Edge Detection



Today's reading

• Forsyth, chapters 8, 15.1

Edge detection

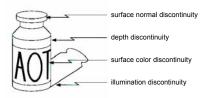




Convert a 2D image into a set of curves

- · Extracts salient features of the scene
- · More compact than pixels

Origin of Edges



Edges are caused by a variety of factors

Edge detection





How can you tell that a pixel is on an edge?

snoop demo

Image gradient

The gradient of an image:

$$\nabla f = \left[\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y} \right]$$

The gradient points in the direction of most rapid change in intensity







The gradient direction is given by:

$$\theta = \tan^{-1} \left(\frac{\partial f}{\partial u} / \frac{\partial f}{\partial x} \right)$$

• how does this relate to the direction of the edge?

The edge strength is given by the gradient magnitude

$$\|\nabla f\| = \sqrt{\left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2}$$

The discrete gradient

How can we differentiate a digital image f[x,y]?

- · Option 1: reconstruct a continuous image, then take gradient
- Option 2: take discrete derivative (finite difference)

$$\frac{\partial f}{\partial x}[x,y]\approx f[x+\mathbf{1},y]-f[x,y]$$

How would you implement this as a cross-correlation?



filter demo

The Sobel operator

Better approximations of the derivatives exist

· The Sobel operators below are very commonly used

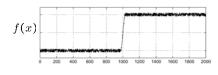


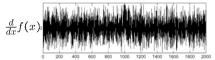
- · The standard defn. of the Sobel operator omits the 1/8 term
 - doesn't make a difference for edge detection
 - the 1/8 term is needed to get the right gradient value, however

Effects of noise

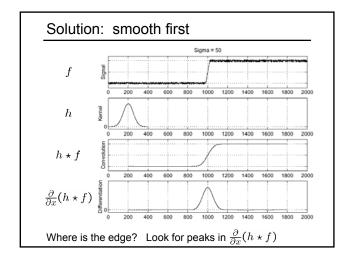
Consider a single row or column of the image

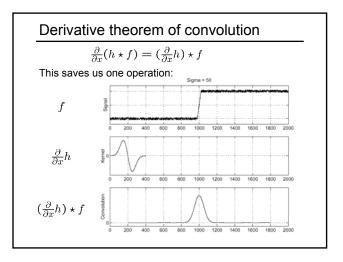
· Plotting intensity as a function of position gives a signal

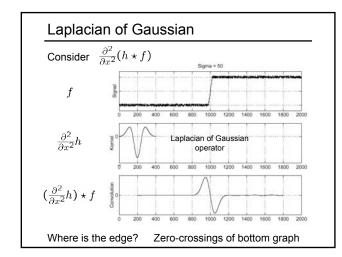


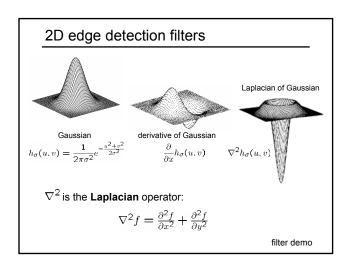


Where is the edge?









The Canny edge detector



original image (Lena)

The Canny edge detector



norm of the gradient

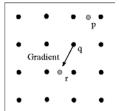
The Canny edge detector



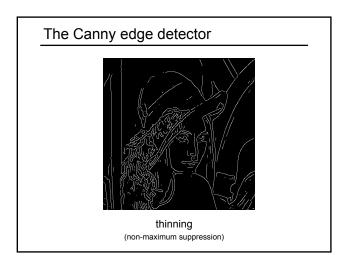
thresholding

Non-maximum suppression





Check if pixel is local maximum along gradient direction requires checking interpolated pixels p and r



Effect of σ (Gaussian kernel size)



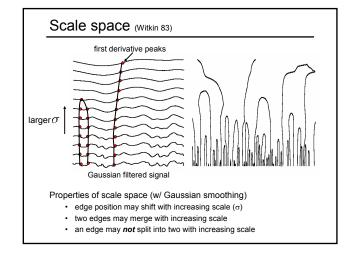
original

Canny with $\,\sigma=1\,$

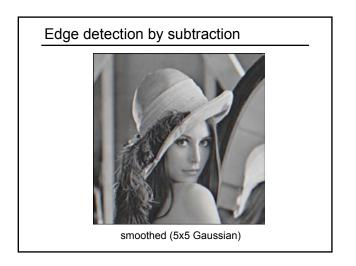
Canny with $\,\sigma=2\,$

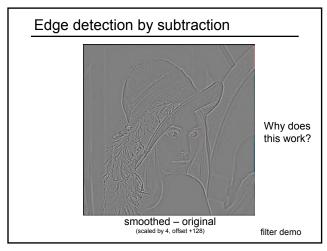
The choice of σ depends on desired behavior

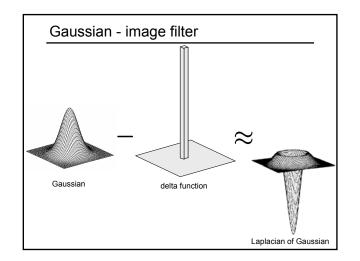
- large σ detects large scale edges
- small σ detects fine features

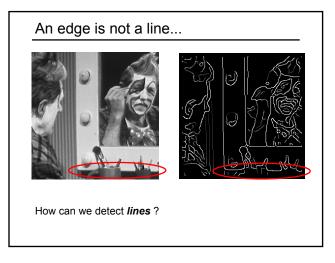


Edge detection by subtraction original









Finding lines in an image

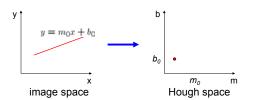
Option 1:

- · Search for the line at every possible position/orientation
- · What is the cost of this operation?

Option 2:

Use a voting scheme: Hough transform

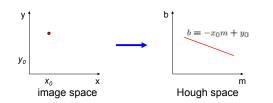
Finding lines in an image



Connection between image (x,y) and Hough (m,b) spaces

- A line in the image corresponds to a point in Hough space
- To go from image space to Hough space:
 - given a set of points (x,y), find all (m,b) such that y = mx + b

Finding lines in an image



Connection between image (x,y) and Hough (m,b) spaces

- A line in the image corresponds to a point in Hough space
- To go from image space to Hough space:
 - given a set of points (x,y), find all (m,b) such that y = mx + b
- What does a point (x₀, y₀) in the image space map to?
 - A: the solutions of $b = -x_0m + y_0$
 - this is a line in Hough space

Hough transform algorithm

Typically use a different parameterization

$$d = x cos\theta + y sin\theta$$

- d is the perpendicular distance from the line to the origin
- θ is the angle this perpendicular makes with the x axis
- Why?

Hough transform algorithm

Typically use a different parameterization

```
d = x cos\theta + y sin\theta
```

- d is the perpendicular distance from the line to the origin
- θ is the angle this perpendicular makes with the x axis
- · Why?

Basic Hough transform algorithm

- 1. Initialize H[d, θ]=0
- 2. for each edge point I[x,y] in the image

for
$$\theta = 0$$
 to 180
 $d = x\cos\theta + y\sin\theta$
 $H[d, \theta] += 1$

- 3. Find the value(s) of (d, $\theta)$ where H[d, $\theta]$ is maximum
- 4. The detected line in the image is given by $d = x\cos\theta + y\sin\theta$

What's the running time (measured in # votes)?

Hough line demo

Extensions

Extension 1: Use the image gradient

- 1. same
- 2. for each edge point I[x,y] in the image

compute unique (d, $\theta)$ based on image gradient at (x,y) H[d, $\theta]$ += 1

- 3. same
- 4. same

What's the running time measured in votes?

Extensions

Extension 1: Use the image gradient

- 1. same
- 2. for each edge point I[x,y] in the image

compute unique (d, $\boldsymbol{\theta})$ based on image gradient at (x,y)

 $H[d, \theta] += 1$

- 3. same
- same

What's the running time measured in votes?

Extension 2

give more votes for stronger edges

Extension 3

- change the sampling of (d, θ) to give more/less resolution

Extension 4

The same procedure can be used with circles, squares, or any other shape

Hough circle demo