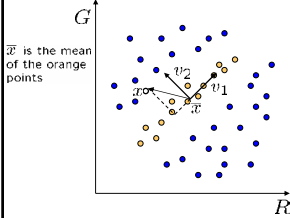
- Here, X is an image region
 - dimension = # pixels
 - each face can be thought of as a point in a high dimensional space



H. Schneiderman, T. Kanade, "A Statistical Method for 3D Object Detection Applied to Faces and Cars", IEEE Conference on Computer Vision and Pattern Recognition (CVPR 2000)
<http://www-2.cs.cmu.edu/af/cs.cmu.edu/user/hws/www/CVPR01.pdf>

H. Schneiderman and T. Kanade

Linear subspaces



convert \mathbf{x} into $\mathbf{v}_1, \mathbf{v}_2$ coordinates

$$\mathbf{x} \rightarrow ((\mathbf{x} - \bar{\mathbf{x}}) \cdot \mathbf{v}_1, (\mathbf{x} - \bar{\mathbf{x}}) \cdot \mathbf{v}_2)$$

What does the \mathbf{v}_2 coordinate measure?

- distance to line
- use it for classification—near 0 for orange pts

What does the \mathbf{v}_1 coordinate measure?

- position along line
- use it to specify which orange point it is

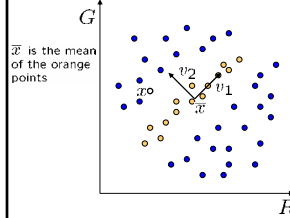
Classification is still expensive

- Must either search (e.g., nearest neighbors) or store large PDF's

Suppose the data points are arranged as above?

- Idea—fit a line, classifier measures distance to line

Dimensionality reduction

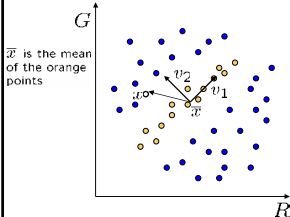


How to find \mathbf{v}_1 and \mathbf{v}_2 ?
- work out on board

Dimensionality reduction

- We can represent the orange points with *only* their \mathbf{v}_1 coordinates
 - since \mathbf{v}_2 coordinates are all essentially 0
- This makes it much cheaper to store and compare points
- A bigger deal for higher dimensional problems

Linear subspaces



Consider the variation along direction \mathbf{v} among all of the orange points:

$$\text{var}(\mathbf{v}) = \sum_{\text{orange point } \mathbf{x}} \|(\mathbf{x} - \bar{\mathbf{x}})^T \cdot \mathbf{v}\|^2$$

What unit vector \mathbf{v} minimizes var ?

$$\mathbf{v}_2 = \min_{\mathbf{v}} \{\text{var}(\mathbf{v})\}$$

What unit vector \mathbf{v} maximizes var ?

$$\mathbf{v}_1 = \max_{\mathbf{v}} \{\text{var}(\mathbf{v})\}$$

$$\begin{aligned} \text{var}(\mathbf{v}) &= \sum_{\mathbf{x}} \|(\mathbf{x} - \bar{\mathbf{x}})^T \cdot \mathbf{v}\|^2 \\ &= \sum_{\mathbf{x}} \mathbf{v}^T (\mathbf{x} - \bar{\mathbf{x}})(\mathbf{x} - \bar{\mathbf{x}})^T \mathbf{v} \\ &= \mathbf{v}^T \left[\sum_{\mathbf{x}} (\mathbf{x} - \bar{\mathbf{x}})(\mathbf{x} - \bar{\mathbf{x}})^T \right] \mathbf{v} \\ &= \mathbf{v}^T \mathbf{A} \mathbf{v} \text{ where } \mathbf{A} = \sum_{\mathbf{x}} (\mathbf{x} - \bar{\mathbf{x}})(\mathbf{x} - \bar{\mathbf{x}})^T \end{aligned}$$

Solution: \mathbf{v}_1 is eigenvector of \mathbf{A} with *largest* eigenvalue
 \mathbf{v}_2 is eigenvector of \mathbf{A} with *smallest* eigenvalue

Principle component analysis

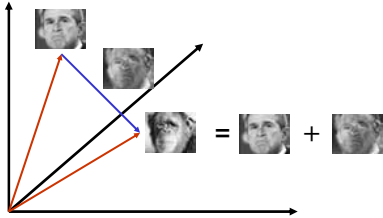
Suppose each data point is N-dimensional

- Same procedure applies:

$$\begin{aligned} \text{var}(\mathbf{v}) &= \sum_{\mathbf{x}} \|(\mathbf{x} - \bar{\mathbf{x}})^T \cdot \mathbf{v}\|^2 \\ &= \mathbf{v}^T \mathbf{A} \mathbf{v} \text{ where } \mathbf{A} = \sum_{\mathbf{x}} (\mathbf{x} - \bar{\mathbf{x}})(\mathbf{x} - \bar{\mathbf{x}})^T \end{aligned}$$

- The eigenvectors of \mathbf{A} define a new coordinate system
 - eigenvector with largest eigenvalue captures the most variation among training vectors \mathbf{x}
 - eigenvector with smallest eigenvalue has least variation
- We can compress the data by only using the top few eigenvectors
 - corresponds to choosing a "linear subspace"
 - » represent points on a line, plane, or "hyper-plane"

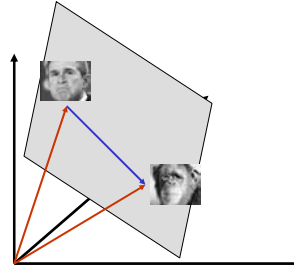
The space of faces



An image is a point in a high dimensional space

- An $N \times M$ image is a point in R^{NM}
- We can define vectors in this space as we did in the 2D case

Dimensionality reduction



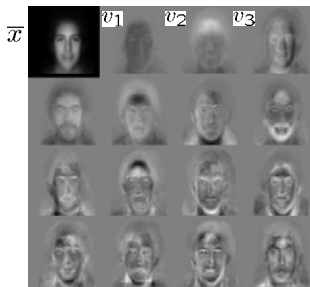
The set of faces is a "subspace" of the set of images

- Suppose it is K dimensional
- We can find the best subspace using PCA
- This is like fitting a "hyper-plane" to the set of faces
 - spanned by vectors v_1, v_2, \dots, v_K
 - any face $x \approx \bar{x} + a_1 v_1 + a_2 v_2 + \dots + a_k v_k$

Eigenfaces

PCA extracts the eigenvectors of A

- Gives a set of vectors v_1, v_2, v_3, \dots
- Each one of these vectors is a direction in face space
 - what do these look like?



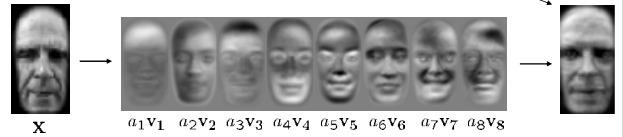
Projecting onto the eigenfaces

The eigenfaces v_1, \dots, v_K span the space of faces

- A face is converted to eigenface coordinates by

$$x \rightarrow \left(\underbrace{(x - \bar{x}) \cdot v_1}_{a_1}, \underbrace{(x - \bar{x}) \cdot v_2}_{a_2}, \dots, \underbrace{(x - \bar{x}) \cdot v_K}_{a_K} \right)$$

$$x \approx \bar{x} + a_1 v_1 + a_2 v_2 + \dots + a_K v_K$$



Recognition with eigenfaces

Algorithm

1. Process the image database (set of images with labels)
 - Run PCA—compute eigenfaces
 - Calculate the K coefficients for each image
2. Given a new image (to be recognized) \mathbf{x} , calculate K coefficients

$$\mathbf{x} \rightarrow (a_1, a_2, \dots, a_K)$$

3. Detect if \mathbf{x} is a face

$$\|\mathbf{x} - (\bar{\mathbf{x}} + a_1\mathbf{v}_1 + a_2\mathbf{v}_2 + \dots + a_K\mathbf{v}_K)\| > \text{threshold}$$

4. If it is a face, who is it?
 - Find closest labeled face in database
 - nearest-neighbor in K-dimensional space

Limits of PCA

Attempts to fit a *hyperplane* to the data

- can be interpreted as fitting a Gaussian, where A is the covariance matrix
- this is not a good model for some data

If you know the model in advance, don't use PCA

- regression techniques to fit parameters of a model

Several alternatives/improvements to PCA have been developed

- LLE: <http://www.cs.toronto.edu/~roweis/lle/>
- isomap: <http://isomap.stanford.edu/>
- kernel PCA: http://www.cs.ucsd.edu/classes/fa01/cse291/kernelPCA_article.pdf
- For a survey of such methods applied to object recognition
 - Moghaddam, B., "Principal Manifolds and Probabilistic Subspaces for Visual Recognition", *IEEE Transactions on Pattern Analysis and Machine Intelligence (PAMI)*, June 2002 (Vol 24, Issue 6, pps 780-788)
<http://www.merl.com/papers/TR2002-13/>

Object recognition

This is just the tip of the iceberg

- We've talked about using pixel color as a feature
- Many other features can be used:
 - edges
 - motion (e.g., optical flow)
 - object size
 - ...
- Classical object recognition techniques recover 3D information as well
 - given an image and a database of 3D models, determine which model(s) appears in that image
 - often recover 3D pose of the object as well
 - new work (e.g., Linda Shapiro's group at UW), seeks to recognize 3D objects (meshes) by training on 3D scan data