

Announcements

- Project 1 artifact voting (email announce later today)
- Project 2 out today (help session at end of class)
- **IMPORTANT:** choose Proj 2 partner and SIGNUP for panorama equip TODAY:
 - <http://www.cs.washington.edu/htbin-post/admin/preserve.cgi/www/htdocs/education/courses/cse576/panorama>

Mosaics



<http://www.panoramas.dk/>
http://www.vrseattle.com/html/vrview.php?cat_id=11&vrs_id=vrs380

Today's Readings

- R. Szeliski and H.-Y. Shum. Creating full view panoramic image mosaics and texture-mapped models, Computer Graphics (SIGGRAPH'97), pages 251-258, August 1997
- J. F. Blinn, Jim Blinn's Corner: Compositing, Part 1: Theory, IEEE Computer Graphics and Application, 14(5), Sept. 1994, pp 83-87

Image Mosaics



Goal

- Stitch together several images into a seamless composite

How to do it?

Basic Procedure

- Take a sequence of images from the same position
 - Rotate the camera about its optical center
- Compute transformation between second image and first
 - Lucas & Kanade registration
- Shift the second image to overlap with the first
- Blend the two together to create a mosaic
- If there are more images, repeat

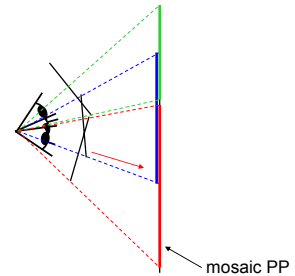
Aligning images



How to account for warping?

- Translations are not enough to align the images
- [Photoshop demo](#)

Image reprojection



The mosaic has a natural interpretation in 3D

- The images are reprojected onto a common plane
 - idea: replace camera with slide projector, project onto new PP
- The mosaic is formed on this plane

Image reprojection

Basic question

- How to relate two images from the same camera center?
 - how to map a pixel from PP1 to PP2

Answer

- Cast a ray through each pixel in PP1
- Draw the pixel where that ray intersects PP2

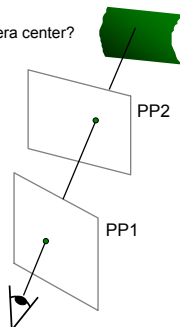
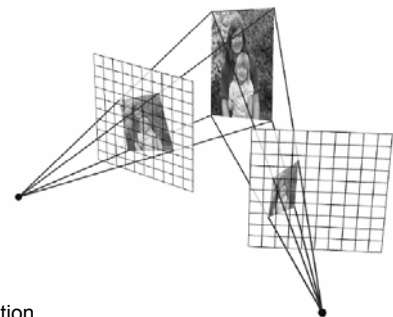


Image reprojection



Observation

- Rather than thinking of this as a 3D reprojection, think of it as a 2D image warp from one image to another

Homographies

Perspective projection of a plane

- Lots of names for this:
 - **homography**, texture-map, colineation, planar projective map
- Modeled as a 2D warp using homogeneous coordinates

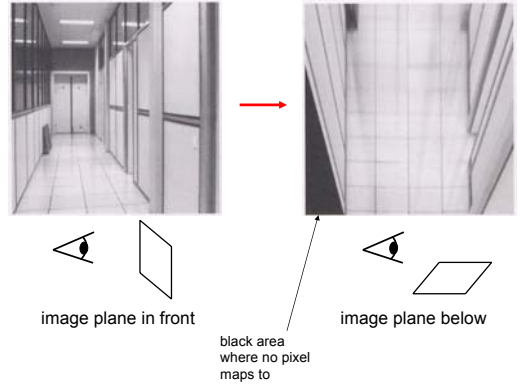
$$\begin{bmatrix} wx' \\ wy' \\ w \end{bmatrix} = \begin{bmatrix} * & * & * \\ * & * & * \\ * & * & * \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$\mathbf{p}' \quad \mathbf{H} \quad \mathbf{p}$

To apply a homography \mathbf{H}

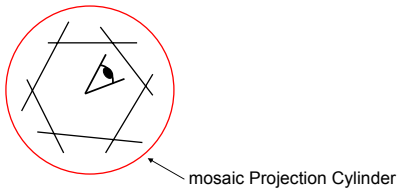
- Compute $\mathbf{p}' = \mathbf{H}\mathbf{p}$ (regular matrix multiply)
- Convert \mathbf{p}' from homogeneous to image coordinates
 - divide by w (third) coordinate

Image warping with homographies

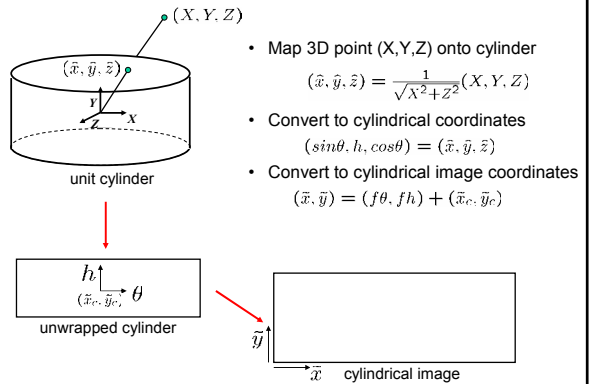


Panoramas

What if you want a 360° field of view?

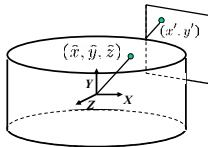


Cylindrical projection

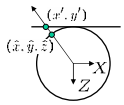


Cylindrical reprojection

How to map from a cylinder to a planar image?



side view



top-down view

- Apply camera projection matrix
 - for project 2, account for focal length and assume principle point is at center of image
 - » $x'_c = \frac{1}{2}$ image width, $y'_c = \frac{1}{2}$ image height

$$\begin{bmatrix} wx' \\ wy' \\ w \end{bmatrix} = \begin{bmatrix} -f & 0 & w/2 & 0 \\ 0 & -f & h/2 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} \hat{x} \\ \hat{y} \\ \hat{z} \\ 1 \end{bmatrix}$$

- Convert to image coordinates
 - divide by third coordinate (w)

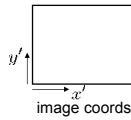


image coords

Cylindrical reprojection



Image 384x300

f = 180 (pixels)

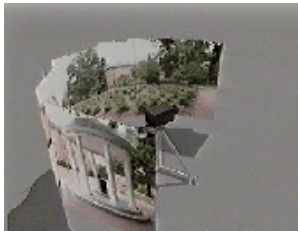
f = 280

f = 380

Map image to cylindrical coordinates

- need to know the camera focal length

Cylindrical panoramas



Steps

- Reproject each image onto a cylinder
- Blend
- Output the resulting mosaic

Cylindrical image stitching



What if you don't know the camera rotation?

- Solve for the camera rotations
 - Note that a rotation of the camera is a **translation** of the cylinder!
 - Use Lukas-Kanade to solve for translations of cylindrically-warped images

Full-view Panorama



Different projections are possible

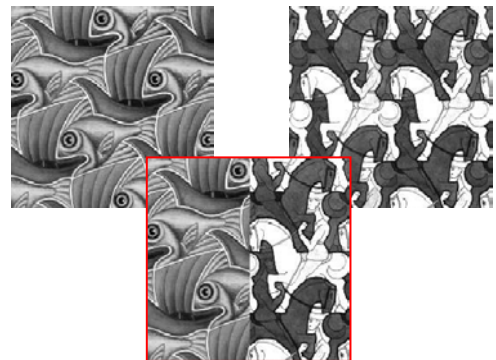


Szeliski-Shum, SIGGRAPH 97 video

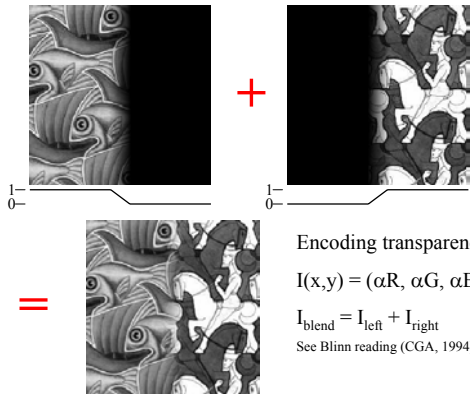
Project 2 (out today)

1. Take pictures on a tripod (or handheld)
2. Warp to cylindrical coordinates
3. Automatically compute pair-wise alignments
4. Correct for drift
5. Blend the images together
6. Crop the result and import into a viewer

Image Blending



Feathering



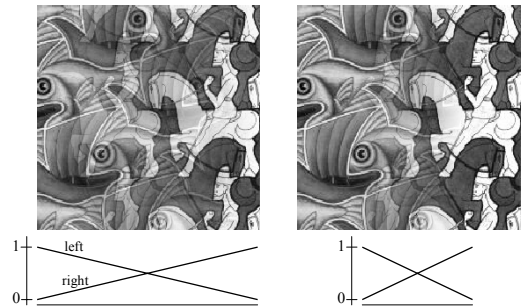
Encoding transparency

$$I(x,y) = (\alpha R, \alpha G, \alpha B, \alpha)$$

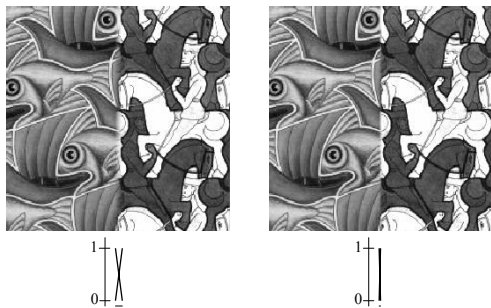
$$I_{\text{blend}} = I_{\text{left}} + I_{\text{right}}$$

See Blinn reading (CGA, 1994) for details

Effect of window size



Effect of window size



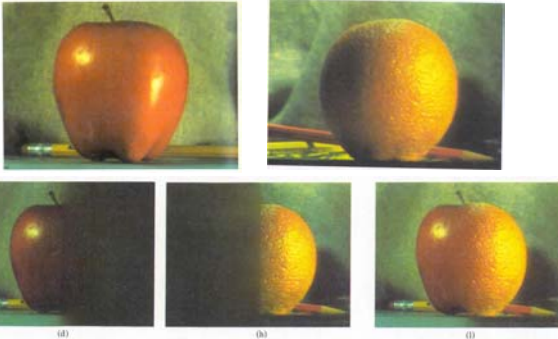
Good window size



"Optimal" window: smooth but not ghosted

- Doesn't always work...

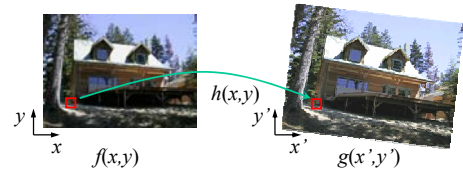
Pyramid blending



Create a Laplacian pyramid, blend each level

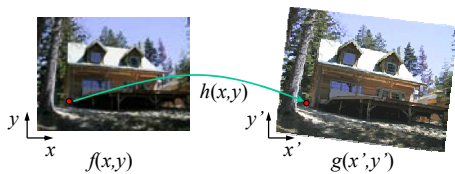
- Burt, P. J. and Adelson, E. H., [A multiresolution spline with applications to image mosaics](#), ACM Transactions on Graphics, 42(4), October 1993, 217-236.

Image warping



Given a coordinate transform $(x',y') = h(x,y)$ and a source image $f(x,y)$, how do we compute a transformed image $g(x',y') = f(h(x,y))$?

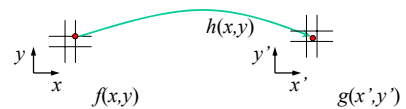
Forward warping



Send each pixel $f(x,y)$ to its corresponding location $(x',y') = h(x,y)$ in the second image

Q: what if pixel lands "between" two pixels?

Forward warping

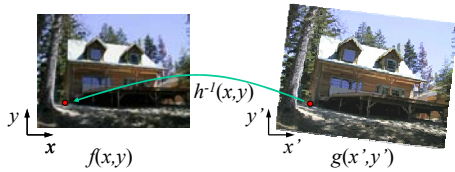


Send each pixel $f(x,y)$ to its corresponding location $(x',y') = h(x,y)$ in the second image

Q: what if pixel lands "between" two pixels?

A: distribute color among neighboring pixels (x',y')
 - Known as "splatting"

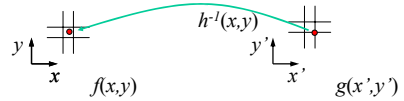
Inverse warping



Get each pixel $g(x',y')$ from its corresponding location $(x,y) = h^{-1}(x',y')$ in the first image

Q: what if pixel comes from “between” two pixels?

Inverse warping



Get each pixel $g(x',y')$ from its corresponding location $(x,y) = h^{-1}(x',y')$ in the first image

Q: what if pixel comes from “between” two pixels?

A: *resample* color value

- We discussed resampling techniques before
 - nearest neighbor, bilinear, Gaussian, bicubic

Forward vs. inverse warping

Q: which is better?

A: usually inverse—eliminates holes

- however, it requires an invertible warp function—not always possible...

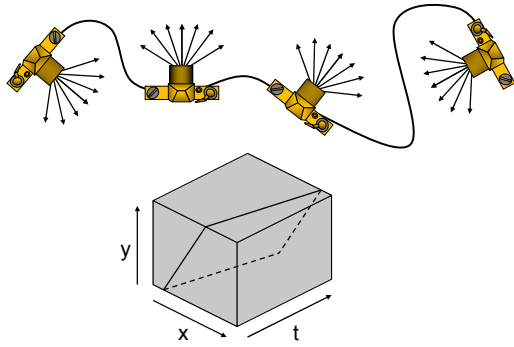
Other types of mosaics



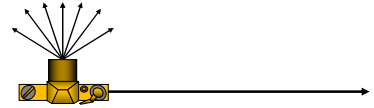
Can mosaic onto *any* surface if you know the geometry

- See NASA's [Visible Earth project](http://visibleearth.nasa.gov) for some stunning earth mosaics
 - <http://earthobservatory.nasa.gov/Newsroom/BlueMarble/>

Path Images

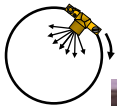


Pushbroom image



<http://grail.cs.washington.edu/projects/stereo/>

Cyclograph



<http://grail.cs.washington.edu/projects/stereo/>

Some path image references

Manifold mosaics:

- S. Peleg and J. Herman. Panoramic mosaics by manifold projection. In *IEEE Conf. on Computer Vision and Pattern Recognition (CVPR)*, 997, pp. 338-343, (extended version in [PAMI 2000](#))
 - <http://www.cs.huji.ac.il/labs/vision/papers/cvpr97-manifold.pdf>

Stereo Panoramas

- S. Peleg, Y. Pritch, and M. Ben-Ezra, *Cameras for Stereo Panoramic Imaging*, CVPR'00, 2000, pp. 208-214.
 - <http://www.cs.huji.ac.il/~peleg/papers/cvpr00-stereocamera.pdf>
- S. M. Seitz and J. Kim, The Space of All Stereo Images, *Proc. Intl. Conf. on Computer Vision (ICCV)*, 2001, pp. 307-314.
 - <http://grail.cs.washington.edu/projects/stereo/>

Concentric Mosaics

- H.-Y. Shum and L.-W. He, Rendering with concentric mosaics, *Proc. SIGGRAPH*, 1999, pp. 299-306.
 - <http://www.research.microsoft.com/users/lhe/papers/cm-siggraph99.pdf>