CSE 573: Introduction to Artificial Intelligence

Hanna Hajishirzi Search (Un-informed, Informed Search)

slides adapted from Dan Klein, Pieter Abbeel ai.berkeley.edu And Dan Weld, Luke Zettelmoyer

Recap: Search

• Search problem:

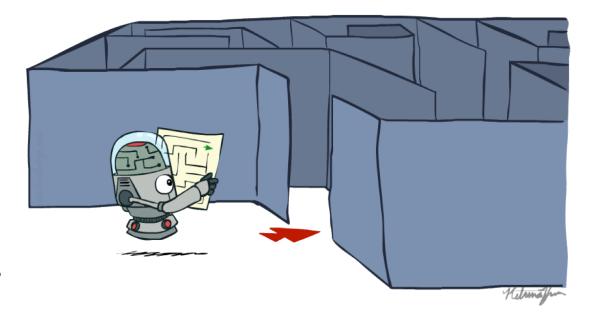
- States (configurations of the world)
- Actions and costs
- Successor function (world dynamics)
- Start state and goal test

• Search tree:

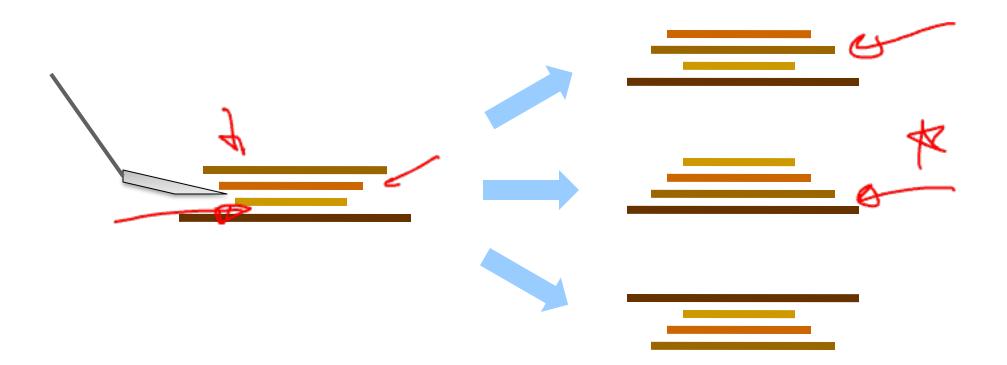
• Nodes: represent plans for reaching states

• Search algorithm:

- Systematically builds a search tree
- Chooses an ordering of the fringe (unexplored nodes)
- Optimal: finds least-cost plans



Example: Pancake Problem



Cost: Number of pancakes flipped

Example: Pancake Problem

BOUNDS FOR SORTING BY PREFIX REVERSAL

William H. GATES

Microsoft, Albuquerque, New Mexico

Christos H. PAPADIMITRIOU*†

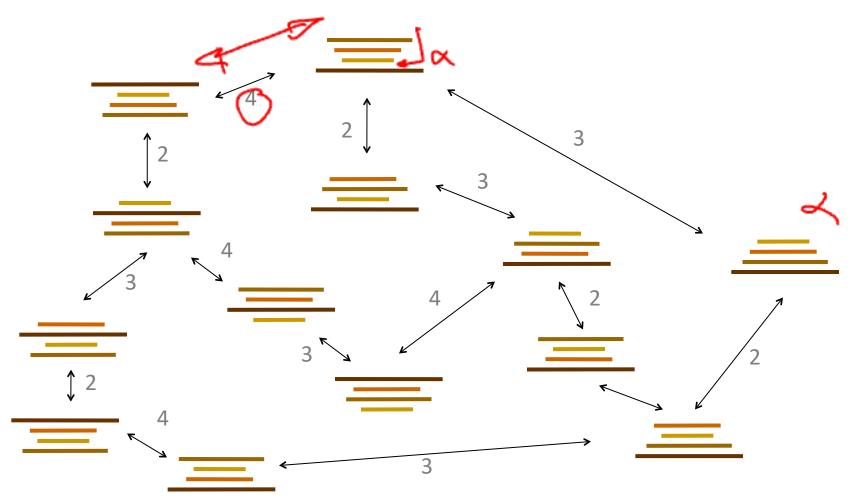
Department of Electrical Engineering, University of California, Berkeley, CA 94720, U.S.A.

Received 18 January 1978 Revised 28 August 1978

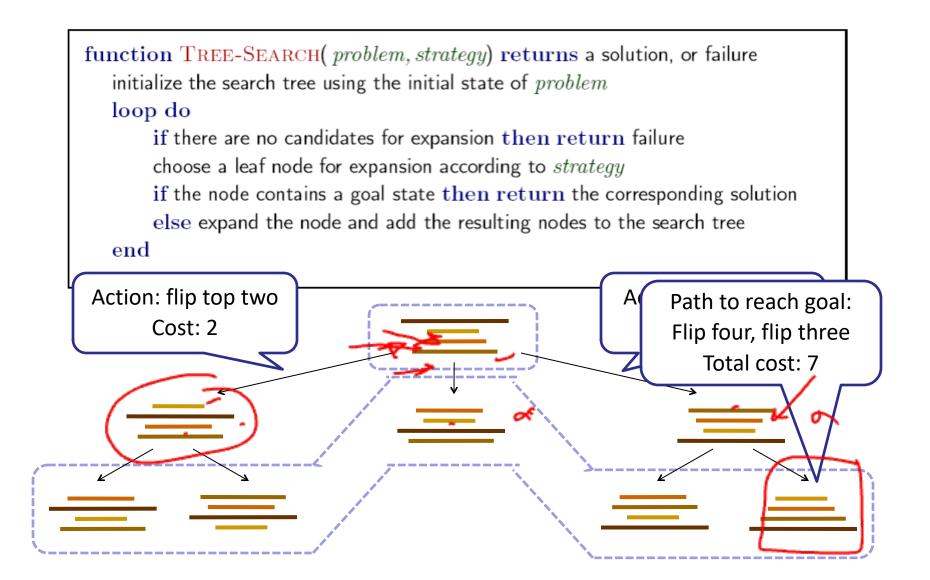
For a permutation σ of the integers from 1 to *n*, let $f(\sigma)$ be the smallest number of prefix reversals that will transform σ to the identity permutation, and let f(n) be the largest such $f(\sigma)$ for all σ in (the symmetric group) S_n . We show that $f(n) \leq (5n+5)/3$, and that $f(n) \geq 17n/16$ for *n* a multiple of 16. If, furthermore, each integer is required to participate in an even number of reversed prefixes, the corresponding function g(n) is shown to obey $3n/2 - 1 \leq g(n) \leq 2n + 3$.

Example: Pancake Problem

State space graph with costs as weights



General Tree Search



Uniform Cost Issues

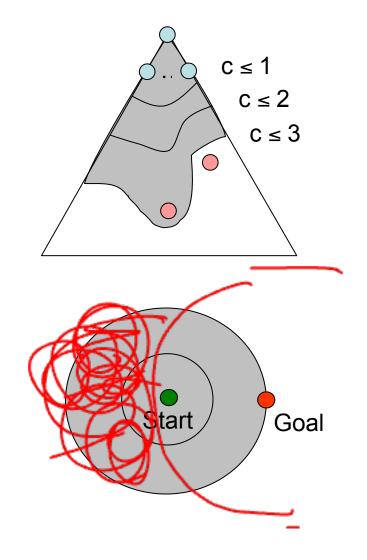
• Remember: UCS explores increasing cost contours

• The good: UCS is complete and optimal!

The bad:
 • Explores options in every "direction"

• No information about goal location

• We'll fix that soon!



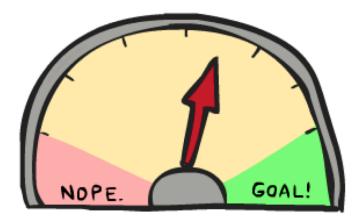
Up next: Informed Search

• Uninformed Search

- DFS
- BFS
- o UCS

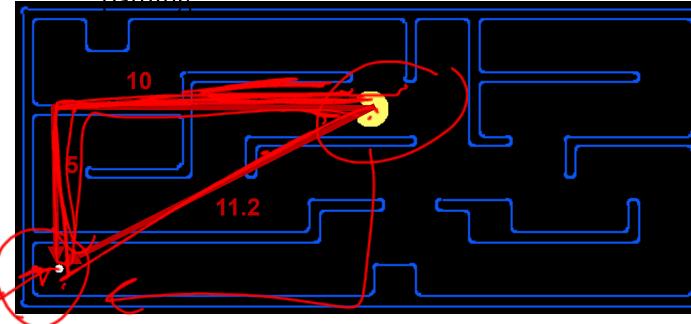
Informed Search

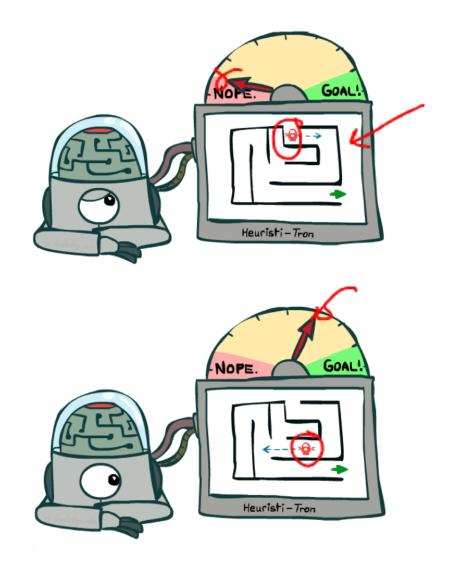
- Heuristics
- Greedy Search
- A* Search
- Graph Search



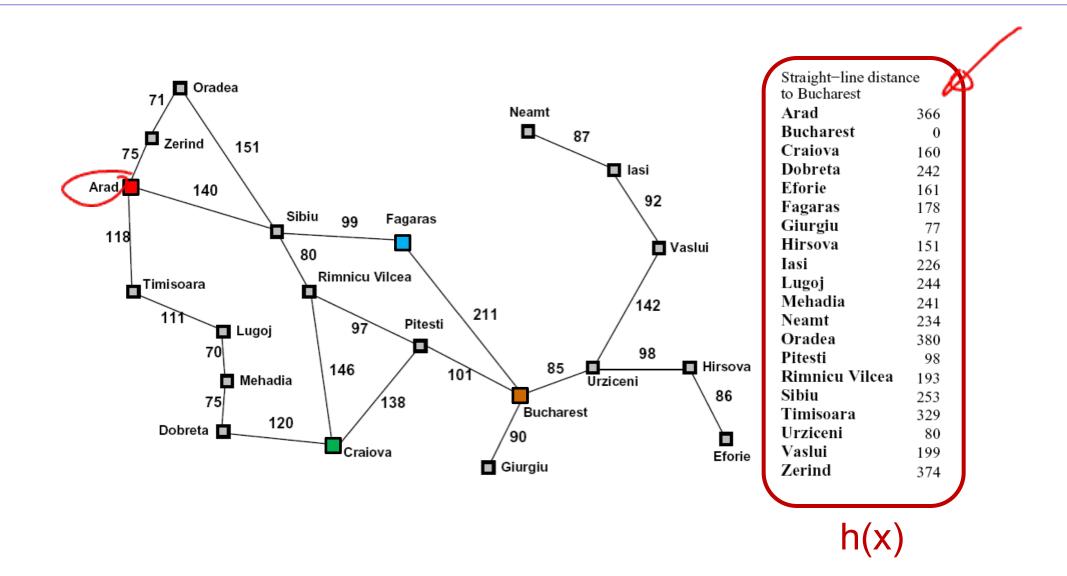
Search Heuristics

- A heuristic is:
 - A function that *estimates* how close a state is to a goal
 - Designed for a particular search problem
 - Pathing?
 - Examples: Manhattan distance, Euclidean distance for pathing



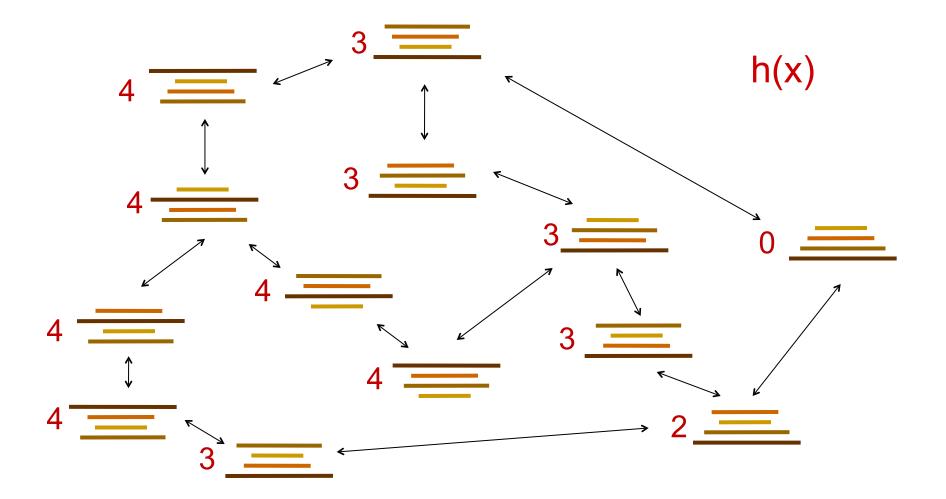


Example: Heuristic Function



Example: Heuristic Function

Heuristic: the number of the largest pancake that is still out of place



CSE 573: Introduction to Artificial Intelligence

Hanna Hajishirzi Search (Un-informed, Informed Search)

slides adapted from Dan Klein, Pieter Abbeel ai.berkeley.edu And Dan Weld, Luke Zettelmoyer

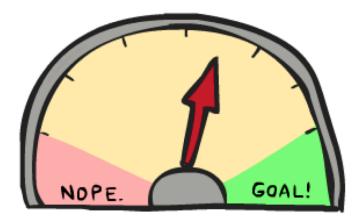
Up next: Informed Search

• Uninformed Search

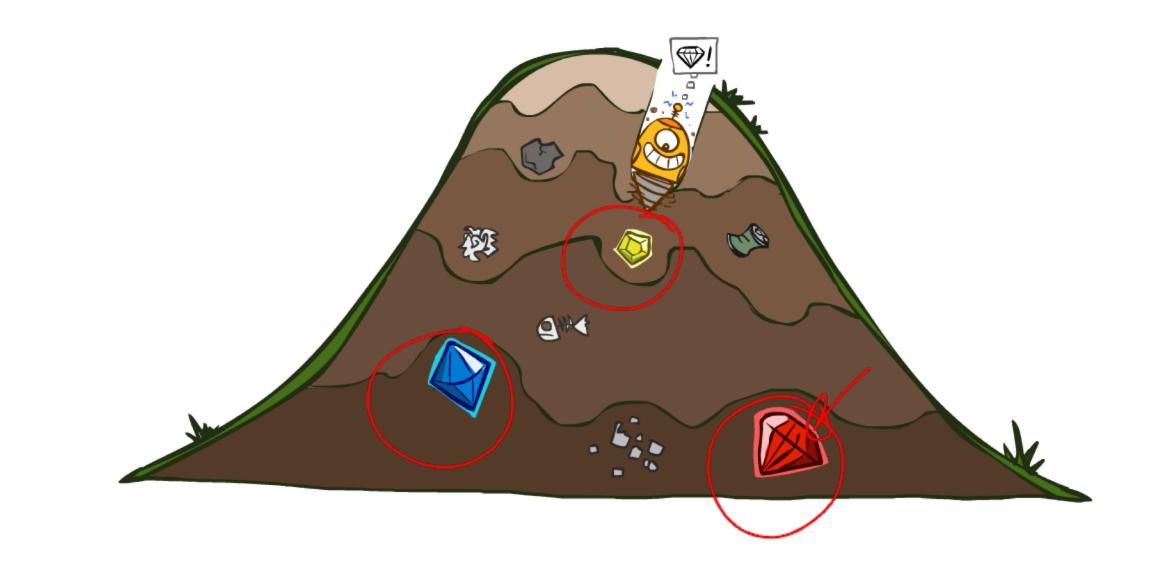
- DFS
- BFS
- o UCS

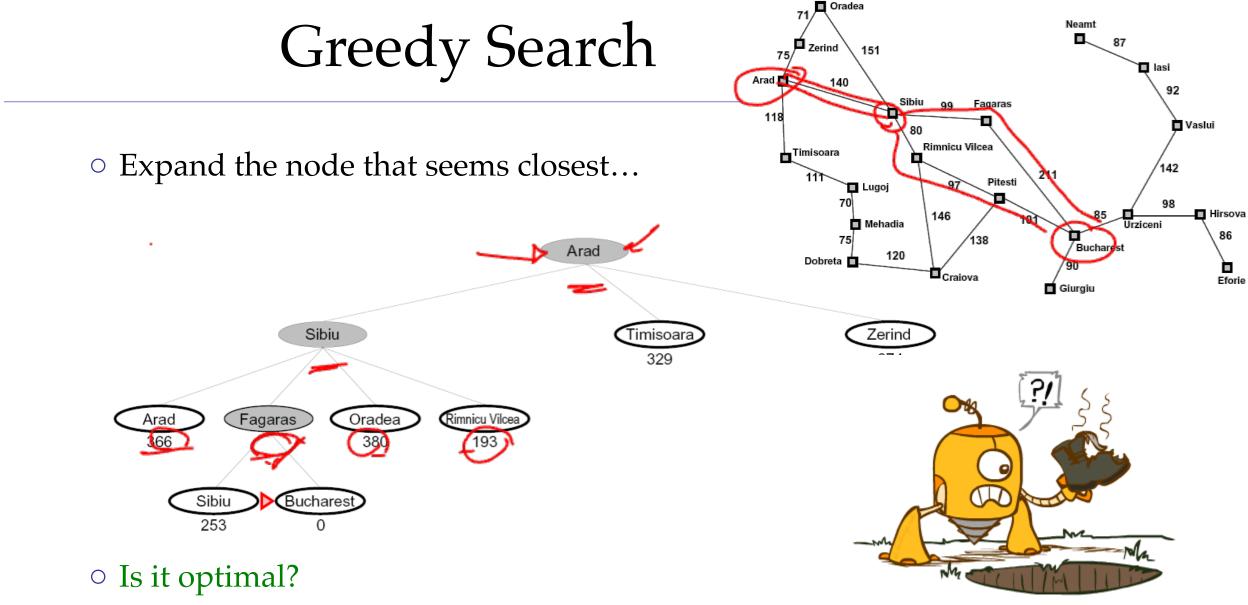
Informed Search

- Heuristics
- Greedy Search
- A* Search
- Graph Search



Greedy Search





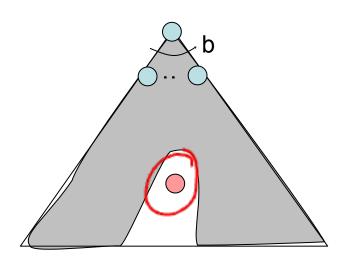
• No. Resulting path to Bucharest is not the shortest!

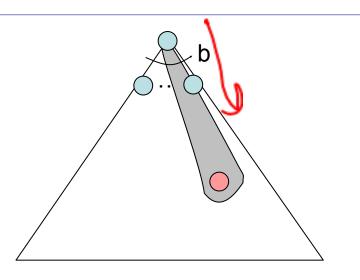
Greedy Search

- Strategy: expand a node that you think is closest to a goal state
 - Heuristic: estimate of distance to nearest goal for each state

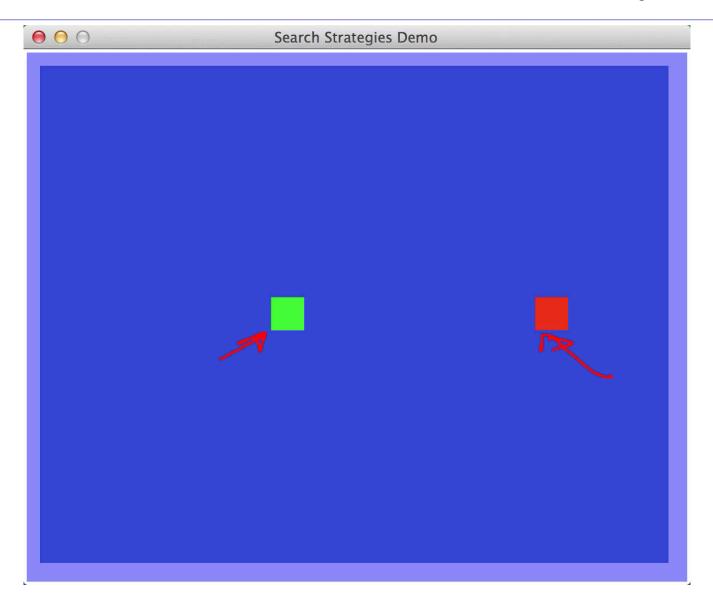


• Worst-case: like a badly-guided DFS

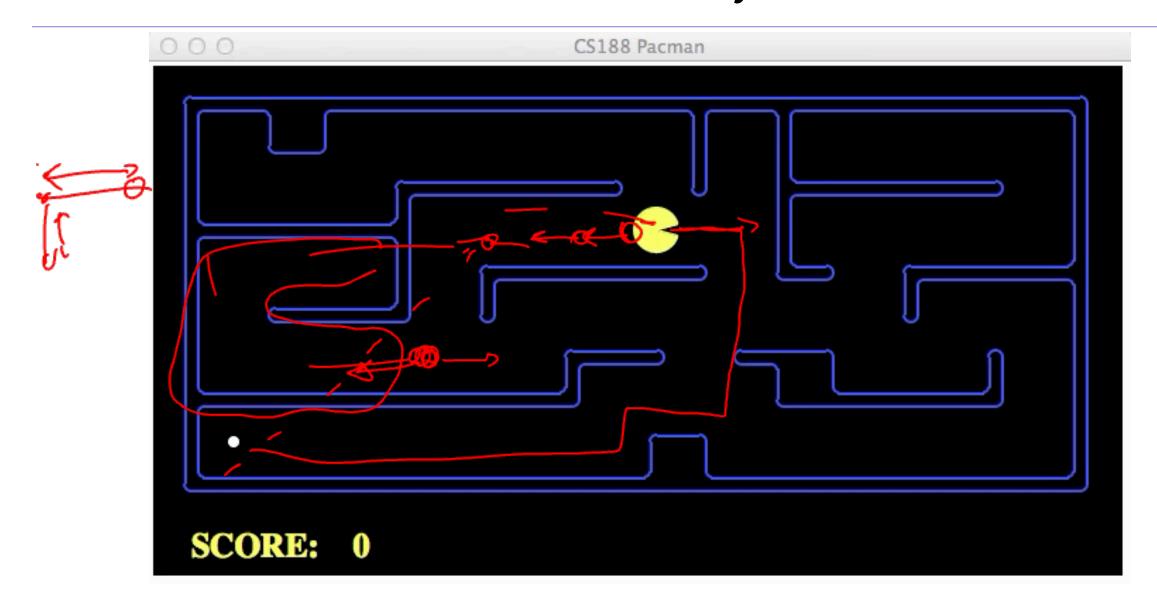




Video of Demo Contours Greedy (Empty)



Video of Demo Contours Greedy (Pacman Small Maze)

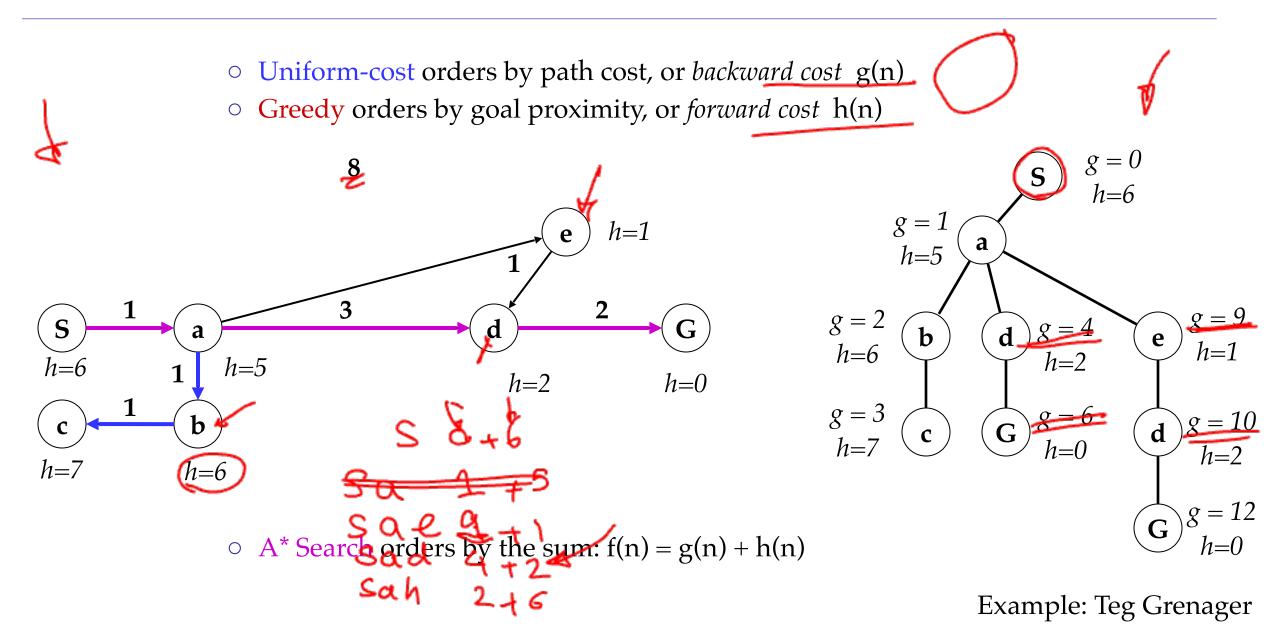


A* Search

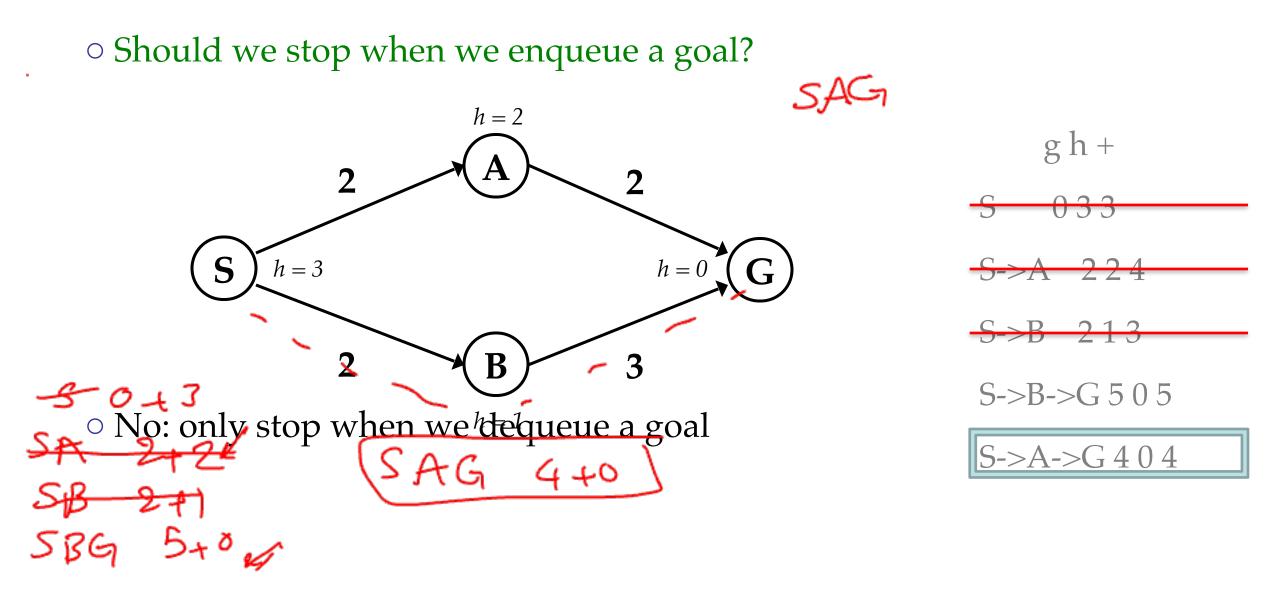


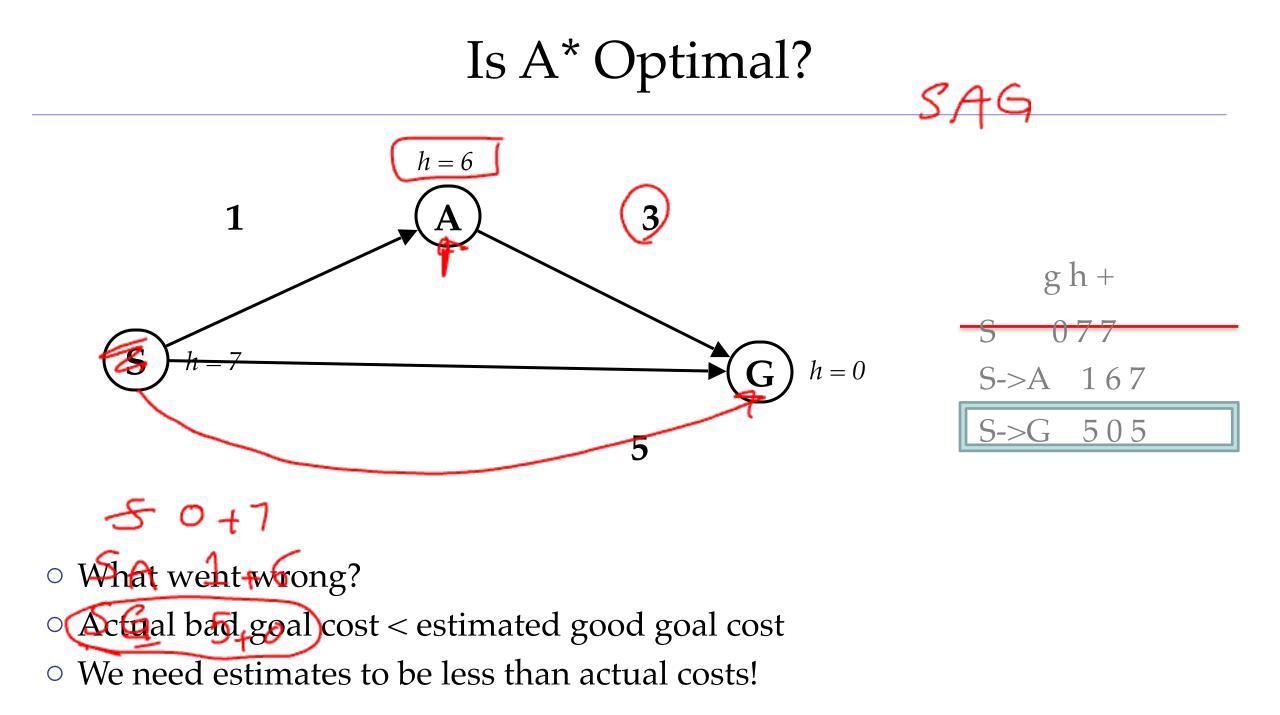
UCS Greedy A* Search - UCS

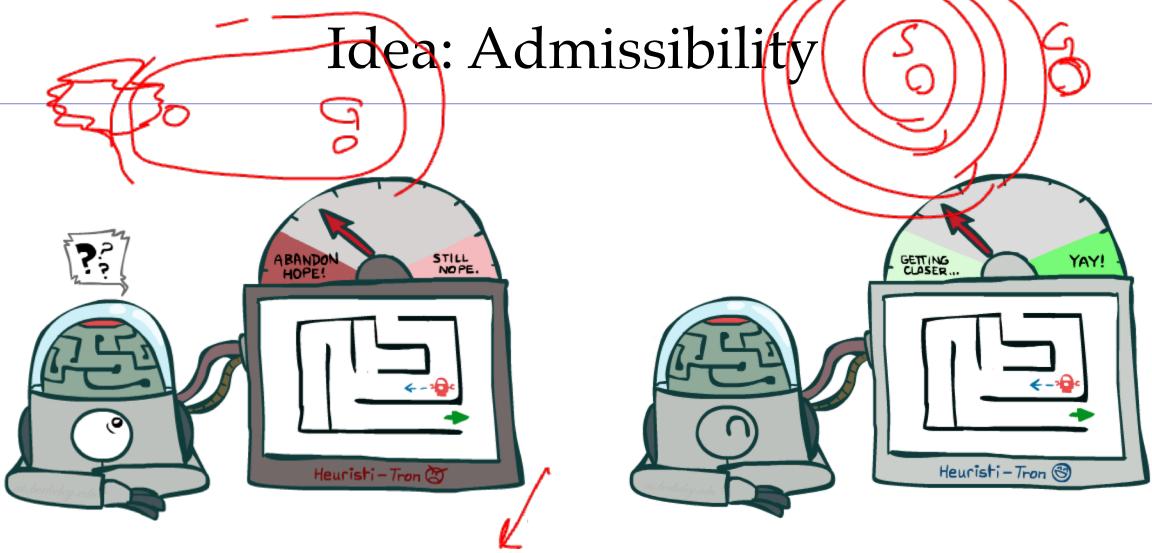
Combining UCS and Greedy



When should A* terminate?

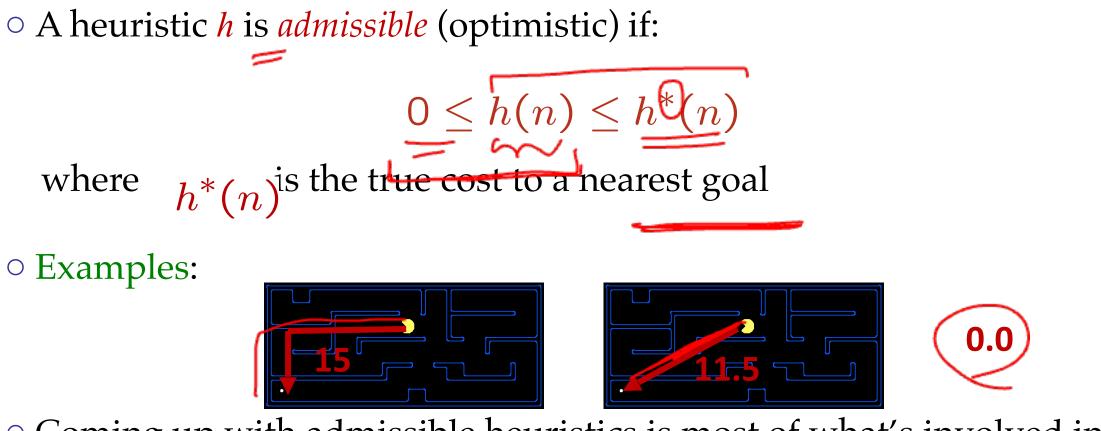






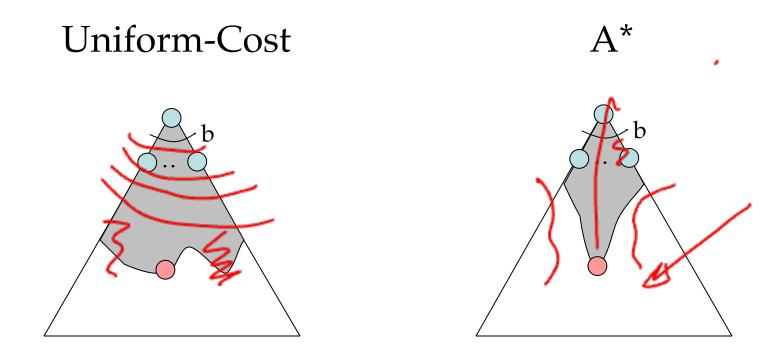
Inadmissible (pessimistic) heuristics break optimality by trapping good plans on the fringe Admissible (optimistic) heuristics slow down bad plans but never outweigh true costs

Admissible Heuristics



 Coming up with admissible heuristics is most of what's involved in using A* in practice.

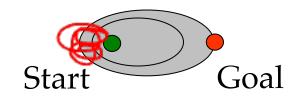
Properties of A*

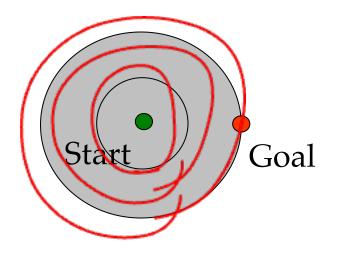


UCS vs A* Contours

Uniform-cost expands equally in all "directions"

• A* expands mainly toward the goal, but does hedge its bets to ensure optimality

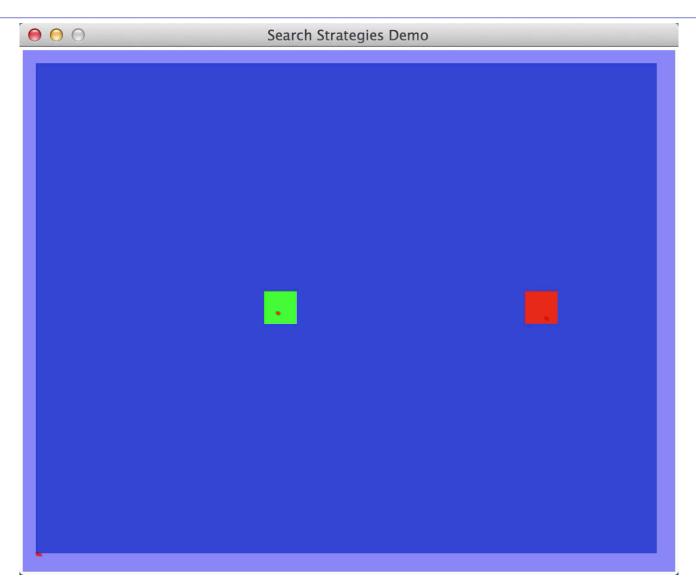




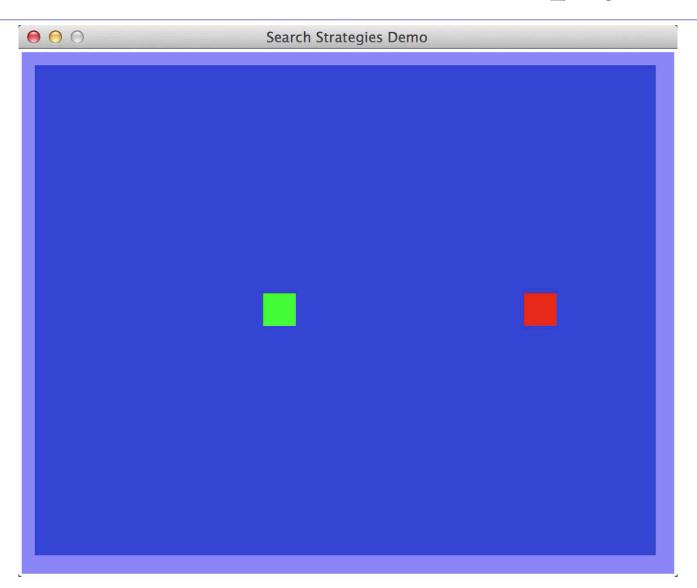
Comparison



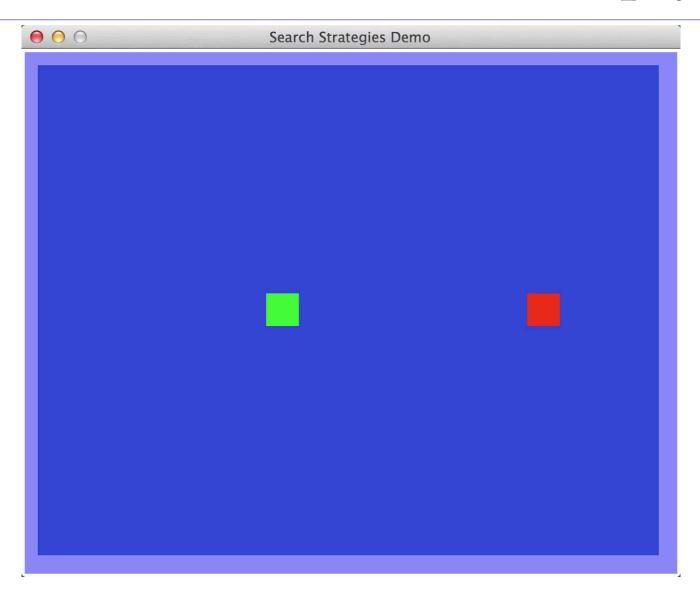
Video of Demo Contours (Empty) --(UCS)



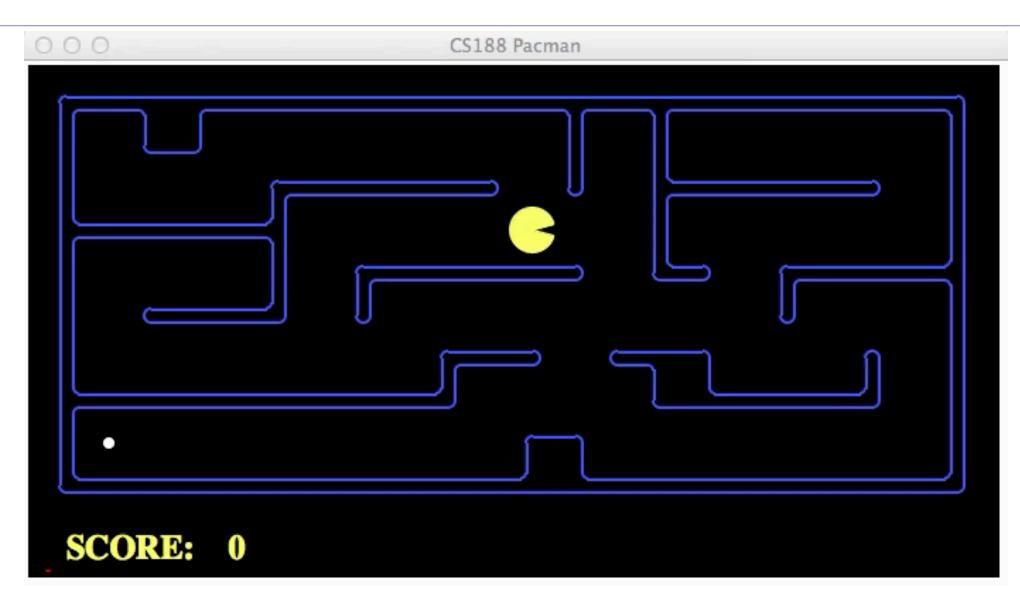
Video of Demo Contours (Empty) -- Greedy



Video of Demo Contours (Empty) – A*



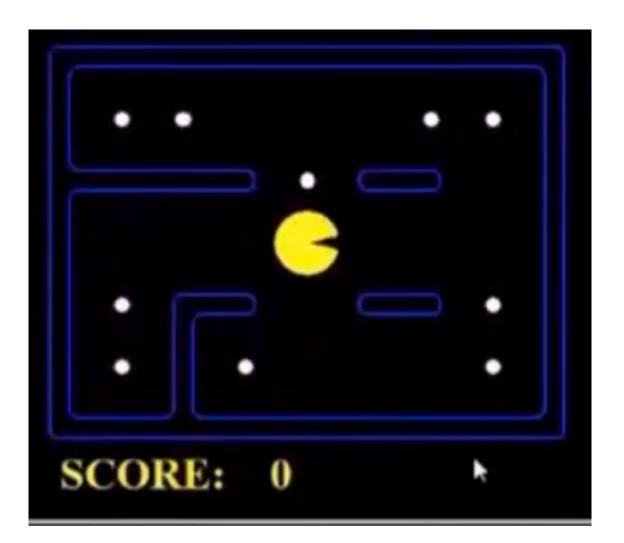
Video of Demo Contours (Pacman Small Maze) – A*



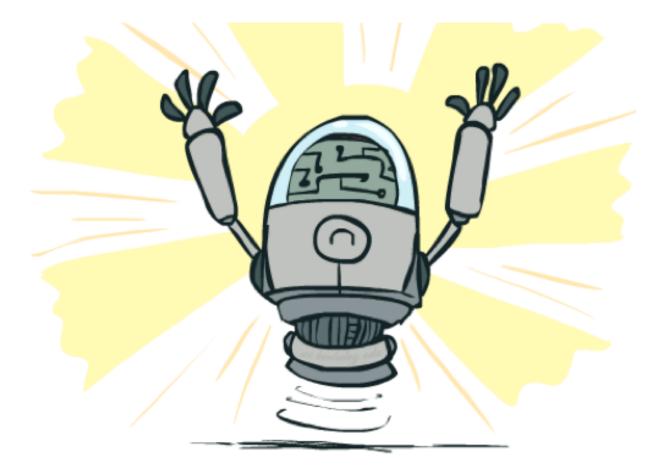
Which algorithm?



Which algorithm?



Optimality of A* Tree Search



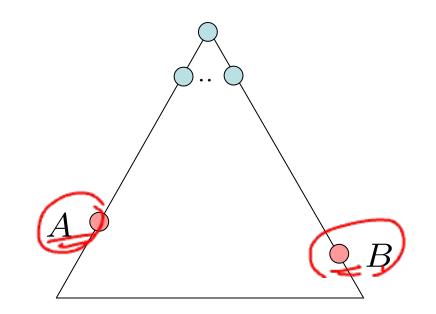
Optimality of A* Tree Search

Assume:

A is an optimal goal node
B is a suboptimal goal node
h is admissible

Claim:

• A will exit the fringe before B



Optimality of A* Tree Search: Blocking

Proof:

- Imagine B is on the fringe
- Some ancestor *n* of A is on the fringe, too (maybe A!)
- Claim: *n* will be expanded before B

1. f(n) is less or equal to f(A)

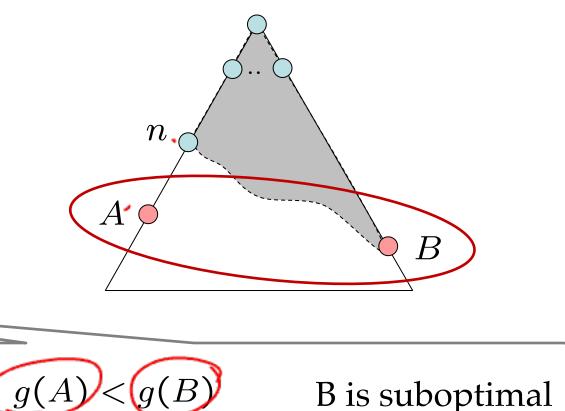
nge,
B

$$f(n) = g(n) + h(n)$$

Optimality of A* Tree Search: Blocking

Proof:

- Imagine B is on the fringe
- Some ancestor *n* of A is on the fringe, too (maybe A!)
- Claim: *n* will be expanded before B
 - 1. f(n) is less or equal to f(A)
 - 2. f(A) is less than f(B)



h = 0 at a goal

Optimality of A* Tree Search: Blocking

fin) < f(A) < f(B,

n

 $f(n) \le f(A) < f(B)$

Proof:

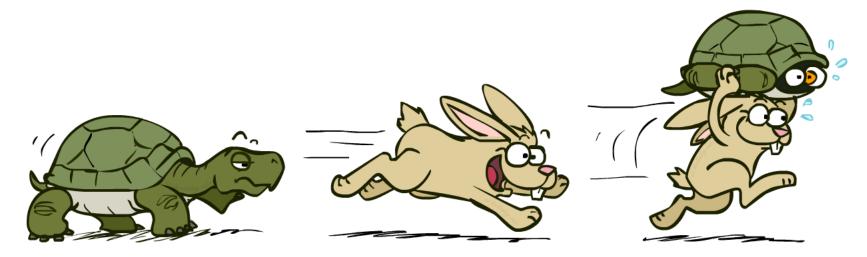
- Imagine B is on the fringe
- Some ancestor *n* of A is on the fringe, too (maybe A!)
- Claim: *n* will be expanded before B
 - 1. f(n) is less or equal to f(A)
 - 2. f(A) is less than f(B)
 - 3. *n* expands before B
- All ancestors of A expand before B
- A expands before B
- A* search is optimal

A*: Summary



A*: Summary

- A* uses both backward costs and (estimates of) forward costs
- A* is optimal with admissible (optimistic) heuristics
- Heuristic design is key: often use relaxed problems



Video of Demo Empty Water Shallow / Deep – Guess Algorithm

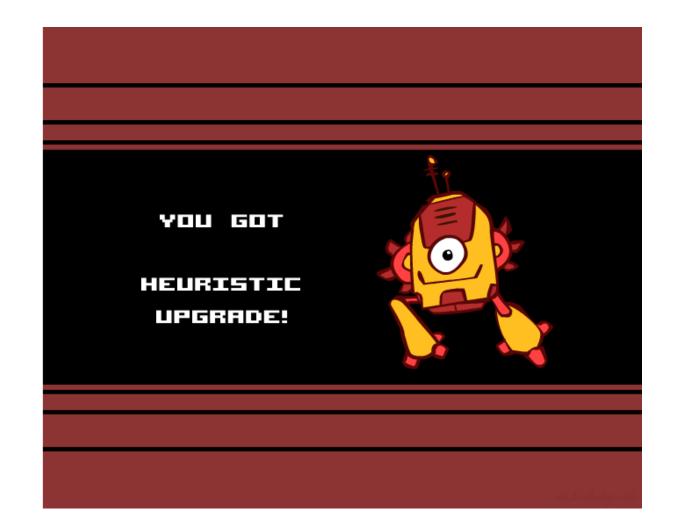
9-81 & 1 \$\$-(rch Broject Run Window Help O • Q • C • C • C • C • C • C • C • C • C	판 🙋 Pydev 着 Tea
	🧉 1 search plan tiny astar	
	🧉 1 search plan tiny astar	
	2 search plan tiny ucs 3 search demo empty 4 search contours greedy vs ucs (greedy) 5 search contours greedy vs ucs (ucs) 6 search contours greedy vs ucs (astar) 6 search greedy bad 7 search greedy good 9 search demo maze search demo maze search demo costs Run As Run Configurations Organize Favorites	•
Facman emerges v	expanded: 182 e nodes expanded: 182 victorious! Score: 573], 'results': ['Win'], 'numMoves': [27], 'scores': [573])	
.4		

.

.....

8/30/2012

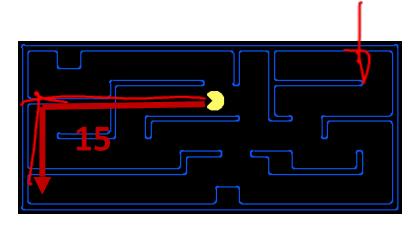
Creating Heuristics



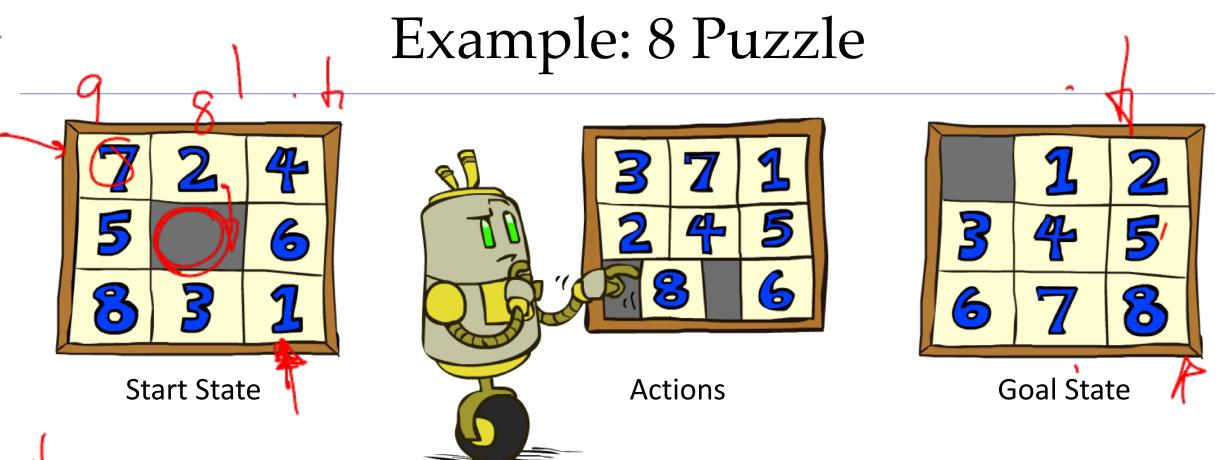
Creating Admissible Heuristics

- Most of the work in solving hard search problems optimally is in coming up with admissible heuristics
- Often, admissible heuristics are solutions to *relaxed problems*, where new actions are available





• Inadmissible heuristics are often useful too



- What are the states?
 - How many states?
 - What are the actions?
 - How many successors from the start state?
 - What should the costs be?

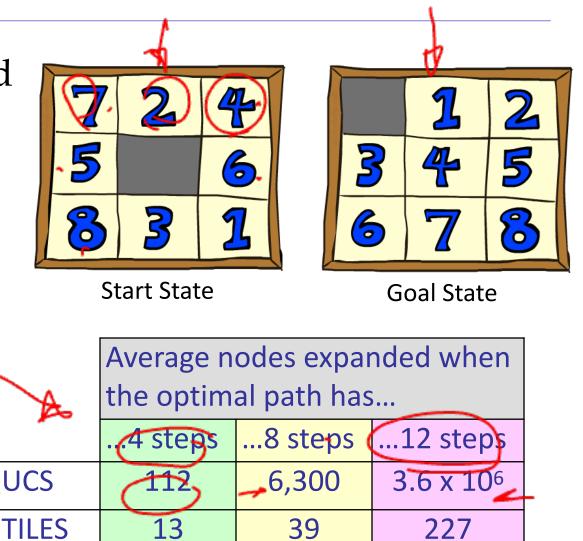
Admissible heuristics?

8 Puzzle I

6

- Heuristic: Number of tiles misplaced
- Why is it admissible?
 h(start) = ⁸
- This is a *relaxed-problem* heuristic

90

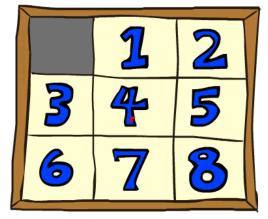


8 Puzzle II

- What if we had an easier 8-puzzle where any tile could slide any direction at any time, ignoring other tiles?
- Total Manhattan distance Ο

0

Start State



• Why is it admissible? $3 + 1 + 2 + \dots \neq 18$	Average nodes expanded when the optimal path has			
• h(start) = 222		4 steps	8 steps	12 steps
	TILES	13 🍾	39	.227
	MANHATTAN	12	25	73 🗸

8 Puzzle III

• How about using the *actual cost* as a heuristic?

- Would it be admissible?
- Would we save on nodes expanded?
- What's wrong with it?



• With A*: a trade-off between quality of estimate and work per node

• As heuristics get closer to the true cost, you will expand fewer nodes but usually do more work per node to compute the heuristic itself

Semi-Lattice of Heuristics

Trivial Heuristics, Dominance

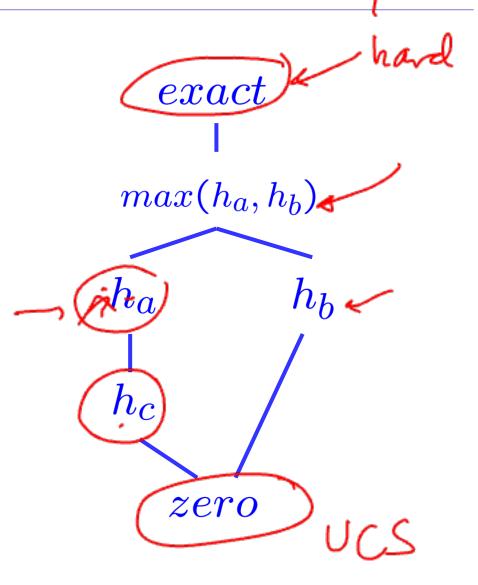
Dominance: $h_a \ge h_c$ if 0 $\forall n : (h_a(n) \ge h_a(n) \checkmark$

Heuristics form a semi-lattice:

 Max of admissible heuristics is admissible
 h(n) = max(h_a(n), h_b(n))

• Trivial heuristics

- Bottom of lattice is the zero heuristic (what does this give us?)
- Top of lattice is the exact heuristic

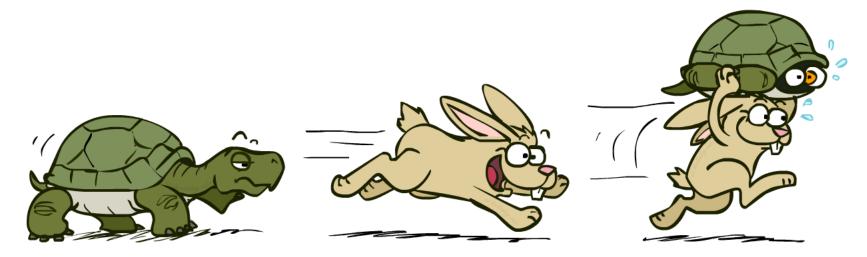


A*: Summary

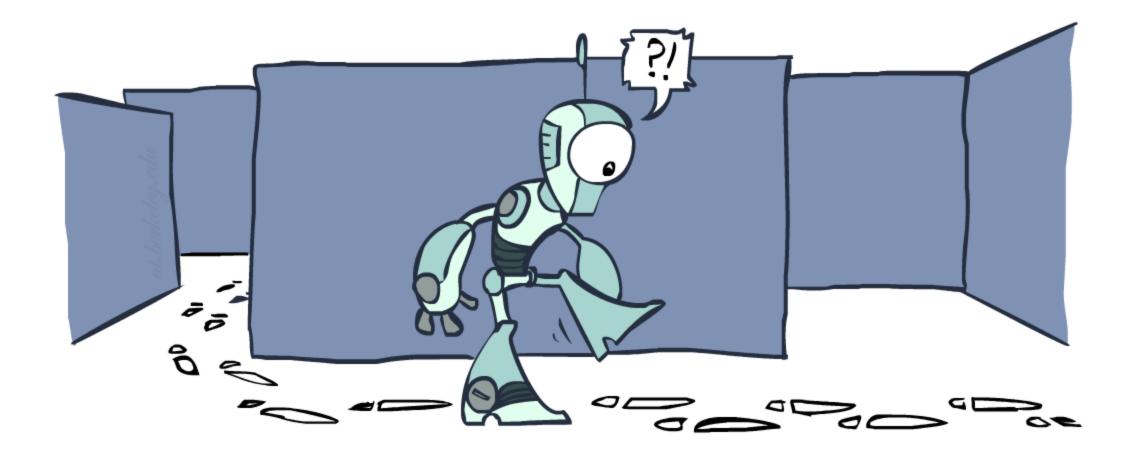


A*: Summary

- A* uses both backward costs and (estimates of) forward costs
- A* is optimal with admissible (optimistic) heuristics
- Heuristic design is key: often use relaxed problems

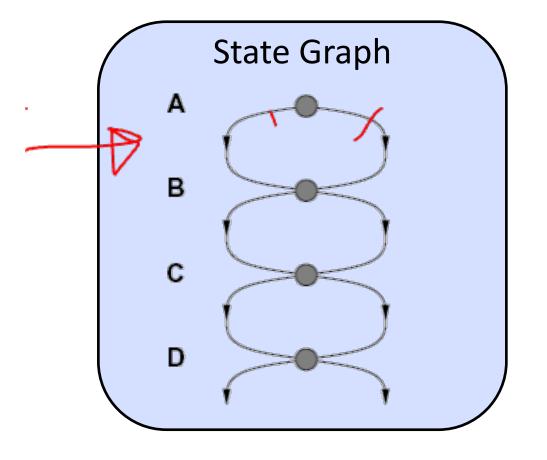


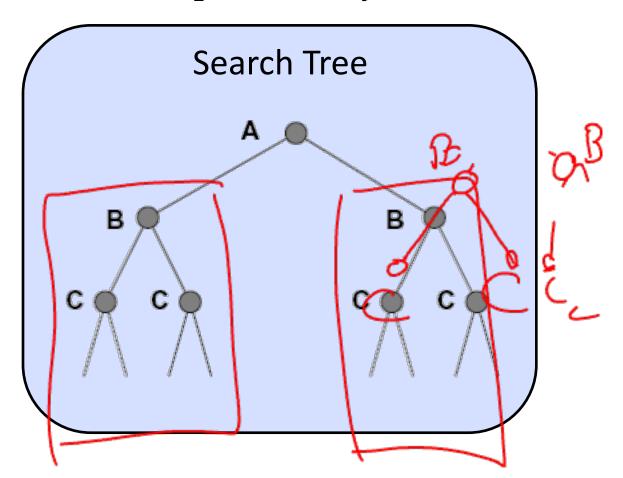
Graph Search



Tree Search: Extra Work!

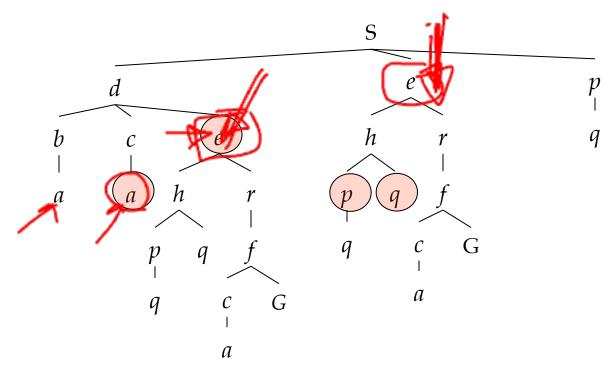
• Failure to detect repeated states can cause exponentially more work.





Graph Search

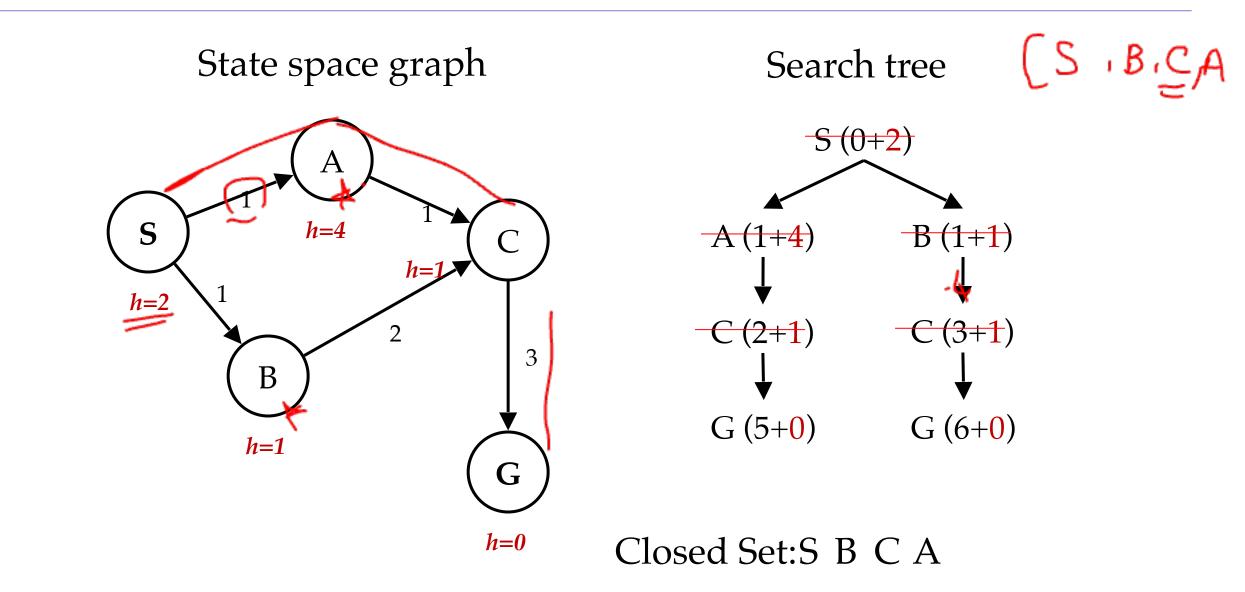
 In BFS, for example, we shouldn't bother expanding the circled nodes (why?)



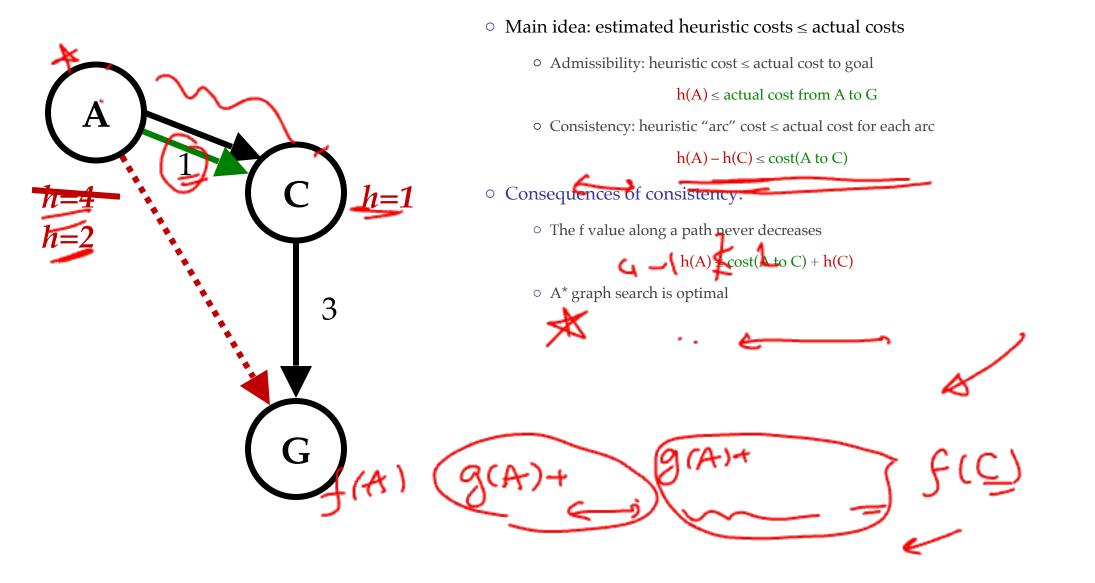
Graph Search

- Idea: never expand a state twice
- How to implement:
 - Tree search + set of expanded states ("closed set")
 - Expand the search tree node-by-node, but...
 - Before expanding a node, check to make sure its state has never been expanded before
 - If not new, skip it, if new add to closed set
- Important: store the closed set as a set, not a list
- Can graph search wreck completeness? Why/why not?
- How about optimality?

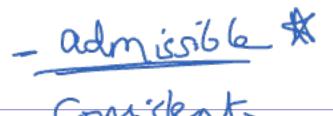
A* Graph Search Gone Wrong?



Consistency of Heuristics

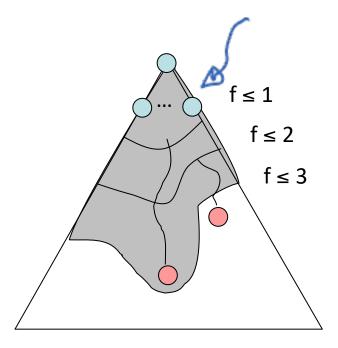


A* Graph Search



- Sketch: consider what A* does with a consistent heuristic:
 - Fact 1: In tree search, A* expands nodes in increasing total f value (f-contours)
 - Fact 2: For every state s, nodes that reach s optimally are expanded before nodes that reach s suboptimally

• Result: A* graph search is optimal



Optimality of A* Search

With a admissible heuristic, Tree A* is optimal.
With a consistent heuristic, Graph A* is optimal.
With h=0, the same proof shows that UCS is optimal.

Pseudo-Code

```
function TREE-SEARCH(problem, fringe) return a solution, or failure

fringe \leftarrow INSERT(MAKE-NODE(INITIAL-STATE[problem]), fringe)

loop do

if fringe is empty then return failure

node \leftarrow REMOVE-FRONT(fringe)

if GOAL-TEST(problem, STATE[node]) then return node

for child-node in EXPAND(STATE[node], problem) do

fringe \leftarrow INSERT(child-node, fringe)

end

end
```

A* Applications

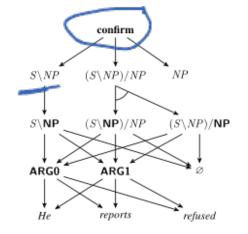
- Video games
- Pathing / routing problems
- Resource planning problems
- Robot motion planning
- Language analysis
- Machine translation
- Speech recognition

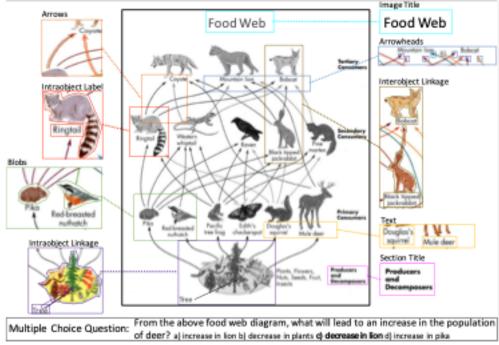
0...

A* in Literature

Joint A* CCG Parsing and Semantic Role Labeling (EMNLP'15)

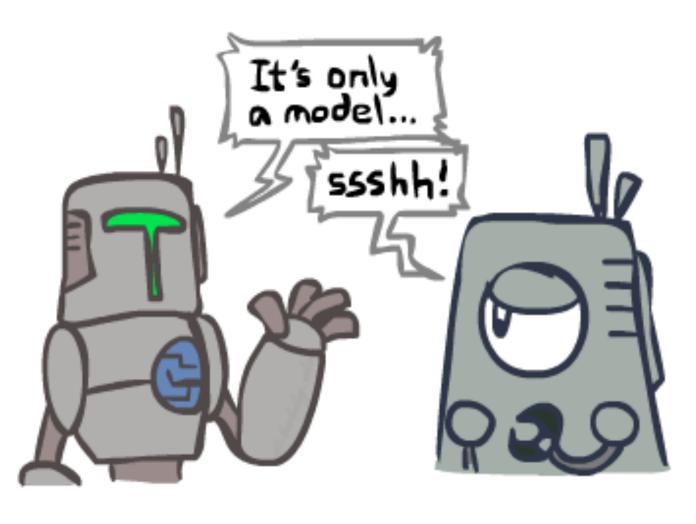
Diagram Understanding (ECCV'17)



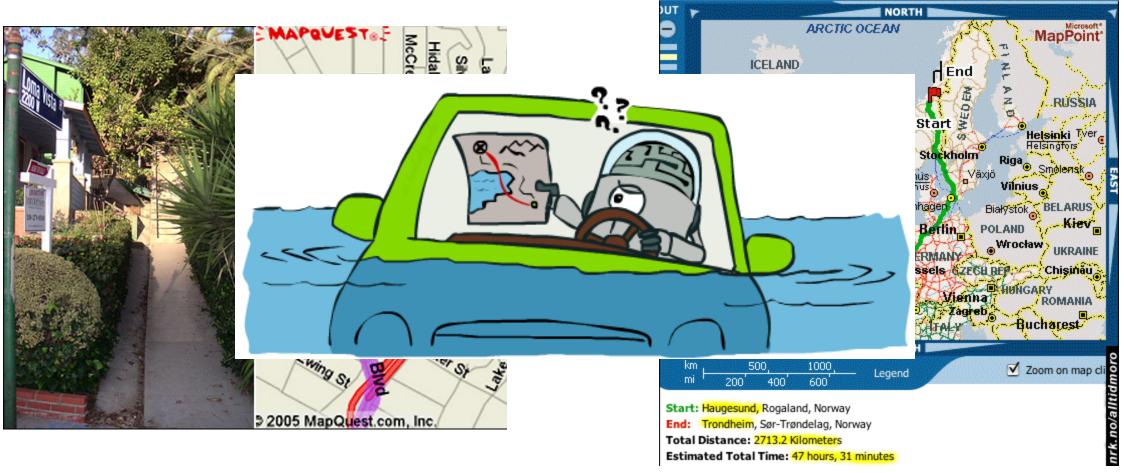


Search and Models

- Search operates over models of the world
 - The agent doesn't
 actually try all the plans
 out in the real world!
 - Planning is all "in simulation"
 - Your search is only as good as your models...



Search Gone Wrong?



Estimated Total Time: 47 hours, 31 minutes