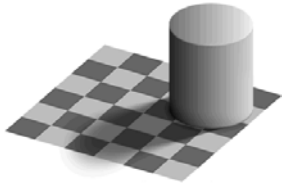# Light

by Ted Adelson

Readings
- Forsyth, Chapters 4, 6 (through 6.2)

Properties of light

Today
- What is light?
- How do we measure it?
- How does light propagate?
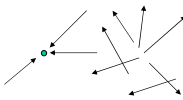- How does light interact with matter?

What is light?

Electromagnetic radiation (EMR) moving along rays in space
- $R(\lambda)$ is EMR, measured in units of power (watts)
  - λ is wavelength

Light field
- We can describe all of the light in the scene by specifying the radiation (or **"radiance"** along all light rays) arriving at every point in space and from every direction
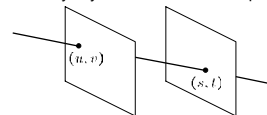

$$R(X, Y, Z, \theta, \phi, \lambda, t)$$

The light field

$$R(X, Y, Z, \theta, \phi, \lambda, t)$$
- Known as the **plenoptic function**
- If you know *R*, you can predict how the scene would appear from any viewpoint. How?

The **light field** $R(u, v, s, t)$ —— t is *not* time (different from above t !)
- Assume radiance does not change along a ray
  - what does this assume about the world?
- Parameterize rays by intersection with two planes:

(u, v)
(s, t)

- Usually drop λ and time parameters
- How could you capture a light field?

Stanford light field gantry
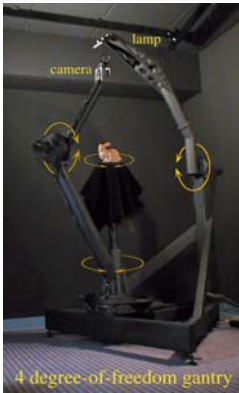
More info on light fields

If you're interested to read more:

The plenoptic function
- **Original reference:** E. Adelson and J. Bergen, "The Plenoptic Function and the Elements of Early Vision," in M. Landy and J. A. Movshon, (eds) Computational Models of Visual Processing, MIT Press 1991.
- L. McMillan and G. Bishop, "Plenoptic Modeling: An Image-Based Rendering System", Proc. SIGGRAPH, 1995, pp. 39-46.

The light field
- M. Levoy and P. Hanrahan, "Light Field Rendering", Proc SIGGRAPH 96, pp. 31-42.
- S. J. Gortler, R. Grzeszczuk, R. Szeliski, and M. F. Cohen, "The lumigraph," in Proc. SIGGRAPH, 1996, pp. 43-54.

show video

What is light?

Electromagnetic radiation (EMR) moving along rays in space
- $R(\lambda)$ is EMR, measured in units of power (watts)
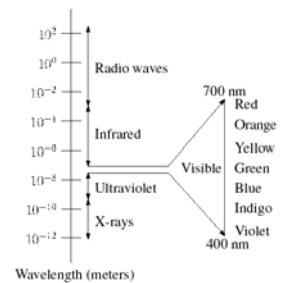 - λ is wavelength

Perceiving light
- How do we convert radiation into "color"?
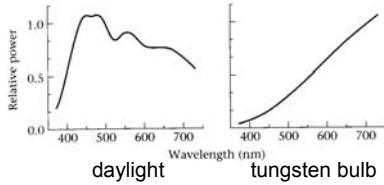- What part of the spectrum do we see?

The visible light spectrum

We "see" electromagnetic radiation in a range of wavelengths

Light spectrum
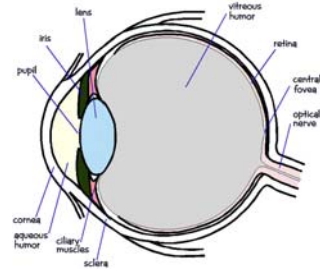
The appearance of light depends on its power **spectrum**
  - How much power (or energy) at each wavelength

daylight   tungsten bulb

Our visual system converts a light spectrum into "color"
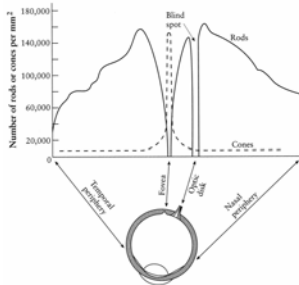 - This is a rather complex transformation

---

The human visual system

Color perception
  - Light hits the retina, which contains photosensitive cells
    – rods and cones
  - These cells convert the spectrum into a few discrete values

---

Density of rods and cones

Rods and cones are *non-uniformly* distributed on the retina
  - Rods responsible for intensity, cones responsible for color
  - **Fovea** - Small region (1 or 2°) at the center of the visual field containing the highest density of cones (and no rods).
  - Less visual acuity in the periphery—many rods wired to the same neuron

---

Demonstrations of visual acuity

With one eye shut, at the right distance, all of these letters should appear equally legible (Glassner, 1.7).

Demonstrations of visual acuity

*With left eye shut, look at the cross on the left. At the right
distance, the circle on the right should disappear (Glassner, 1.8).*

Brightness contrast and constancy

The apparent brightness depends on the surrounding region
- **brightness contrast**: a constant colored region seem lighter or darker depending on the surround:

  – http://www.sandlotscience.com/Contrast/CheckerBoard_illusion.htm

- **brightness constancy**: a surface looks the same under widely varying lighting conditions.

Light response is nonlinear

Our visual system has a large *dynamic range*
- We can resolve both light and dark things at the same time
- One mechanism for achieving this is that we sense light intensity on a *logarithmic scale*
  - an exponential intensity ramp will be seen as a linear ramp
- Another mechanism is *adaptation*
  - rods and cones adapt to be more sensitive in low light, less sensitive in bright light.

Visual dynamic range

Background	Luminance (candelas per square meter)
Horizon sky	
Moonless overcast night	0.00003
Moonless clear night	0.0003
Moonlit overcast night	0.003
Moonlit clear night	0.03
Deep twilight	0.3
Twilight	3
Very dark day	30
Overcast day	300
Clear day	3,000
Day with sunlit clouds	30,000
Daylight fog	
Dull	300–1,000
Typical	1,000–3,000
Bright	3,000–16,000
Ground	
Overcast day	30–100
Sunny day	300
Snow in full sunlight	16,000

FIGURE 1.13
Luminance of everyday backgrounds. *Source:* Data from Rea, ed., *Lighting Handbook 1984
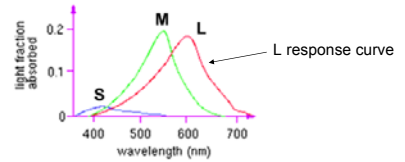Reference and Application*, fig. 3-44, p. 3-24.

After images

Tired photoreceptors
- Send out negative response after a strong stimulus

Color perception

L response curve
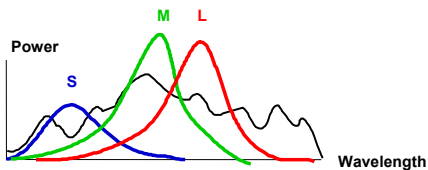
Three types of cones
- Each is sensitive in a different region of the spectrum
  - but regions overlap
  - Short (S) corresponds to blue
  - Medium (M) corresponds to green
  - Long (L) corresponds to red
- Different sensitivities: we are more sensitive to green than red
- Colorblindness—deficiency in at least one type of cone

Color perception

Rods and cones act as filters on the spectrum
- To get the output of a filter, multiply its response curve by the spectrum, integrate over all wavelengths
  - Each cone yields one number
- Q: How can we represent an entire spectrum with 3 numbers?
- A: We can't! Most of the information is lost.
  - As a result, two different spectra may appear indistinguishable
    » such spectra are known as **metamers**
    » http://www.cs.brown.edu/exploratories/freeSoftware/repository/edu/brown/cs/exploratories/applets/spectrum/metamers_guide.html

Perception summary

The mapping from radiance to perceived color is quite complex!
- We throw away most of the data
- We apply a logarithm
- Brightness affected by pupil size
- Brightness contrast and constancy effects
- Afterimages

Camera response function

Now how about the mapping f from radiance to pixels?
- • It's also complex, but better understood
- • This mapping f known as the film or camera *response function*

How can we recover radiance values given pixel values?

Why should we care?
- • Useful if we want to estimate material properties
- • Shape from shading requires radiance
- • Enables creating high dynamic range images

What does the response function depend on?

$f(shutter\ speed,\ aperture,\ film\ stock,\ digitizer,\ ...)$
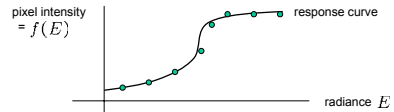

Recovering the camera response

Method 1
- • Carefully model every step in the pipeline
  - – measure aperture, model film, digitizer, etc.
  - – this is *really* hard to get right

Method 2
- • Calibrate (estimate) the response function
  - – Image several objects with known radiance
  - – Measure the pixel values
  - – Fit a function

pixel intensity = $f(E)$ response curve

radiance E

- – Find the inverse: f^{-1} maps pixel intensity to radiance

---

Recovering the camera response

Method 3
- • Calibrate the response function from several images
  - – Consider taking images with shutter speeds 1/1000, 1/100, 1/10, and 1
  - – Q: What is the relationship between the radiance or pixel values in consecutive images?
  - – A: 10 times as much radiance
  - – Can use this to recover the camera response function

pixel intensity = $f(E\Delta t)$ response curve

exposure ≅ radiance * time = $E\Delta t$
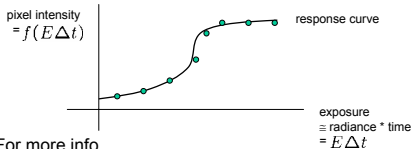
For more info
- • P. E. Debevec and J. Malik. *Recovering High Dynamic Range Radiance Maps from Photographs*. In *SIGGRAPH 97*, August 1997
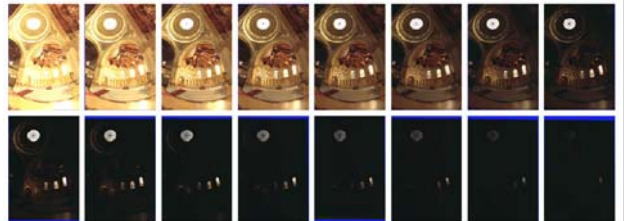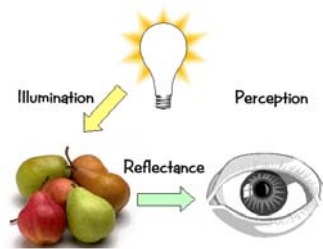

High dynamic range imaging

Figure 6: Sixteen photographs of a church taken at 1-stop increments from 30 sec to $\frac{1}{1000}$ sec. The sun is directly behind the rightmost stained glass window, making it especially bright. The blue borders seen in some of the image margins are induced by the image registration process.
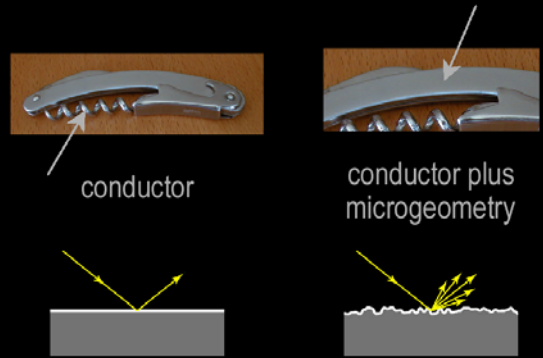
Techniques
- • Debevec: http://www.debevec.org/Research/HDR/
- • Columbia: http://www.cs.columbia.edu/CAVE/tomoo/RRHomePage/rrgallery.html

Light transport

Illumination • Perception • Reflectance

Materials

conductor

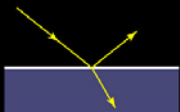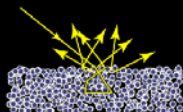conductor plus microgeometry

insulator

insulator plus microgeometry

The interaction of light and matter

What happens when a light ray hits a point on an object?
- Some of the light gets absorbed
  - converted to other forms of energy (e.g., heat)
- Some gets transmitted through the object
  - possibly bent, through "refraction"
- Some gets reflected
 - as we saw before, it could be reflected in multiple directions at once

Let's consider the case of reflection in detail
- In the most general case, a single incoming ray could be reflected in all directions. How can we describe the amount of light reflected in each direction?
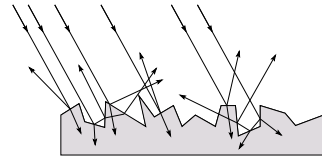
The BRDF

The Bidirectional Reflection Distribution Function
- Given an incoming ray (θ_i, ϕ_i) and outgoing ray (θ_e, ϕ_e) what proportion of the incoming light is reflected along outgoing ray?
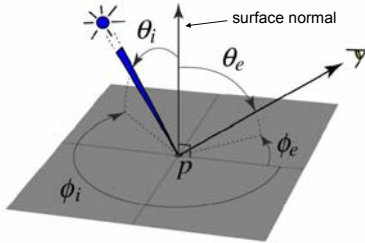
Answer given by the BRDF: $\rho(\theta_i, \phi_i, \theta_e, \phi_e)$

Diffuse reflection

Diffuse reflection
- Dull, matte surfaces like chalk or latex paint
- Microfacets scatter incoming light randomly
- Effect is that light is reflected equally in all directions
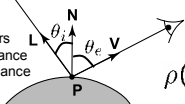
Diffuse reflection

Diffuse reflection governed by **Lambert's law**
- Viewed brightness does not depend on viewing direction
- Brightness *does* depend on direction of illumination
- This is the model most often used in computer vision
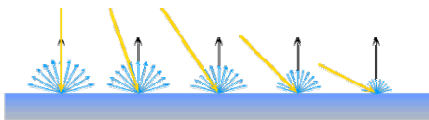
Lambert's Law: $I_e = k_d \mathbf{N} \cdot \mathbf{L} I_i$

L, **N**, **V** unit vectors
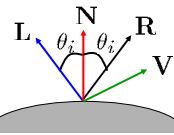I_e = outgoing radiance
I_i = incoming radiance

BRDF for **Lambertian surface**
$\rho(\theta_i, \phi_i, \theta_e, \phi_e) = k_d cos\theta_i$

Specular reflection
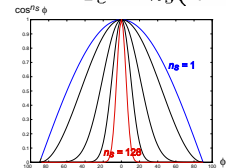
For a perfect mirror, light is reflected about **N**

$I_e = \begin{cases} I_i & \text{if } \mathbf{V} = \mathbf{R} \\ 0 & \text{otherwise} \end{cases}$

Near-perfect mirrors have a **highlight** around **R**
- common model: $I_e = k_s (\mathbf{V} \cdot \mathbf{R})^{n_s} I_i$

conductor plus microgeometry

Phong illumination model

Phong approximation of surface reflectance
- Assume reflectance is modeled by three components
  - Diffuse term
  - Specular term
  - Ambient term (to compensate for inter-reflected light)

$$I_e = k_a I_a + I_i \left[k_d (\mathbf{N} \cdot \mathbf{L})_+ + k_s (\mathbf{V} \cdot \mathbf{R})_+^{n_s} \right]$$

L, **N**, **V** unit vectors
I_e = outgoing radiance
I_i = incoming radiance
I_a = ambient light
k_a = ambient light reflectance factor
$(x)_+$ = max(x, 0)

Measuring the BRDF

traditional   **design by Greg Ward**
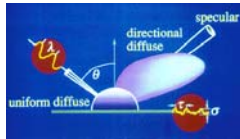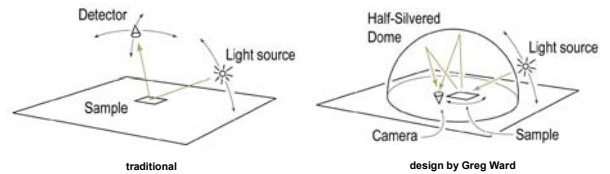
Gonioreflectometer
- Device for capturing the BRDF by moving a camera + light source
- Need careful control of illumination, environment

Columbia-Utrecht Database

Captured BRDF models for a variety of materials
- http://www.cs.columbia.edu/CAVE/curet/.index.html

Advanced topics

Ongoing research in BRDF's seeks to:
- Recover BRDF's from "just a few" images, model global light transport
  - Yu, Debevec, Malik and Hawkins, "Inverse Global Illumination", SIGGRAPH 1999.
- Model semi-transparent, refractive surfaces
  - Zongker, Werner, Curless, and Salesin, "Environment Matting and Compositing", SIGGRAPH 99, pp. 205-214.
- Model sub-surface scattering
  - Jensen, Marschner, Levoy and Hanrahan: "A Practical Model for Subsurface Light Transport", SIGGRAPH'2001.

videos