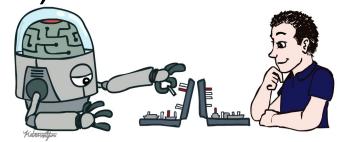
CSE 573: Artificial Intelligence

Hanna Hajishirzi

Search (Un-informed, Informed Search)



slides adapted from Dan Klein, Pieter Abbeel ai.berkeley.edu And Dan Weld, Luke Zettlemoyer

Announcements

PS1 Due April 15 Office hours:

- o Check the website
- o HW1 will be released soon.

Recap: Search

• Search problem:

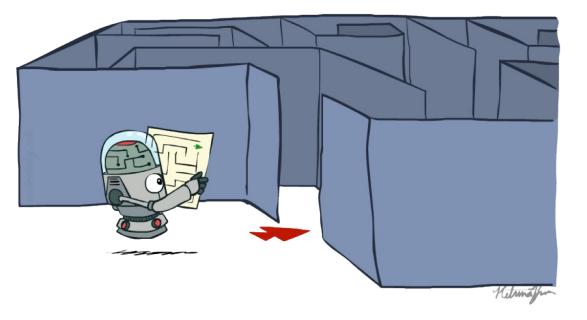
- States (configurations of the world)
- o Actions and costs
- o Successor function (world dynamics)
- o Start state and goal test

• Search tree:

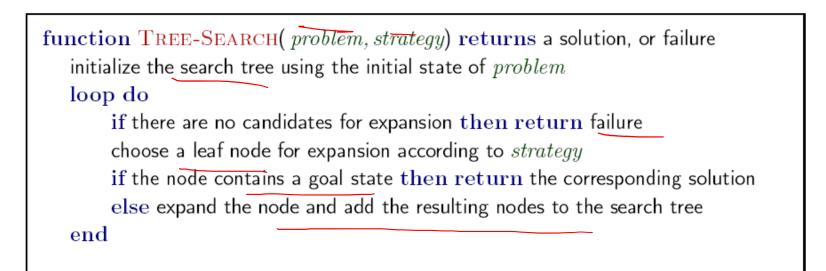
Nodes: represent plans for reaching states

• Search algorithm:

- o Systematically builds a search tree
- Chooses an ordering of the fringe (unexplored nodes)
- o Optimal: finds least-cost plans



General Tree Search



Uniform Cost Issues

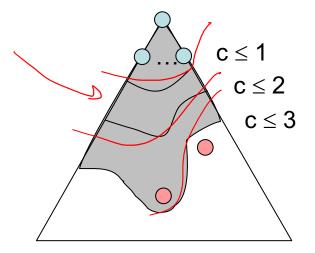
• Remember: UCS explores increasing cost contours

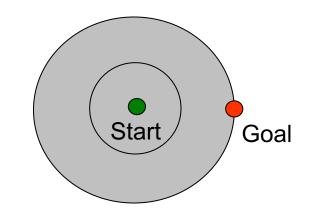
• The good: UCS is complete and optimal!

• The bad:

o Explores options in every "direction"o No information about goal location

• We'll fix that soon!





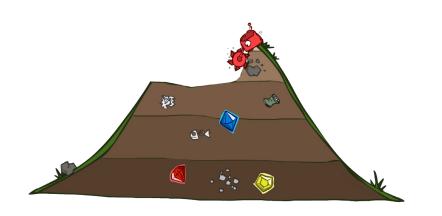
Up next: Informed Search

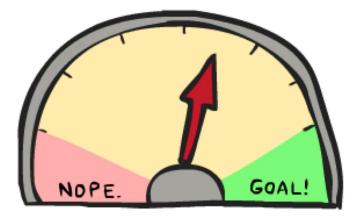
o Uninformed Search

- o DFS
- o BFS
- o UCS

Informed Search

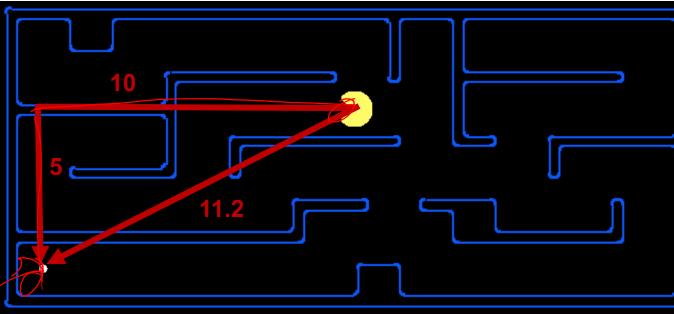
- Heuristics
- Greedy Search
- A* Search
- Graph Search/

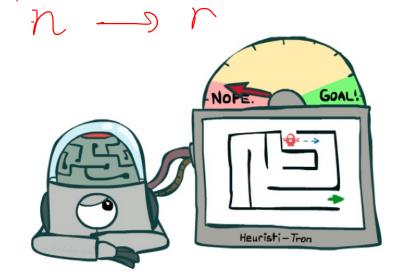


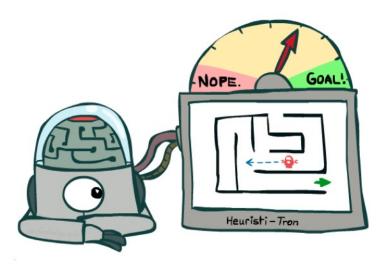


Search Heuristics

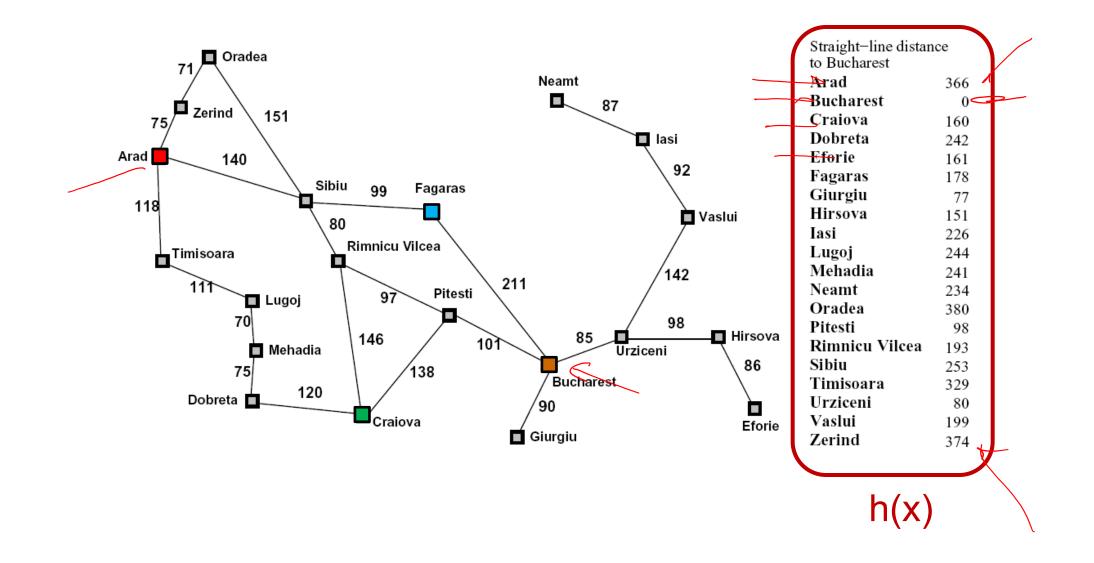
- A heuristic is:
 - A function that *estimates* how close a state is to a goal
 - Designed for a particular search problem
 - Pathing?
 - Examples: Manhattan distance, Euclidean distance for pathing





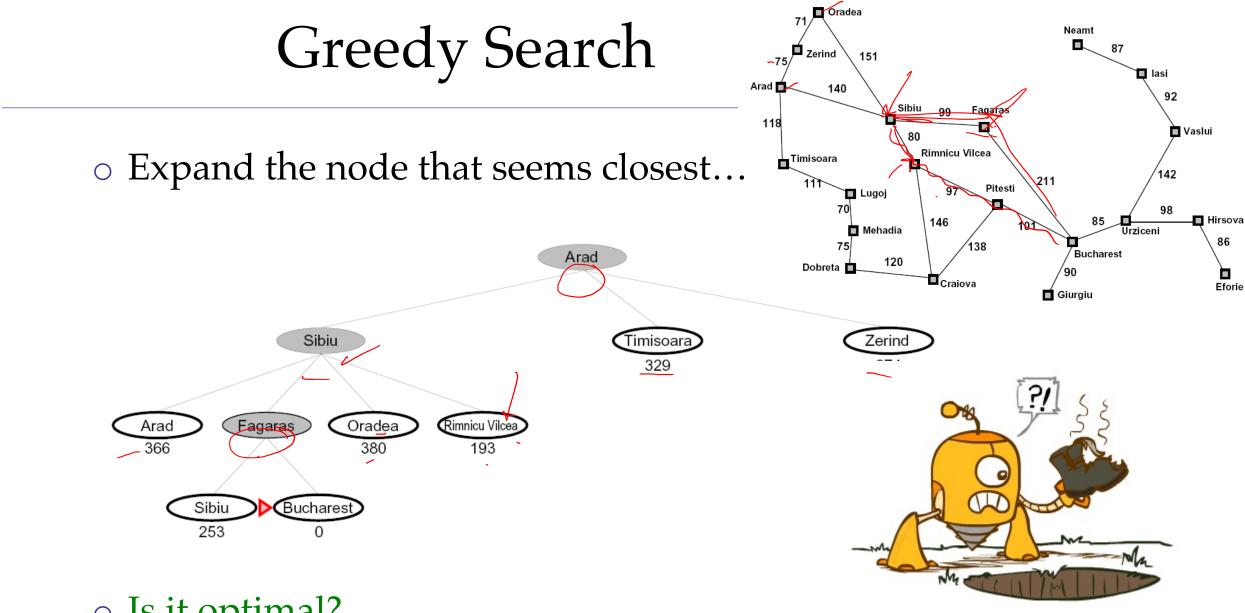


Example: Heuristic Function



Greedy Search





• Is it optimal?

o No. Resulting path to Bucharest is not the shortest!

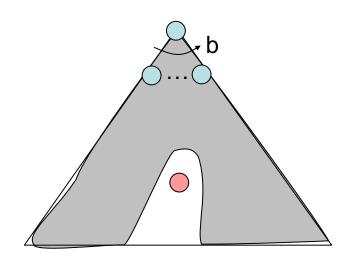
Greedy Search

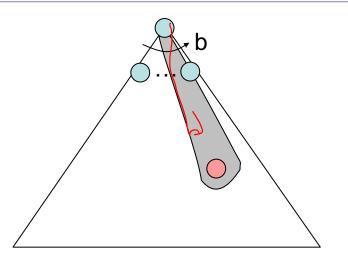
- Strategy: expand a node that you think is closest to a goal state
 - o Heuristic: estimate of distance to nearest goal for each state

• A common case:

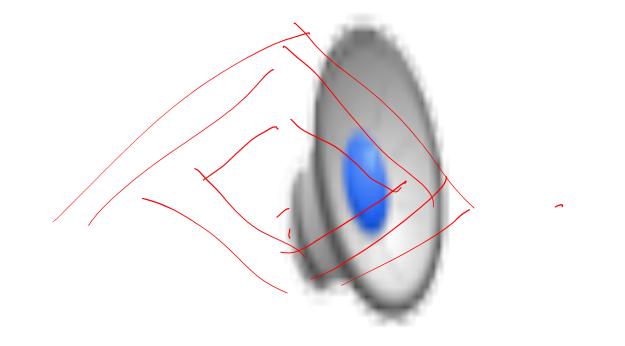
o Best-first takes you straight to the (wrong) goal

• Worst-case: like a badly-guided DFS

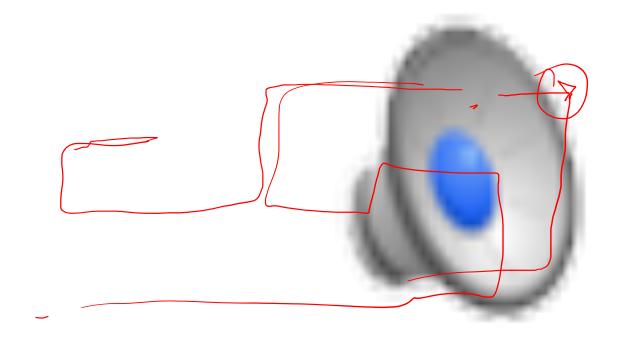




Video of Demo Contours Greedy (Empty)



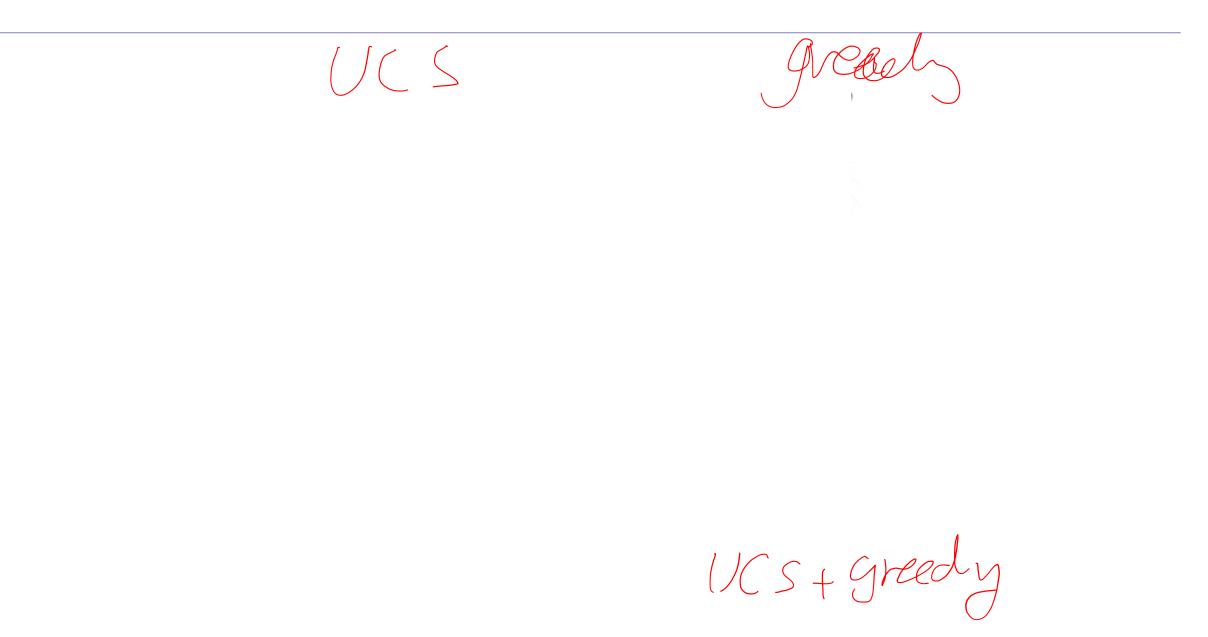
Video of Demo Contours Greedy (Pacman Small Maze)



A* Search

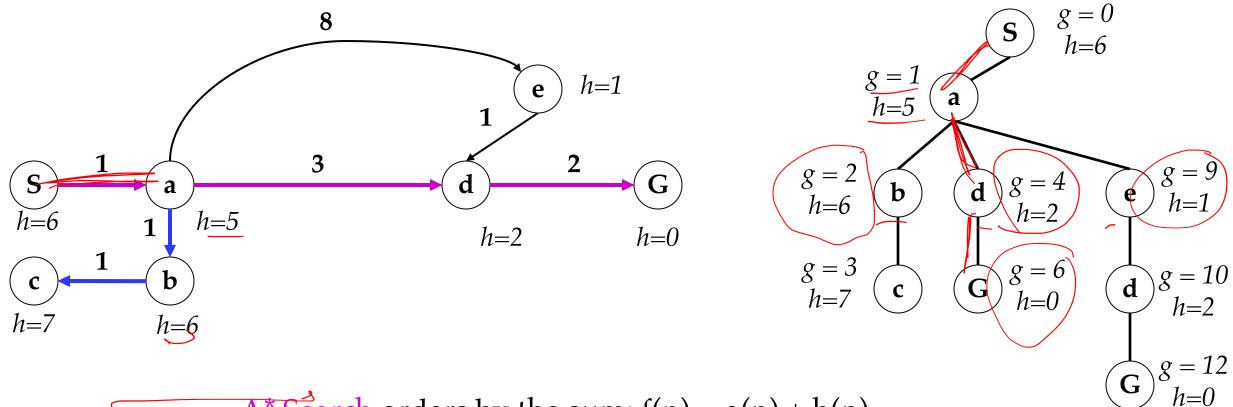


A* Search



Combining UCS and Greedy

Uniform-cost orders by path cost, or *backward cost* g(n)
Greedy orders by goal proximity, or *forward cost* h(n)

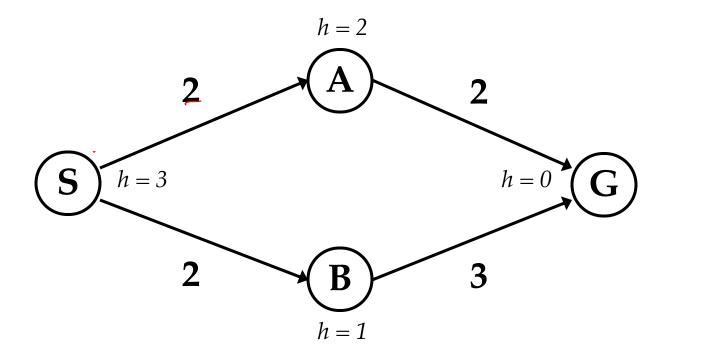


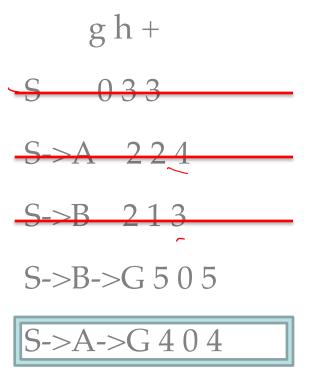
• A* Search orders by the sum: f(n) = g(n) + h(n)

Example: Teg Grenager

When should A* terminate?

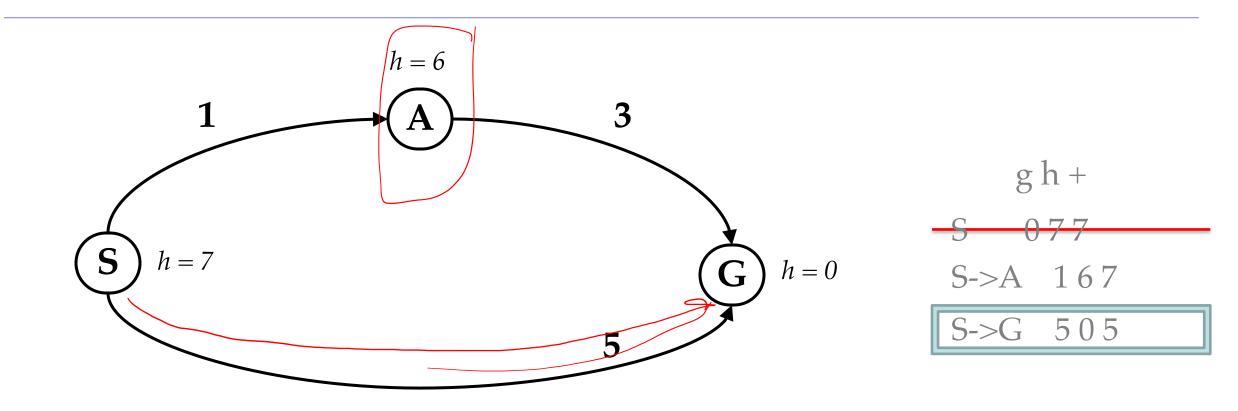
• Should we stop when we enqueue a goal?





• No: only stop when we dequeue a goal

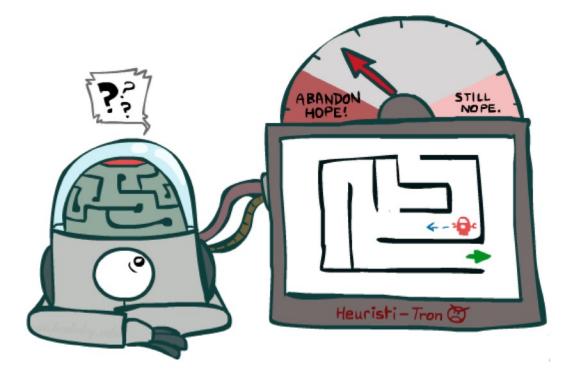
Is A* Optimal?



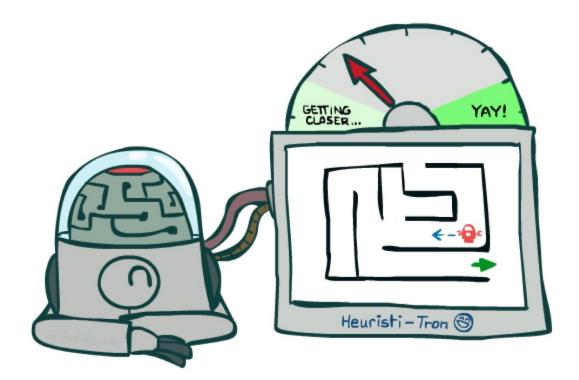
• What went wrong?

- Actual bad goal cost < estimated good goal cost
- We need estimates to be less than actual costs!

Idea: Admissibility

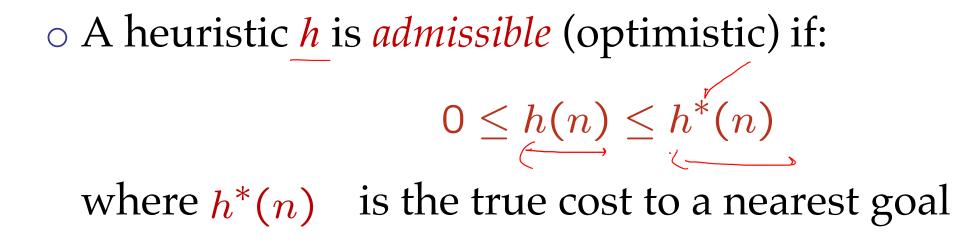


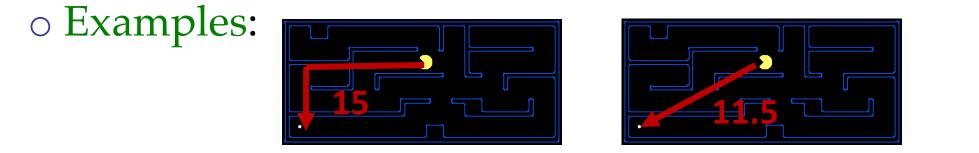
Inadmissible (pessimistic) heuristics break optimality by trapping good plans on the fringe



Admissible (optimistic) heuristics slow down bad plans but onever outweigh true costs

Admissible Heuristics





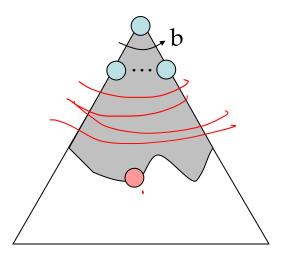
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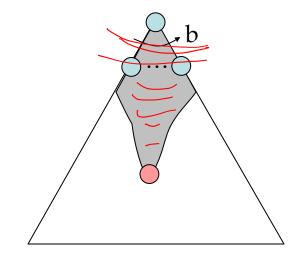
 Coming up with admissible heuristics is most of what's involved in using A* in practice.

Properties of A*

Uniform-Cost



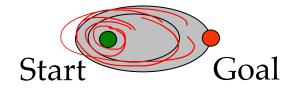


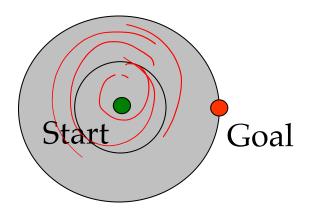


UCS vs A* Contours

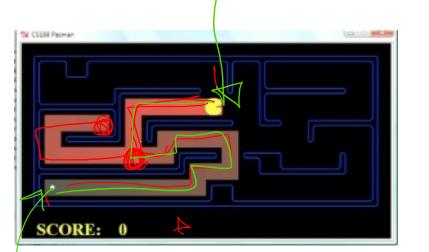
Uniform-cost expands equally in all "directions"

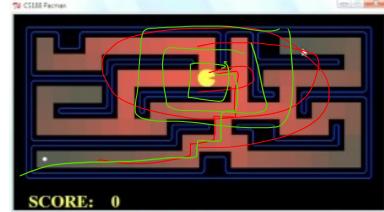
 A* expands mainly toward the goal, but does hedge its bets to ensure optimality

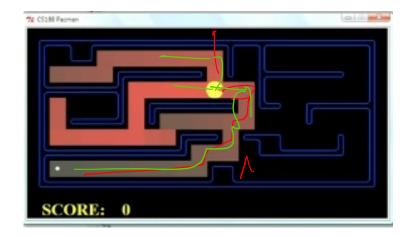




Comparison







Greedy

Uniform Cost

A*

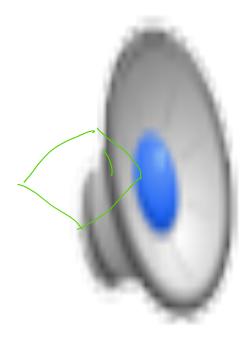
Video of Demo Contours (Empty) -- UCS



Video of Demo Contours (Empty) -- Greedy



Video of Demo Contours (Empty) – A*



A*: Summary



A*: Summary

- A* uses both backward costs and (estimates of) forward costs
- A* is optimal with admissible (optimistic) heuristics
- Heuristic design is key: often use relaxed problems



Video of Demo Empty Water Shallow / Deep – Guess Algorithm

ydev - Eclipse		
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Number of Facman eme	15	
<terminated>1 Total cost Number of Number of Facman eme</terminated>	15 t: 27 nodes expanded: 182 unique nodes expanded: 182 erges victorious! Score: 573	

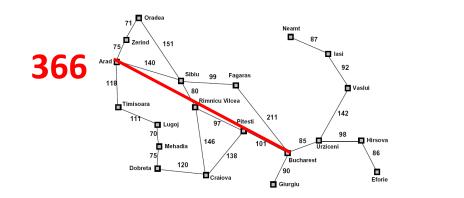
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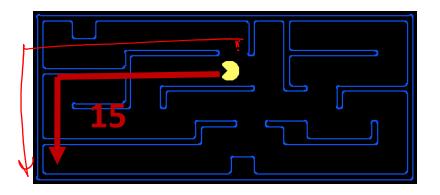
Creating Heuristics



Creating Admissible Heuristics

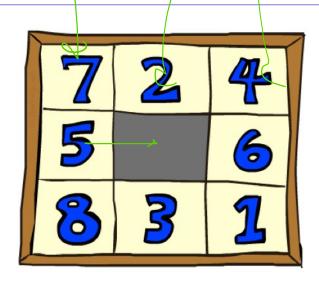
- Most of the work in solving hard search problems optimally is in coming up with admissible heuristics
- Often, admissible heuristics are solutions to *relaxed problems*, where new actions are available



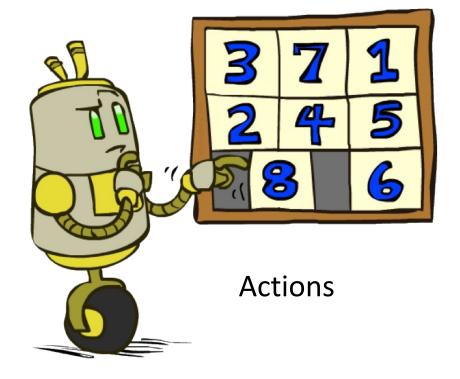


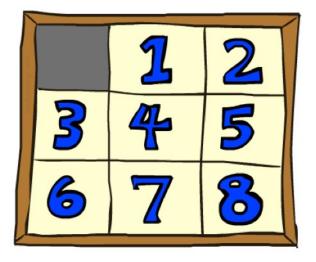
• Inadmissible heuristics are often useful too

Example: 8 Puzzle



Start State





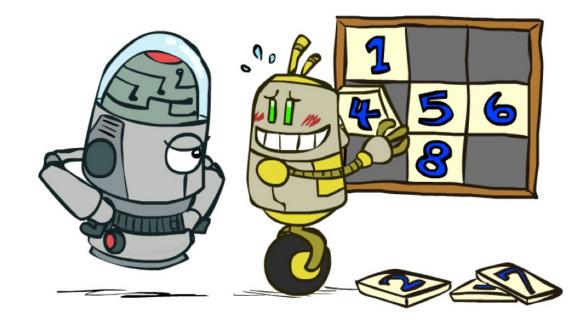
Goal State

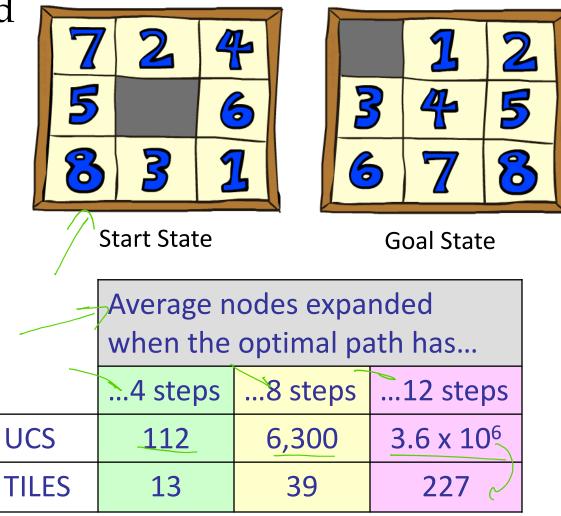
- What are the states?
- How many states?
- What are the actions?
- How many successors from the start state?
- What should the costs be?

Admissible heuristics?

8 Puzzle I

- Heuristic: Number of tiles misplaced
 Why is it admissible?
 h(start) =8
- This is a *relaxed-problem* heuristic

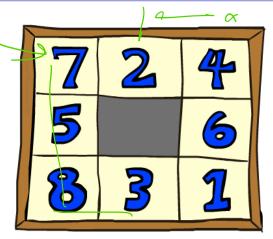




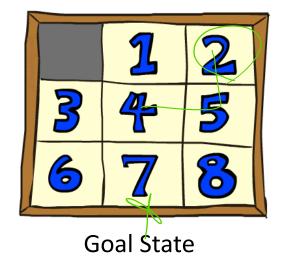
Statistics from Andrew Moore

8 Puzzle II

- What if we had an easier 8-puzzle where any tile could slide any direction at any time, ignoring other tiles?
- Total *Manhattan* distance
- Why is it admissible?
- \circ h(start) = 3 + 1 + 2 + ... = 18



Start State



Average nodes expanded when the optimal path has		
4 steps	8 steps	12 steps
} 13	39	227 🛩
12	25	73
	when the 4 steps ⁷ 13	when the optimal pa 4 steps8 steps γ 13 39

8 Puzzle III

• How about using the *actual cost* as a heuristic?

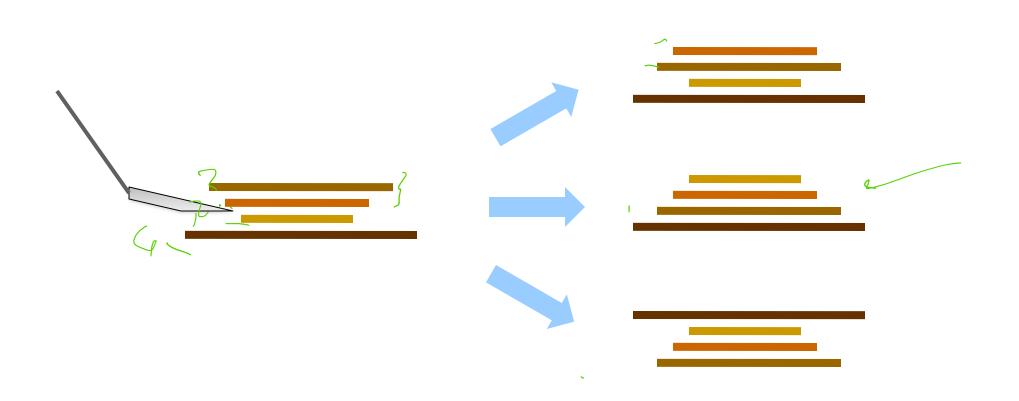
- Would it be admissible?
- o Would we save on nodes expanded?
- o What's wrong with it?



• With A*: a trade-off between quality of estimate and work per node

• As heuristics get closer to the true cost, you will expand fewer nodes but usually do more work per node to compute the heuristic itself

Example: Pancake Problem



Cost: Number of pancakes flipped

Example: Pancake Problem

BOUNDS FOR SORTING BY PREFIX REVERSAL

William H. GATES

Microsoft, Albuquerque, New Mexico

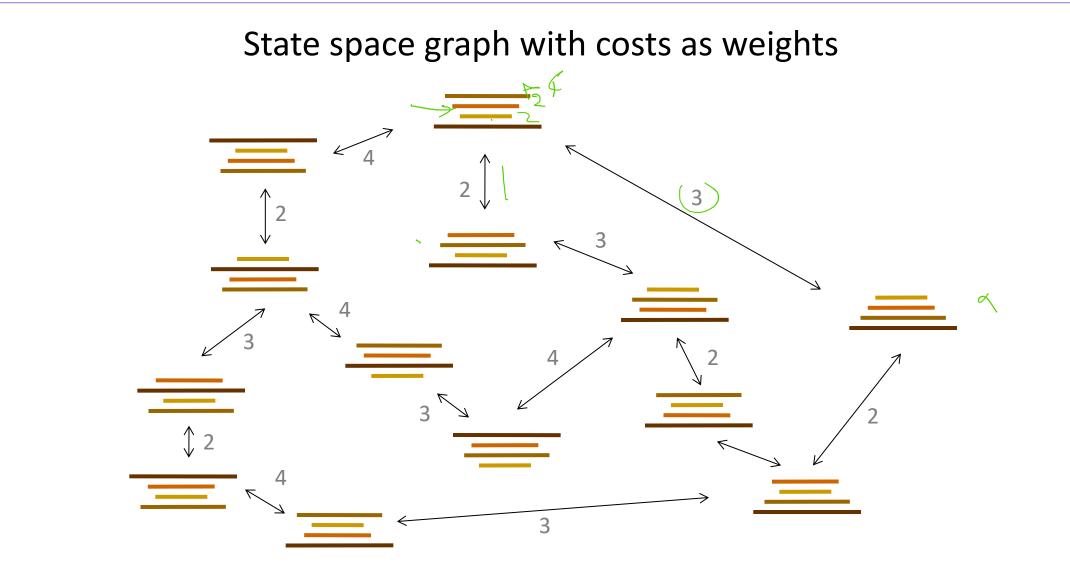
Christos H. PAPADIMITRIOU*†

Department of Electrical Engineering, University of California, Berkeley, CA 94720, U.S.A.

Received 18 January 1978 Revised 28 August 1978

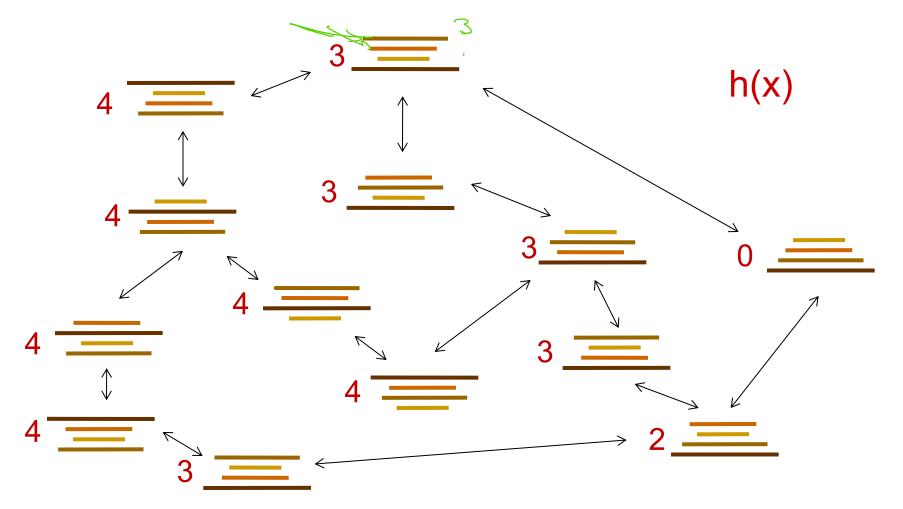
For a permutation σ of the integers from 1 to *n*, let $f(\sigma)$ be the smallest number of prefix reversals that will transform σ to the identity permutation, and let f(n) be the largest such $f(\sigma)$ for all σ in (the symmetric group) S_n . We show that $f(n) \leq (5n+5)/3$, and that $f(n) \geq 17n/16$ for *n* a multiple of 16. If, furthermore, each integer is required to participate in an even number of reversed prefixes, the corresponding function g(n) is shown to obey $3n/2 - 1 \leq g(n) \leq 2n + 3$.

Example: Pancake Problem



Example: Heuristic Function

Heuristic: the number of the largest pancake that is still out of place



Semi-Lattice of Heuristics

Trivial Heuristics, Dominance

• Dominance: $h_a \ge h_c$ if

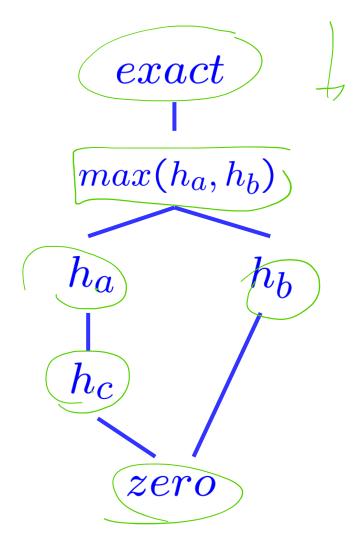
 $\forall n : h_a(n) \ge h_c(n)$

• Heuristics form a semi-lattice:

o Max of admissible heuristics is admissible

 $\underbrace{h(n)}_{\smile} = \max(\underset{\smile}{h_a(n)}, \underset{\smile}{h_b(n)})$

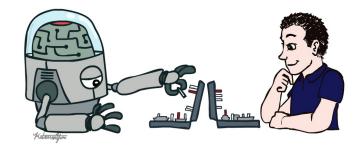
- Trivial heuristics
 - Bottom of lattice is the zero heuristic (what does this give us?)
 - Top of lattice is the exact heuristic



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Search (Informed Search)



slides adapted from Dan Klein, Pieter Abbeel ai.berkeley.edu And Dan Weld, Luke Zettlemoyer

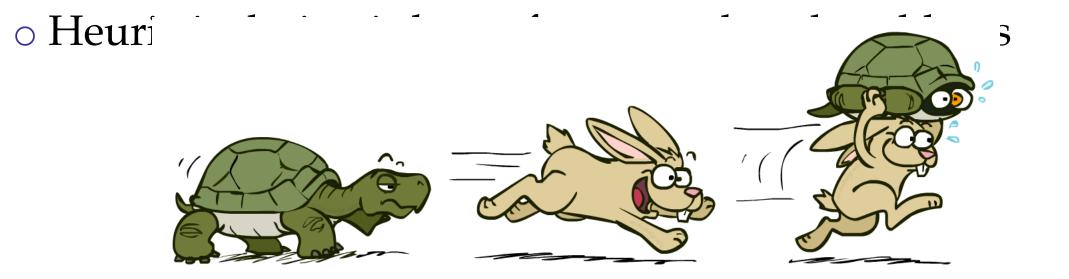
Announcements

o PS1

- o April 15
- o HW1 will be released today
 - o April 22
- Guest lectures next two weeks, still will follow the schedule
 Today: A* (continued) + Games (Adversarial search)
 Next week: Adversarial search (Continued) + Expectimax
- Next next week: Markov Decision Processes

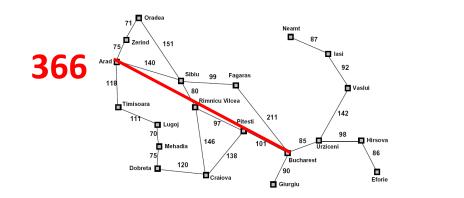
A*: Summary

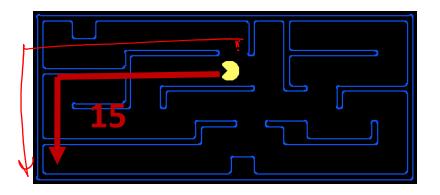
Still looking at search problems A* uses both backward costs and (estimates of) forward costs A* is optimal with admissible (optimistic) heuristics



Creating Admissible Heuristics

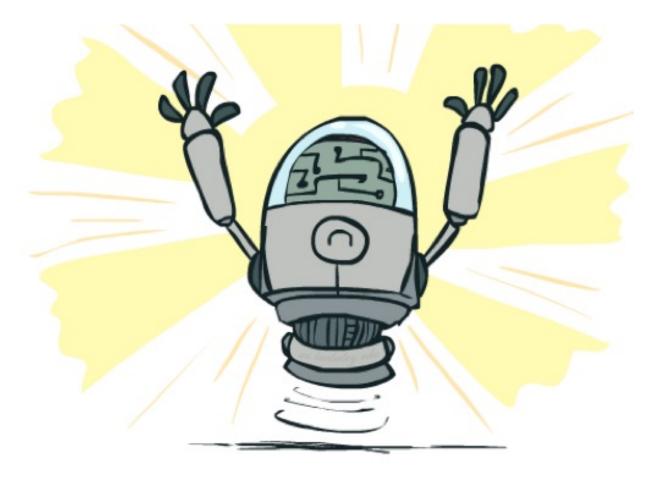
- Most of the work in solving hard search problems optimally is in coming up with admissible heuristics
- Often, admissible heuristics are solutions to *relaxed problems*, where new actions are available





• Inadmissible heuristics are often useful too

Optimality of A* Tree Search



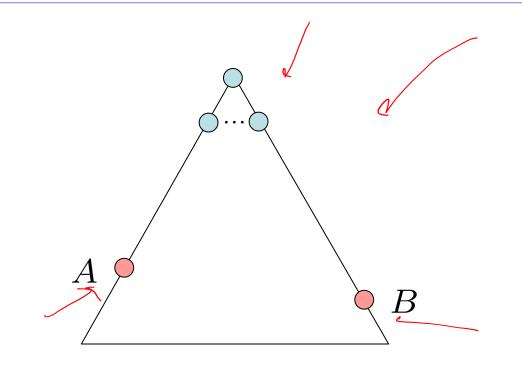
Optimality of A* Tree Search

Assume:

A is an optimal goal node
B is a suboptimal goal node
h is admissible

Claim:

• A will exit the fringe before B



Optimality of A* Tree Search: Blocking

Proof:

- Imagine B is on the fringe
- Some ancestor *n* of A is on the fringe, too (maybe A!)
- Claim: *n* will be expanded before B
 - 1. f(n) is less or equal to f(A)

f(n) = g(n) + h(n) $f(n) \le g(A)$ g(A) = f(A)

Definition of f-cost Admissibility of h h = 0 at a goal

B

Optimality of A* Tree Search: Blocking

n

g(A) < g(B)

f(A) < f(B)

B

B is suboptimal

h = 0 at a goal

Proof:

- Imagine B is on the fringe
- Some ancestor *n* of A is on the fringe, too (maybe A!)
- Claim: *n* will be expanded before B
 - 1. f(n) is less or equal to f(A)
 - 2. f(A) is less than f(B)

Optimality of A* Tree Search: Blocking

n

 $f(n) \leq f(A)$

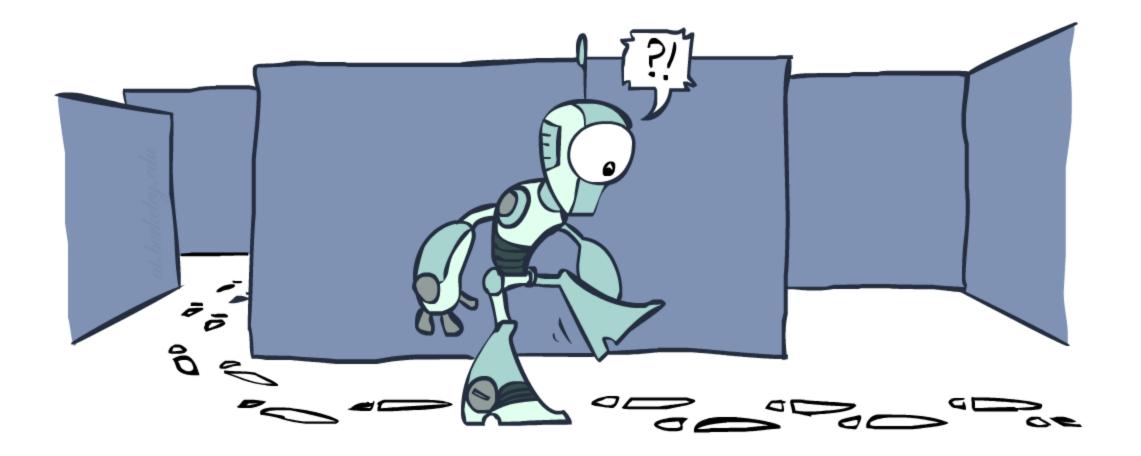
B

A

Proof:

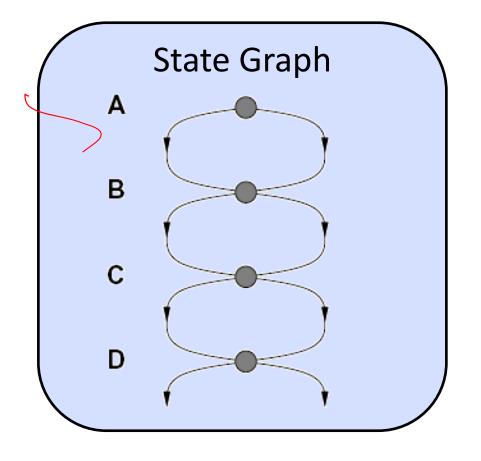
- Imagine B is on the fringe
- Some ancestor *n* of A is on the fringe, too (maybe A!)
- Claim: *n* will be expanded before B
 - 1. f(n) is less or equal to f(A)
 - 2. f(A) is less than f(B)
 - 3. *n* expands before B
- All ancestors of A expand before B
- A expands before B
- A* search is optimal (admisible

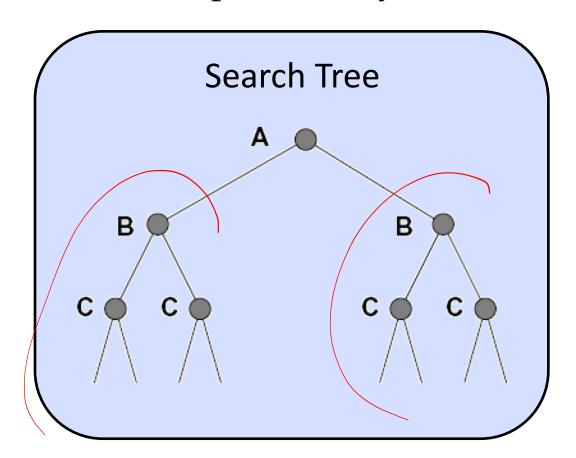
Graph Search



Tree Search: Extra Work!

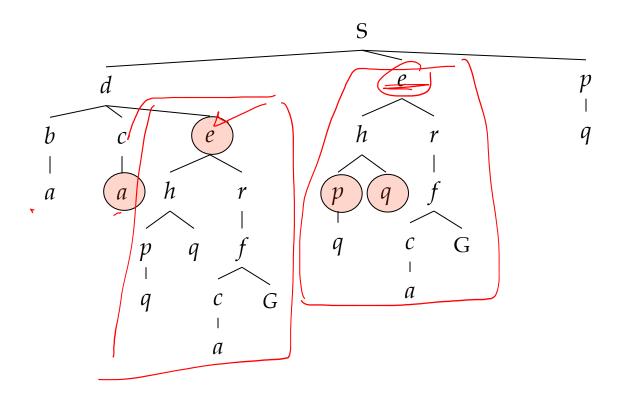
• Failure to detect repeated states can cause exponentially more work.





Graph Search

 In BFS, for example, we shouldn't bother expanding the circled nodes (why?)



Graph Search optiel

• Idea: never expand a state twice

• How to implement:



- Tree search + set of expanded states ("closed set")
- Expand the search tree node-by-node, but...
- Before expanding a node, check to make sure its state has never been expanded before

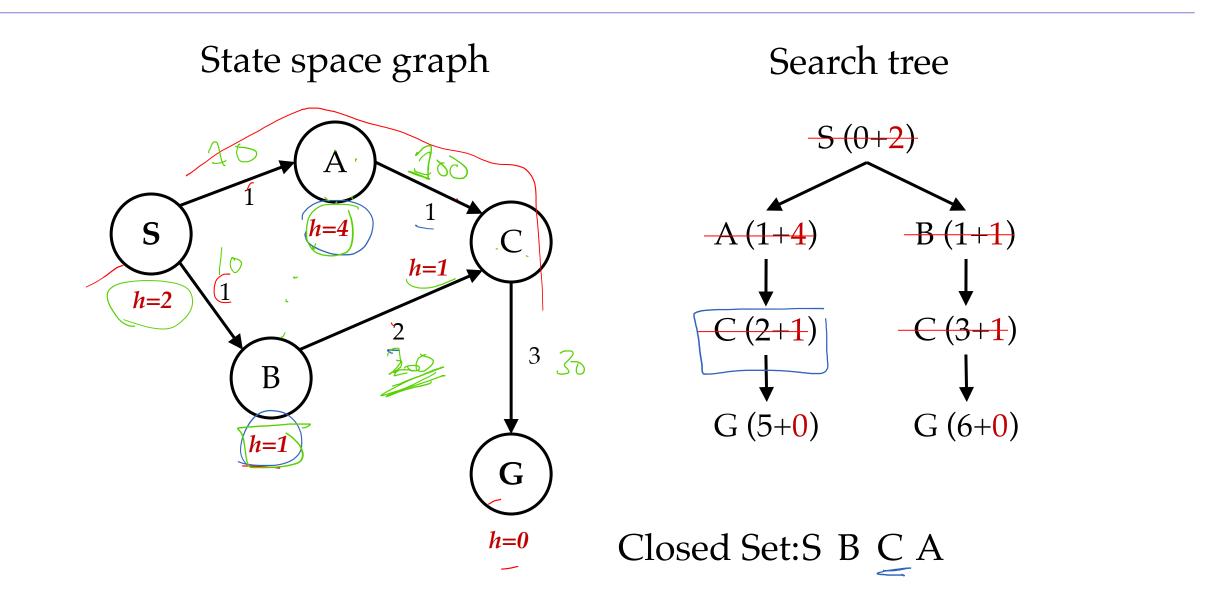
• If not new, skip it, if new add to closed set

• Important: store the closed set as a set, not a list

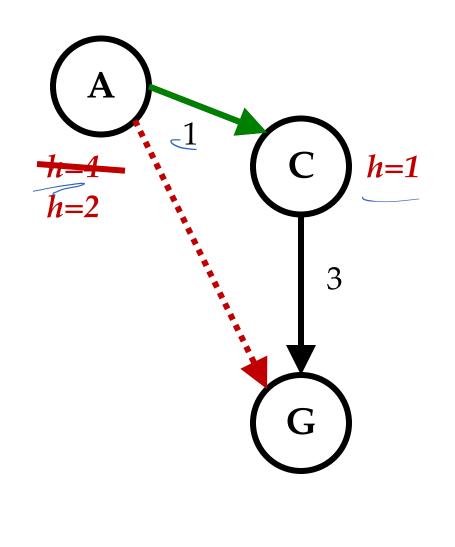
• Can graph search wreck completeness? Why/why not?

• How about optimality?

A* Graph Search Gone Wrong?



Consistency of Heuristics



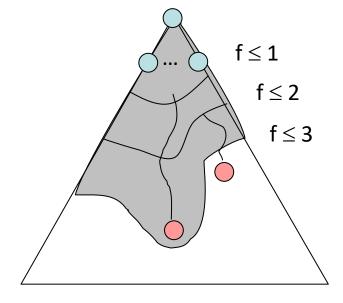
- Main idea: estimated heuristic costs ≤ actual costs
 Admissibility: heuristic cost ≤ actual cost to goal
 h(A) ≤ actual cost from A to G
 Consistency: heuristic "arc" cost ≤ actual cost for each arc
 - $h(A) h(C) \le cost(A \text{ to } C)$
- Consequences of consistency:
 - The f value along a path never decreases

→ $h(A) \le cost(A \text{ to } C) + h(C)$ → A^* graph search is optimal

A* Graph Search

- Sketch: consider what A* does with a consistent heuristic:
 - Fact 1: In tree search, A* expands nodes in increasing total f value (f-contours)
 - Fact 2: For every state s, nodes that reach s optimally are expanded before nodes that reach s suboptimally

• Result: A* graph search is optimal



Optimality of A* Search

With a admissible heuristic, Tree A* is optimal.
With a consistent heuristic, Graph A* is optimal.
With h=0, the same proof shows that UCS is optimal.

Pseudo-Code

```
 \begin{array}{l} \textbf{function Tree-Search}(problem, fringe) return a solution, or failure \\ fringe \leftarrow INSERT(MAKE-NODE(INITIAL-STATE[problem]), fringe) \\ \textbf{loop do} \\ \textbf{if } fringe \text{ is empty then return failure} \\ node \leftarrow REMOVE-FRONT(fringe) \\ \textbf{if } GOAL-TEST(problem, STATE[node]) \textbf{ then return } node \\ \textbf{for } child-node \text{ in } EXPAND(STATE[node], problem) \textbf{ do} \\ fringe \leftarrow INSERT(child-node, fringe) \\ \textbf{end} \\ \textbf{end} \end{array}
```

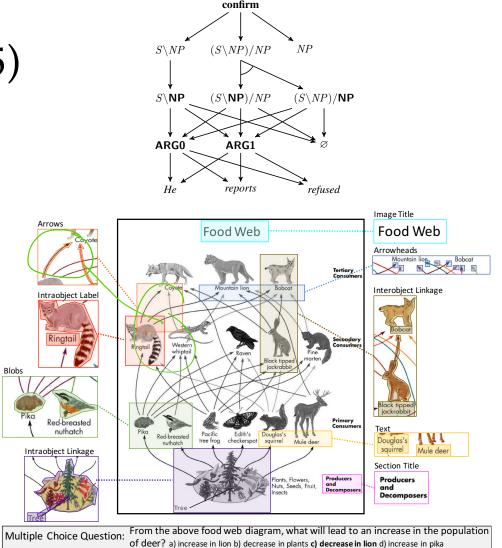
A* Applications

• Video games • Pathing / routing problems • Resource planning problems • Robot motion planning • Language analysis • Machine translation • Speech recognition

0 ...

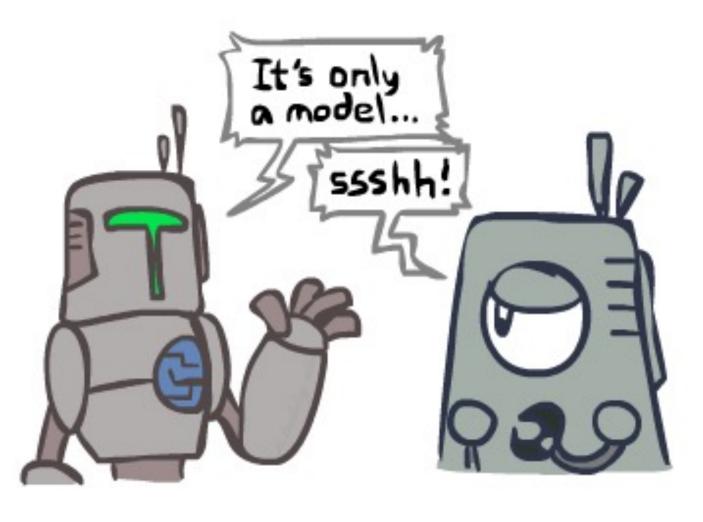
A* in Recent Literature

• Joint A* CCG Parsing and Semantic Role Labeling (EMLN'15) Arrows • Diagram Understanding (ECCV'17) Intraobiect Labe Blobs Pika Red-breasted nuthatch



Search and Models

- Search operates over models of the world
 - The agent doesn't actually try all the plans out in the real world!
 - Planning is all "in simulation"
 - Your search is only as good as your models...



Search Gone Wrong?

